

Safe Memory Deallocation for Non-Terminating Programs

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Abstract We propose a type system to prevent programs infinitely consuming memory cells. The main idea is based on the previous type system that augments pointer types with fractional ownerships [1] and behavioral type system that abstracts the behavior of programs. Thanks to the previous type system, we can focus on the behavioral types to count the upper bound of the consumed memory cells soundly.

1 Introduction

Manual memory management primitives (e.g., `malloc` and `free` in C) often cause serious problems such as double frees, memory leaks, and illegal read/write to a deallocated memory cell. Verifying *safe memory deallocation* – a program not leading to such an unsafe state – is an important problem.

Most of safe memory deallocation verification techniques proposed so far [1, 2, 3, 4] focus on the memory leak for *terminating* programs: if a program terminates, the program satisfies safe memory deallocation. For example, the type system by Suenaga and Kobayashi [1] guarantees that (1) a well-typed program does not perform read/write/free operations to any deallocated memory cell and that (2) after execution of a well-typed program, all the memory cells are deallocated.

Currently, we are investigating safe memory deallocation for non-terminating programs, because the safe memory deallocation is very important in real world programs such as Web servers and operating systems.

The main idea of our approach is to decompose this problem into two subproblems: (1) partial correctness and (2) *behavioral correctness*. The former is verified based on the previous type system [1], whereas the latter based on the behavioral type system that is mainly used to abstract the behavior of a program. Behavioral types are heavily used in the context of concurrent program verification [5, 6, 7]. I will describe the concept “memory leak” and our key idea by several examples written in an ML-like language as shown in Figure 1 and Figure 2.

A program *leaks* memory if the program consumes unbounded number of memory cells. For example, the left-hand side program in Figure 1 does not leak memory, whereas

<pre> 1 f(x)= 2 let x = malloc() in 3 free(x); f(x) </pre>	<pre> g(x)= let x = malloc() in g(x); free(x) </pre>
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Figure 1. Explanation for memory leak.

the right-hand side does; the former consumes at most one memory cell at once but the latter consumes unbounded number of memory cells. Notice that these two programs are all partially corrected by the previous type system, because they do not terminate.

<pre> 1 h(x)= 2 let x = malloc() in 3 let y = malloc() in 4 free(x); free(y); h(x) </pre>	<pre> h'(x)= let x = malloc() in let y = malloc() in free(x); h'(x); free(y) </pre>
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Figure 2. Example for demonstrating the main observation.

Let us consider examples in Figure 2 for demonstrating the main observation. The same to examples in Figure 1, the left-hand side program does not leak memory but the right-hand side does; these two are all partially corrected by previous type system. Another thing about programs in Figure 2 we should notice is that once partial correctness is guaranteed, we can guarantee memory-leak freedom by estimating upper bound of memory consumption *ignoring the relation between variables and pointers to memory cells*. Specially speaking, partial correctness has proved that there is no double free in programs, which means if allocating a memory cell in the program, definitely there is a deallocation to that pointer. Say, in order to verify h consumes at most two cells at once, we can ignore variable x and y in h ; We can focus on the fact that h executes **malloc** twice, **free** twice, and then calls h . This abstraction is sound because the correspondence between allocations and deallocations is guaranteed by the partial correctness verification. And from the abstraction of h , we know the number of **malloc** and **free** is balanced, so we can say that function h is memory-leak freedom. About the function h' , its behavior is abstracted as **malloc** twice, **free** once, calls h' itself, and then **free** once. So, the number of **malloc** exceeds the number of **free** once, which makes the recursive function h' consume infinitely memory cells.

Thanks to the previous type system, which guarantes partial correctness, We can focus on the abstraction of behaviour by *behavioral type system*. In our paper, the behaviour of a program is abstracted by CCS-like processes. For example, the behaviour of f is abstracted as $\mu\alpha.\mathbf{malloc}; \mathbf{free}; \alpha$; the behaviour of g is abstracted as $\mu\alpha.\mathbf{malloc}; \alpha; \mathbf{free}$; the behaviour of h is abstracted as $\mu\alpha.\mathbf{malloc}; \mathbf{malloc}; \mathbf{free}; \mathbf{free}; \alpha$; the behaviour of h' is abstracted as $\mu\alpha.\mathbf{malloc}; \mathbf{malloc}; \mathbf{free}; \alpha; \mathbf{free}$.

The rest of this paper is structured as follows. Section 2 introduces a simple imperative language, as well as its syntax and operational semantics. Section 3 introduces the behavioral type system and its semantics.

2 Language

This section introduces a sublanguage of Suenaga and Kobayashi [1] with primitives for memory allocation/deallocation. And the values in our paper are only pointers.

The syntax of language is as follows.

2.1 Syntax

$$\begin{aligned}
 s \text{ (statements)} & ::= \mathbf{skip} \mid s_1; s_2 \mid *x \leftarrow y \mid \mathbf{free}(x) \\
 & \quad \mid \mathbf{let } x = \mathbf{malloc}() \mathbf{in } s \mid \mathbf{let } x = \mathbf{null} \mathbf{in } s \\
 & \quad \mid \mathbf{let } x = y \mathbf{in } s \mid \mathbf{let } x = *y \mathbf{in } s \\
 & \quad \mid \mathbf{ifnull } (x) \mathbf{then } s_1 \mathbf{else } s_2 \mid f(\vec{x}) \\
 d \text{ (definition)} & ::= f(x_1, \dots, x_n) = s
 \end{aligned}$$

A program is a pair (D, s) , where D is the set of definition.

The command **skip** does nothing. The command $s_1; s_2$ is executed as a sequence, first executing s_1 and then s_2 . The command $*x \leftarrow y$ update the content of the memory cell which is pointed by pointer x with value y . The command **free**(x) deallocates the memory cell which is pointed by pointer x . Then command **let** $x = e$ **in** s first evaluates the expression e and binds the return value of e to x and then executes statement s . The command **let** $x = \mathbf{malloc}$ **in** s first allocates a memory cell to a pointer x and then executes the statement s . The command **let** $x = \mathbf{null}$ **in** s first allocates a null pointer to x and then executes s . The command **let** $x = y$ **in** s assign the pointer y to x , so the pointer x and y are said aliases for the same memory cell, and then executes statement s . The command **let** $x = *y$ **in** s transfers a part of memory cells pointed by y and then executes statement s . The command **ifnull** (x) **then** s_1 **else** s_2 denotes that executing statement s_1 if pointer x is a null pointer, if not, executing statement s_2 . The command $f(\vec{x})$ is a function call in which \vec{x} denotes mutually distinct variables like $\{x_1, \dots, x_n\}$. The notation d denotes the definition of function $f(\vec{x})$ which has a body of statement s . And examples are described by this syntax you can see in Figure 1 and Figure 2.

2.2 Operational Semantics

Because we want to estimate the number of available memory cells at every operation step, we extend the triple $\langle H, R, s \rangle$ that is represented as run-time state in previous type system to a quadruple $\langle H, R, s, n \rangle$ in our paper. The introduced notation n denotes the number of available memory cells. When executing the operation **malloc**, the number of available memory cells will decrease 1, which is denoted as $(n - 1)$; when executing the operation **free**, the number of available memory cells will increase 1, which is denoted as $(n + 1)$. The notation H , which models heap memory, is a mapping from finite subset of \mathcal{H} to $\mathcal{H} \cup \{\mathbf{null}\}$, where \mathcal{H} represents the set of *heap addresses*. R , which models registers, is a mapping from finite set of variables to $\mathcal{H} \cup \{\mathbf{null}\}$.

Transition rules are listed in Figure 3. In these rules, $f\{x \rightarrow v\}$ is defined as a function $f'(y)$ such that $f'(y) = v$ if $x = y$, otherwise $f'(y) = f(y)$. n represents the

number of available memory cells, so it is a nature number.

$$\begin{array}{c}
\frac{n \in \mathbb{N}}{\langle H, R, \mathbf{skip}; s, n \rangle \longrightarrow_D \langle H, R, s, n \rangle} \quad (\text{E-Skip}) \\
\\
\frac{R(x) \in \text{dom}(H), n \in \mathbb{N}}{\langle H, R, *x \leftarrow y, n \rangle \longrightarrow_D \langle H \{R(x) \rightarrow R(y)\}, R, \mathbf{skip}, n \rangle} \quad (\text{E-Assign}) \\
\\
\frac{R(x) \in \text{dom}(H), n \in \mathbb{N}}{\langle H, R, \mathbf{free}(\mathbf{x}), n \rangle \xrightarrow{\mathbf{free}}_D \langle H \setminus \{R(x)\}, R, \mathbf{skip}, n+1 \rangle} \quad (\text{E-Free}) \\
\\
\frac{x' \notin \text{dom}(R)}{\langle H, R, \mathbf{let } x = \mathbf{null in } s, n \rangle \longrightarrow_D \langle H, R \{x' \rightarrow \mathbf{null}\}, [x'/x]s, n \rangle} \quad (\text{E-LetNull}) \\
\\
\frac{x' \notin \text{dom}(R)}{\langle H, R, \mathbf{let } x = y \mathbf{ in } s, n \rangle \longrightarrow_D \langle H, R \{x' \rightarrow R(y)\}, [x'/x]s, n \rangle} \quad (\text{E-LetEq}) \\
\\
\frac{x' \notin \text{dom}(R)}{\langle H, R, \mathbf{let } x = *y \mathbf{ in } s, n \rangle \longrightarrow_D \langle H, R \{x' \rightarrow H(R(y))\}, [x'/x]s, n \rangle} \quad (\text{E-LetDref}) \\
\\
\frac{h \notin \text{dom}(H)}{\langle H, R, \mathbf{let } x = \mathbf{malloc}() \mathbf{ in } s, n \rangle \xrightarrow{\mathbf{malloc}}_D \langle H \{h \rightarrow v\}, R \{x' \rightarrow h\}, [x'/x]s, n-1 \rangle} \quad (\text{E-Malloc}) \\
\\
\frac{R(x) = \mathbf{null}}{\langle H, R, \mathbf{ifnull}(x) \mathbf{ then } s_1 \mathbf{ else } s_2, n \rangle \longrightarrow_D \langle H, R, s_1, n \rangle} \quad (\text{E-IfNullT}) \\
\\
\frac{R(x) \neq \mathbf{null}}{\langle H, R, \mathbf{ifnull}(x) \mathbf{ then } s_1 \mathbf{ else } s_2, n \rangle \longrightarrow_D \langle H, R, s_2, n \rangle} \quad (\text{E-IfNullF}) \\
\\
\frac{f(\vec{y}) = s \in D}{\langle H, R, f(\vec{x}), n \rangle \longrightarrow_D \langle H, R, [\vec{x}/\vec{y}]s, n \rangle} \quad (\text{E-Call}) \\
\\
\frac{R(x) = \mathbf{null}}{\langle H, R, *x \leftarrow y, n \rangle \longrightarrow_D \text{NullEx}} \quad (\text{E-AssignNullError}) \\
\\
\frac{R(y) = \mathbf{null}}{\langle H, R, x = *y, n \rangle \longrightarrow_D \text{NullEx}} \quad (\text{E-DrefNullError}) \\
\\
\frac{R(x) \notin \text{dom}(H) \cup \{\mathbf{null}\}}{\langle H, R, *x \leftarrow y, n \rangle \longrightarrow_D \text{Error}} \quad (\text{E-AssignError}) \\
\\
\frac{R(y) \notin \text{dom}(H) \cup \{\mathbf{null}\}}{\langle H, R, \mathbf{let } x = *y \mathbf{ in } s, n \rangle \longrightarrow_D \text{Error}} \quad (\text{E-DrefError}) \\
\\
\frac{R(x) \notin \text{dom}(H) \cup \{\mathbf{null}\}}{\langle H, R, \mathbf{free}(\mathbf{x}), n \rangle \xrightarrow{\mathbf{free}}_D \text{Error}} \quad (\text{E-FreeError}) \\
\\
\frac{R(x) = \mathbf{null}}{\langle H, R, \mathbf{free}(\mathbf{x}), n \rangle \xrightarrow{\mathbf{free}}_D \text{NullEx}} \quad (\text{E-FreeNullError}) \\
\\
\langle H, R, \mathbf{let } x = \mathbf{malloc}() \mathbf{ in } s, 0 \rangle \xrightarrow{\mathbf{malloc}}_D \text{Error} \quad (\text{E-MallocError})
\end{array}$$

3 Type System

This section elaborate the behavioral type system to prevent leaking memory in non-terminating programs. We define behavioral types, CCS-like processes that abstract the behavior of programs, as follows.

3.1 Syntax of Types

$$\begin{aligned}
P(\text{behavioral types}) &::= & \mathbf{0} \mid P_1; P_2 \mid P_1 + P_2 \mid \mathbf{malloc} \\
& & \mid \mathbf{free} \mid \alpha \mid \mu\alpha.P \\
\tau(\text{value types}) &::= & \mathbf{Ref} \\
\sigma(\text{function types}) &::= & (\tau_1, \dots, \tau_n)P
\end{aligned}$$

The type $\mathbf{0}$ abstracts the behavior of **skip** and means "does nothing". $P_1; P_2$ is for sequential execution. $P_1 + P_2$ is abstracted as contional. **malloc** is the behavior of a program that allocates a memory cell exactly once. **free** is for deallocating memory cell exactly once. $\mu\alpha.P$ is a recursive type. For example, the behavior of the body of function h in Figure 2 is abstracted as $\mu\alpha.\mathbf{malloc}; \mathbf{malloc}; \mathbf{free}; \mathbf{free}; \alpha$. α is a type variable and bounded to the recursive constructor $\mu\alpha$.

The only value in our paper is reference, and its type is **Ref**.

The function type is described as $(\tau_1, \dots, \tau_n)P$, which means a function receives some pointers as arguments and then executes its body abstracted as behavioral type P .

3.2 Semantics of Behavioral Types

The semantics of behavioral type are given by labeled transition system, and listed as follows:

$$\begin{aligned}
& \mathbf{0}; P \rightarrow P \\
& \mathbf{malloc} \xrightarrow{\mathbf{malloc}} \mathbf{0} \\
& \mathbf{free} \xrightarrow{\mathbf{free}} \mathbf{0} \\
& \mu\alpha.P \rightarrow [\mu\alpha.P/\alpha]P \\
& P_1 + P_2 \longrightarrow P_1 \\
& P_1 + P_2 \longrightarrow P_2 \\
& \frac{P_1 \xrightarrow{\alpha} P'_1}{P_1; P_2 \xrightarrow{\alpha} P'_1; P_2}
\end{aligned}$$

The notation \rightarrow denotes that a behavioral type can be reduced by the internal action. Notation $\xrightarrow{\alpha}$ means that a behavioral type can be reduced by executing α actions, and the α here is $\{\mathbf{malloc}, \mathbf{free}\}$.

3.3 Typing Rules

The type judgement of our type system is given by the form $\Theta; \Gamma \vdash s : P$, where Θ is a mapping from function variables to function types, Γ is a type environment that denotes a mapping from variables to value types. It reads “the behavior of s is abstracted as P under Θ and Γ environments”. We design the type system so that this type judgement implies the property: when s executes **malloc**(resp. **free**), then P is equivalent to **malloc**; P' (resp. **free**; P') for a type P' such that $\Theta; \Gamma \vdash s' : P'$, where s' is the continuation of s . This property guarantees the behavioral type soundly abstracts the upper bound of the consumed memory cells.

Typing rules are presented in Figure. In the rule for assignment, the behavior of $*x \leftarrow y$ is **0**. The rule for **free** represents that the behavior of **free**(x) is **free**. The rule T-Malloc represents that **let** $x = \mathbf{malloc}()$ **in** s has the behavior **malloc**; P , where P is the behavior of statement s . The rule for function call represents that function f has the behavior P which is the behavior of the body of this function.

In the rule for subtyping, $P_1 \leq P_2$ represents that P_1 is the subtype of P_2 and means that:

- (1) if $P_1 \xrightarrow{\alpha} P'_1$ then $\exists P'_2$ s.t. $P_2 \xRightarrow{\alpha} P'_2$ and $P'_1 \leq P'_2$
 - (2) if $P_1 \rightarrow P'_1$ then $\exists P'_2$ s.t. $P_2 \rightarrow^* P'_2$ and $P'_1 \leq P'_2$
- where $\xRightarrow{\alpha}$ means that: $\rightarrow^* \xrightarrow{\alpha} \rightarrow^*$.

In the rule for program, the main statement s is executed under Θ and Γ environments without free variables. At the end of s , memory leak freedom is guaranteed by $OK_n(P)$, where P is the behavior of s . $OK_n(P)$ is defined as **Definition 1** in which $\sharp_{\mathbf{malloc}}(\alpha)$ and $\sharp_{\mathbf{free}}(\alpha)$ are functors to count the number of **malloc** and **free** actions in α respectively. This definition, intuitively, means at every running step the number of allocated memory cells will never go out of memory scope.

Definition 1. $OK_n(P) \iff \forall P', P \xrightarrow{\alpha}^* P' \text{ then } \sharp_{\mathbf{malloc}}(\alpha) - \sharp_{\mathbf{free}}(\alpha) \leq n.$

$$\begin{array}{c}
\Theta; \Gamma \vdash \mathbf{skip} : \mathbf{0} \quad (\text{T-Skip}) \\
\\
\frac{\Theta; \Gamma \vdash s_1 : P_1 \quad \Theta; \Gamma \vdash s_2 : P_2}{\Theta; \Gamma \vdash s_1; s_2 : P_1; P_2} \quad (\text{T-Seq}) \\
\\
\frac{\Theta; \Gamma \vdash y : \mathbf{Ref} \quad \Theta; \Gamma \vdash x : \mathbf{Ref}}{\Theta; \Gamma \vdash *x \leftarrow y : \mathbf{0}} \quad (\text{T-Assign}) \\
\\
\frac{\Theta; \Gamma \vdash x : \mathbf{Ref}}{\Theta; \Gamma \vdash \mathbf{free}(x) : \mathbf{free}} \quad (\text{T-Free}) \\
\\
\frac{\Theta; \Gamma, x : \mathbf{Ref} \vdash s : P}{\Theta; \Gamma \vdash \mathbf{let } x = \mathbf{malloc}() \mathbf{ in } s : \mathbf{malloc}; P} \quad (\text{T-Malloc}) \\
\\
\frac{\Theta; \Gamma \vdash y : \mathbf{Ref} \quad \Theta; \Gamma, x : \mathbf{Ref} \vdash s : P}{\Theta; \Gamma \vdash \mathbf{let } x = y \mathbf{ in } s : P} \quad (\text{T-LetEq}) \\
\\
\frac{\Theta; \Gamma \vdash y : \mathbf{Ref} \quad \Theta; \Gamma, x : \mathbf{Ref} \vdash s : P}{\Theta; \Gamma \vdash \mathbf{let } x = *y \mathbf{ in } s : P} \quad (\text{T-LetDref})
\end{array}$$

$$\frac{\Theta; \Gamma, x : \mathbf{Ref} \vdash s : P}{\Theta; \Gamma \vdash \mathbf{let } x = \mathbf{null in } s : P} \quad (\text{T-LetNull})$$

$$\frac{\Theta; \Gamma \vdash s : P_1 \quad P_1 \leq P_2}{\Theta; \Gamma \vdash s : P_2} \quad (\text{T-Sub})$$

$$\frac{\Theta; \Gamma \vdash x : \mathbf{Ref} \quad \Theta; \Gamma \vdash s_1 : P \quad \Theta; \Gamma \vdash s_2 : P}{\Theta; \Gamma \vdash \mathbf{ifnull } (x) \mathbf{ then } s_1 \mathbf{ else } s_2 : P} \quad (\text{T-IfNull})$$

$$\frac{\Theta(f) = P}{\Theta; \Gamma, \vec{x} : \vec{\tau} \vdash f(\vec{x}) : P} \quad (\text{T-Call})$$

$$\frac{\vdash D : \Theta \quad \Theta; \emptyset \vdash s : P \quad OK_n(P)}{\vdash (D, s)} \quad (\text{T-Program})$$

3.4 Type Soundness

This subsection describes some theorems and lemmas for type safety.

Theorem 3.1. *If $\vdash (D, s)$ then (D, s) does not lead to memory leak.*

Memory leak freedom: $\exists n \in \mathbb{N} \text{ s.t. } \langle \emptyset, \emptyset, s, n \rangle \rightarrow^ \text{Error}$*

This theorem says that a well typed program guarantees memory leak freedom.

Lemma 3.2 (Preservation I). *If $OK_n(P)$, $\Theta; \Gamma \vdash s : P$ and $\langle H, R, s, n \rangle \xrightarrow{\alpha} \langle H', R', s', n' \rangle$, then $\exists P' \text{ s.t.}$*

- (1) $\Theta; \Gamma \vdash s' : P'$
- (2) $P \xRightarrow{\alpha} P'$
- (3) $OK_{n'}(P')$

Lemma 3.3 (Preservation II). *If $OK_n(P)$, $\Theta; \Gamma \vdash s : P$ and $\langle H, R, s, n \rangle \rightarrow \langle H', R', s', n' \rangle$, then $\exists P' \text{ s.t.}$*

- (1) $\Theta; \Gamma \vdash s' : P'$
- (2) $P \rightarrow^* P'$
- (3) $OK_{n'}(P')$

Lemma 3.4. *The partial correctness is guaranteed $\vdash \langle H, R, s \rangle$, so that if $\vdash \langle H, R, s, n \rangle$, then $\vdash \langle H', R', s', n' \rangle \rightarrow \text{Error}$*

4 Type Inference Algorithm

This section describes how to construct syntax directed typing rules according to the typing rules of above section, and it provides an algorithm which inputs statements and returns a pair containing constraints and behavior types.

4.1 Syntax Directed Typing Rules

Typing rules showed in Figure x are not immediately suitable for type inference. The reason is that the subtyping rule can be applied to any kind of term. This means that, any kind of term s can be applied by either subtyping rule or the other rule whose conclusion matches the shape of the s [8].

In order to yield a type inference algorithm, we should do something with the subtyping rule. The method is to merge the subtyping rule with the other rules by introducing a set C of constraints, where C consists of subtype constraints on behavioral types of the form $P_1 \leq P_2$ and $OK_n(P)$.

Syntax directed typing rules are listed in Figure.

$$\begin{array}{c}
\frac{C = \emptyset}{\Theta; \Gamma; C \vdash \mathbf{skip} : \mathbf{0}} \quad (\text{ST-Skip}) \\
\frac{\Theta; \Gamma; C_1 \vdash s_1 : P_1 \quad \Theta; \Gamma; C_2 \vdash s_2 : P_2 \quad C = C_1 \cup C_2 \cup \{P_1; P_2 \leq P\}}{\Theta; \Gamma; C \vdash s_1; s_2 : P} \quad (\text{ST-Seq}) \\
\frac{\Theta; \Gamma; C_1 \vdash y \quad \Theta; \Gamma; C_2 \vdash x : \mathbf{Ref} \quad C = C_1 \cup C_2}{\Theta; \Gamma; C \vdash *x \leftarrow y : \mathbf{0}} \quad (\text{ST-Assign}) \\
\frac{C = \emptyset}{\Gamma; C \vdash \mathbf{free}() : \mathbf{free}} \quad (\text{ST-Free}) \\
\frac{\Theta; \Gamma, x; C_1 \vdash s : P_1 \quad C = C_1 \cup \{P_1 \leq P\}}{\Theta; \Gamma; C \vdash \mathbf{let } x = \mathbf{malloc}() \mathbf{ in } s : \mathbf{malloc}; P} \quad (\text{ST-Malloc}) \\
\frac{\Theta; \Gamma; C_1 \vdash y \quad \Theta; \Gamma, x; C_2 \vdash s : P_1 \quad C = C_1 \cup C_2 \cup \{P_1 \leq P\}}{\Theta; \Gamma; C \vdash \mathbf{let } x = y \mathbf{ in } s : P} \quad (\text{ST-LetEq}) \\
\frac{\Theta; \Gamma; C_1 \vdash y : \mathbf{Ref} \quad \Theta; \Gamma, x; C_2 \vdash s : P_1 \quad C = C_1 \cup C_2 \cup \{P_1 \leq P\}}{\Theta; \Gamma; C \vdash \mathbf{let } x = *y \mathbf{ in } s : P} \quad (\text{ST-LetDref}) \\
\frac{\Theta; \Gamma; C_1 \vdash x \quad \Theta; \Gamma; C_2 \vdash s_1 : P_1 \quad \Theta; \Gamma; C_3 \vdash s_2 : P_2 \quad C = C_1 \cup C_2 \cup C_3 \{P_1 \leq P, P_2 \leq P\}}{\Theta; \Gamma; C \vdash \mathbf{ifnull } (x) \mathbf{ then } s_1 \mathbf{ else } s_2 : P} \quad (\text{ST-IfNull}) \\
\frac{\Theta(f) = P_1 \quad C = P_1 \leq P}{\Gamma, \vec{x} : \vec{\tau} \vdash f(\vec{x}) : P} \quad (\text{ST-Call}) \\
\frac{\Theta \vdash D : \Theta \quad \Theta; \emptyset; C_1 \vdash s : P \quad C = C_1 \cup \{OK_n(P)\}}{C \vdash (D, s)} \quad (\text{ST-Program})
\end{array}$$

4.2 Algorithm

By syntax directed typing rules, the type inference algorithm is presented as follows. $PT_v(x) = (\emptyset, \emptyset)$, where x maybe a value or reference.

PT_Θ is a mapping from statements to a pair of constraints and types with function Θ from function names to function types, like $\Theta(f) = P$.

$PT_\Theta(f) =$

$\mathbf{let } \alpha = \Theta(f)$
 $\mathbf{in } (C = \{\alpha \leq \beta\}, \beta)$

$$PT_{\Theta}(\mathbf{skip}) = (\emptyset, 0)$$

$$\begin{aligned} PT_{\Theta}(s_1; s_2) = \\ & \mathbf{let} \ (C_1, P_1) = PT_{\Theta}(s_1) \\ & \quad (C_2, P_2) = PT_{\Theta}(s_2) \\ & \mathbf{in} \ (C_1 \cup C_2 \cup \{P_1; P_2 \leq \beta\}, \beta) \end{aligned}$$

$$\begin{aligned} PT_{\Theta}(*x \leftarrow y) = \\ & \mathbf{let} \ (C_1, \emptyset) = PT_v(*x) \\ & \quad (C_2, \emptyset) = PT_v(y) \\ & \mathbf{in} \ (C_1 \cup C_2, 0) \end{aligned}$$

$$PT_{\Theta}(\mathbf{free}(x)) = (\emptyset, \mathbf{free}; 0)$$

$$\begin{aligned} PT_{\Theta}(\mathbf{let} \ x = \mathbf{malloc}() \ \mathbf{in} \ s) = \\ & \mathbf{let} \ (C_1, P_1) = PT_v(s) \\ & \mathbf{in} \ (C_1 \cup \{P_1 \leq \beta\}, \mathbf{malloc}; \beta) \end{aligned}$$

$$\begin{aligned} PT_{\Theta}(\mathbf{let} \ x = y \ \mathbf{in} \ s) = \\ & \mathbf{let} \ (C_1, \emptyset) = PT_v(y) \\ & \quad (C_2, P_1) = PT_{\Theta}(s) \\ & \mathbf{in} \ (C_1 \cup C_2 \cup \{P_1 \leq \beta\}, \beta) \end{aligned}$$

$$\begin{aligned} PT_{\Theta}(\mathbf{let} \ x = *y \ \mathbf{in} \ s) = \\ & \mathbf{let} \ (C_1, \emptyset) = PT_v(y) \\ & \quad (C_2, P_1) = PT_{\Theta}(s) \\ & \mathbf{in} \ (C_1 \cup C_2 \cup \{P_1 \leq \beta\}, \beta) \end{aligned}$$

$$\begin{aligned} PT_{\Theta}(\mathbf{ifnull} \ (x) \ \mathbf{then} \ s_1 \ \mathbf{else} \ s_2) = \\ & \mathbf{let} \ (C_1, P_1) = PT_{\Theta}(s_1) \\ & \quad (C_2, P_2) = PT_{\Theta}(s_2) \\ & \quad (C_3, \emptyset) = PT_v(x) \\ & \mathbf{in} \ (C_1 \cup C_2 \cup C_3 \cup \{P_1 \leq \beta, P_2 \leq \beta\}, \beta) \end{aligned}$$

$$\begin{aligned}
PT(< D, s >) = \\
& \text{let } \Theta = \{f_1 : \alpha_1, \dots, f_n : \alpha_n\} \\
& \quad \text{where } \{f_1, \dots, f_n\} = \text{dom}(D) \text{ and } \alpha_1, \dots, \alpha_n \text{ are fresh} \\
& \text{in let } (C_i, P_i) = PT_{\Theta}(D(f_i)) \text{ for each } i \\
& \text{in let } C'_i = \{\alpha_i \leq P_i\} \text{ for each } i \\
& \text{in let } (C, P) = PT_{\Theta}(s) \\
& \text{in } (C_i \cup C'_i) \cup C \cup \{OK(P)\}, P)
\end{aligned}$$

5 Future Work

We have described a type-based approach to safe memory deallocation for non-terminating programs. The approach is based on the idea of decomposing safe memory memory deallocation into partial correctness, which is verified by previous type system, and behavioral correctness. We designed a behavioral type system in our paper for verification of behavioral correctness. Currently, we are looking for a model checker to estimate an upper bound of consumption given a behavioral type and planning to implement a verifier and conduct experiment to see whether our approach is feasible.

References

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