

Bright γ rays source and nonlinear Breit-Wheeler pairs in the collision of high density particle beams

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The collision of ultrashort high-density e^- or e^- and e^+ beams at 10s of GeV, to be available at the FACET II and in laser wakefield accelerator experiments, can produce highly collimated γ rays (few GeVs) with peak brilliance of 10^{27} ph/s mm² mrad² 0.1%BW and up to 10^5 nonlinear Breit-Wheeler pairs. We provide analytical estimates of the photon source properties and of the yield of secondary pairs, finding excellent agreement with full-scale 3D self-consistent particle-in-cell simulations that include quantum electrodynamics effects. Our results show that beam-beam collisions can be exploited as secondary sources of γ rays and provide an alternative to beam-laser setups to probe quantum electrodynamics effects at the Schwinger limit.

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I. INTRODUCTION

Colliders are a cornerstone of fundamental physics of paramount importance to probe the constituents of matter. At the interaction point of a collider, several detrimental beam-beam effects should be avoided, chief among these are beam disruption [1,2], beamstrahlung radiation [3,4], and pair creation [5]. Beam disruption arises when the collective field of these beams focuses (unlike charges e^-e^+), deflects, or blows apart (like charges e^-e^-) each beam [1,2] such that the beam density profile is significantly altered or the number of collisions may be reduced. During this process, beamstrahlung photons are emitted via nonlinear Compton scattering, and in turn can decay into electron-positron pairs via the multiphoton Breit-Wheeler mechanism [5,6]. They become more relevant in the quantum regime, when the relativistic invariant parameter χ exceeds unity. The parameter $\chi = \frac{1}{E_s} \sqrt{(\gamma \mathbf{E} + \frac{\mathbf{p} \times \mathbf{B}}{mc})^2 - (\frac{\mathbf{p} \cdot \mathbf{E}}{mc})^2}$ [7] measures the closeness to the Schwinger limit $E_s = m^2 c^3 / e \hbar$ of a particle with momentum \mathbf{p} and Lorentz factor γ , crossing an electromagnetic field \mathbf{E} , \mathbf{B} , where m is the electron rest mass, c is the

speed of light, e is the elementary charge and \hbar is the Planck constant. The classical regime is identified by $\chi \ll 1$, the full quantum regime by $\chi \gg 1$ and the quantum transition regime ranges from $0.1 \lesssim \chi \lesssim 1$. In designs for linear colliders at the energy frontier (TeV) disruption and beamstrahlung can be major issues due the large charge and small spot sizes that are needed to achieve large luminosity. As a result, such linear colliders are usually designed to avoid beam disruption and the quantum regime by using flat and elongated beams [8] since photons and secondary pairs represent an energy loss for the beams [9–11] and a source of background noise for the detectors [5,11], respectively. On the contrary, in this work we show that disruption, beamstrahlung, and pair production, which were previously regarded as detrimental effects, do have appealing potential from a fundamental physics and from a secondary source perspective. The quantum regime is actually accessible in electron-positron, or similarly electron-electron, collisions of round beams at considerably lower energy ($\mathcal{E} \sim 10$ s GeV), if the spot size at the collision is small ($\sigma_0 \sim \mu\text{m}$) and the beam current ($I \sim 100$ s kA) is high. Such beams should be available at the new SLAC facility, FACET II [12], and in the next generation of Laser Wakefield Accelerators (LWFA) experiments, opening new exciting opportunities. LWFA experiments already deliver beams with 10s of kAs of current and micron spot sizes within a single acceleration stage [13–15], and are advancing towards a multistage configuration to reach higher energies [16,17], with the ultimate goal of a TeV LWFA collider [18]. Recent advances, along with theoretical

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models and full scale simulations [19–21], predict 10–30 GeV beams from LWFA accelerators driven by 250 J class lasers in a single stage that should be soon available [22–24].

In this article, we show that **bright γ rays and copious secondary pairs** are produced during the collision of electron-electron and electron-positron beams for the range of parameters soon to be available. We introduce an analytical model that is in excellent agreement with 3D QED-PIC simulations performed with QED-OSIRIS [25–30]. Our results attest that, at the **threshold of the quantum regime**, beamstrahlung and pair production are **driven by the maximum collective field region**, with a clear experimental signature, which cannot be described by the uniform average field model [3,5]. As a consequence, the yield of secondary pairs can be orders of magnitude higher than what has been predicted before [5]. This can open the door to the experimental observation of nonlinear Breit-Wheeler pair production. Furthermore, the collisions of ultrahigh current electron beams at 10's of GeV could be exploitable as a secondary source of GeV γ rays reaching peak brilliance of 10^{27} ph/s mm² mrad² 0.1%BW leveraging on the small divergence angle at which the γ rays are emitted during the beam-beam interaction. This idea was briefly mentioned but overlooked in the context of TeV colliders [10,31].

model agrees with OSIRIS

II. PHYSICAL PICTURE

The propagation of a **single relativistic beam** is almost force-free as the contribution of the beam space charge and the beam current to the Lorentz force **nearly balance** to the order of $1/\gamma^2$ [32]. However, when two **counterpropagating beams overlap**, either the charge density (e^-e^+ collisions) or the current density (e^-e^- collisions) **vanishes**, such that the two contributions to the Lorentz force are **no longer in balance**. This generates very large focusing (e^-e^+) or defocusing (e^-e^-) forces which lead to the **disruption** of the beams. The magnitude of this effect is measured through the disruption parameter [1]

$$D = \sqrt{\pi/2} (\omega_b^2/\gamma) (\sigma_z/c)^2, \quad (1)$$

where $\omega_b = \sqrt{4\pi e^2 n_0/m}$ is the plasma frequency associated with the beam peak density n_0 , and σ_z is the beam length. This parameter is related to the number of relativistic plasma periods contained within the beam duration time ($\sim\sqrt{D}$) and it distinguishes **three regimes**: (i) the low disruption regime $D \lesssim 1$, (ii) the transition regime $1 < D < 10$, and (iii) the confinement regime $D > 10$. The disruption parameter can also be cast in the form

$$D \simeq 0.075 (\sigma_z/\sigma_0)^2 I[\text{MA}]/\mathcal{E}[\text{GeV}] \sim 10^{-3}, \quad (2)$$

for the beam parameters discussed above. In the low disruption regime, the beam duration (collision time) is

single beam: E and B force roughly balance

three regime depends on D

considerably smaller than the relativistic plasma period and the particles are almost free streaming leading to similar interaction dynamics for e^-e^- and e^-e^+ collisions. Even for low disruption, beamstrahlung radiation and consequent pair production can **rise significantly** if the two beams interact in the **quantum regime**. Beamstrahlung and pair production are commonly described via the **parameter χ_{mean}** which is the ratio of an effective mean field strength over the Schwinger field [3,5]. However, this description fails to describe the quantum transition regime where photon emission and pair production are driven by the maximum field region. For round colliding beams, the maximum χ is

$$\hat{\chi} \simeq 0.081 I[\text{MA}] \mathcal{E}[\text{GeV}]/\sigma_0[\mu\text{m}] \simeq 0.1 - 1, \quad (3)$$

for the beam parameters discussed above. In particular, the transition from the classical to the quantum regime is marked by an **exponential growth of the Breit-Wheeler cross section** with respect to the **local value of χ** . In this regime the detailed description of the field configuration is of absolute importance. The field of a beam resembles a half cycle laser with wavelength $\lambda \simeq 4\sigma_z$. The field nonlinearity parameter of a laser is $a_0 = eE/mc\omega_0$, where ω_0 is the laser frequency. Similarly, the parameter a_0 can be estimated for the **collective field of a relativistic beam** as $a_0 = \sqrt{\frac{2}{\pi}} \frac{r_e}{\sigma_0} N$, where N is the number of particles in the beam and r_e is the classical electron radius. For $a_0 \ll 1$ the pair production process involves two photons, one emitted by beamstrahlung and one from the collective electromagnetic field. For $a_0 \gg 1$ the pair production process becomes multiquantum (nonlinear Breit-Wheeler), it involves one photon emitted by beamstrahlung and several photons from the collective field. The nonlinear Breit-Wheeler process has only been approached experimentally [33].

Different photon processes based on a_0

III. ANALYTICAL MODEL

In the proper frame of reference (primed) of one beam, the collective field is purely electrostatic $\mathbf{E}' \neq 0$, $\mathbf{B}' = 0$. In the laboratory frame (unprimed), this field is Lorentz transformed as a crossed electromagnetic field, $\mathbf{E} = \gamma\mathbf{E}' - \frac{\gamma^2}{\gamma+1}\boldsymbol{\beta}(\boldsymbol{\beta} \cdot \mathbf{E}')$ and $\mathbf{B} = \gamma\boldsymbol{\beta} \times \mathbf{E}'$ where \mathbf{B}_\perp is perpendicular to \mathbf{E}_\perp with the same magnitude $B_\perp = E_\perp \sqrt{1 - 1/\gamma^2} \simeq E_\perp$ and $E_\parallel = E_\perp/\gamma$, $B_\parallel = 0$, with the parallel component along z , the propagation axis, and the perpendicular component along r . Particles are deflected by the collective fields giving rise to the disruption of the beams and to a growth in the **emittance $\epsilon \simeq D\sigma_0^2/2\sigma_z$** . However in the low disruption regime, particles are almost free streaming, and the field configuration is not altered during the two beams interaction time. Thus, the local parameter χ is given by $\chi = 2\gamma E_\perp/E_s$. If **either the beam energy loss is negligible or the number of emitted photons is less than one per**

frame of beam: electrostatic

lab frame (observer): Lorentz transformed

primary particle, then γ can be assumed to be constant. In this case, the local value of the differential probability rate of photon emission W_ω and the rate of pair production W_p are determined uniquely by the local value of $\chi(E_\perp)$. The photon spectrum generated by a primary electron that crosses such field is given by $s_\omega(\xi, r) = \int_{-\infty}^{\infty} W_\omega dt$ where $t = z/2c$ and $\xi = \hbar\omega/\gamma mc^2$ is the normalized photon energy. On its turn, a photon of energy ξ emitted at time t has a probability $\mathcal{P}_{\omega \rightarrow p}(r, t) = \int_t^\infty W_p dt'$ to decay in an electron-positron pair. The joint probability to produce a secondary pair from a primary particle is then $y_p(r) = \int_0^1 \int_{-\infty}^{\infty} W_\omega \mathcal{P}_{\omega \rightarrow p} dt d\xi$. We consider the field $E_\perp = 4\pi en_0 \sigma_0 \exp(-z^2)[1 - \exp(-r^2)]/(\sqrt{2}r) = 4\pi en_0 \sigma_0 f(r, z)$ of a beam with Gaussian density profile, $n(r, z) = n_0 \exp(-r^2 - z^2)$, where r and z coordinates are normalized to $\sqrt{2}\sigma_0$ and to $\sqrt{2}\sigma_z$ respectively. By averaging $s_\omega(\xi, r)$ over the beam density profile, we obtain the collective photon spectrum:

$$\mathcal{S}_\omega(\xi) = \frac{\int_0^\infty n(r) s_\omega(\xi, r) r dr}{\int_0^\infty n(r) r dr} \quad (4a)$$

$$\simeq \frac{\alpha^2 \sigma_z}{2\sqrt{3} r_e \gamma} \left[\frac{9}{5} \sqrt{\frac{2}{\pi}} \Xi_{2/3} + \frac{\xi^2}{1 - \xi} \Xi_{1/2} \right] \quad (4b)$$

with

$$\Xi_\nu = \frac{l_\nu \exp(-m_\nu)}{1 + m_\nu} \{1 + \sqrt{\pi} \Sigma_\nu [1 + \operatorname{erf}(\Sigma_\nu)] \exp(\Sigma_\nu^2)\},$$

$$\Sigma_\nu = \frac{m_\nu}{\sqrt{1 + m_\nu}},$$

where $l_\nu = \frac{\hat{b}^\nu}{\sqrt{\nu + \hat{b}}} \exp(-\hat{b})$ and $m_\nu = \frac{3}{5} [\hat{b} + \nu + \frac{\hat{b}}{2(\nu + \hat{b})}]$ (For a derivation of l_ν and m_ν see Appendix A). In the classical regime the parameter $b = \frac{2}{3\chi} \frac{\xi}{1 - \xi}$ reduces to $b \simeq \frac{2}{3\chi} \xi \simeq \frac{\xi}{\xi_c}$ where $\xi_c = 3\chi/2 = \hbar\omega_c/\gamma mc^2$ is the critical frequency for synchrotron radiation, $\omega_c \simeq 3\gamma^2 e(2B_\perp)/2mc$. Here $\hat{b} = \frac{2}{3\chi} \frac{\xi}{1 - \xi}$ refers to the maximum field region located around $r = 1$, $z = 0$. The fraction of radiated photons is $\mathcal{Y}_\omega = \int_0^1 \mathcal{S}(\xi) d\xi$ producing in the beam a fractional average energy loss of $\eta_\omega = \int_0^1 \xi \mathcal{S}(\xi) d\xi$ where the mean photon energy is $\bar{\xi} = \eta_\omega/\mathcal{Y}_\omega$. The radiated photons are confined within the portion of space occupied by the beam, thus the peak photon flux is $\Phi_\omega \simeq \mathcal{Y}_\omega N c / \sqrt{2\pi} \sigma_z$. If the disruption angle $\alpha_D \sim r_e N / \sigma_0 \gamma$ is larger than the photon emission cone $\alpha_\omega \sim 1/\gamma$, the divergence of the photon source is driven by the emittance of the primary beam and the photon brightness amounts to Φ_ω/ϵ^2 . At the threshold of the quantum regime, the majority of beamstrahlung energy is emitted and converted into pairs around the region of maximum field ($\hat{\chi} = 8\pi \frac{r_e^2}{\alpha} \gamma n_0 \sigma_0 f(1, 0)$). By averaging $y_p(r)$ over the

beam density profile, we obtain the yield of the secondary pairs:

$$\mathcal{Y}_p = \frac{\int_0^\infty n(r) y_p(r) r dr}{\int_0^\infty n(r) r dr} \simeq \frac{1}{\sqrt{6}} \left(\frac{\pi \alpha^2 \sigma_z}{15 r_e \gamma} \right)^2 \left[\frac{9}{5} \sqrt{\frac{2}{\pi}} \Xi_{2/3} + \frac{4}{3} \Xi_{1/2} \right]. \quad (5)$$

Here, the function Ξ_ν applies to $l_\nu = \frac{\hat{\psi}^{-(3/2+\nu)} \exp(-4\hat{\psi})}{\sqrt{(\nu + \hat{\psi})(1 + 3\hat{\psi})}}$ and $m_\nu = \frac{3}{5} [4\hat{\psi} + \frac{3}{2} + \nu + \frac{\hat{\psi}(1 + 3\hat{\psi}) + 3(\nu + \hat{\psi})}{(\nu + \hat{\psi})(1 + 3\hat{\psi})}]$, where $\hat{\psi} = 4/3\hat{\chi}$ (Full derivation in Appendix B). This model works within the following limits: $D \ll 1$, $\hat{\chi} \lesssim 1$, and $\eta_\omega \ll 1$ or $\mathcal{Y}_\omega \lesssim 1$.

IV. SIMULATIONS

To illustrate and to complement our analytical estimates, we simulated the collision of two beams for a wide range of conditions. Here we consider beams with $\sigma_0 = 1 \mu\text{m}$, $\sigma_z = 3 \mu\text{m}$, the number of particles in each beam is $N = 4, 5, 5.8 \times 10^{10}$, for energies of $\mathcal{E} = 25, 30 \text{ GeV}$. The center of each beam is set at $z_c = \pm 3\sigma_z$ at $t = 0$, and they counter propagate for a total simulated time of $6\sigma_z/c$, when the two beams completely crossed each other. Each beam is composed of 5×10^7 simulation particles. The simulation box size is $L_z \gtrsim 18\sigma_z$, $L_x = L_y \gtrsim 6\sigma_0$. The spatial and temporal resolutions range from $dx = dy = 0.1$ to $dz = 0.4c/\omega_b$ and $dt = 0.007 - 0.07\omega_b^{-1}$. The collective field corresponding to the initial beam density in vacuum is initialized with a Poisson solver [34] in the proper frame of reference of each beam and then Lorentz transformed into the laboratory frame. This allows a self-consistent treatment of the initial field configuration at the interaction point. The photon emission rate in the simulations does respect the local constant field approximation [35] (See Appendix C for a detailed discussion).

The produced photon density (seen on Fig. 1) vanishes on axis, where the collective field vanishes and photon emission and pair production are suppressed. On the other hand the probability of photon emission is maximum around $r \simeq 1$, where the collective field is maximum. However, it is the joint contribution of both the collective field and the density shape of the beam that determines the radius where the photon density is maximum. On a plane perpendicular to the photon propagation direction, the photon beam has a ring shape which reveals that beamstrahlung occurs mostly in a specific region of space. In the peak field region, the regime $\chi \sim 1$ is approached. Here, the likelihood of emitting energetic photons as well as the likelihood for these photons to decay into new secondary pairs increases exponentially.

Figure 2(a) and 2(b) show the beamstrahlung photon energy spectrum predicted by Eq. (4a), Eq. (4b) and obtained from the simulations in comparison with the

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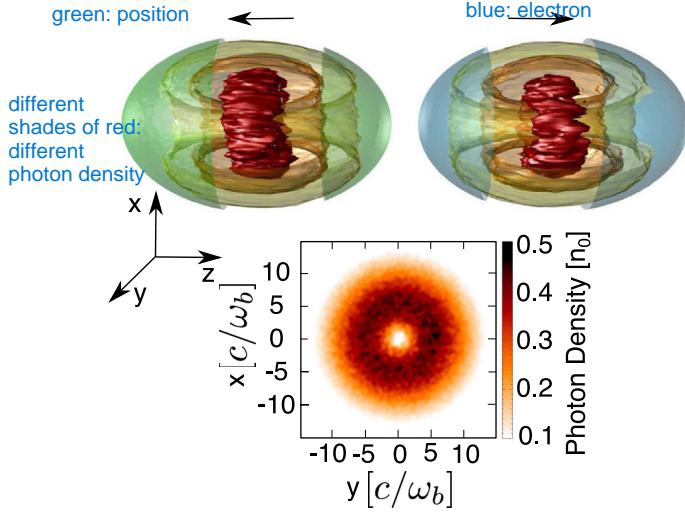


FIG. 1. The produced photon beam is represented by different iso-surfaces of the photon density [$n_\omega = 0.35, 0.5, 0.65(n_0)$] (yellow, orange, and red, respectively). The photon density is zero on axis, where the collective field vanishes, and it is maximum for $R \sim 5 c/\omega_b$. The positron beam is shown in green, and the electron beam in blue.

uniform average field model [3]. As it can be seen in Fig. 2(b), the uniform average field model underestimates the number of beamstrahlung photons in the high energy tail which are the photons with the highest probability to decay into secondary pairs. Figure 2(c) shows the secondary pairs energy spectrum, with a very large mean energy of $\bar{\mathcal{E}}_p \sim 10$ GeV, and a small energy spread (rms) $\Delta\mathcal{E}_p/\bar{\mathcal{E}}_p \sim 30\%$, as compared with other secondary sources of neutral lepton jets [36,37].

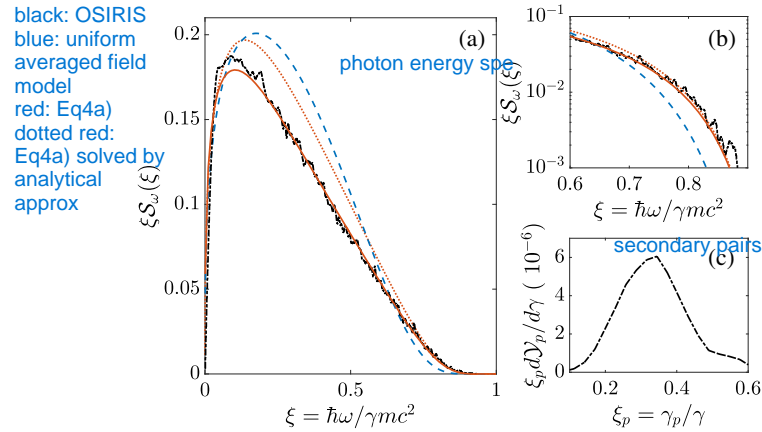


FIG. 2. (a, b) Beamstrahlung energy spectrum, for two colliding beams of $N = 5.8 \times 10^{10}$ particles, $\mathcal{E} = 30$ GeV energy, $\sigma_0 = 1 \mu\text{m}$ spot size and $\sigma_z = 3 \mu\text{m}$ length. The blue dashed line represents the uniform averaged field model [3], the black dot-dashed line represents the OSIRIS simulation, the red solid line is the numerical evaluation of Eq. (4a), and the second red dotted line is the analytical approximation of Eq. (4a) given by Eq. (4b). (c) Energy spectrum of secondary pairs energy from the OSIRIS simulation.

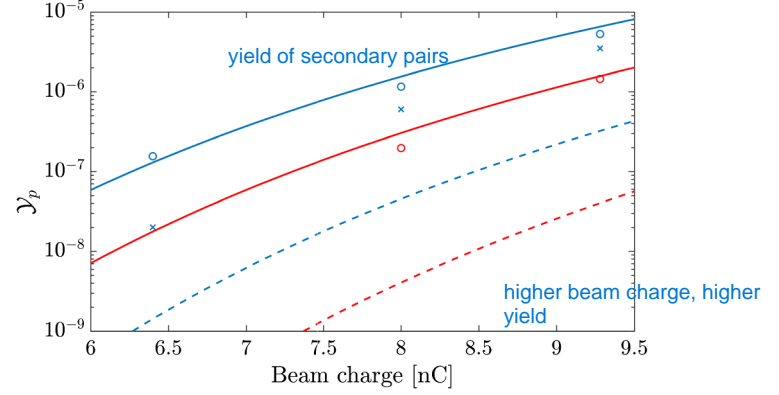


FIG. 3. Yield of the secondary pairs for two colliding beams with $\sigma_0 = 1 \mu\text{m}$ spot size and $\sigma_z = 3 \mu\text{m}$ length, for $\mathcal{E} = 25, 30$ GeV energy (red and blue, respectively), with the dashed line for the uniform averaged field model [5], OSIRIS simulation results represented by (\circ), and the solid line representing Eq. (5). The uniform average field model underestimates significantly the pair yield. The OSIRIS simulations for elliptic beams ($\sigma_x/\sigma_y = 2.25$) are denoted by (\times).

Figure 3 shows the yield of secondary pairs predicted by Eq. (5) and obtained from simulations in comparison with the uniform average field model [5]. As the pair production process is exponentially dependent on the local field strength, only the highest region of the collective field drives secondary pair production. With this regard, the uniform average field model underestimates the yield of secondary pairs. We performed as well simulations with elliptic beams, $\sigma_x/\sigma_y = 2.25$, where the transverse beam section is preserved ($\sigma_0^2 = \sigma_x\sigma_y$). We observe a reduced pair yield for the elliptic beams compared to the round ones in agreement with the qualitative predictions [5].

V. DISCUSSION AND CONCLUSIONS

In order to contextualize the properties of the source predicted for this configuration, we report, in Table I, the

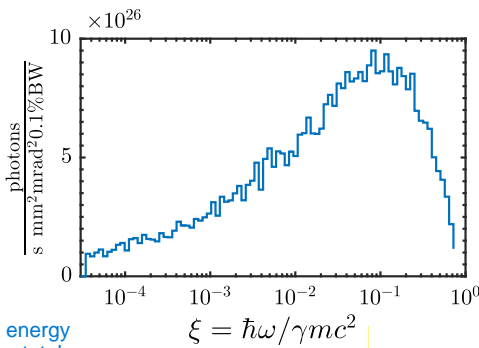
TABLE I. Beamstrahlung γ rays source, simulation (BS) and model (BM) for beams of $N = 5.8 \times 10^{10}$, $\mathcal{E} = 30$ GeV, $\sigma_0 = 1 \mu\text{m}$ and $\sigma_z = 3 \mu\text{m}$. Comparison with free electron lasers (FEL) [38], synchrotron sources (SY) [38], exotic laser-based (ELB) sources [39], Compton sources (LCS) [40], and nonlinear Compton sources (NLCS) [41]. Photon flux Φ_ω in ph/s, peak brilliance in ph/s $\text{mm}^2 \text{mrad}^2 0.1\% \text{BW}$, and energy in eV.

	η_ω	\mathcal{Y}_ω	Φ_ω	Brilliance	Energy
BS	0.085	0.95	2.2×10^{24}	9×10^{26}	10^9
BM	0.096	0.96	1.9×10^{24}	4.5×10^{26}	...
FEL	$10^{28}-10^{34}$	$10-10^5$
SY	$10^{19}-10^{25}$	$1-10^6$
ELB	$10^{-3}-0.4$	$10^{23}-10^{26}$	10^7-10^9
LCS	10^{19}	10^6
NLCS	0.02	10^{29}	10^7

characteristics of the beamstrahlung γ rays source compared to existing and proposed sources [38–41]. The beamstrahlung source dimensions at the interaction point are determined by the primary beam both in spot size and duration. In the case considered here, the transverse spot size is $1 \mu\text{m}$ and the duration is 10 fs. The high brightness 10^{30} ph/s $\text{mm}^2 \text{mrad}^2$ and brilliance 10^{27} ph/s $\text{mm}^2 \text{mrad}^2 0.1\% \text{BW}$ are achieved operating in the low disruption regime that allows to confine the radiation over a small angle $\alpha_D \simeq 2.7 \times 10^{-3}$ rad.

Compared to free electron laser sources, beamstrahlung radiation sources have a broader spectrum, providing higher energy photons but lower brilliance. Bremsstrahlung sources from relativistic electron beams shot into a solid target produce a broad spectrum in the keV–10s of MeV range with a much lower brilliance, $\lesssim 10^{20}$ ph/s $\text{mm}^2 \text{mrad}^2 0.1\% \text{BW}$, compared to the sources previously considered [42]. The possibility of synchrotron emission from solid targets by leveraging on nanowire array targets or on plasma instabilities has also been recently investigated [43,44]. Compared to storage rings for synchrotron sources, the collective field of the beams (100s of MGauss) is much stronger than the one that bending magnets usually provide (10s of kGauss). This enables to reach much higher photon energies. The emission angle of beamstrahlung, $r_e N / \sigma_0 \gamma$, gives a higher divergence to the source compared to storage rings where the emission angle is $1/\gamma$. However, the beamstrahlung source provides a higher brilliance compared to conventional synchrotron sources as the larger divergence of the beam is compensated by a higher flux the emitted photons. Figure 4 shows the brilliance as a function of the normalized photon energy ξ .

The theoretical, numerical, and experimental investigation of radiation reaction [29,45] and of pair production [27,28,30] at the Schwinger limit with a beam-laser or a laser-laser setup has known a surge of interest in connection with the upcoming laser facilities [22–24]. A beam-beam configuration has also been proposed for studying non-perturbative QED far beyond the Schwinger limit [46]. These facilities are expected to open new opportunities on laboratory astrophysics, e.g., to study pair cascades



x axis is photon energy
normalised to the total energy

FIG. 4. Brilliance of the beamstrahlung γ rays source, for two colliding beams of $N = 5.8 \times 10^{10}$ particles, $\mathcal{E} = 30$ GeV energy, $\sigma_0 = 1 \mu\text{m}$ spot size and $\sigma_z = 3 \mu\text{m}$ length.

[47–50]. However, the experimental observation of a few nonlinear Breit-Wheeler pairs was only achieved in the SLAC experiment E-144 in the collision of an electron beam with an optical laser [33]. In the SLAC experiment E-144 the nonlinear regime for pair production was only approached, $a_0 \simeq 0.1$ –1 (field nonlinearity threshold at $a_0 = 1$). For the beam parameters discussed before, $N = 5.8 \times 10^{10}$ and $\sigma_0 = 1 \mu\text{m}$ the field nonlinearity parameter for a two colliding beams setup would be $a_0 \simeq 41$, thus the nonlinear Breit-Wheeler pair production process could be probed far beyond the threshold $a_0 \simeq 1$ with a considerable yield, 10^5 , of secondary pairs.

In conclusion, our results show that in the low disruption regime, beamstrahlung radiation can effectively be employed as highly collimated γ rays source at GeV energy with unprecedented brilliance. Moreover, given the high yield of nonlinear Breit-Wheeler pairs, this setup may be a viable alternative for studying QED effects, approaching the Schwinger limit, compared to beam-laser setups.

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F. D. G. and T. G. contributed equally to this work.

APPENDIX A: DERIVATION OF THE PHOTON SPECTRUM

In a constant crossed field, the differential probability rate for photon emission is [7]

$$W_\omega = \frac{\alpha}{\sqrt{3}\pi\tau_c\gamma} \left[\int_b^\infty K_{5/3}(x)dx + \frac{\xi^2}{1-\xi} K_{2/3}(b) \right], \quad (\text{A1})$$

where $b = 2\xi/3\chi_e(1-\xi)$ and $\xi = \hbar\omega/\gamma mc^2$. The modified Bessel function of the second kind is indicated by K_ν , the fine structure constant is α , and the Compton time is τ_c . The classical synchrotron spectrum is given by the integral $\int_b^\infty K_{5/3}(x)dx$, which can be approximated by $\int_b^\infty K_{5/3}(x)dx \simeq \frac{9}{5}b^{-2/3}\exp(-b)$. The second term contributes mainly to the high energy part of the spectrum and can be approximated, in the limit for large arguments, by $K_{2/3}(b) \simeq \sqrt{\frac{\pi}{2b}}\exp(-b)$. The parameter b is a function of time, of space, and of energy, given by $b = \frac{2}{3}b_0 \frac{\xi}{1-\xi} \frac{x \exp(u^2)}{1-\exp(-x^2)} = \frac{2}{3}b_0 b_\xi b_x b_u$, where $x = r/\sqrt{2}\sigma_0$ is the

normalized radius and $u = \sqrt{2}ct/\sigma_z$ is the normalized time that accounts for the relative velocity between the two colliding beams. The constant b_0 is $b_0 = \frac{E_s}{4\sqrt{2}\pi e\gamma n_b \sigma_0}$. The integration of W_ω in time yields

$$s(\xi, x) = \int W_\omega dt = \frac{1}{\sqrt{6\pi} c\tau_c \gamma} \left[\frac{9}{5} F_{2/3} + \frac{\xi^2}{1-\xi} \sqrt{\frac{\pi}{2}} F_{1/2} \right]. \quad (\text{A2})$$

We have used the expansion $b_u = \exp(u^2) \simeq (1+u^2)$ around the peak of the collective field at $u=0$, and we introduced the function $F_\nu = (\frac{2}{3} b_0 b_\xi b_x)^{-\nu} (\nu + \frac{2}{3} b_0 b_\xi b_x)^{-1/2} \times \exp(-\frac{2}{3} b_0 b_\xi b_x)$. The weighted integration over space of F_ν is $\int q(x) F_\nu(x, \xi) dx$, with $q(x) = 2x \exp(-x^2)$ the transverse density profile of the beam. For the integration, we approximate the function $F_\nu(x, \xi)$ with a Gaussian form $f_\nu(x, \xi) = l_\nu(\xi) \exp[-m_\nu(\xi)(x - \hat{x})^2]$. The position of the maximum for $F_\nu(x, \xi)$ is located at $\hat{x} \simeq 1$. The second derivative of $F_\nu(x, \xi)$ is evaluated at \hat{x} as

$$\begin{aligned} \partial_x^2 F_\nu|_{\hat{x}} &= -F_\nu \left[1 + \frac{\nu}{(\frac{2}{3} b_0 b_\xi b_x)} + \frac{1}{2[\nu + (\frac{2}{3} b_0 b_\xi b_x)]} \right] \\ &\times \left(\frac{2}{3} b_0 b_\xi \right) \partial_x^2 b_x \Big|_{\hat{x}} \\ &= - \left[1 + \frac{\nu}{\hat{b}} + \frac{1}{2(\nu + \hat{b})} \right] \frac{2(2\hat{x} - 1)\hat{b} F_\nu(\hat{b})}{\exp(\hat{x}^2) - 1}, \end{aligned} \quad (\text{A3})$$

where $\hat{b} = \frac{2}{3} b_0 b_\xi b_x(\hat{x})$. The parameters $l_\nu(\xi)$ and $m_\nu(\xi)$ are then obtained as

$$l_\nu(\xi) = F_\nu(\hat{x}, \xi), \quad (\text{A4})$$

$$\begin{aligned} m_\nu(\xi) &= - \frac{\partial_x^2 F_\nu(x, \xi)|_{\hat{x}}}{2l_\nu(\xi)} \\ &= \left[1 + \frac{\nu}{\hat{b}} + \frac{1}{2(\nu + \hat{b})} \right] \frac{(2\hat{x} - 1)\hat{b}}{\exp(\hat{x}^2) - 1}. \end{aligned} \quad (\text{A5})$$

The weighted integration over space $\int q(x) F_\nu(x, \xi) dx \simeq \int q(x) f_\nu(x, \xi) dx = \Xi_\nu(\xi)$ then gives

$$\begin{aligned} \Xi_\nu &= \frac{l_\nu \exp(-\hat{x}^2 m_\nu)}{1 + m_\nu} \left\{ 1 + \sqrt{\pi} \frac{\hat{x} m_\nu}{\sqrt{1 + m_\nu}} \right. \\ &\times \left. \exp\left(\frac{\hat{x}^2 m_\nu^2}{1 + m_\nu}\right) \left[1 + \operatorname{erf}\left(\frac{\hat{x} m_\nu}{\sqrt{1 + m_\nu}}\right) \right] \right\}, \end{aligned} \quad (\text{A6})$$

and the photon spectrum reads

$$\begin{aligned} \mathcal{S}_\omega(\xi) &= \int q(x) s(x, \xi) dx \\ &\simeq \frac{1}{\sqrt{6\pi} c\tau_c \gamma} \left[\frac{9}{5} \Xi_{2/3} + \frac{\xi^2}{1-\xi} \sqrt{\frac{\pi}{2}} \Xi_{1/2} \right]. \end{aligned} \quad (\text{A7})$$

APPENDIX B: DERIVATION OF THE YIELD OF SECONDARY PAIRS

In a constant crossed field, the rate of pair creation can be computed as [7]

$$W_p \simeq \frac{2\pi\alpha}{25\tau_c \gamma} \frac{1}{\psi} \exp\left(-\frac{2\psi}{\xi}\right), \quad (\text{B1})$$

valid in the limit $\chi_e \lesssim 1$, with $\psi = 4/3 \chi_e = \frac{4}{3} b_0 b_x b_u$. The probability of creating a pair from a photon with energy ξ emitted at time t is

$$\begin{aligned} \mathcal{P}_{\omega \rightarrow p} &= \int_t^\infty W_p dt' \\ &= \frac{\pi\alpha\sigma_z}{25c\tau_c \gamma} \sqrt{\frac{\pi}{2}} \frac{3 \exp(-\frac{8b_0 b_x}{3\xi})}{4b_0 b_x \sqrt{1 + 8b_0 b_x/3\xi}} \\ &\times [1 - \operatorname{erf}(u\sqrt{1 + 8b_0 b_x/3\xi})]. \end{aligned} \quad (\text{B2})$$

We employed the Taylor expansion $b_u = \exp(u^2) \simeq (1+u^2)$ around the peak of the collective field at $u=0$. The joint probability to produce a secondary pair from a primary particle is then $y_p(x) = \iint W_\omega \mathcal{P}_{\omega \rightarrow p} dt d\xi = \int s(x, \xi) \mathcal{P}_{\omega \rightarrow p}(x, \xi, u=0) d\xi$. By using the exponential function $\exp[-\frac{8}{3\xi} b_0 b_x - \frac{2}{3} b_0 b_\xi b_x] = \exp[-\frac{2b_0 b_x}{3} (\frac{4}{\xi} + \frac{\xi}{1-\xi})]$ with the maximum located at $\hat{\xi} = 2/3$, the saddle point method gives

$$y_p(x) = s(x, \hat{\xi}) \mathcal{P}_{\omega \rightarrow p}(x, \hat{\xi}, u=0) \sqrt{\frac{\pi}{27b_0 b_x}}. \quad (\text{B3})$$

By denoting $\psi_x = \frac{4}{3} b_0 b_x = \frac{2}{3} b_0 b_\xi(\hat{\xi}) b_x$, $y_p(x)$ is

$$\begin{aligned} y_p(x) &= \frac{1}{\sqrt{6}} \left(\frac{\pi\alpha\sigma_z}{15c\tau_c \gamma} \right)^2 \left[\frac{9}{5} \sqrt{\frac{2}{\pi}} \frac{\psi_x^{-2/3}}{\sqrt{2/3 + \psi_x}} \right. \\ &\times \left. \frac{4}{3} \frac{\psi_x^{-1/2}}{\sqrt{1/2 + \psi_x}} \right] \frac{\psi_x^{-3/2} \exp(-4\psi_x)}{\sqrt{1 + 3\psi_x}}. \end{aligned} \quad (\text{B4})$$

We define the function $F_\nu = \frac{\psi_x^{-(3/2+\nu)} \exp(-4\psi_x)}{\sqrt{(\nu+\psi_x)(1+3\psi_x)}}$, analogously to what used for the photon spectrum. The weighted integration over space of F_ν is $\int q(x) F_\nu dx$, with $q(x) = 2x \exp(-x^2)$ the transverse density profile of the beam. For the integration, we approximate the function F_ν with a Gaussian form $f_\nu = l_\nu \exp[-m_\nu(x - \hat{x})^2]$. The position of the maximum of F_ν is also located at $\hat{x} \simeq 1$. The second derivative of F_ν is evaluated at \hat{x} as

$$\partial_{\hat{x}}^2 F_\nu|_{\hat{x}} = -F_\nu(\hat{x}) \left[4 + \frac{3/2 + \nu}{\hat{\psi}} + \frac{1}{2} \frac{(1 + 3\hat{\psi}) + 3(\nu + \hat{\psi})}{(\nu + \hat{\psi})(1 + 3\hat{\psi})} \right] \times \frac{2(\hat{x} - 1)\hat{\psi}}{\exp(\hat{x}^2) - 1}, \quad (\text{B5})$$

where $\hat{\psi} = \frac{4}{3} b_0 b_x(\hat{x})$. The parameters l_ν and m_ν are then obtained as

$$l_\nu = F_\nu(\hat{x}), \quad (\text{B6})$$

$$m_\nu = -\frac{\partial_{\hat{x}}^2 F_\nu(x)|_{\hat{x}}}{2l_\nu} = \left[4 + \frac{3/2 + \nu}{\hat{\psi}} + \frac{1}{2} \frac{(1 + 3\hat{\psi}) + 3(\nu + \hat{\psi})}{(\nu + \hat{\psi})(1 + 3\hat{\psi})} \right] \frac{2(\hat{x} - 1)\hat{\psi}}{\exp(\hat{x}^2) - 1}. \quad (\text{B7})$$

The weighted integration over space $\int q(x) F_\nu(x) dx \simeq \int q(x) f_\nu(x) dx = \Xi_\nu$ gives the same function in l_ν and m_ν obtained previously, Eq. (A6). The yield of secondary pairs then reads

$$\mathcal{Y}_p \simeq \frac{1}{\sqrt{6}} \left(\frac{\pi \alpha \sigma_z}{15 c \tau_c \gamma} \right)^2 \left[\frac{9}{5} \sqrt{\frac{2}{\pi}} \Xi_{2/3} + \frac{4}{3} \Xi_{1/2} \right]. \quad (\text{B8})$$

APPENDIX C: THE LOCAL CONSTANT CROSSED FIELD APPROXIMATION

In the case of an arbitrary field the differential probability rates for photon emission W_ω and for pair production W_p depend on three Lorentz invariants: f , g , and χ , defined below. For a constant crossed field ($E = B$, and $\mathbf{E} \cdot \mathbf{B} = 0$), the invariants f and g vanish. In the general case, according to Ritus [7], if the fields are much smaller than E_s then f , $g \ll 1$. Moreover, if the particle have a large Lorentz factor $\gamma \gg 1$, these two invariants are also much smaller than χ^2 . Under these conditions, f and g can be neglected and the probabilities $W_{\omega,p}(f, g, \chi)$ are well approximated by $W_{\omega,p}(0, 0, \chi)$. In the proper frame of reference of the beam (primed) there is only an electrostatic field \mathbf{E}' , thus the invariant

$$g = \frac{F'^{\mu,\nu} F'^{*}_{\mu,\nu}}{4E_s^2} = \frac{\mathbf{E}' \cdot \mathbf{B}'}{E_s^2} \quad (\text{C1})$$

is identically zero. The difference in amplitude between \mathbf{E}' and \mathbf{B}' is determined by the invariant

$$f = \frac{F'^{\mu,\nu} F'_{\mu,\nu}}{4E_s^2} \quad (\text{C2})$$

$$= \frac{E'^2 - B'^2}{E_s^2} = \frac{E'^2}{E_s^2}. \quad (\text{C3})$$

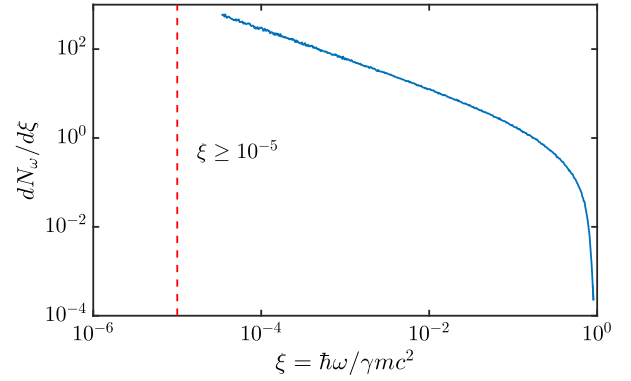


FIG. 5. Photon spectrum (solid blue) for beam parameters of $N = 5.8 \times 10^{10}$, $\mathcal{E} = 30$ GeV, $\sigma_0 = 1 \mu\text{m}$ and $\sigma_z = 3 \mu\text{m}$. The local constant field approximation limit of validity (dashed red) is respected by all photons in the simulation.

This invariant relates to χ^2 of a particle with velocity \mathbf{v}' and Lorentz factor γ' as $f = \chi^2 (E'^2_\perp + E'^2_\parallel) / (\gamma'^2 E'^2_\perp + E'^2_\parallel)$, where the parallel and perpendicular components are defined with respect to the velocity. Thus, as the ordering is $E'_\perp \sim E'_\parallel \ll \gamma' E'_\perp$ then $f \sim \chi^2 / \gamma'^2 \ll \chi^2$, which shows that $f, g \ll 1$ and $f, g \ll \chi^2$.

Finally, if the formation length $L_f = mc^2 / eE_\perp$ is much smaller than the gradient scale of the field $|E_\perp / \nabla E_\perp| \sim \sigma_z$ the emission process is local and the field leading to the emission can be considered as constant. This condition can be cast in the form $\sigma_0 \sigma_z \gg d_e^2$ which breaks for diluted beams but holds for dense beams where the electron skin depth d_e is much smaller than the beam dimensions. In the conditions explored in the paper, $\sigma_0 \sim 5d_e$, $\sigma_z = 3\sigma_0$ and thus $\sigma_0 \sigma_z \sim 75d_e^2 \gg d_e^2$. For the above mentioned reasons, the collective field of a dense relativistic beam can be regarded as a constant crossed field, where the differential probability rates for photon emission and for pair production derived by Ritus [7] are applicable. However, the local constant field approximation might break for the description of nonlinear Compton scattered photons with energy lower than $\xi \ll \chi / a_0^3$ [35]. Figure 5 shows that all photons in our simulation do respect the local constant field approximation limit of validity. Here the equivalent a_0 of the beam is $a_0 = 41$ and the worst case scenario is at $\chi = 1$, this determines that all simulated photons must respect $\xi \geq 1.45 \times 10^{-5}$.

- [1] R. Hollebeek, *Nucl. Instrum. Methods Phys. Res.* **184**, 333 (1981).
- [2] P. Chen and K. Yokoya, Disruption effects from the interaction of round e^+e^- beams, *Phys. Rev. D* **38**, 987 (1988).
- [3] P. Chen, Differential luminosity under multiphoton beamstrahlung, *Phys. Rev. D* **46**, 1186 (1992).

- [4] R. Blankenbecler and S. D. Drell, Quantum treatment of beamstrahlung, *Phys. Rev. D* **36**, 277 (1987).
- [5] P. Chen and V. I. Telnov, Coherent Pair Creation in Linear Colliders, *Phys. Rev. Lett.* **63**, 1796 (1989).
- [6] G. Breit and J. A. Wheeler, Collision of two light quanta, *Phys. Rev.* **46**, 1087 (1934).
- [7] V. I. Ritus, Quantum effects of the interaction of elementary particles with an intense electromagnetic field, *J. Sov. Laser Res.* **6**, 497 (1985).
- [8] Stanford Linear Accelerator Center Report No. DE96009136, 1995.
- [9] R. J. Noble, Beamstrahlung from colliding electron-positron beams with negligible disruption, *Nucl. Instrum. Methods Phys. Res., Sect. A* **256**, 427 (1987).
- [10] R. Blankenbecler and S. D. Drell, Quantum Beamstrahlung: Prospects for a Photon-Photon Collider, *Phys. Rev. Lett.* **61**, 2324 (1988).
- [11] S. Chattopadhyay, D. Whittum, and J. Wurtele, Advanced accelerator technologies-A Snowmass'96 subgroup summary, eConf C **960625** (1996).
- [12] G. White, in *FACET-II Science Workshop, California, 2017* (2017), <https://conf.slac.stanford.edu/facet-2-2017/agenda>.
- [13] S. Kneip *et al.*, Near-GeV Acceleration of Electrons by a Nonlinear Plasma Wave Driven by a Self-Guided Laser Pulse, *Phys. Rev. Lett.* **103**, 035002 (2009).
- [14] N. A. M. Hafz, T. M. Jeong, I. W. Choi, S. K. Lee, K. H. Pae, V. V. Kulagin, J. H. Sung, T. J. Yu, K.-H. Hong, T. Hosokai, J. R. Cary, D.-K. Ko, and J. Lee, Stable generation of GeV-class electron beams from self-guided laser-plasma channels, *Nat. Photonics* **2**, 571 (2008).
- [15] W. P. Leemans, B. Nagler, A. J. Gonsalves, Cs. Toth, K. Nakamura, C. G. R. Geddes, E. Esarey, C. B. Schroeder, and S. M. Hooker, GeV electron beams from a centimetre-scale accelerator, *Nat. Phys.* **2**, 696 (2006).
- [16] S. Steinke, J. van Tilborg, C. Benedetti, C. G. R. Geddes, C. B. Schroeder, J. Daniels, K. K. Swanson, A. J. Gonsalves, K. Nakamura, N. H. Matlis, B. H. Shaw, E. Esarey, and W. P. Leemans, Multistage coupling of independent laser-plasma accelerators, *Nature (London)* **530**, 190 (2016).
- [17] H. T. Kim, K. H. Pae, H. J. Cha, I. J. Kim, T. J. Yu, J. H. Sung, S. K. Lee, T. M. Jeong, and J. Lee, Enhancement of Electron Energy to the Multi-GeV Regime by a Dual-Stage Laser-Wakefield Accelerator Pumped by Petawatt Laser Pulses, *Phys. Rev. Lett.* **111**, 165002 (2013).
- [18] W. Leemans and E. Esarey, Laser-driven plasma-wave electron accelerators, *Phys. Today* **62**, No. 3, 44 (2009).
- [19] W. Lu, M. Tzoufras, C. Joshi, F. S. Tsung, W. B. Mori, J. Vieira, R. A. Fonseca, and L. O. Silva, Generating multi-GeV electron bunches using single stage laser wakefield acceleration in a 3D nonlinear regime, *Phys. Rev. ST Accel. Beams* **10**, 061301 (2007).
- [20] L. O. Silva, F. Fiuza, R. A. Fonseca, J. L. Martins, S. F. Martins, J. Vieira, C. Huang, W. Lu, F. Tsung, M. Tzoufras, and W. B. Mori, Laser electron acceleration with 10 PW lasers, *C.R. Phys.* **10**, 167 (2009).
- [21] S. F. Martins, R. A. Fonseca, W. Lu, W. B. Mori, and L. O. Silva, Exploring laser-wakefield-accelerator regimes for near-term lasers using particle-in-cell simulation in Lorentz-boosted frames, *Nat. Phys.* **6**, 311 (2010).
- [22] Extreme Light Infrastructure, <https://eli-laser.eu/>.
- [23] Vulcan, <http://spie.org/x103688.xml/>.
- [24] J. P. Zou *et al.*, Design and current progress of the Apollon 10 PW project, *High Power Laser Sci. Eng.* **3**, e2 (2015).
- [25] R. A. Fonseca, L. O. Silva, F. S. Tsung, V. K. Decyk, W. Lu, C. Ren, W. B. Mori, S. Deng, S. Lee, T. Katsouleas, and J. C. Adam, *Computational Science—ICCS 2002 Lecture Notes in Computer Science*, Vol. 2331 (Springer, Berlin, Heidelberg, 2002), p. 342351.
- [26] R. A. Fonseca, S. F. Martins, L. O. Silva, J. W. Tonge, F. S. Tsung, and W. B. Mori, One-to-one direct modeling of experiments and astrophysical scenarios: pushing the envelope on kinetic plasma simulations, *Plasma Phys. Controlled Fusion* **50**, 124034 (2008).
- [27] T. Grismayer, M. Vranic, J. L. Martins, R. A. Fonseca, and L. O. Silva, Seeded QED cascades in counterpropagating laser pulses, *Phys. Rev. E* **95**, 023210 (2017).
- [28] T. Grismayer, M. Vranic, J. L. Martins, R. A. Fonseca, and L. O. Silva, Laser absorption via quantum electrodynamics cascades in counter propagating laser pulses, *Phys. Plasmas* **23**, 056706 (2016).
- [29] M. Vranic, T. Grismayer, R. A. Fonseca, and L. O. Silva, Quantum radiation reaction in head-on laser-electron beam interaction, *New J. Phys.* **18**, 073035 (2016).
- [30] M. Vranic, T. Grismayer, R. A. Fonseca, and L. O. Silva, Electron-positron cascades in multiple-laser optical traps, *Plasma Phys. Controlled Fusion* **59**, 014040 (2017).
- [31] P. Chen and R. B. Palmer, Coherent pair creation as a positron source for linear colliders, *AIP Conf. Proc.* **279**, 888 (1992).
- [32] T. Katsouleas, J. J. Su, W. B. Mori, and J. M. Dawson, Plasma physics at the final focus of high-energy colliders, *Phys. Fluids B* **2**, 1384 (1990).
- [33] D. L. Burke, R. C. Field, G. Horton-Smith, J. E. Spencer, D. Walz, S. C. Berridge, W. M. Bugg, K. Shmakov, A. W. Weidemann, C. Bula, K. T. McDonald, E. J. Prebys, C. Bamber, S. J. Boege, T. Koffas, T. Kotseroglou, A. C. Melissinos, D. D. Meyerhofer, D. A. Reis, and W. Ragg, Positron Production in Multiphoton Light-by-Light Scattering, *Phys. Rev. Lett.* **79**, 1626 (1997).
- [34] A. Balzarini, R. A. Fonseca, J. Vieira, E. Boella, and L. Silva, Initialization of charged particle beam in OSIRIS, in *42nd European Physical Society Conference on Plasma Physics*, Portugal, 2015 (2015), P1.206, <http://ocs.ciemat.es/EPS2015ABS/pdf/P1.206.pdf>.
- [35] A. Di Piazza, M. Tamburini, S. Meuren, and C. H. Keitel, Implementing nonlinear Compton scattering beyond the local-constant-field approximation, *Phys. Rev. A* **98**, 012134 (2018).
- [36] H. Chen, F. Fiuza, A. Link, A. Hazi, M. Hill, D. Hoarty, S. James, S. Kerr, D. D. Meyerhofer, J. Myatt, J. Park, Y. Sentoku, and G. J. Williams, Scaling the Yield of Laser-Driven Electron-Positron Jets to Laboratory Astrophysical Applications, *Phys. Rev. Lett.* **114**, 215001 (2015).
- [37] G. Sarri *et al.*, Generation of neutral and high-density electron-positron pair plasmas in the laboratory, *Nat. Commun.* **6**, 6747 (2015).

- [38] I. Robinson, G. Gruebel, and S. Mochrie, Focus on x-ray beams with high coherence, *New J. Phys.* **12**, 035002 (2010).
- [39] A. Gonoskov, A. Bashinov, S. Bastrakov, E. Efimenko, A. Ilderton, A. Kim, M. Marklund, I. Meyerov, A. Muraviev, and A. Sergeev, Ultrabright GeV Photon Source via Controlled Electromagnetic Cascades in Laser-Dipole Waves, *Phys. Rev. X* **7**, 041003 (2017).
- [40] S. Chen, N. D. Powers, I. Ghebregziabher, C. M. Maharjan, C. Liu, G. Golovin, S. Banerjee, J. Zhang, N. Cunningham, A. Moorti, S. Clarke, S. Pozzi, and D. P. Umstadter, MeV-Energy X Rays from Inverse Compton Scattering with Laser-Wakefield Accelerated Electrons, *Phys. Rev. Lett.* **110**, 155003 (2013).
- [41] A. G. R. Thomas, C. P. Ridgers, S. S. Bulanov, B. J. Griffin, and S. P. D. Mangles, Strong Radiation-Damping Effects in a Gamma-Ray Source Generated by the Interaction of a High-Intensity Laser with a Wakefield-Accelerated Electron Beam, *Phys. Rev. X* **2**, 041004 (2012).
- [42] F. Albert and A. G. R. Thomas, Applications of laser wakefield accelerator-based light sources, *Plasma Phys. Controlled Fusion* **58**, 103001 (2016).
- [43] B. Martinez, E. d'Humières, and L. Gremillet, Synchrotron emission from nanowire array targets irradiated by ultra-intense laser pulses, *Plasma Phys. Controlled Fusion* **60**, 074009 (2018).
- [44] A. Benedetti, M. Tamburini, and C. H. Keitel, Giant collimated gamma-ray flashes, *Nat. Photonics* **12**, 319 (2018).
- [45] K. Poder *et al.*, Experimental Signatures of the Quantum Nature of Radiation Reaction in the Field of an Ultra-intense Laser, *Phys. Rev. X* **8**, 031004 (2018).
- [46] V. Yakimenko, S. Meuren, F. Del Gaudio, C. Baumann, A. Fedotov, F. Fiuza, T. Grismayer, M. J. Hogan, A. Pukhov, L. O. Silva, and G. White, On the prospect of studying nonperturbative QED with beam-beam collisions, [arXiv:1807.09271v2](https://arxiv.org/abs/1807.09271v2).
- [47] A. R. Bell and J. G. Kirk, Possibility of Prolific Pair Production with High-Power Lasers, *Phys. Rev. Lett.* **101**, 200403 (2008).
- [48] E. N. Nerush, I. Y. Kostyukov, A. M. Fedotov, N. B. Narozhny, N. V. Elkina, and H. Ruhl, Laser Field Absorption in Self-Generated Electron-Positron Pair Plasma, *Phys. Rev. Lett.* **106**, 035001 (2011).
- [49] V. F. Bashmakov, E. N. Nerush, I. Y. Kostyukov, A. M. Fedotov, and N. B. Narozhny, Effect of laser polarization on quantum electrodynamical cascading, *Phys. Plasmas* **21**, 013105 (2014).
- [50] M. Jirka, O. Klimo, S. V. Bulanov, T. Z. Esirkepov, E. Gelfer, S. S. Bulanov, S. Weber, and G. Korn, Electron dynamics and γ and e^-e^+ production by colliding laser pulses, *Phys. Rev. E* **93**, 023207 (2016).