

Exceeding

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N28a

Long Multiplication
Integers

1) $17 \times 32 = \underline{\hspace{2cm}}$

2) $24 \times 62 = \underline{\hspace{2cm}}$

3) $13 \times 156 = \underline{\hspace{2cm}}$

4) $528 \times 16 = \underline{\hspace{2cm}}$

5) $34 \times 466 = \underline{\hspace{2cm}}$

N28b

Long Multiplication
Decimals

$$1) \quad 1.5 \times 22 = \underline{\hspace{2cm}}$$

$$2) \quad 7.6 \times 2.1 = \underline{\hspace{2cm}}$$

$$3) \quad 4.5 \times 9.99 = \underline{\hspace{2cm}}$$

$$4) \quad 19.7 \times 6.3 = \underline{\hspace{2cm}}$$

$$5) \quad 0.35 \times 0.12 = \underline{\hspace{2cm}}$$

N28b

Long Multiplication Decimals

- 1) Work out what the $*$ must be.

a)

$$\begin{array}{r}
 1 * 5 \\
 \times * 2 \\
 \hline
 * 7 0 \\
 1 3 5 0 \\
 \hline
 * * * 0
 \end{array}$$

b)

\times	$**$	3
80	4800	$***$
$*$	120	6

answer: $* * * *$

c)

$$\begin{array}{r}
 4 * \\
 \times 7 \\
 \hline
 3 * 3 \\
 * 9 0 \\
 \hline
 * * 3
 \end{array}$$

d)

\times	$* 0$	$*$
$***$	$*****$	$***$
40	$**00$	$***$
$*$	450	25

answer: 13775

- 2) A school organises a trip to a museum.

They set off in 13 minibuses, each minibus containing 24 pupils who will each pay to go into the museum.

Entrance to the museum costs £1.20 per person.

- How many people made the trip?
- What was the total cost?

N29a

Long Division
Integers

$$1) \quad 288 \div 12 = \underline{\hspace{2cm}}$$

$$2) \quad 285 \div 15 = \underline{\hspace{2cm}}$$

$$3) \quad 425 \div 25 = \underline{\hspace{2cm}}$$

$$4) \quad 784 \div 56 = \underline{\hspace{2cm}}$$

$$5) \quad 874 \div 38 = \underline{\hspace{2cm}}$$

N29b

Long Division
Decimals

$$1) \ 79.2 \div 22 = \underline{\hspace{2cm}}$$

$$2) \ 5.89 \div 19 = \underline{\hspace{2cm}}$$

$$3) \ 9.87 \div 47 = \underline{\hspace{2cm}}$$

$$4) \ 330.2 \div 13 = \underline{\hspace{2cm}}$$

$$5) \ 42.624 \div 16 = \underline{\hspace{2cm}}$$

- 1) a) If 48 luxurious pens cost £768,
how much would one of them cost?

b) If 25 tee shirts cost £77.50,
how much would one of them cost?

c) If 53 mobile phones cost £2119.47,
how much would one of them cost?

- 2) Cans of juice cost 24p each.

Wendy has £8.65 to spend.

a) What is the maximum number of cans Wendy
can buy?

b) How much change does she get?

- 3) Find the missing digits.

a)

$$\begin{array}{r} 3 \square \\ \hline 14 \overline{) \square 0 4} \end{array}$$

b)

$$\begin{array}{r} 2 \square \\ \hline \square 2 \overline{) 2 \square 2} \end{array}$$

N30a/b

Prime Numbers
Introduction and Factorisation

- 1) Write down the first 9 prime numbers.

- 2) Write down the first prime number that comes after 62.

- 3) Split up the following numbers into the product of their prime factors.

a) 12	d) 120
b) 45	e) 550
c) 72	f) 1296

- 4) Find the Highest Common Factor (HCF) of the following numbers.

a) 4 and 6	d) 300 and 525
b) 8 and 16	e) 374 and 918
c) 36 and 48	f) 45, 90 and 105

N31 a/b

Highest Common Factor
Lowest Common Multiple

- 1) Find the Highest Common Factor (HCF) of the following numbers.
 - a) 4 and 6
 - b) 8 and 16
 - c) 36 and 48
 - d) 300 and 525
 - e) 374 and 918
 - f) 45, 90 and 105

- 2) Find the Lowest Common Multiple (LCM) of the following numbers.
 - a) 8 and 12
 - b) 30 and 45
 - c) 15 and 18
 - d) 4, 6 and 8
 - e) 24 and 84
 - f) 72 and 96

- 3) The bells at Kings School ring every 6 minutes.
At Queens School the bells ring every 5 minutes.
At Princess School the bells ring every 9 minutes.
All three bells ring together at 8.30 am.
When is the next time the bells of the three schools will ring together?

N32

Decimals, Fractions and Percentages

1) Complete the tables.

a)

Fraction	Decimal	Percentage
		50%
	0.25	
$\frac{1}{10}$		
$\frac{1}{3}$		
	0.7	
		40%

b)

Fraction	Decimal	Percentage
$\frac{68}{100}$		
		35%
	0.6	
	$0.\dot{6}$	
		5%
$\frac{13}{50}$		

2) Put these fractions, decimals and percentages in order, smallest to largest.

- a) $\frac{1}{2}$, 49%, $\frac{3}{5}$, 0.55
- b) 27%, 0.2, $\frac{1}{4}$, $\frac{3}{10}$
- c) $\frac{9}{10}$, 95%, 0.99, $\frac{97}{100}$
- d) $\frac{1}{3}$, 0.6, $\frac{2}{3}$, 30%
- e) 0.125, 10%, $\frac{11}{100}$, 0.09

3) Chris says that $\frac{3}{4}$ is halfway between 0.5 and 100%.

Is Chris correct? You must explain your answer.

4) Emily says that 0.2 is halfway between 10% and $\frac{3}{5}$.

Is Emily correct? You must explain your answer.

N33

Fraction of an Amount

1) Find the following:

a) $\frac{1}{3}$ of 24

b) $\frac{2}{3}$ of 24

c) $\frac{1}{5}$ of 30

d) $\frac{3}{5}$ of 30

e) $\frac{1}{8}$ of 40

f) $\frac{5}{8}$ of 40

2) Work out:

a) $\frac{7}{10}$ of £30

b) $\frac{3}{7}$ of £84

c) $\frac{4}{5}$ of £1.50

d) $\frac{11}{20}$ of £19

e) $\frac{2}{9}$ of £10.98

f) $\frac{8}{13}$ of £31.85

3) Julie has £4.50 pocket money every week.

If she spends $\frac{2}{5}$ of it on a magazine and $\frac{1}{3}$ of it on a dance lesson, how much of the pocket money does she have left?

4) Paul has £7.80 pocket money each week.

He always saves $\frac{1}{3}$ of it.

With the remaining money he spends $\frac{5}{8}$ on comics and the rest on sweets.

(i) How much does he save?

(ii) How much is spent on comics?

(iii) How much does he spend on sweets?

N33

Fraction of an Amount

- 1) a) Find $\frac{1}{2}$ of $\left(\frac{2}{3} \text{ of } 60\right)$
b) Find $\frac{3}{4}$ of $\left(\frac{1}{2} \text{ of } 80\right)$
c) Find $\frac{1}{2}$ of $\frac{4}{9}$ of $\frac{3}{4}$ of 42

- 2) a) If $\frac{3}{4}$ of a number is 60, what is the number?
b) If $\frac{3}{7}$ of a number is 21, what is the number?
c) If $\frac{4}{9}$ of a number is 12.3, what is the number?

- 3) If $\frac{1}{2}$ of $\frac{1}{5}$ of a number is 6, what is the number?

- 4) If $\frac{1}{2}$ of $\frac{1}{3}$ of $\frac{1}{4}$ of $\frac{1}{5}$ of a number is 2.5, what is the number?

- 5) If $\frac{3}{5}$ of $\frac{1}{2}$ of $\frac{2}{3}$ of a number is 3.8, what is the number?

N34

Ordering Fractions

- 1) Put the following fractions in order of size starting with the smallest.

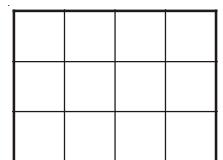
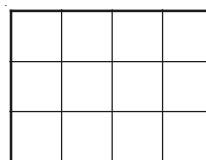
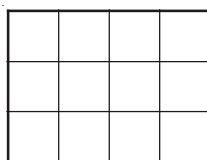
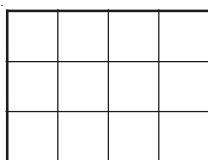
You can use the grids to help if you wish.

$$\frac{3}{4}$$

$$\frac{5}{6}$$

$$\frac{2}{3}$$

$$\frac{7}{12}$$



- 2) Put the following fractions in order of size starting with the smallest.

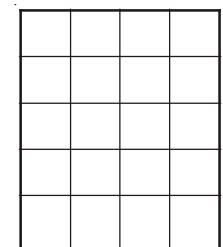
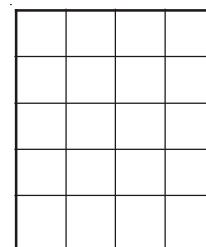
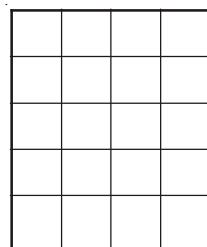
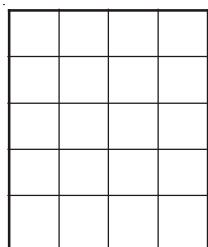
You can use the grids to help if you wish.

$$\frac{13}{20}$$

$$\frac{3}{5}$$

$$\frac{3}{4}$$

$$\frac{7}{10}$$



- 3) Put the following fractions in order of size starting with the smallest.

$$\frac{7}{12}$$

$$\frac{1}{2}$$

$$\frac{5}{8}$$

$$\frac{13}{24}$$

- 4) Put the following fractions in order of size starting with the smallest.

$$\frac{2}{5}$$

$$\frac{3}{10}$$

$$\frac{1}{3}$$

$$\frac{1}{6}$$

N34

Ordering Fractions

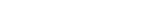
Place the fractions on the cards in order of size from smallest to largest.

Smallest

$\frac{2}{3}$

$\frac{17}{30}$

$\frac{2}{5}$



Largest

$\frac{9}{20}$

$\frac{1}{2}$

$\frac{47}{60}$

$\frac{1}{3}$

$\frac{7}{15}$

$\frac{15}{24}$

$\frac{3}{4}$

$\frac{3}{8}$

$\frac{7}{12}$



N35

Improper Fractions Mixed Numbers

1) Convert the following improper fractions to mixed numbers.

a) $\frac{5}{4}$

f) $\frac{25}{3}$

b) $\frac{8}{3}$

g) $\frac{30}{7}$

c) $\frac{12}{7}$

h) $\frac{75}{8}$

d) $\frac{20}{9}$

i) $\frac{47}{12}$

e) $\frac{16}{5}$

j) $\frac{100}{9}$

2) Convert the following mixed numbers to improper fractions.

a) $1\frac{3}{5}$

f) $10\frac{1}{9}$

b) $2\frac{1}{4}$

g) $7\frac{5}{8}$

c) $5\frac{2}{3}$

h) $9\frac{4}{5}$

d) $3\frac{3}{5}$

i) $6\frac{3}{11}$

e) $11\frac{2}{7}$

j) $12\frac{3}{4}$

3) Put these numbers in order, lowest to highest.

a) $3.5, 3\frac{1}{5}, \frac{11}{3}$

b) $7\frac{1}{4}, 7.14, \frac{34}{5}$

c) $1\frac{1}{10}, 98\%, \frac{5}{4}, 1$

Fractions

N36 Adding and Subtracting

- 1) Work out the following, simplifying your answers where possible.

a) $\frac{2}{7} + \frac{3}{7} = \frac{\square}{7}$

e) $\frac{1}{6} + \frac{2}{3} = \frac{\square}{18} + \frac{\square}{18} =$

b) $\frac{3}{8} + \frac{1}{8} =$

f) $\frac{1}{6} + \frac{2}{3} = \frac{\square}{6} + \frac{\square}{6} =$

c) $\frac{7}{9} - \frac{2}{9} = \frac{\square}{9}$

g) $\frac{4}{5} - \frac{1}{2} =$

d) $\frac{5}{10} - \frac{1}{10} =$

h) $\frac{14}{15} - \frac{3}{5} = \frac{\square}{15} - \frac{\square}{15} =$

- 2) Work out the following, simplifying your answers where possible.

a) $\frac{3}{8} + \frac{4}{8} =$

f) $\frac{5}{6} - \frac{1}{4} =$

b) $\frac{9}{11} - \frac{5}{11} =$

g) $\frac{5}{12} + \frac{1}{6} =$

c) $\frac{1}{2} + \frac{1}{3} =$

h) $\frac{4}{5} - \frac{1}{10} =$

d) $\frac{5}{7} - \frac{3}{5} =$

i) $\frac{3}{8} + \frac{1}{2} =$

e) $\frac{1}{2} + \frac{2}{5} =$

j) $\frac{8}{9} - \frac{5}{6} =$

- 3) Write the missing numbers in each of these fraction sums.

a) $\frac{1}{3} + \frac{\square}{6} = 1$

b) $\frac{3}{7} + \frac{12}{\square} = 1$

c) $\frac{8}{5} - \frac{\square}{15} = 1$

d) $\frac{15}{\square} - \frac{1}{4} = 1$

N37a/b

Fractions - Multiplying and Dividing an Integer

1) Work out the following, giving your answers in their simplest forms

a) $3 \times \frac{1}{4}$

e) $4 \times \frac{4}{9}$

b) $7 \times \frac{1}{7}$

f) $10 \times \frac{3}{8}$

c) $2 \times \frac{4}{5}$

g) $\frac{8}{9} \times 6$

d) $9 \times \frac{1}{3}$

h) $\frac{2}{15} \times 3$

2) Work out the following, giving your answers in their simplest forms

a) $\frac{1}{2}$ of £40

e) $\frac{2}{5}$ of 30 cm

b) $\frac{1}{5}$ of 20 km

f) $\frac{7}{8}$ of £16

c) $\frac{1}{4}$ of 120 kg

g) $\frac{4}{7}$ of 7000 g

d) $\frac{1}{9}$ of £99

h) $\frac{3}{4}$ of £500

3) Work out the following, giving your answers in their simplest forms

a) $3 \div \frac{1}{4}$

e) $10 \div \frac{2}{3}$

b) $7 \div \frac{1}{2}$

f) $8 \div \frac{4}{5}$

c) $12 \div \frac{1}{3}$

g) $3 \div \frac{5}{7}$

d) $9 \div \frac{1}{5}$

h) $15 \div \frac{2}{3}$

4) An industrial machine takes $\frac{3}{4}$ of an hour to produce a very special tool.

How long would it take the machine to produce 12 of the tools?

5) A road is 20 km long. Road signs are to be installed every $\frac{2}{3}$ of a kilometre. How many signs will be needed?

N38

Rounding Significant Figures

1) Round the following to 1 significant figure.

- a) 478 cm
- b) 450 cm
- c) 449 cm
- d) 12761 m
- e) 28481 km

2) Round the following to 1 significant figure.

- a) 673.8 cm
- b) 4017.9 kg
- c) 246.83 m
- d) £45.38
- e) 20482.1 kg

3) Round the following to 1 significant figure.

- a) 0.26 ml
- b) 0.043 g
- c) 0.0671 m
- d) 0.000256 km
- e) 0.3822 m

4) Round the following to 1 significant figure.

- a) 962 m
- b) 0.923 cm
- c) 0.971 cm
- d) 0.096 km
- e) 0.00985 km

5) Round the following to 1 significant figure.

- a) £631428
- b) 0.00573 g
- c) £3614.68
- d) 0.493 ml
- e) £968

Percentages

N39a Change to a Percentage



1) Change the following to percentages:

- a) 83 out of 100
- b) 24 out of 50
- c) 9 out of 25
- d) 7 out of 20
- e) 6 out of 10
- f) 72 out of 200
- g) 12 out of 40
- h) 36 out of 60



2) Nas scores 24 out of 60 in a test.

What is his percentage score?



3) Change the following to percentages, giving your answers to 1 decimal place:

- a) 7 out of 24
- b) 35 out of 41
- c) 92 out of 143



4) Jamie scores 48 out of 70 in his Science test and 38 out of 52 in his Maths test.

He says, "I did better in Science because 48 is a higher score than 38."

Is he correct? Explain your answer.

N39b Percentages Comparing Quantities



- 1) A supermarket does a taste-test of cola.
40 people try cola A, 26 people like it.
50 people try cola B, 32 people like it.
Which cola was liked by the higher percentage of people?
You must show your working.



- 2) Leon does a spelling test and a times tables test.
He scores 7 out of 20 in the spelling test and 9 out of 25 in the times tables test.
In which test did he get the higher percentage score?
You must show your working.



- 3) In a survey carried out in the year 2000, 50 000 people were asked if they had a mobile phone. 26 000 did.
In a similar survey, carried out in the year 2014, 33 000 people were asked if they had a mobile phone. 22 000 did.
In which year did the higher percentage of people own a mobile phone?
You must show your working.

A16

Trial and Improvement

- 1) Using a trial and improvement method,
solve the equation $x^2 - x = 56$
You must show ALL your working.

- 2) Using a trial and improvement method,
solve the equation $x^2 + 4x = 21$
You must show ALL your working.

- 3) Using a trial and improvement method,
solve the equation $x^3 + 2x = 72$
You must show ALL your working.

- 4) Using a trial and improvement method,
solve the equation $x^3 - 3x = 110$
You must show ALL your working.

A17

Forming and Solving Basic equations

- 1) Using the statement: "*I think of a number, double it, and subtract 1. I get 7.*"
 - a) Form an equation.
 - b) Solve the equation to find the number that was thought of.

- 2) Using the statement: "*I think of a number, multiply it by 7, and add 3. I get 80.*"
 - a) Form an equation.
 - b) Solve the equation to find the number that was thought of.

- 3) Using the statement: "*I think of a number, multiply it by 2, divide the result by 3 and then subtract 5. I get 5.*"
 - a) Form an equation.
 - b) Solve the equation to find the number that was thought of.

A18

Expanding Brackets Harder Questions

1) Expand and simplify

- a) $(x + 2)(x + 2)$
- b) $(x + 3)(x + 5)$
- c) $(x + 7)(x + 1)$
- d) $(x + 4)(x + 3)$
- e) $(x + 7)(x + 2)$

2) Expand and simplify

- a) $(2x + 1)(3x + 2)$
- b) $(4x + 3)(2x + 1)$
- c) $(3x + 4)(3x + 2)$
- d) $(5x + 2)(5x + 7)$
- e) $(2x + 10)(2x + 4)$

3) Expand and simplify

- a) $(x + 5)(x - 3)$
- b) $(x - 2)(x + 4)$
- c) $(x - 6)(x - 2)$
- d) $(x + 7)(x + 3)$
- e) $(x - 8)(x - 2)$

4) Expand and simplify

- a) $(2x - 1)(3x + 4)$
- b) $(5x - 2)(3x - 1)$
- c) $(3x + 4)(2x - 3)$
- d) $(5x - 1)(5x - 2)$
- e) $(4x + 2)(3x - 5)$

5) Expand and simplify

- a) $(x + 5)^2$
- b) $(x - 2)^2$
- c) $(2x + 3)^2$
- d) $(3x - 1)^2$
- e) $(4x + 3)^2$

Solving Harder Equations

A19a/b

1) Solve the following

- a) $2x + 3 = 19$
- b) $3x - 2 = 13$
- c) $5x - 1 = 9$
- d) $3 + 2x = 23$
- e) $12 - 3x = 9$

2) Solve the following

- a) $2(3x - 1) = 22$
- b) $3(x + 7) = 18$
- c) $4(5x - 2) = 12$
- d) $66 = 6(2x + 3)$
- e) $20 = 5(x - 6)$

3) Solve the following

- a) $\frac{x-6}{2} = 3$
- b) $\frac{x+8}{3} = 5$
- c) $\frac{2x-1}{3} = 5$
- d) $\frac{6x+1}{2} = 8$
- e) $\frac{7x-3}{5} = 5$

4) Solve the following

- a) $2x + 7 = x + 12$
- b) $4x - 5 = 2x + 3$
- c) $7x + 2 = 3x + 26$
- d) $6x - 7 = 4x - 5$
- e) $3x + 4 = x - 7$

5) Solve the following

- a) $x - 6 = 2x - 13$
- b) $3x + 4 = 5x - 8$
- c) $4x + 17 = x - 4$
- d) $5 - 2x = x - 7$
- e) $2x - 1 = 14 - 3x$

6) Solve the following

- a) $2(3x - 1) = 4x + 7$
- b) $3(x + 4) = 2(x - 5)$
- c) $5(2x - 3) = 3(3x + 4)$
- d) $2(2x - 1) = 5(2x - 4)$
- e) $2(2x + 3) = 5(x + 3)$

7) Solve the following

- a) $\frac{2(x+1)}{3} = 6$
- b) $\frac{4(2x-3)}{5} = 4$
- c) $\frac{2(4x-5)}{3} = x + 10$
- d) $\frac{3(5x+4)}{2} = 7x - 8$
- e) $4 - x = \frac{2(x+7)}{3}$

A20a

Inequalities Introduction

- 1) Represent the inequalities on the number lines.

a) $x \leq 3$



b) $-1 < x \leq 4$



c) $-3 \leq x \leq 3$

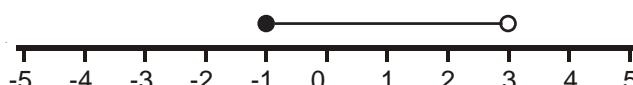


- 2) Write down the inequalities shown below

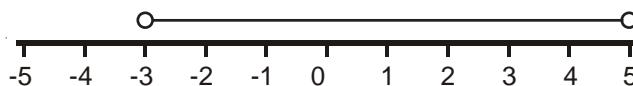
a)



b)



c)



- 3) If x is an integer, what are the possible values of x ?

a) $-4 \leq x \leq 2$

b) $-3 \leq x < 1$

c) $1 < x \leq 5$

d) $-3 < x \leq 4$

e) $-7 \leq x \leq -4$

A20b

Inequalities Solving

1) Solve

- a) $2x - 1 \geq 7$
- b) $3x + 4 < 19$
- c) $5x - 7 \leq 18$
- d) $2x + 9 > 5$
- e) $4x + 11 \leq 14$

2) Solve

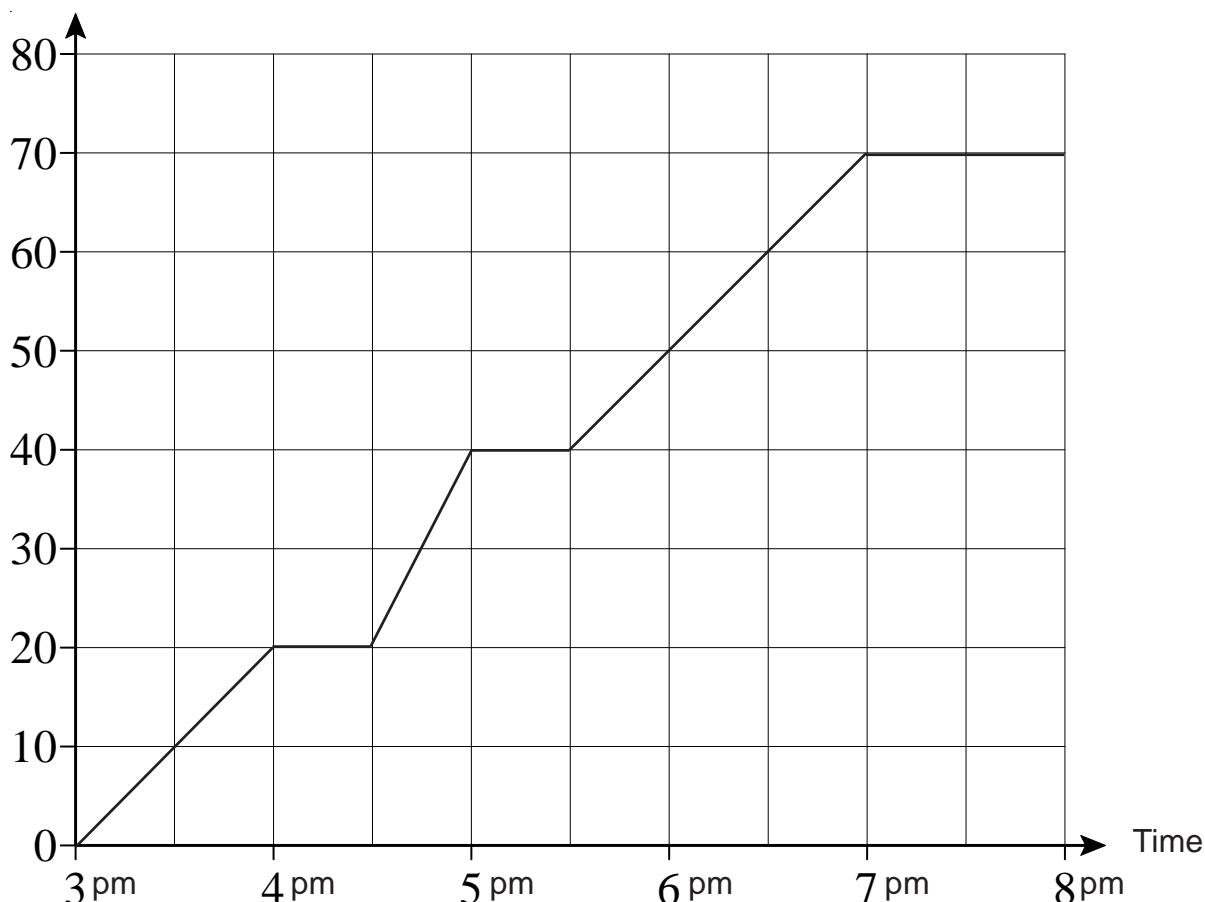
- a) $\frac{x}{3} < 7$
- b) $\frac{x}{5} - 1 \geq 3$
- c) $\frac{2x}{3} + 4 \leq 9$
- d) $12 \geq 2x - 1$
- e) $20 < 5 + 5x$

3) Solve

- a) $2(5x - 1) \leq 18$
- b) $3(4x + 2) > 60$
- c) $42 > 2(6x + 15)$
- d) $4(1 + x) \leq 12$
- e) $8(2x - 1) > 12$

4) Solve

- a) $2x + 7 \leq x + 9$
- b) $x - 6 > 3x - 18$
- c) $4x + 3 < 2x - 9$
- d) $2x - 4 \geq 7x - 34$
- e) $2(x + 3) < x - 1$

A21a**Real-Life Graphs**
Distance-TimeDistance
in miles

The graph, above, shows Jade's journey by scooter from her house to university with some stops along the way.

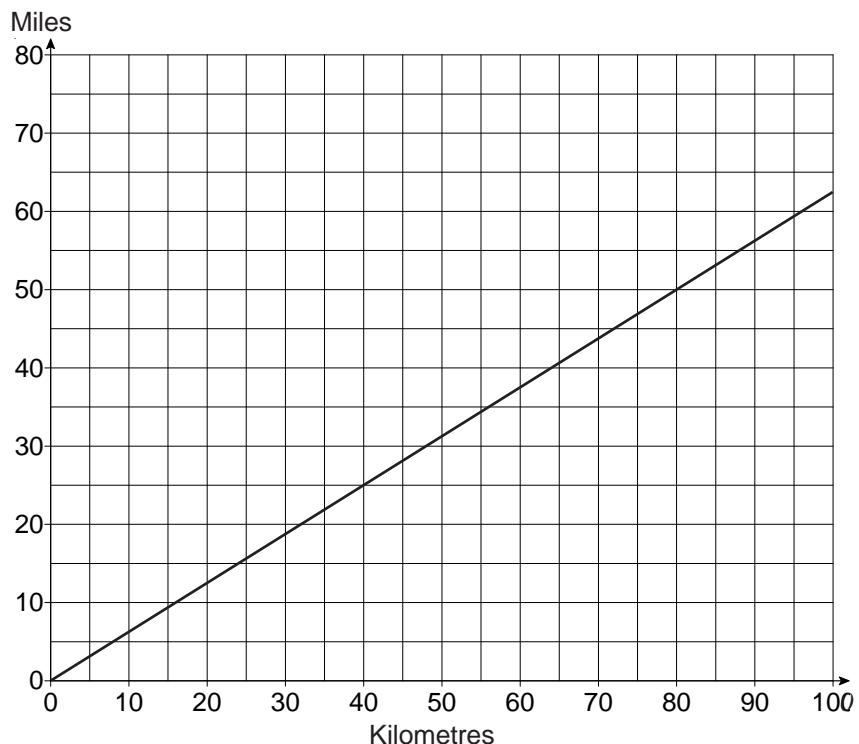
- How long did the journey take?
- How many breaks did Jade take throughout her journey?
- At what time did Jade take her first break?
- How long did the first break last?
- What was Jade's average speed between 3 pm and 4 pm?
- What was Jade's average speed between 4.30 pm and 5 pm?
- What was Jade's average speed between 5.30 pm and 7 pm?

A21b

Real-Life Graphs Other Types

- 1) Use the conversion graph below to convert :

- a) 80 km to miles
- b) 35 miles to km
- c) 40 km to miles
- d) 60 miles to km
- e) 100 miles to km
- f) 140 km to miles



- 2) The graph below shows three different mobile phone tariffs.

Tariff 1

Pay as you go
50p per minute.

Tariff 2

£15 per month and
30p per minute

Tariff 3

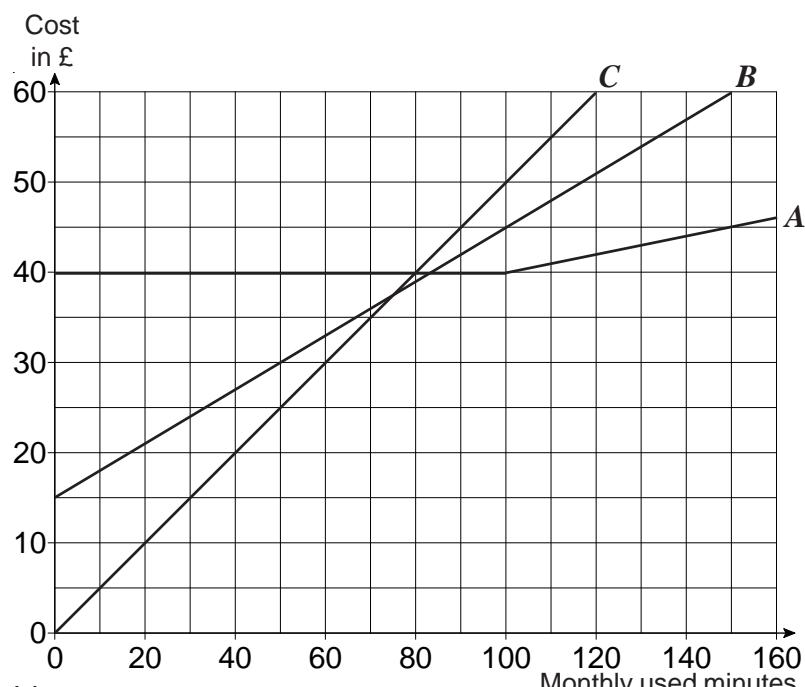
£40 per month,
100 free minutes then
10p per minute

- a) Match each tariff with its graph, A, B or C

- b) Every month, James needs about 90 mins talk time.

Work out which tariff would be best for him. Explain your answer.

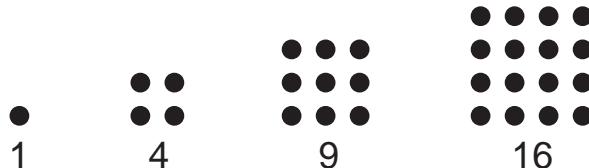
- c) Tariff 4 is announced. This is £10 per month, 40 free minutes then 30p per minute. Draw a line on the graph to show this tariff.



A22

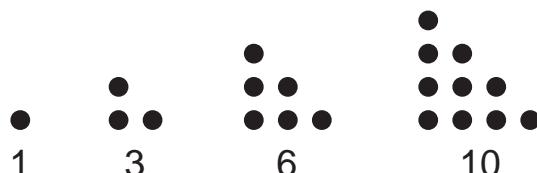
Special Sequences

- 1) Here is a pattern of square numbers:



What are the next two numbers in the pattern?

- 2) Here is the pattern of triangular numbers:



What are the next three numbers in the pattern?

- 3) Here is part of a Fibonacci sequence:

$$5, 8, 13, 21, 34$$

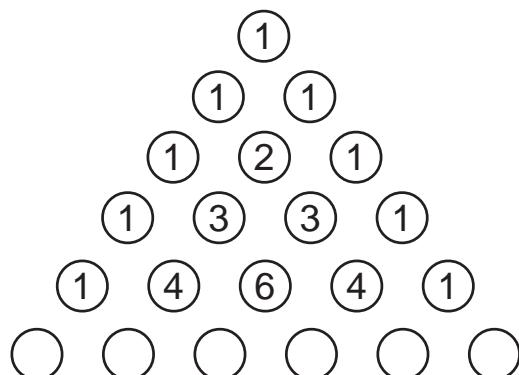
What are the next three numbers in the sequence?

- 4) Here is part of a number pattern:

$$3, 4, 6, 9, 13$$

What are the next three numbers in the pattern?

- 5) Can you work out a rule and fill in the bottom row?



A23a/b

Quadratic Sequences

- 1) Find the n th term of
 - a) 1, 4, 9, 16, 25,
 - b) 2, 5, 10, 17, 26,
 - c) 0, 3, 8, 15, 24,

- 2) Find the n th term of
 - a) 1, 4, 9, 16, 25,
 - b) 2, 8, 18, 32, 50,
 - c) 0.5, 2, 4.5, 8, 12.5,

- 3) Find the n th term of
 - a) 3, 9, 19, 33, 51,
 - b) 1, 7, 17, 31, 49,
 - c) 11, 41, 91, 161, 251,

- 4) For the following n th terms,
find the first three terms and the tenth term
 - a) $n^2 + 4$
 - b) $n^2 - 3$
 - c) $n^2 + 10$
 - d) $n^2 + 2n$
 - e) $n^2 - n$

- 5) For the following n th terms,
find the first three terms and the tenth term
 - a) $4n^2$
 - b) $2n^2 + 3n$
 - c) $3n^2 - 2n$
 - d) $n^2 + n + 1$
 - e) $2n^2 + 4n - 3$

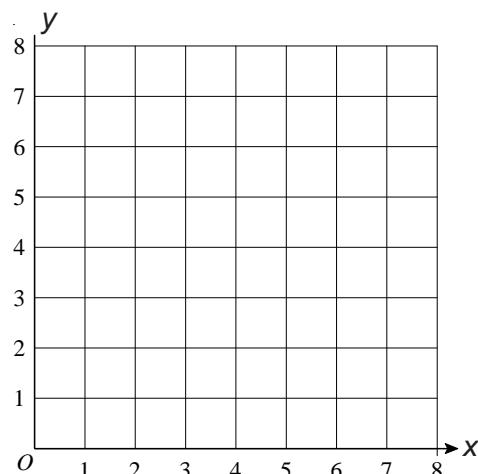
Simultaneous Equations

A24a/b

- 1) a) Complete the table of values for $y = x + 2$
- b) Draw the graph of $y = x + 2$
- c) Complete the table of values for $x + y = 7$
- d) Draw the graph of $x + y = 7$
- e) Use your graph to solve the simultaneous equations $y = x + 2$ and $x + y = 7$

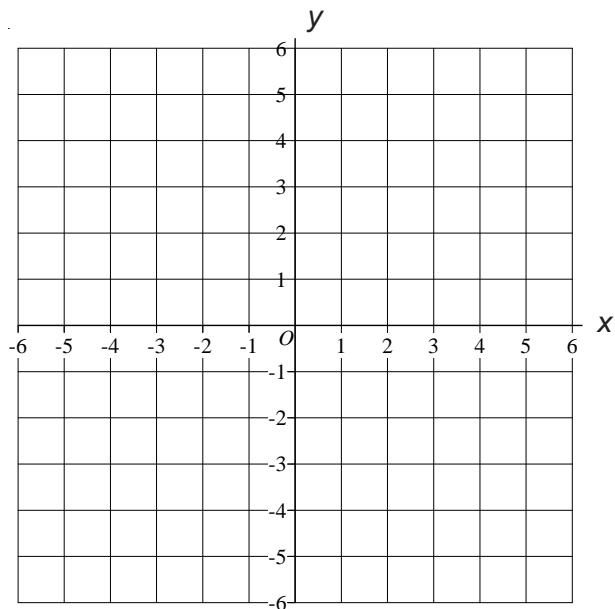
x	0	1	2	3	4
y					

x	0	1	2	3	4
y					



- 2) Using a graphical method, solve the simultaneous equations

$$y = 2x - 3 \text{ and } y = 6 - x$$



- 3) Solve the simultaneous equations $y = x + 6$ and $y = 3 - x$
- 4) Solve the simultaneous equations $y = x - 14$ and $y = 2 - 3x$

R9a Increase/Decrease by a Percentage - Basics

- 1) Describe how you would increase a number by 10%.
- 2) Describe how you would decrease a number by 10%.
- 3) Increase the following numbers by 10%

a) 40	e) 75
b) 140	f) 505
c) 810	g) 12
d) 320	h) 123
- 4) Decrease the following numbers by 10%

a) 20	e) 25
b) 160	f) 445
c) 80	g) 13
d) 190	h) 7
- 5) Work out the following:

a) Increase £400 by 5%	e) Increase 250 m by 50%
b) Decrease £120 by 15%	f) Decrease £820 by 75%
c) Decrease 500 km by 20%	g) Increase 60 kg by 60%
d) Increase 96 kg by 10%	h) Decrease £26 by 35%
- 6) A shop is having a sale and all prices are reduced by 25%.
 - a) Work out the sale price of an item normally priced at £18.40
 - b) Work out the sale price of an item normally priced at £99

Increase/Decrease R9b by a Percentage - Multiplier

- 1) a) Increase £400 by 16%
b) Increase £750 by 24%
c) Increase £2000 by 38%
d) Increase £14500 by 19%
e) Increase £16.50 by 30%

- 2) a) Decrease £700 by 32%
b) Decrease £36 by 14%
c) Decrease £1970 by 40%
d) Decrease £3000 by 12.5%
e) Decrease £3124 by 16.25%

- 3) A sports shop reduces the price of all its trainers by 15% in the Spring sale.
Before the sale, one pair of trainers cost £74.
How much are they after the reduction?

- 4) Tim took up weightlifting.
In his first session he could bench-press 45 kg.
Four weeks later he could bench-press 22% more.
How much could he now lift to the nearest kg?

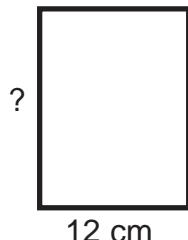
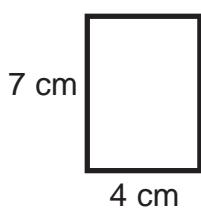
- 5) If a manager of a shop reduces the price of a £1500 piano by 15% and then, four weeks later, increases the reduced price by 15%, how much does it now cost?

R10Scale Factors
Similar Shapes

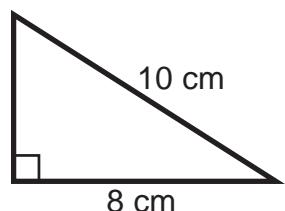
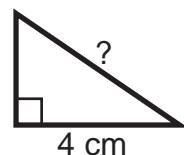
- 1) In each of the following questions, the two shapes are mathematically similar.

Work out the lengths of the missing sides.

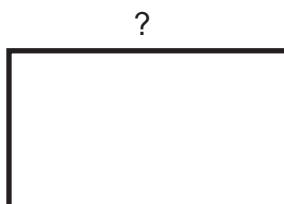
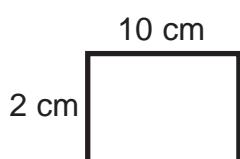
a)



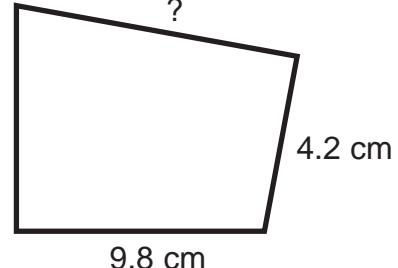
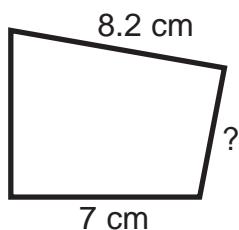
b)



c)

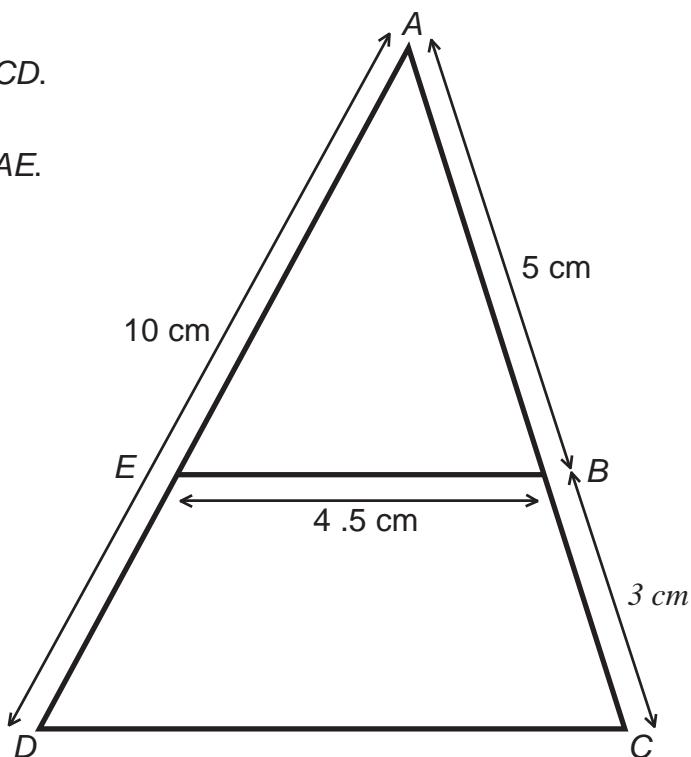


d)



- 2) a) Work out the length of CD .

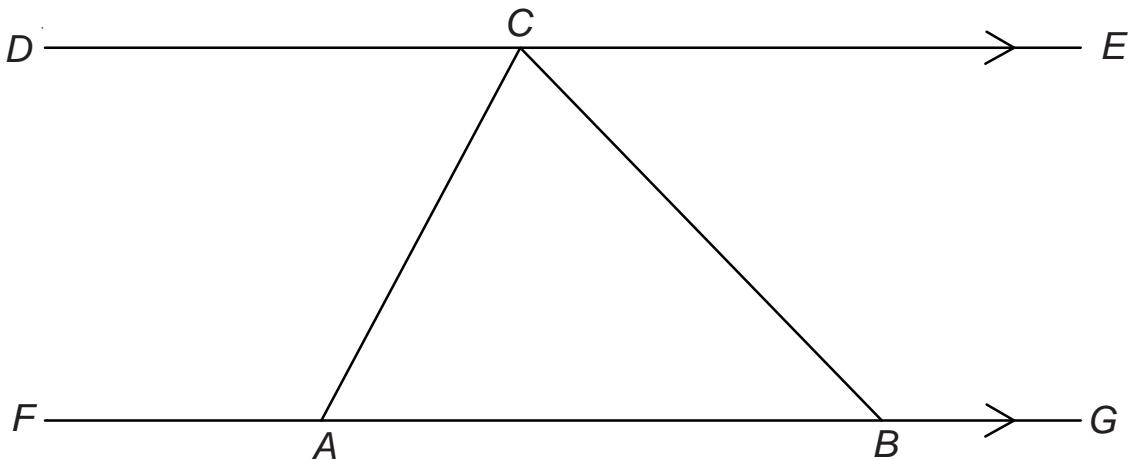
- b) Work out the length of AE .



G23

Angles in a Triangle Proof

Fill in the missing parts:



Angle DCA is equal to angle CAB because they are _____

Angle ECB is equal to angle CBA because they are _____

Angle _____ is in triangle ABC and on straight line DCE .

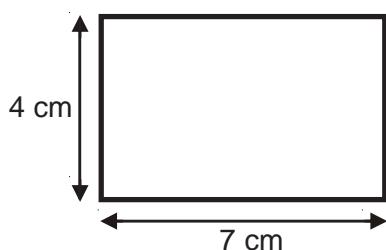
Angles DCA , ACB , and ECB lie on a straight line so they must add up to ____°

Therefore, angles CAB , CBA , and ACB must also add up to ____°

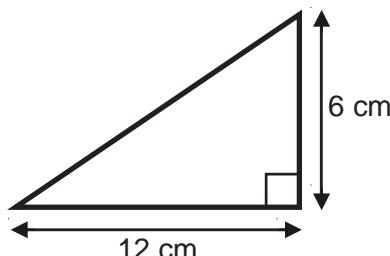
The angles in a _____ add up to ____°

1) Find the areas of the following shapes:

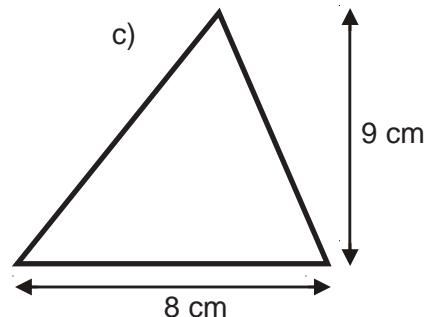
a)



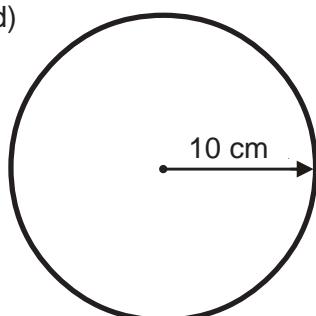
b)



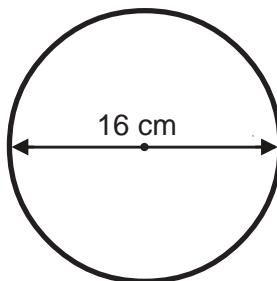
c)



d)



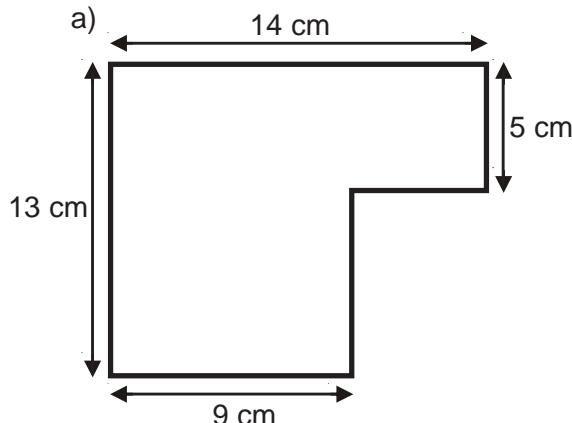
e)



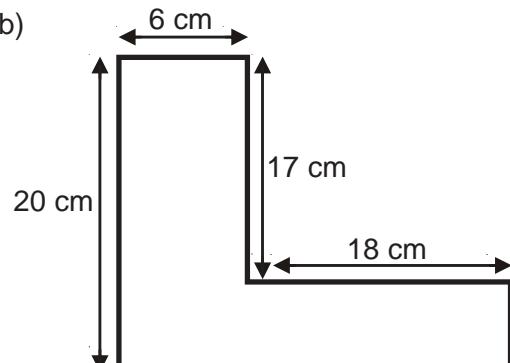
Take π to be 3.142

2) Find the areas of the following shapes:

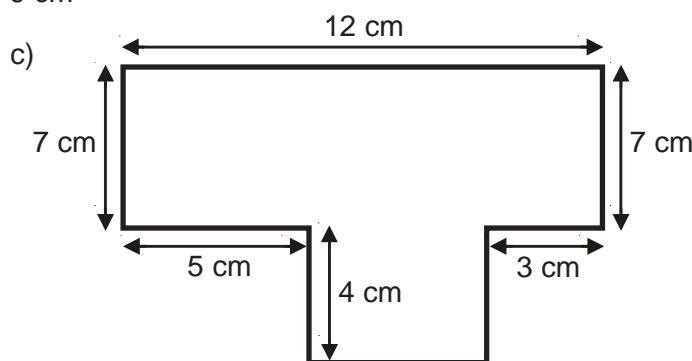
a)



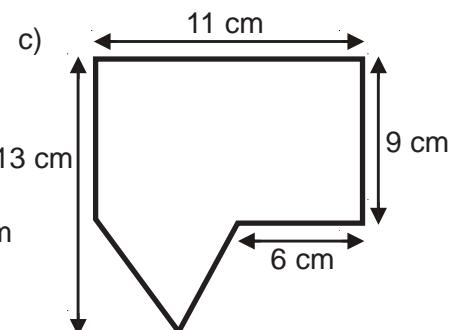
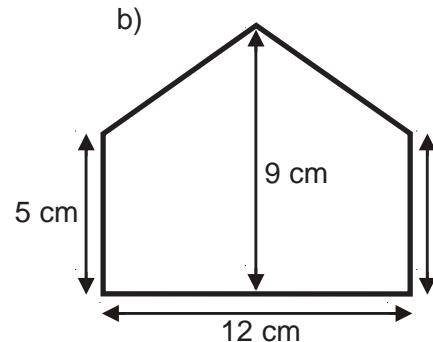
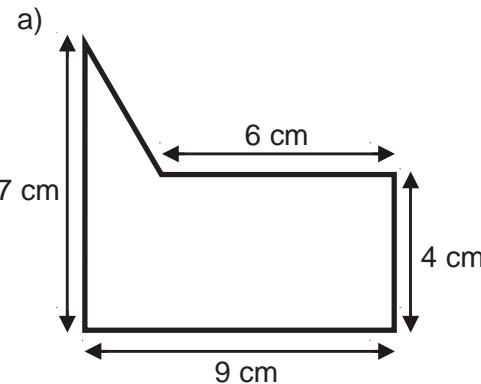
b)



c)

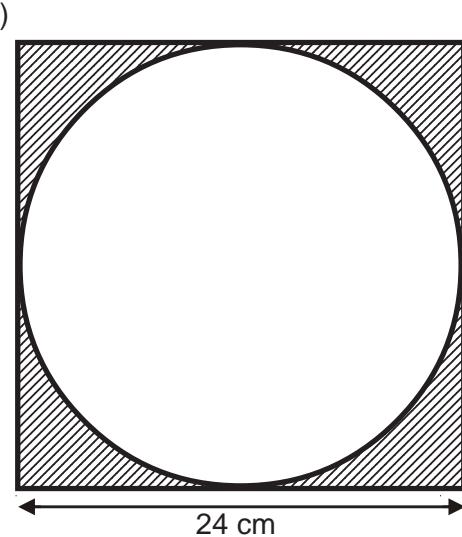
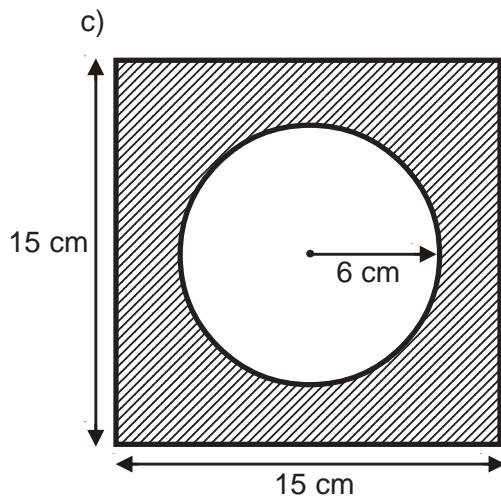
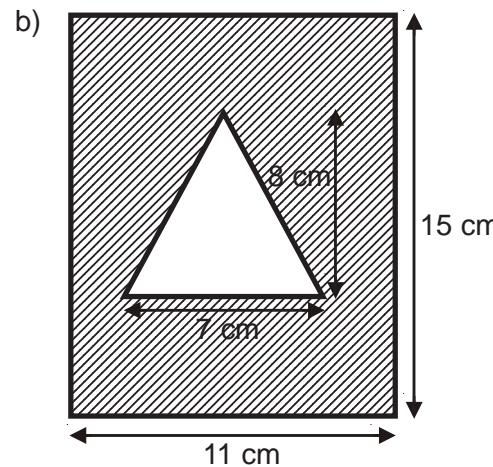
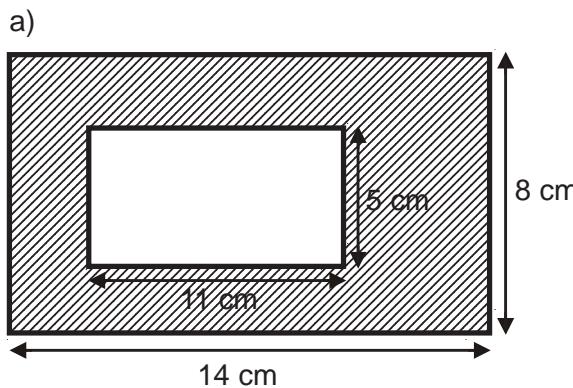


1) Find the areas of the following shapes:



2) Find the areas of the shaded parts of the following:

Take π to be 3.142 when needed.



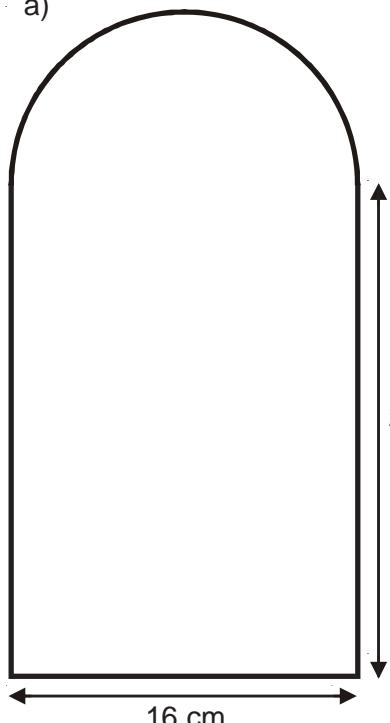
G24

Area Composite Shapes

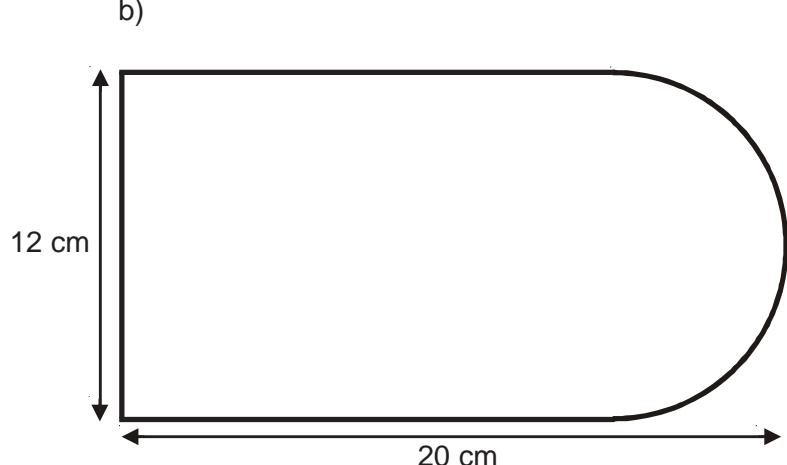
Find the areas of the shapes below:

Take π to be 3.142

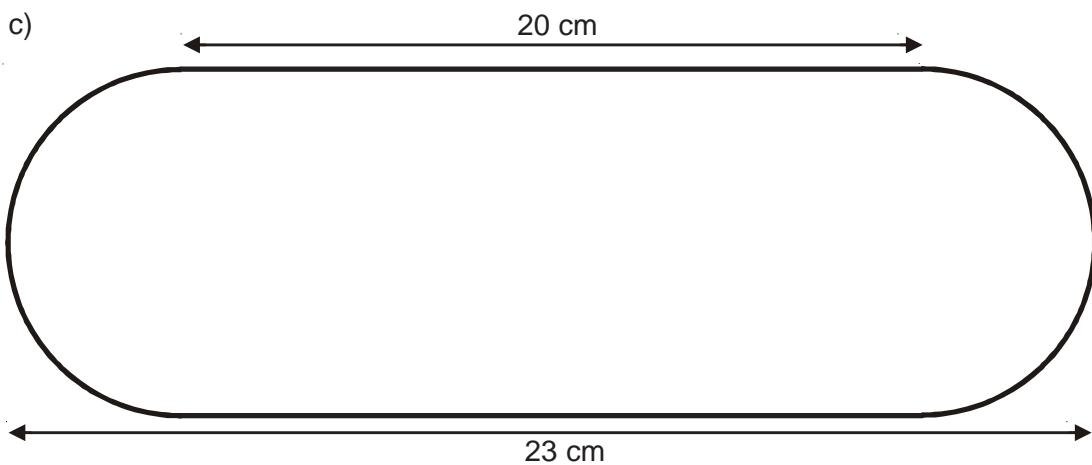
a)



b)



c)



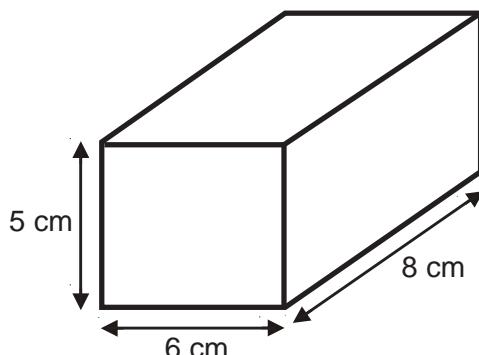
G25a

Prisms Volume

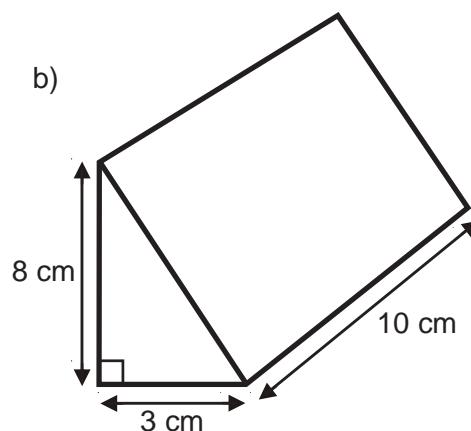
Find the volumes of the prisms, below.

Take π to be 3.142 for questions c and d.

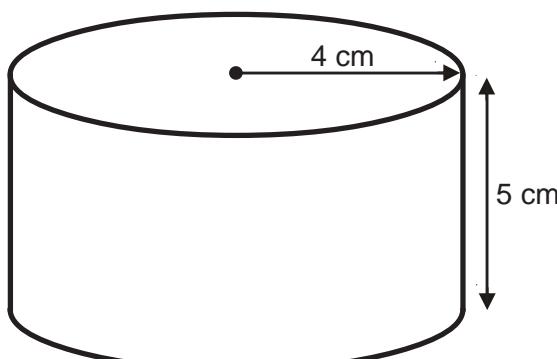
a)



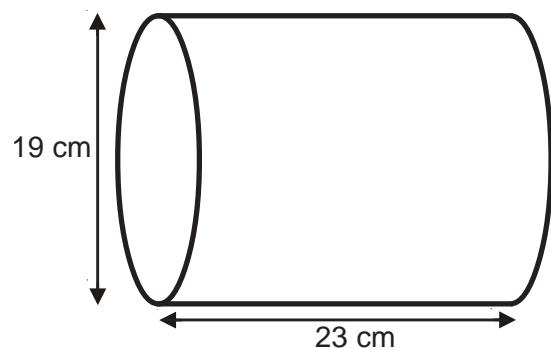
b)



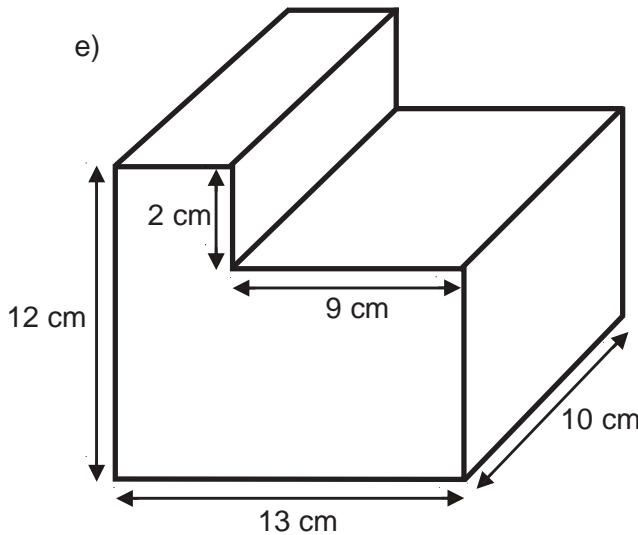
c)



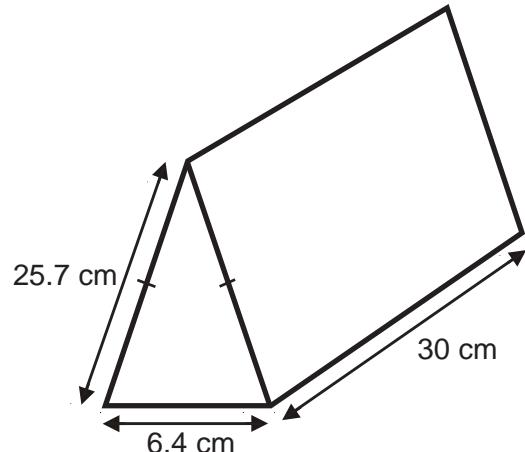
d)



e)

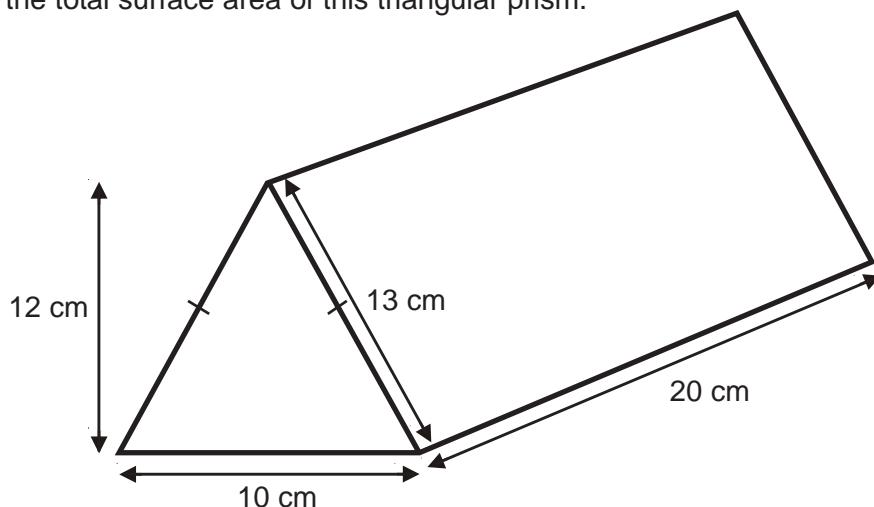


f)

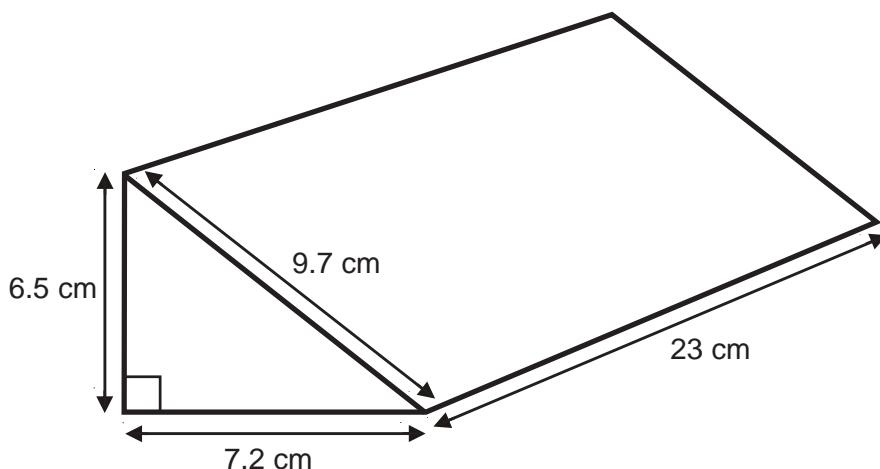


G25bPrisms
Surface Area

- 1) Find the total surface area of this triangular prism.

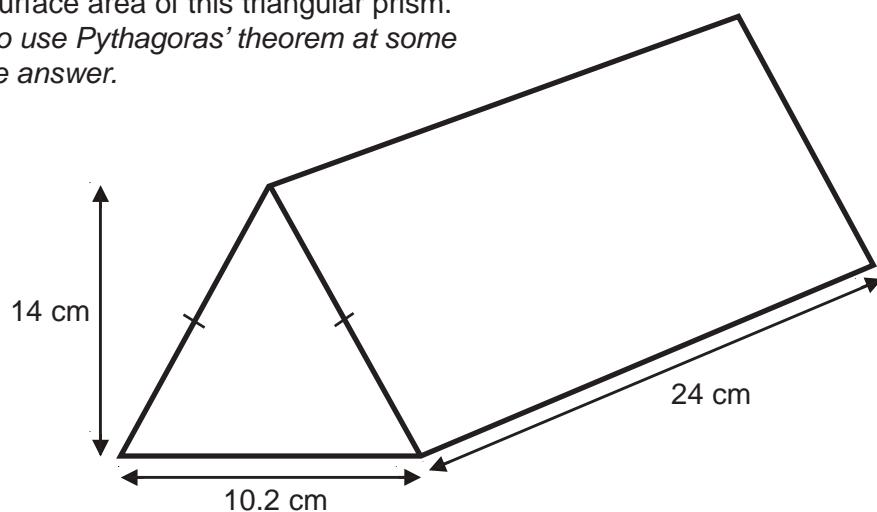


- 2) Find the total surface area of this triangular prism.



- 3) Find the total surface area of this triangular prism.

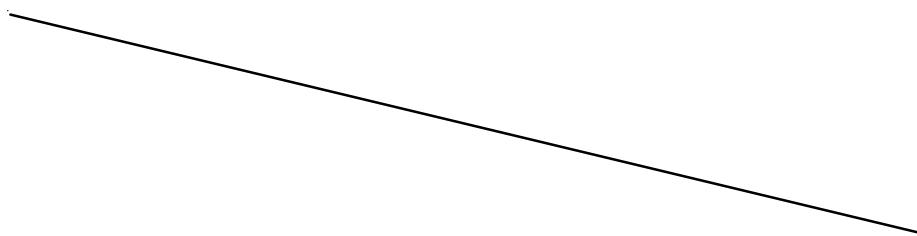
You will need to use Pythagoras' theorem at some stage to get the answer.



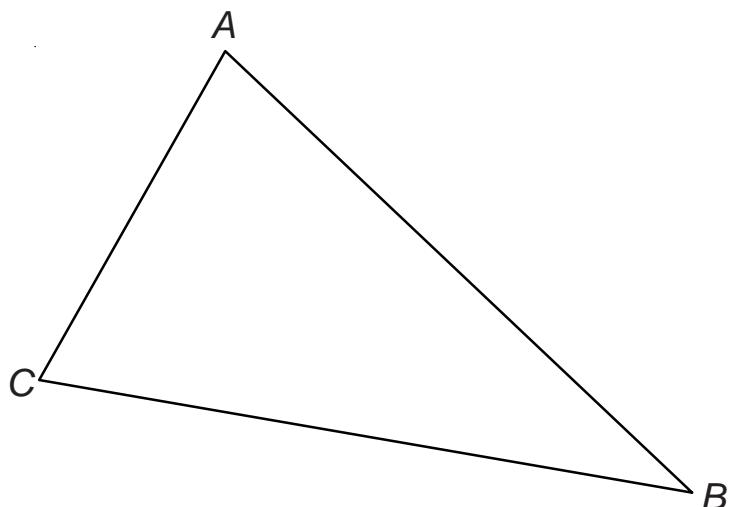
G26a

Constructions Bisecting a Line

- 1) Use compasses and a ruler to bisect this line.



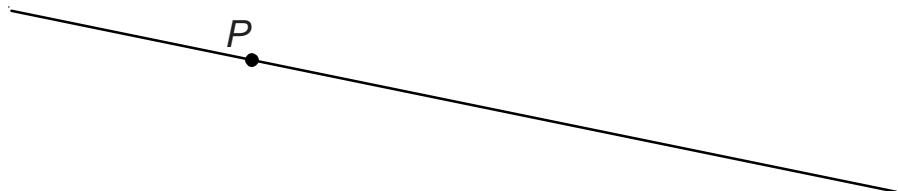
- 2) Using compasses and a ruler
 - a) Bisect lines AB , BC and AC .
 - b) Place your compass point where your three lines cross and open them out until your pencil is touching A .
Draw a circle.



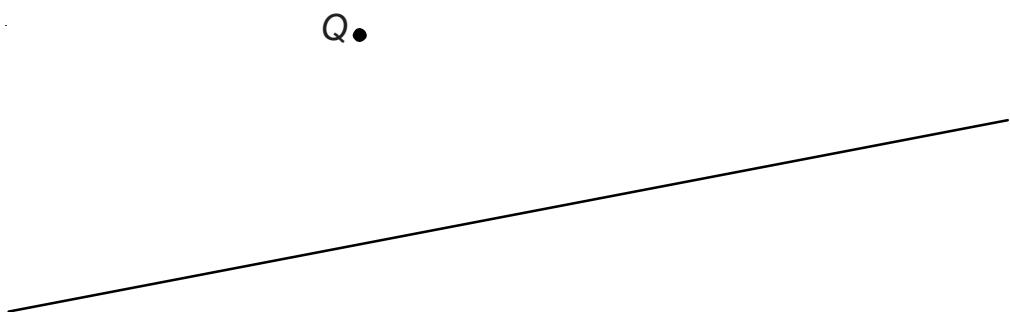
G26b

Constructions Perpendiculars

- 1) Using compasses and a ruler, construct a perpendicular to the line at the point P .

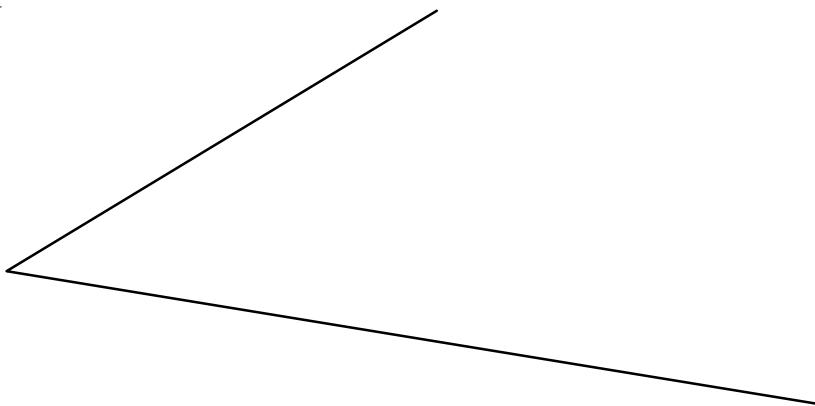


- 2) Using compasses and a ruler, construct a perpendicular to the line from the point Q .

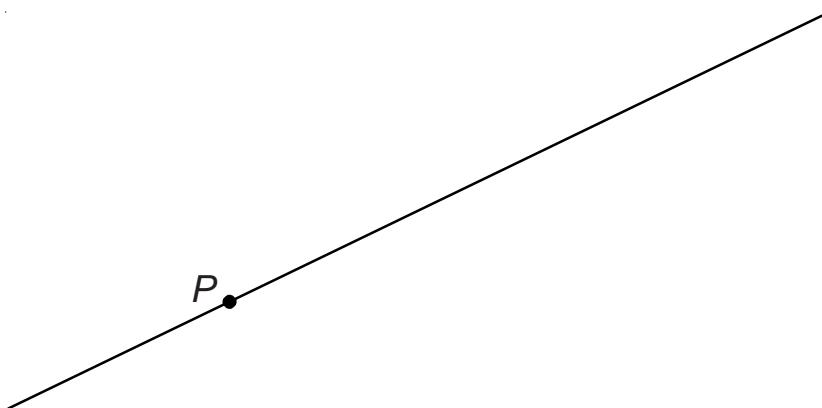


G26c Constructions Bisecting an Angle

- 1) Using compasses and a ruler, bisect this angle.



- 2) Using compasses and a ruler,
 - a) Construct a perpendicular to the line at the point P .



- b) Bisect the angle where your perpendicular meets line AB .
 - c) What size is the angle you have just constructed?

G27

Loci

- 1) Draw the locus of all the points that are 1.2 cm away from the line AB .



- 2) Draw the locus of all the points that are 1.5 cm away from the rectangle $ABCD$.



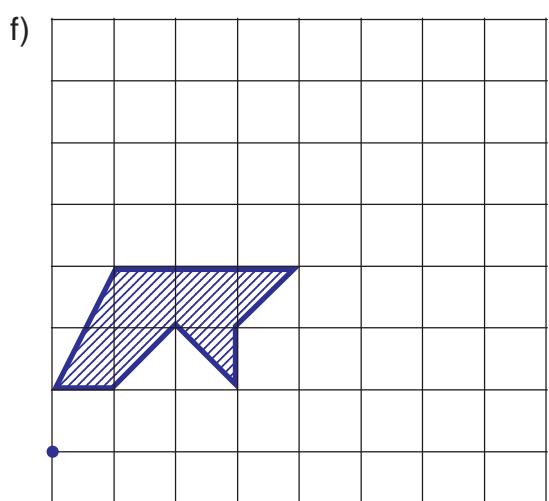
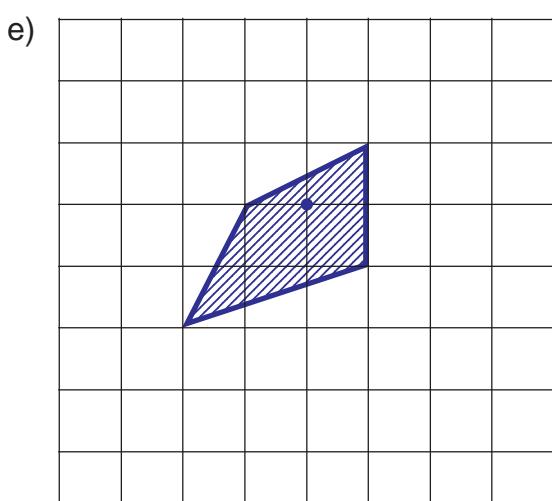
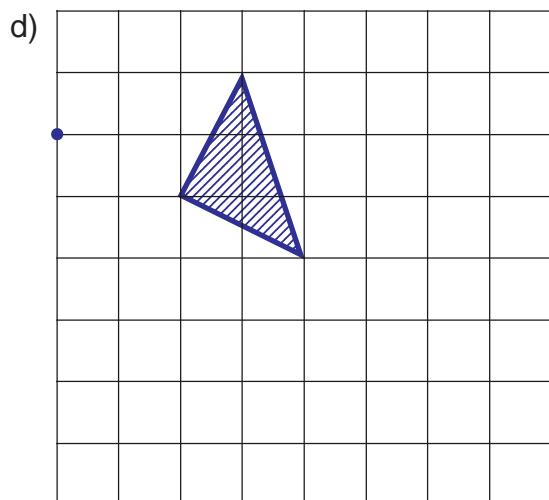
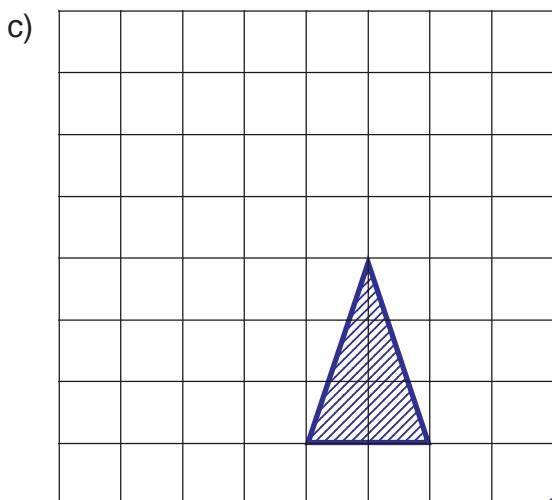
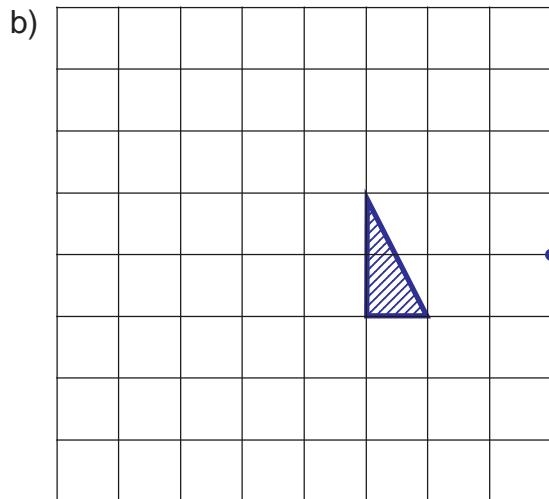
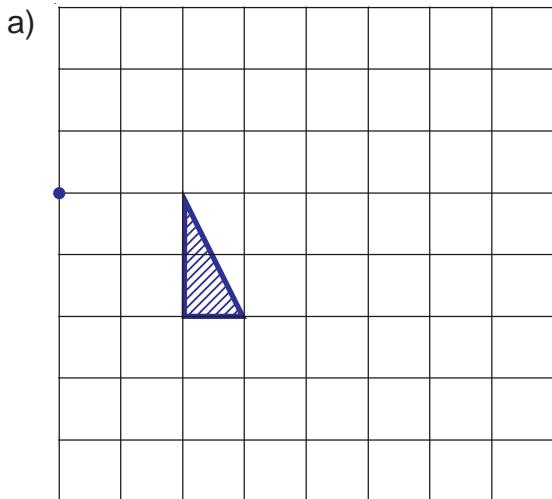
- 3) Radio signals can be heard within a 4.5 km radius of transmitter A and a 5.5 km radius of transmitter B. Show, by shading, the area where radio signals can be heard from both transmitters at the same time. *Use a scale of 1 cm represents 1 km.*

A

B

G28 Enlargement

Enlarge the following shapes with scale factor 2, using the dot as the centre of enlargement.

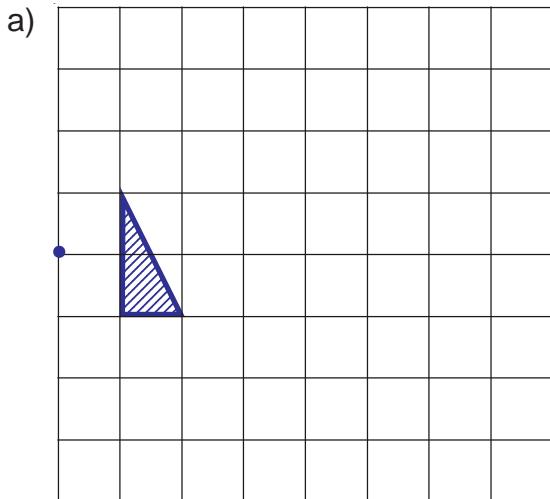


G28

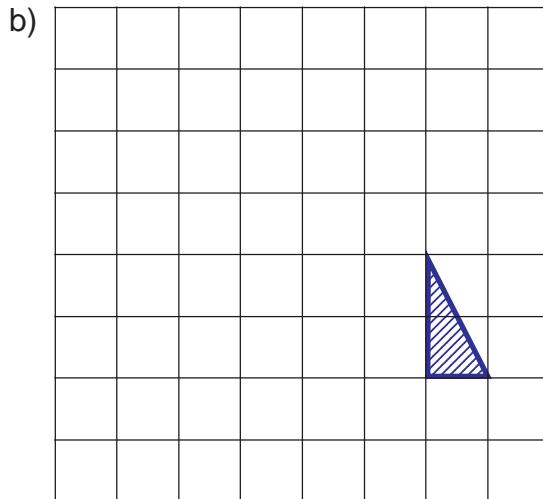
Enlargement

- 1) Enlarge the following shapes using the dots as the centres of enlargement.

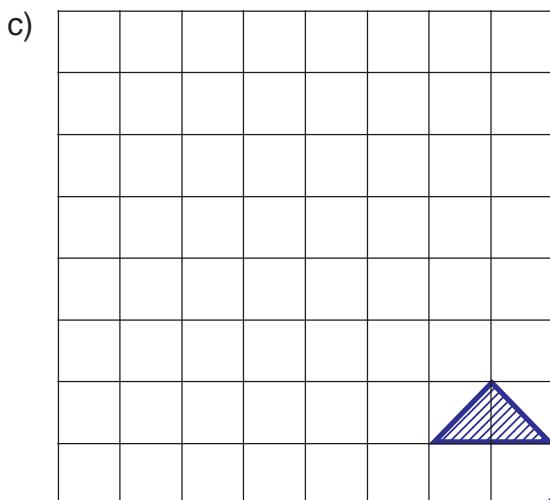
Scale factor 3



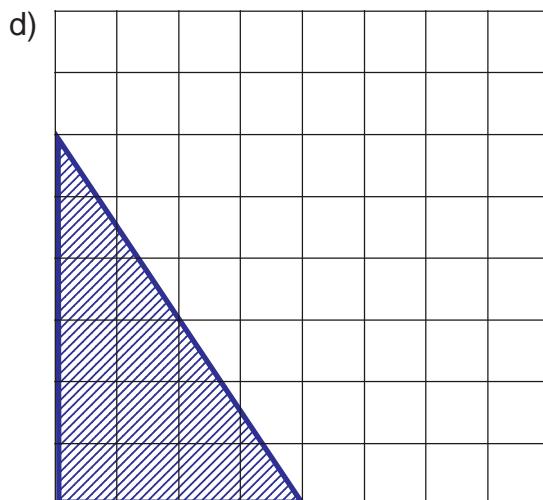
Scale factor 3



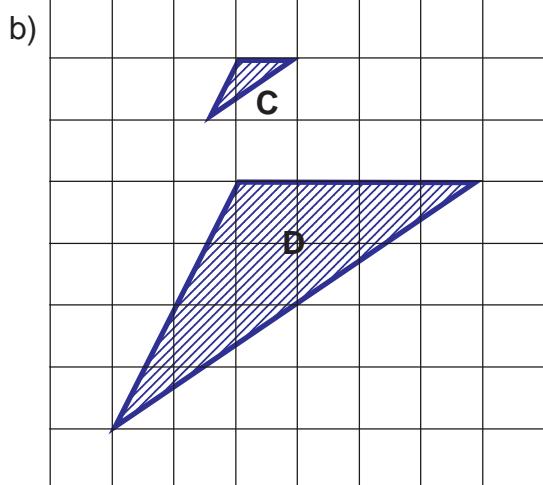
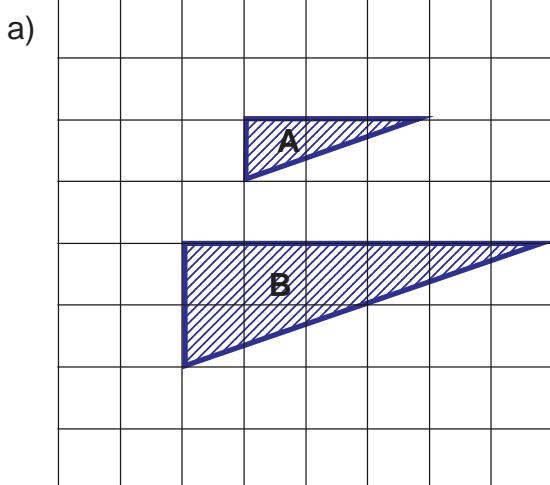
Scale factor 4



Scale factor 0.5



- 2) Use dots to mark on the grids the positions of the centres of enlargement.



G29

Bounds

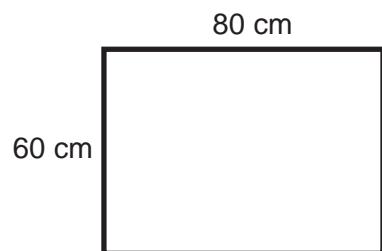
- 1) The length of a bracelet is 24 cm measured to the nearest centimetre.
 - a) Work out the lower bound of the length of the bracelet.
 - b) Work out the upper bound of the length of the bracelet.

- 2) The length of a snake is 80 cm measured to the nearest 10 centimetres.
 - a) Work out the lower bound of the length of the snake.
 - b) Work out the upper bound of the length of the snake.

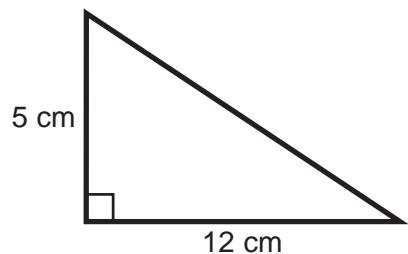
- 3) The weight of a necklace is 145 g measured to the nearest 5 grams.
 - a) Work out the lower bound of the weight of the necklace.
 - b) Work out the upper bound of the weight of the necklace.

- 4) The length of a line is given as 17.2 cm measured to the nearest tenth of a centimetre.
 - a) Work out the lower bound of the length of the line.
 - b) Work out the upper bound of the length of the line.

- 5) A rectangle has a length of 80 cm and a width of 60 cm, both measured to the nearest 10 cm.
 - a) Work out the lower bound of the area of the rectangle.
 - b) Work out the upper bound of the perimeter of the rectangle.



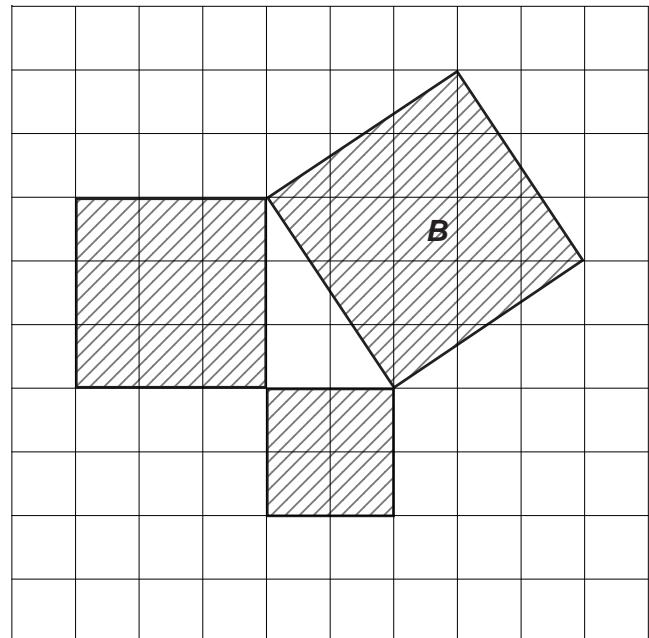
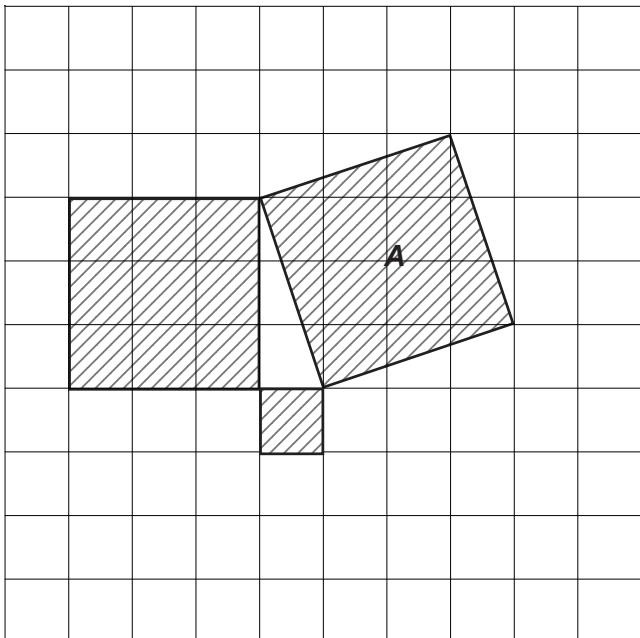
- 6) A right-angled triangle has lengths as shown, all measured to the nearest centimetre.
 - a) Work out the lower bound of the area of the triangle.
 - b) Work out the upper bound of the area of the triangle.



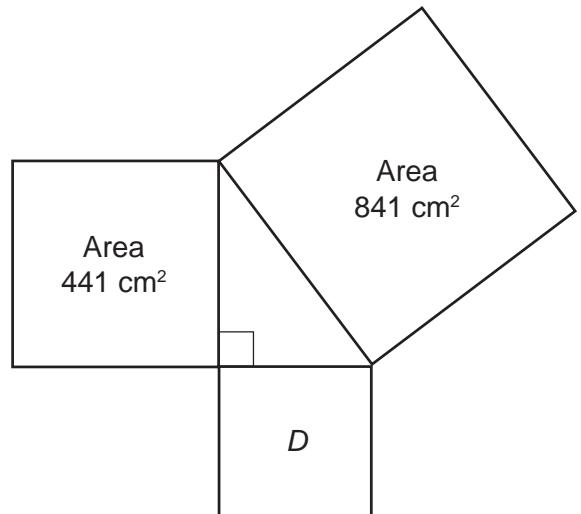
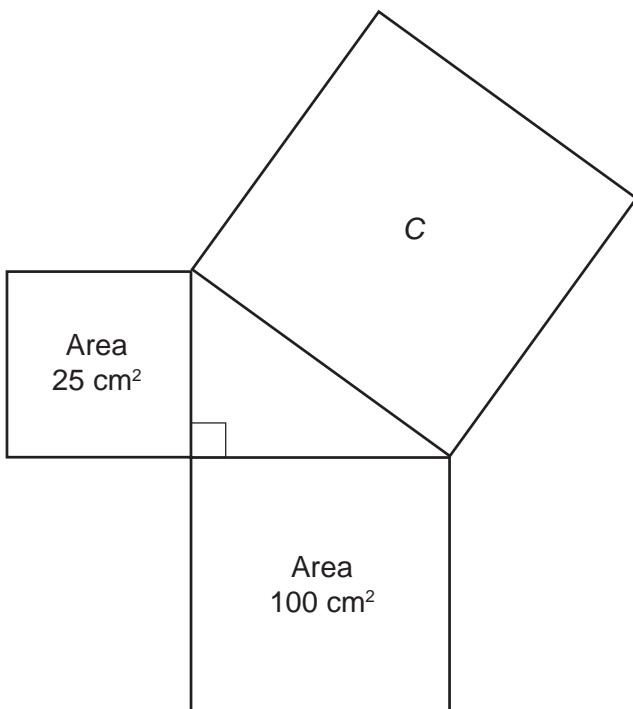
G30

Pythagoras

- 1) Use Pythagoras' theorem to work out the areas of squares *A* and *B*.



- 2) Use Pythagoras' theorem to work out the areas of squares *C* and *D*.



G30

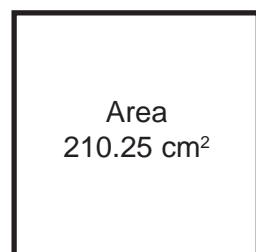
Pythagoras

- 1) Find the lengths of the sides of these three squares.

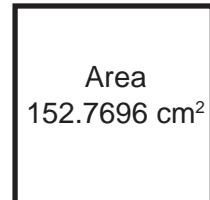
a)



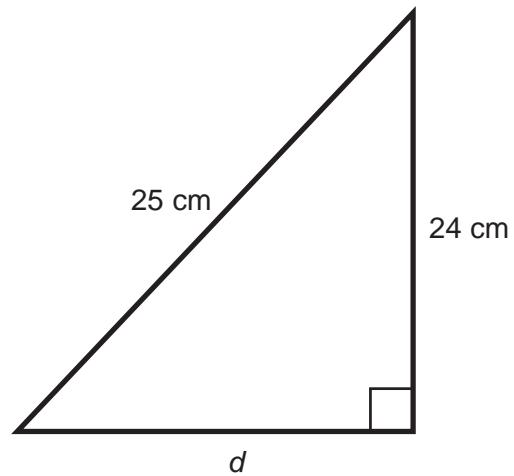
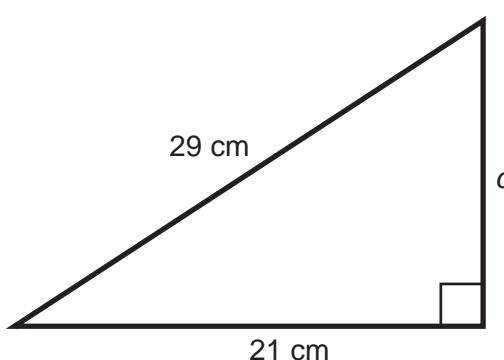
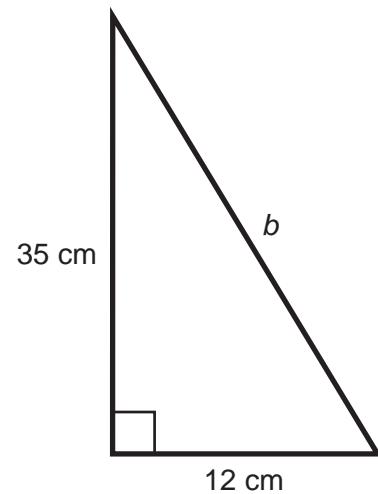
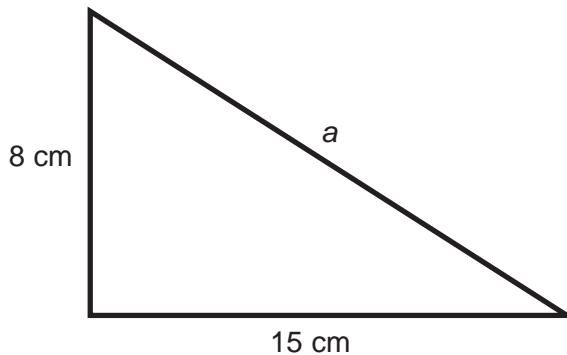
b)



c)



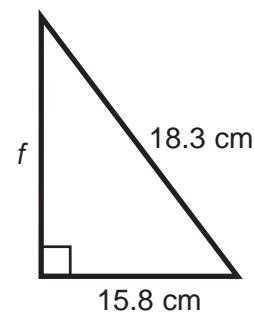
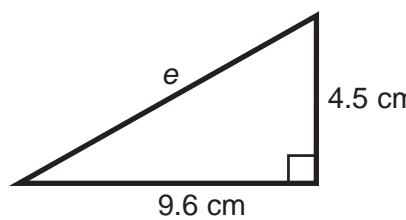
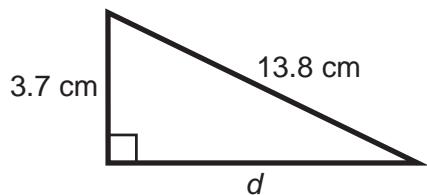
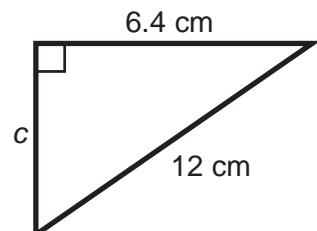
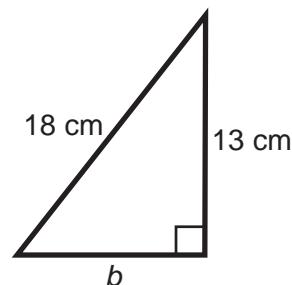
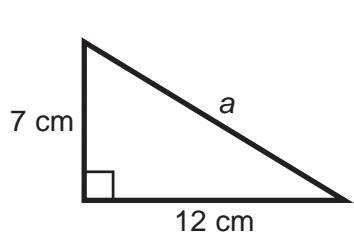
- 2) Find the lengths of the sides labelled a to d.



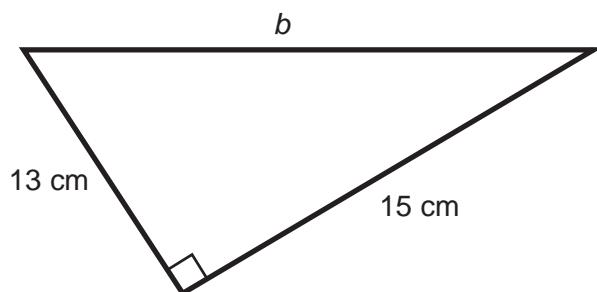
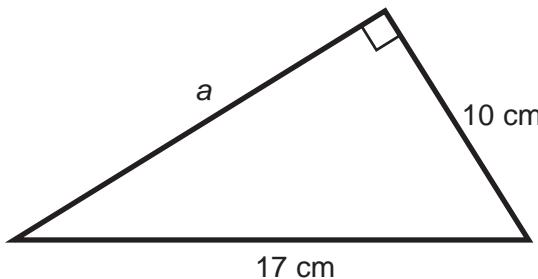
G30

Pythagoras

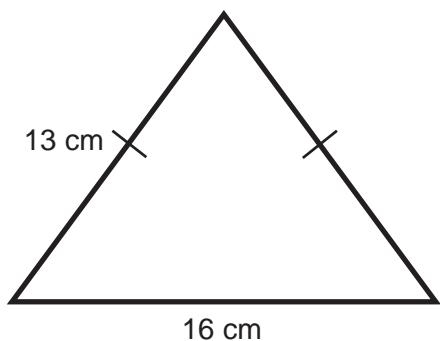
- 1) Calculate the lengths of the sides a to f , giving each answer to 1 decimal place.



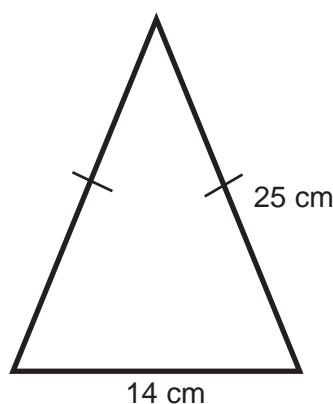
- 2) Calculate the lengths of the sides a and b , giving each answer to 1 decimal place.



- 3) Find the height of this isosceles triangle.
Give your answer to 1 decimal place.



- 4) Find the area of this isosceles triangle.



- 1) The two-way table shows the favourite colours of boys and girls.

	Red	Blue	Green	Total
Boys	9	8		28
Girls	7		12	
Total		21		60

- Complete the two-way table.
- What is the probability that a person chosen at random is a boy whose favourite colour is green?
- What is the probability that a person chosen at random is a girl whose favourite colour is red?
- What is the probability that a person chosen at random is a girl or has favourite colour blue or both?
- What is the probability that a person chosen at random is a boy or has favourite colour green or both?

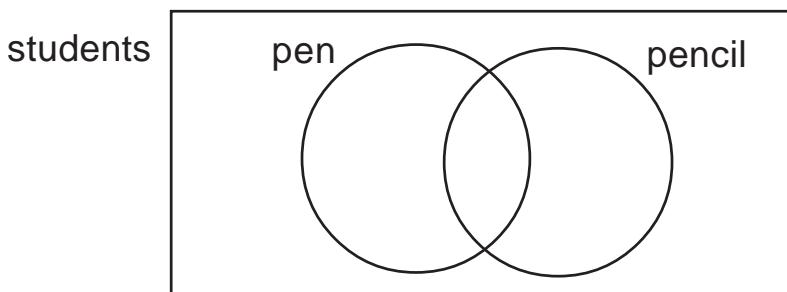
- 1) In a class of 25 students:

19 have a pen

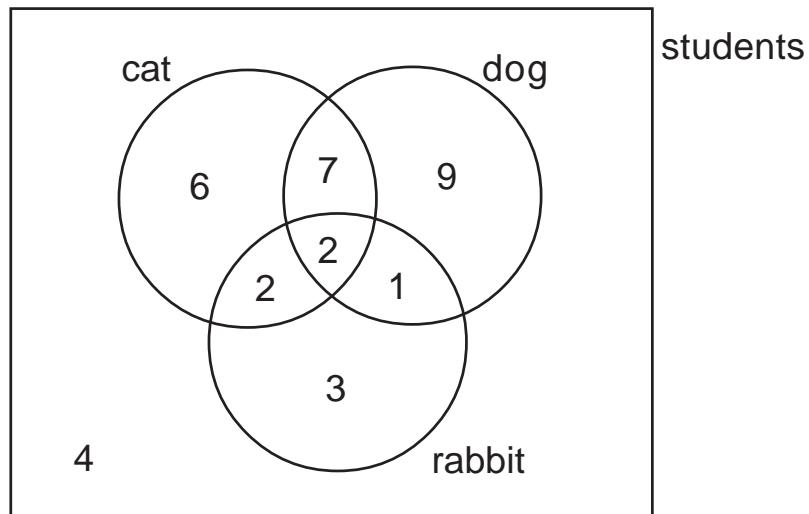
16 have a pencil

3 have neither

Put this information into the Venn diagram.



- 2) This Venn diagram represents the pets owned by a group of students.



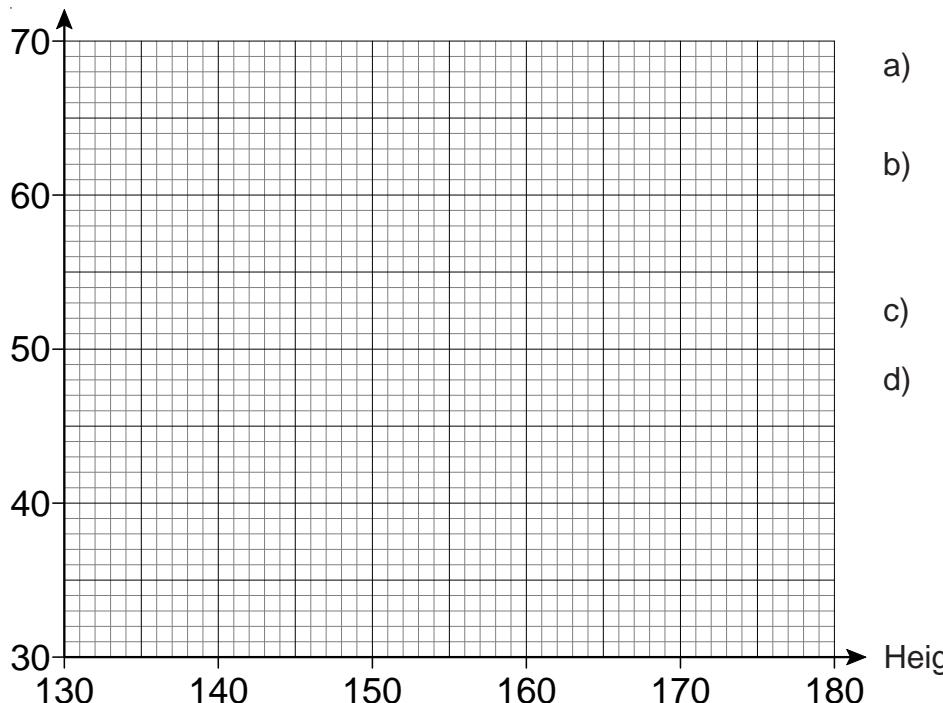
- How many students have a cat only?
- How many students have a cat and a rabbit?
- How many students have either a dog or a cat or both?
- What is the probability that a student, chosen at random, has a dog only?
- What is the probability that a student, chosen at random, has a cat, a rabbit and a dog?
- What is the probability that a student, chosen at random, has a dog or a rabbit or both?

S8

Scatter Diagrams

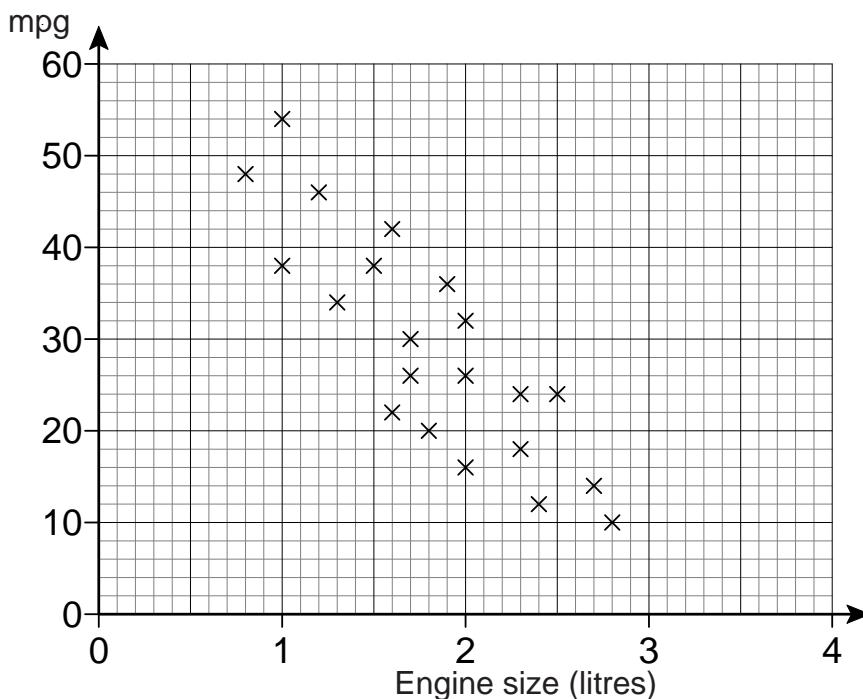
1) The heights and weights of some children are shown in the table, below.

Height (cm)	132	145	150	140	175	168	177	162	170	162	165	149	150	135	159	160
Weight (kg)	34	40	43	35	60	54	62	51	57	51	58	40	41	33	44	50



- a) Plot the information from the table.
- b) Describe the correlation between height and weight.
- c) Draw a line of best fit.
- d) Estimate the weight of a child of similar age to the group above with a height of 155 cm.

2) The scatter graph below relates car engine sizes to their fuel consumption in mpg.



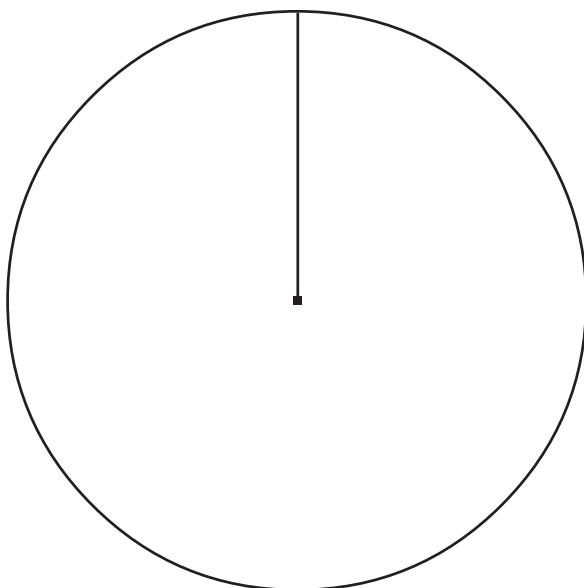
- a) Describe the correlation shown by the data.
- b) A car has an mpg of 25. Estimate the engine size.

S9

Pie Charts

- 1) The table on the right shows how far 90 visitors to a museum have travelled.

Draw a pie chart to show this information.



Distance	Frequency
Within the city	13
Within 30 miles of the city	9
Over 30 miles from the city	20
Overseas	48

- 2) The table shows the land usage of a farm.

Draw a pie chart to show this information.

Land usage	Area (hectares)
Arable	80
Pasture	70
Woodland	50
Waste	40

