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The authors are with the Institute of Power Machinery and Vehicular Engineering, Zhejiang University, Hangzhou 310027, China (e-mail: dfli@zju.edu.cn; jiankanhu@zju.edu.cn).

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가

weighting / dB . Ukita et al. [5] -40 (SVC) -60 가 10-1 10^{-2} 10^0 10^1 가 **SVC** frequency / Hz 가 W_f 가 1. ISO 2631-1:1997 . Saruchi et al. [6] SVC **OCP** 가 Frequency Optimal Shaping Control **Cost Function** Sequence Initial Optimization State State Method Space Vehicle Final State Model Target Position Planned & Velocity Path & Velocity 가 2. 가 .(1).(2)II. 3. A. Algorithm Structure (MSDV) ISO 2631-1:1997 가 2 가 - 1 : McCauley[7] . O'Hanlon (OCP) , [8]가 ISO 2631 가가 OCP 가 ISO 2631 **MSDV** 가 $MSDV = \sqrt{\int_0^T \left[\tilde{a}\left(t\right)\right]^2 dt}$ (1) [5] [6] 가 W_f 가 ISO 2631-1:1997 가 , *T* 가 가 가 W_f 0.16Hz가 0.16Hz B. Vehicle Model 1Hz 3 .[9] 0.0315~0. 가 XOY 25Hz가 xoy

$$\dot{X} = v\cos\left(\theta\right) \tag{2}$$

$$\dot{Y} = v\sin\left(\theta\right) \tag{3}$$

$$\dot{v} = a_x \tag{4}$$

$$\dot{\theta} = v\rho \tag{5}$$

$$\rho = 1/r = l/\tan(\delta) \tag{6}$$

$$r$$
 , l , ho 7 t .
$$a_y = v^2 \
ho$$
 (7)

アト
$$a_x$$
 ρ . a_x a_x ρ . a_x $\dot{\rho}$.

$$\dot{\boldsymbol{x}}_v = \boldsymbol{f}_v \ (\boldsymbol{x}_v, \boldsymbol{u}) \tag{8}$$

$$egin{aligned} oldsymbol{x}_v &= [X,Y,v, heta,a_x,
ho]^T \ oldsymbol{u} &= [u_1,u_2]^T &= [\dot{a}_x,\dot{
ho}]^T \end{aligned}$$

C. Cost Function in OCP Formulation

0]

가

$$J_{a} = J_{ax} + J_{ay} = \int_{0}^{t_{f}} \left\{ \left[a_{x} \left(t \right) \right]^{2} + \left[a_{y} \left(t \right) \right]^{2} \right\} dt$$
 (9)

,

 t_{f}

,

 7
 7
 7
 7

. (9)
$$[a_x(t)]^2$$
 , Parseval [1

$$J_{ax} = \int_0^{t_f} \left[a_x(t) \right]^2 dt = \int_{-\infty}^{+\infty} A_x^*(j\omega) A_x(j\omega) d\omega \quad (10)$$

$$A_x \quad a_x \qquad A_x^* \quad A_x$$

기
$$u(j\omega)$$
 가 $w(j\omega)$

$$J_{ax,w} = \int_{-\infty}^{+\infty} A_x^* (j\omega) w_x (j\omega) A_x (j\omega) d\omega, \qquad (11)$$

$$w_{x}(j\omega)$$
 .
$$w_{x}(j\omega) = p^{*}(j\omega) p(j\omega) . \tag{12}$$

$$7 + a_{x}$$

$$J_{ax,w} = \int_{-\infty}^{+\infty} \left[A_{xw}^* \left(j\omega \right) A_{xw} \left(j\omega \right) \right] d\omega, \qquad (13)$$

$$A_{xw} (j\omega) = p(j\omega) A_x (j\omega)$$
 (14)

가 $p(j\omega)$ 2

$$p(j\omega) = (j\omega)^2 / \left[(j\omega)^2 + j\xi\omega_c\omega + \omega_c^2 \right] , \qquad (15)$$

$$\xi = \sqrt{2} \qquad , \omega_c = 2\pi f_c \quad , f_c$$

$$z_1 \sim z_4$$
 가 가

 a_{xw} a_{yw}

$$\begin{cases}
 a_{xw} = \dot{z}_1 = -\xi \omega_c z_1 - \omega_c^2 z_2 + a_x \\
 \dot{z}_2 = z_1 \\
 a_{yw} = \dot{z}_3 = -\xi \omega_c z_3 - \omega_c^2 z_4 + v^2 \rho \\
 \dot{z}_4 = z_3
\end{cases}$$
(16)

 a_{xw} a_{yw} MSDV . ISO 2631-1:

1997 가 MSDV .

$$MSDV = \sqrt{\int_0^T \left\{ \left[\tilde{a}_x \left(t \right) \right]^2 + \left[\tilde{a}_y \left(t \right) \right]^2 \right\} dt}$$

$$\tilde{a}_x \quad \tilde{a}_y \quad \text{ISO 2631-1:1997} \quad W_f$$
(17)

$$a_x$$
 a_y $bold 2031 1.1357$ W_f
 T
 $t \in [0, t_f]$
 T
 T
 T
 T
 T

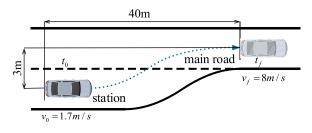
$$J_{aw} = \int_{0}^{t_f} \left\{ \left[a_{xw}(t) \right]^2 + \left[a_{yw}(t) \right]^2 \right\} dt.$$
 (18)

$$J_{aw,tf} = \int_{t_f}^{+\infty} \left\{ \left[a_{xw} \left(t \right) \right]^2 + \left[a_{yw} \left(t \right) \right]^2 \right\} dt \qquad (19)$$

$$7 \quad J_{aw,tf}$$

$$7 \quad J_{t}$$

LI HU: 7717



4.

i.e., $a_x = a_y = 0$, when $t > t_f$. Then we have

$$J_{aw,tf} = \frac{\omega_c z_1^2(t_f)}{\xi} + \frac{\omega_c^2 z_1(t_f) z_2(t_f)}{\xi^2} + \frac{\omega_c z_3^2(t_f)}{\xi} + \frac{\omega_c^2 z_3(t_f) z_4(t_f)}{\xi^2}$$

$$+ \frac{\omega_c^2 z_3(t_f) z_4(t_f)}{\xi^2}$$

$$7$$

$$7$$

$$J_{u_i} = \int_0^{t_f} [u_i(t)]^2 dt, i = 1, 2$$
 (21)

가

$$\min_{\mathbf{u}} J = w_1 J_{aw} + w_1 J_{aw,tf} + w_2 J_{u_1} + w_3 J_{u_2}$$
 (22a)

s.t.
$$\dot{\boldsymbol{x}} = f(\boldsymbol{x}, \boldsymbol{u}), \boldsymbol{x}(0) = \boldsymbol{x}_0, \boldsymbol{g}(x(t_f)) = \boldsymbol{0}$$
 (22b)

$$w_1, w_2, w_3$$
 7 $, \boldsymbol{x} = [\boldsymbol{x}_v^T \ z_1 \ z_2 \ z_3 \ z_4]^T$ (8) (16) $, \boldsymbol{g}(\boldsymbol{x}(t_f)) = \boldsymbol{0}$

MATLAB bvp5 c [11]

(22b)

Pontryagin

OCP

III.

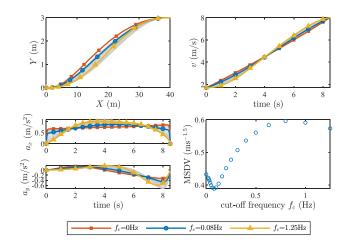
A. Example Scenario for Validation

OCP

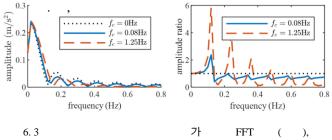
(: RoboBus)

4 가

가 가 가



5. $f_c \in [0, 1.25] \text{ Hz}$



).

0 1.7 m/s

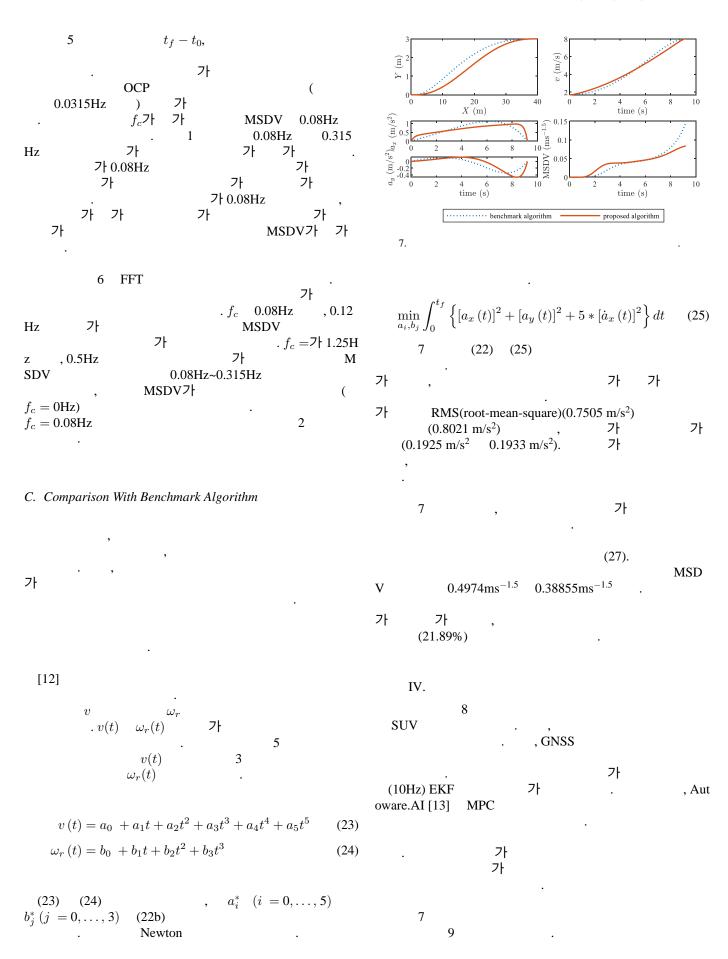
30 km/h가 8m/s v_f

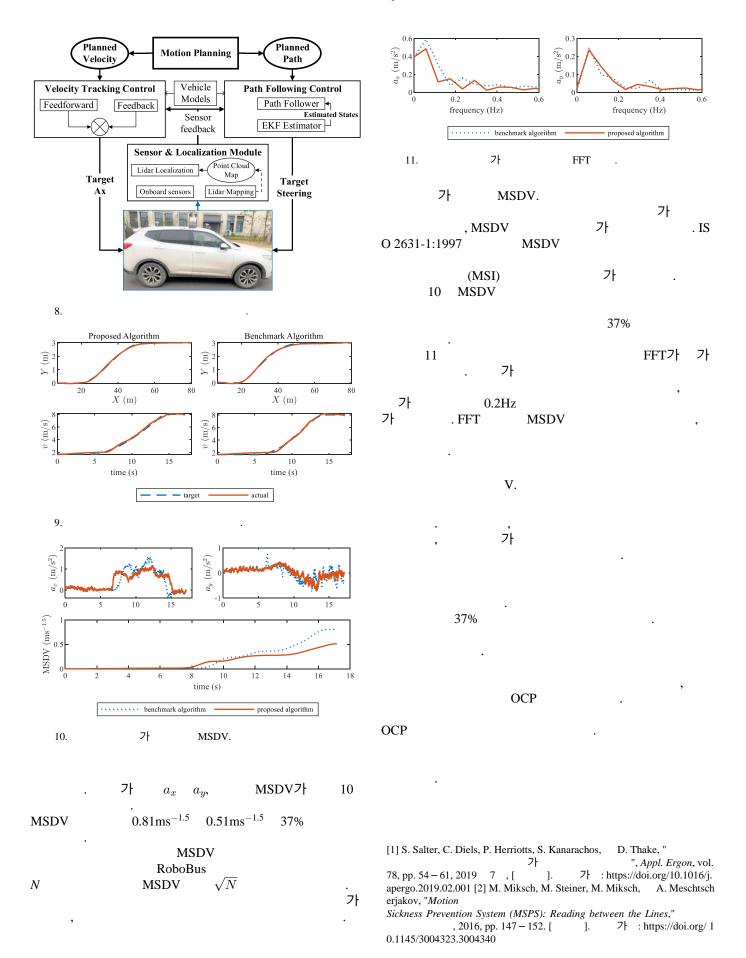
40m 3m,

B. Cut-off Frequency Selection

가 5 . (1 $f_c = 0$ Hz $p(j\omega) = 1$ 5)

가 **MSDV** 6 0, 0.08 1.25Hz FFT(





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