# **FAdo Documentation**

Release 1.2

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## **FAdo: Tools for Language Models Manipulation**

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# WHAT IS FADO?

The **FAdo** system aims to provide an open source extensible high-performance software library for the symbolic manipulation of automata and other models of computation.

To allow high-level programming with complex data structures, easy prototyping of algorithms, and portability (to use in computer grid systems for example), are its main features. Our main motivation is the theoretical and experimental research, but we have also in mind the construction of a pedagogical tool for teaching automata theory and formal languages.

# 1.1 Regular Languages

It currently includes most standard operations for the manipulation of regular languages. Regular languages can be represented by regular expressions (regexp) or finite automata, among other formalisms. Finite automata may be deterministic (DFA), non-deterministic (NFA) or generalized (GFA). In **FAdo** these representations are implemented as Python classes.

Elementary regular languages operations as union, intersection, concatenation, complementation and reverse are implemented for each class. Also several combined operations are available for specific models.

Several conversions between these representations are implemented:

- NFA -> DFA: subset construction
- NFA -> RE: recursive method
- GFA -> RE: state elimination, with possible choice of state orderings
- RE -> NFA: Thompson method, Glushkov method, follow, Brzozowski, and partial derivatives.
- For DFAs several minimization algorithms are available: Moore, Hopcroft, and some incremental algorithms. Brzozowski minimization is available for NFAs.
- An algorithm for hyper-minimization of DFAs
- Language equivalence of two DFAs can be determined by reducing their correspondent minimal DFA to a canonical form, or by the Hopcroft and Karp algorithm.
- Enumeration of the first words of a language or all words of a given length (Cross Section)
- Some support for the transition semigroups of DFAs

# 1.2 Finite Languages

Special methods for finite languages are available:

- Construction of a ADFA (acyclic finite automata) from a set of words
- · Minimization of ADFAs
- · Several methods for ADFAs random generation

• Methods for deterministic cover finite automata (DCFA)

# 1.3 Transducers

Several methods for transducers in standard form (SFT) are available:

- Rational operations: union, inverse, reversal, composition, concatenation, star
- Test if a transducer is functional
- Input intersection and Output intersection operations

# 1.4 Codes

A *language property* is a set of languages. Given a property specified by a transducer, several language tests are possible.

- Satisfaction i.e. if a language satisfies the property
- Maximality i.e. the language satisfies the property and is maximal
- Properties implemented by transducers include: input preserving, input altering, trajectories, and fixed properties
- Computation of the edit distance of a regular language, using input altering transducers

# **MODULE: FINITE AUTOMATA (FA)**

# Finite automata manipulation.

Deterministic and non-deterministic automata manipulation, conversion and evaluation.

# 2.1 Class FA (abstract class for Finite Automata)

#### class fa.FA

Bases: common.Drawable

Base class for Finite Automata.

# Variables

- States set of states
- Sigma alphabet set
- **Initial** the initial state
- Final set of final states
- **delta** the transition function

Note: This is just an abstract class. Not to be used directly!!

# addFinal (stateindex)

A new state is added to the already defined set of final states.

**Parameters stateindex** (*int*) – index of the new final state

# addSigma(sym)

Adds a new symbol to the alphabet.

Parameters sym (str) – symbol to be added

Raises DFAepsilonRedefenition if sym is Epsilon

#### Note:

- •There is no problem with duplicate symbols because Sigma is a Set.
- •No symbol Epsilon can be added.

#### addState (name=None)

Adds a new state to an FA. If no name is given a new name is created.

Parameters name (object) – Name of the state to be added

**Returns** Current number of states (the new state index)

Return type int

```
Raises DuplicateName if a state with that name already exists
conjunction (other)
     A simple literate invocation of __and__
         Parameters other – the other FA
     New in version 0.9.6.
countTransitions()
     Evaluates the size of FA transitionwise
         Returns the number of transitions
         Return type int
     Changed in version 1.0.
delFinal(st)
     Deletes a state from the final states list
         Parameters st (int) – state to be marked as not final
delFinals()
     Deletes all the information about final states.
deleteState(sti)
     Remove the given state and the transitions related with that state.
         Parameters sti (int) – index of the state to be removed
         Raises DFAstateUnknown if state index does not exist
disj(other)
     Another simple literate invocation of or
         Parameters other – the other FA
     New in version 0.9.6.
disjunction(other)
     A simple literate invocation of __or__
         Parameters other – the other FA
dotDrawState (sti, sep='n')
     Draw a state in dot format
         Parameters
              • sti (int) – index of the state
              • sep (str) – separator
         Return type str
dotDrawTransition (st1, sym, st2, sep)
     Draw a transition in dot format
         Parameters
              • st1 (str) – departing state
              • sym (str) – label
              • st2 (str) – arriving state
              • sep (str) – separator
```

dotFormat (size='20, 20', direction='LR', sep='n')

A dot representation **Parameters** 

# Chapter 2. Module: Finite Automata (fa)

- **direction** (*str*) direction of drawing
- **size** (*str*) size of image
- **sep** (*str*) line separator

**Returns** the dot representation

Return type str

New in version 0.9.6.

Changed in version 0.9.8.

#### eliminateDeadName()

Eliminates dead state name (common.DeadName) renaming the state

Attention: works inplace

New in version 1.2.

# equivalentP(other)

Test equivalence

Parameters other – the other automata

Return type bool

New in version 0.9.6.

## evalSymbol()

Evaluation of a single symbol

#### finalP(state)

Tests if a state is final

**Parameters state** (*int*) – state index

Return type bool

# finalsP (states)

Tests if al the states in a set are final

Parameters states (set) – set of state indexes

Return type bool

New in version 1.0.

#### hasStateIndexP(st)

Checks if a state index pertains to an FA

Parameters st (int) – index of the state

Return type bool

# indexList (lstn)

Converts a list of stateNames into a set of stateIndexes.

**Parameters 1stn** (*list*) – list of names

**Returns** the list of state indexes

Return type Set of int

Raises DFAstateUnknown if a state name is unknown

#### initialP (state)

Tests if a state is initial

Parameters state (int) – state index

Return type bool

#### initialSet()

The set of initial states

**Returns** the set of the initial states

Return type set of States

# inputS(i)

Input labels coming out of state i

Parameters i (int) – state

**Returns** set of input labels

Return type set of str

New in version 1.0.

#### noBlankNames()

Eliminates blank names

Returns self

Attention: in place transformation

#### plus()

Plus of a FA (star without the adding of epsilon)

New in version 0.9.6.

# renameState (st, name)

Rename a given state.

#### **Parameters**

- st (int) state index
- name (object) name

Returns self

**Note:** Deals gacefully both with int and str names in the case of name collision.

Attention: the object is modified in place

# renameStates (nameList=None)

Renames all states using a new list of names.

Parameters nameList (list) – list of new names

Raises DFAerror if provided list is too short

Returns self

**Note:** If no list of names is given, state indexes are used.

**Attention:** the object is modified in place

# reversal()

Returns a NFA that recognizes the reversal of the language

Returns NFA recognizing reversal language

Return type NFA

# same\_nullability(s1, s2)

Tests if this two states have the same nullability

#### **Parameters**

- **s1** (*int*) state index
- **s2** (*int*) state index

# Return type bool

## setFinal(statelist)

Sets the final states of the FA

**Parameters statelist** (int|list|set) – a list (or set) of final states indexes

Caution: it erases any previous definition of the final state set.

#### setInitial(stateindex)

Sets the initial state of a FA

**Parameters stateindex** (*int*) – index of the initial state

# setSigma (symbolSet)

Defines the alphabet for the FA.

Parameters symbolSet (list|set) – alphabet symbols

# stateIndex (name, autoCreate=False)

Index of given state name.

#### **Parameters**

- name (object) name of the state
- autoCreate (bool) flag to create state if not already done

**Returns** state index

Return type int

Raises DFAstateUnknown if the state name is unknown and autoCreate==False

Note: Replaces stateName

**Note:** If the state name is not known and flag is set creates it on the fly

New in version 1.0.

#### stateName (\*args, \*\*kwargs)

Index of given state name.

#### **Parameters**

- name (object) name of the state
- autoCreate (bool) flag to create state if not already done

**Returns** state index

Return type int

Raises DFAstateUnknown if the state name is unknown and autoCreate==False

Deprecated since version 1.0: Use: stateIndex() instead

# succintTransitions()

Collapsed transitions :rtype: list

union (other)

A simple literate invocation of \_\_or\_\_

Parameters other – right hand operand

```
words (stringo=True)
```

Lexicografical word generator

Attention: does not generate the empty word

Parameters stringo (bool) – are words strings?

New in version 0.9.8.

# 2.2 Class SemiDFA (Semi-Automata class)

#### class fa.SemiDFA

Bases: common.Drawable

Class of automata without initial or final states

#### Variables

- States list of states
- delta transition function
- Sigma alphabet set

dotDrawState (sti, sep='n')

Dot representation of a state

#### **Parameters**

- **sti** (*int*) state index
- sep (str) separator

Return type str

static dotDrawTransition (st1, lbl1, st2, sep='n')

Draw a transition in dot format

## **Parameters**

- st1 (str) departing state
- **lbl1** (*str*) label
- st2 (str) arriving state
- **sep** (*str*) separator

# Return type str

dotFormat (size='20, 20', direction='LR', sep='n')

Dot format of automata

# **Parameters**

- size (str) image size
- direction direction of drawing
- **sep** (*str*) separator

Return type str

# 2.3 Class OFA (one-way finite automata class)

#### class fa.OFA

Bases: fa.FA

Base class for one-way automata .. inheritance-diagram:: OFA

#### SPRegExp()

Checks if FA is SP (Serial-PArallel), and if so returns the regular expression whose language is recognised by the FA

**Returns** equivalent regular expression

Return type regexp

Raises NotSP if the automaton is not Serial-Parallel

#### See also:

Moreira & Reis, Fundamenta Informatica, Series-Parallel automata and short regular expressions, n.91 3-4, pag 611-629. http://www.dcc.fc.up.pt/~nam/publica/spa07.pdf

Note: Automata must be Serial-Parallel

## acyclicP (strict=True)

Checks if the FA is acyclic

**Parameters strict** (*bool*) – if not True loops are allowed

**Returns** True if the FA is acyclic

Return type bool

#### addTransition(st1, sym, st2)

Add transition :param int st1: departing state :param str sym: label :param int st2: arriving state

# allRegExps()

Evaluates the alphabetic length of the equivalent regular expression using every possible order of state elimination.

Return type list of tuples (int, list of states)

#### complete (dead='@DeaD')

Transforms the automata into a complete one. If Sigma is empty nothing is done.

Parameters dead (str) – dead state name

Returns the complete FA

**Return type** DFA

**Note:** Adds a dead state (if necessary) so that any word can be processed with the automata. The new state is named dead, so this name should never be used for other purposes.

**Attention:** The object is modified in place.

Changed in version 1.0.

#### completeP()

Checks if it is a complete FA (if delta is total)

Returns bool

# cutPoints()

Set of FA's cut points

**Returns** set of states

```
Return type set of int
deleteStates (del_states)
     To be implemented below
         Parameters del_states (list) - states to be deleted
static dotDrawTransition (st1, label, st2, sep='n')
     Draw a transition in Dot Format
         Parameters
              • st1 (str) – starting state
              • st2 (str) – ending state
              • label (str) - symbol
              • sep (str) – separator
         Return type str
dump()
     Returns a python representation of the object
         Returns the python representation (Tags, States, Sigma, delta, Initial, Final)
         Return type tuple
dup()
     Duplicate OFA
         Returns duplicate object
eliminateSingles()
     Eliminates every state that only have one successor and one predecessor.
         Returns GFA after eliminating states
         Return type GFA
eliminateStout(st)
     Eliminate all transitions outgoing from a given state
         Parameters st (int) – the state index to loose all outgoing transitions
       Attention: performs in place alteration of the automata
     New in version 0.9.6.
emptyP()
     Tests if the automaton accepts a empty language
         Return type bool
     New in version 1.0.
evalNumberOfStateCycles()
     Evaluates the number of cycles each state participates
         Returns state->list of cycle lengths
         Return type dict
evalSymbol()
     Eval symbol
finalCompP(s)
     To be implemented below
         Parameters s – state
```

## Return type list

#### initialComp()

Initial component

Return type list

# minimalBrzozowski()

Constructs the equivalent minimal DFA using Brzozowski's algorithm

Returns equivalent minimal DFA

Return type DFA

#### minimalBrzozowskiP()

Tests if the FA is minimal using Brzozowski's algorithm

Return type bool

#### reCG()

Regular expression from state elimination whose language is recognised by the FA. Uses a heuristic to choose the order of elimination.

Returns the equivalent regular expression

Return type regexp

#### reCG nn()

Regular expression from state elimination whose language is recognised by the FA. Uses a heuristic to choose the order of elimination. The FA is not normalized before the state elimination.

**Returns** the equivalent regular expression

Return type regexp

# reDynamicCycleHeuristic()

State elimination Heuristic based on the number of cycles that passes through each state. Here those numbers are evaluated dynamically after each elimination step

Returns an equivalent regular expression

**Return type** regexp

#### See also:

Nelma Moreira, Davide Nabais, and Rogério Reis. State elimination ordering strategies: Some experimental results. Proc. of 11th Workshop on Descriptional Complexity of Formal Systems (DCFS10), pages 169-180.2010. DOI: 10.4204/EPTCS.31.16

# ${\tt reStaticCycleHeuristic} \ ( \ )$

State elimination Heuristic based on the number of cycles that passes through each state. Here those numbers are evaluated statically in the beginning of the process

Returns a equivalent regular expression

Return type regexp

#### See also:

Nelma Moreira, Davide Nabais, and Rogério Reis. State elimination ordering strategies: Some experimental results. Proc. of 11th Workshop on Descriptional Complexity of Formal Systems (DCFS10), pages 169-180.2010. DOI: 10.4204/EPTCS.31.16

# re\_stateElimination(order=None)

Regular expression from state elimination whose language is recognised by the FA. The FA is normalized before the state elimination.

Parameters order (list) – state elimination sequence

Returns the equivalent regular expression

Return type regexp

#### re\_stateElimination\_nn (order=None)

Regular expression from state elimination whose language is recognised by the FA. The FA is not normalized before the state elimination.

**Parameters order** (*list*) – state elimination sequence

Returns the equivalent regular expression

Return type regexp

#### regexpSE()

A regular expression obtained by state elimination algorithm whose language is recognised by the FA.

**Returns** the equivalent regular expression

Return type regexp

#### stateChildren(s)

To be implemented below

**Parameters** s – state

Return type list

#### succintTransitions()

Collapsed transitions

#### toGFA()

To be implemented below

# topoSort()

Topological order for the FA

**Returns** List of state indexes

Return type list of int

**Note:** self loops are taken in consideration

# trim()

Removes the states that do not lead to a final state, or, inclusively, that can't be reached from the initial state. Only useful states remain.

**Attention:** in place transformation

#### trimP()

Tests if the FA is trim: initially connected and co-accessible

Returns bool

# uniqueRepr()

Abstract method

# usefulStates()

To be implemented below

# 2.4 Class DFA (Deterministic Finite Automata)

#### class fa.DFA

Bases: fa.OFA

Class for Deterministic Finite Automata.



#### Delta (state, symbol)

Evaluates the action of a symbol over a state

#### **Parameters**

- state (int) state index
- symbol symbol

**Returns** the action of symbol over state

**Return type** int

# aEquiv()

Computes almost equivalence, used by hyperMinimial

**Returns** partition of states

Return type dictionary

Note: may be optimized to avoid dupped

#### addTransition (sti1, sym, sti2)

Adds a new transition from stil to stil consuming symbol sym.

#### **Parameters**

- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- sym (str) symbol consumed

Raises DFAnotNFA if one tries to add a non deterministic transition

# compat (s1, s2, data)

Tests compatibility between two states.

# **Parameters**

- data –
- s1 (int) state index
- **s2** (*int*) state index

# Return type bool

# completeMinimal()

Completes a DFA assuming it is a minimal and avoiding de destruction of its minimality If the automaton is not complete, all the non final states are checked to see if tey are not already a dead state. Only in the negative case a new (dead) state is added to the automaton.

#### Return type DFA

**Attention:** The object is modified in place. If the alphabet is empty nothing is done

#### completeProduct (other)

Product structure

#### Parameters other – the other DFA

#### computeKernel()

The Kernel of a ICDFA is the set of states that accept a non finite language.

**Returns** triple (comp, center, mark) where comp are the strongly connected components, center the set of center states and mark the kernel states

#### Return type tuple

#### concat (fa2, strict=False)

Concatenation of two DFAs. If DFAs are not complete, they are completed.

#### **Parameters**

- **strict** (*Boolean*) should alphabets be checked?
- fa2 (DFA) the second DFA

**Returns** the result of the concatenation

Return type DFA

Raises DFAdifferentSigma if alphabet are not equal

## concatI (fa2, strict=False)

Concatenation of two DFAs.

#### **Parameters**

- fa2 (DFA) the second DFA
- **strict** (*Boolean*) should alphabets be checked?

**Returns** the result of the concatenation

Return type DFA

Raises DFAdifferentSigma if alphabet are not equal

New in version 0.9.5.

**Note:** this is to be used with non complete DFAs

# **delTransition** (*sti1*, *sym*, *sti2*, \_*no*\_*check*=*False*)

Remove a transition if existing and perform cleanup on the transition function's internal data structure.

## **Parameters**

- \_no\_check (Boolean) use unsecure code?
- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- sym (str) symbol consumed

Note: Unused alphabet symbols will be discarded from Sigma.

# deleteStates (del\_states)

Delete given iterable collection of states from the automaton.

Parameters del\_states - collection of int representing states

**Note:** delta function will always be rebuilt, regardless of whether the states list to remove is a suffix, or a sublist, of the automaton's states list.

#### dist()

Evaluate the distinguishability language for a DFA

## Return type DFA

#### See also:

Cezar Câmpeanu, Nelma Moreira, Rogério Reis: The distinguishability operation on regular languages. NCMA 2014: 85-100

New in version 0.9.8.

#### distMin()

Evaluates the list of minimal words that distinguish each pair of states

**Returns** set of minimal distinguishing words

Return type FL

New in version 0.9.8.

**Attention:** If the DFA is not minimal, the method loops forever

#### distR()

Evaluate the right distinguishability language for a DFA

#### Return type DFA

**..seealso:: Cezar Câmpeanu, Nelma Moreira, Rogério Reis:** The distinguishability operation on regular languages. NCMA 2014: 85-100

#### distRMin()

Compute distRMin for DFA

:rtype FL

**..seealso:: Cezar Câmpeanu, Nelma Moreira, Rogério Reis:** The distinguishability operation on regular languages. NCMA 2014: 85-100

# distTS()

Evaluate the two-sided distinguishability language for a DFA

#### Return type DFA

**..seealso:: Cezar Câmpeanu, Nelma Moreira, Rogério Reis:** The distinguishability operation on regular languages. NCMA 2014: 85-100

#### dup()

Duplicate the basic structure into a new DFA. Basically a copy.deep.

#### Return type DFA

# enumDFA(n=None)

returns the set of words of words of length up to n accepted by self :param n: highest length or all words if finite :type n: int

Return type list of strings or None

# equal (other)

Verify if the two automata are equivalent. Both are verified to be minimum and complete, and then one is matched against the other... Doesn't destroy either dfa...

**Parameters other** (*DFA*) – the other DFA

Return type bool

# evalSymbol(init, sym)

Returns the state reached from given state through a given symbol.

#### **Parameters**

- init (set or list of int) set of current states indexes
- sym (str) symbol to be consumed

Returns reached state

Return type int

#### **Raises**

- **DFAsymbolUnknown** if symbol not in alphabet
- **DFAstopped** if transition function is not defined for the given input

#### evalSymbolI (init, sym)

Returns the state reached from a given state.

#### **Parameters**

- init (int) current state
- sym (str) symbol to be consumed

Returns reached state or -1

Return type set of int

Raises DFAsymbolUnknown if symbol not in alphabet

New in version 0.9.5.

**Note:** this is to be used with non complete DFAs

#### evalSymbolL(ls, sym)

Returns the set of states reached from a given set of states through a given symbol

# **Parameters**

- **ls** (set of int) set of states indexes
- **sym** (*str*) symbol to be read

**Returns** set of reached states

Return type set of int

#### evalSymbolLI (ls, sym)

Returns the set of states reached from a given set of states through a given symbol

# **Parameters**

- **Is** (*set of int*) set of current states
- sym (str) symbol to be consumed

**Returns** set of reached states

Return type set of int

New in version 0.9.5.

**Note:** this is to be used with non complete DFAs

# evalWordP (word, initial=None)

Verifies if the DFA recognises a given word

# **Parameters**

- word (list of symbols.) word to be recognised
- initial (int) starting state index

Return type bool

#### finalCompP(s)

Verifies if there is a final state in strongly connected component containing s.

**Parameters** s (int) – state

Returns 1 if yes, 0 if no

#### hasTrapStateP()

Tests if the automaton has a dead trap state

Return type bool

New in version 1.1.

#### hyperMinimal (strict=False)

Hyperminization of a minimal DFA

Parameters strict (bool) – if strict=True it first minimizes the DFA

Returns an hyperminimal DFA

Return type DFA

#### See also:

M. Holzer and A. Maletti, An nlogn Algorithm for Hyper-Minimizing a (Minimized) Deterministic Automata, TCS 411(38-39): 3404-3413 (2010)

**Note:** if strict=False minimality is assumed

#### inDegree(st)

Returns the in-degree of a given state in an FA

**Parameters** st (*int*) – index of the state

Return type int

# infix()

Returns a dfa that recognizes infix(L(a))

Return type DFA

# initialComp()

Evaluates the connected component starting at the initial state.

**Returns** list of state indexes in the component

**Return type** list of int

#### initialP(state)

Tests if a state is initial

**Parameters state** (*int*) – state index

Return type bool

# initialSet()

The set of initial states

**Returns** the set of the initial states

Return type set of States

# joinStates(lst)

Merge a list of states.

Parameters 1st (iterable of state indexes.) – set of equivalent states

# markNonEquivalent (s1, s2, data)

Mark states with indexes s1 and s2 in given map as non equivalent states. If any back-effects exist, apply them.

#### **Parameters**

- s1 (int) one state's index
- **s2** (*int*) the other state's index
- data the matrix relating s1 and s2

#### mergeStates(f, t)

Merge the first given state into the second. If the first state is an initial state the second becomes the initial state.

#### **Parameters**

- **f** (*int*) index of state to be absorbed
- t (int) index of remaining state

**Attention:** It is up to the caller to remove the disconnected state. This can be achieved with `trim().

# minimal (method='minimalHopcroft', complete=True)

Evaluates the equivalent minimal complete DFA

#### **Parameters**

- **method** method to use in the minimization
- **complete** (*bool*) should the result be completed?

Returns equivalent minimal DFA

Return type DFA

#### minimalHKP()

Tests the DFA's minimality using Hopcroft and Karp's state equivalence algorithm

Returns bool

#### See also:

J. E. Hopcroft and R. M. Karp.A Linear Algorithm for Testing Equivalence of Finite Automata.TR 71–114. U. California. 1971

**Attention:** The automaton must be complete.

# minimalHopcroft()

Evaluates the equivalent minimal complete DFA using Hopcroft algorithm

**Returns** equivalent minimal DFA

Return type DFA

# See also:

John Hopcroft, An nlog{n} algorithm for minimizing states in a finite automaton. The Theory of Machines and Computations. AP. 1971

# minimalHopcroftP()

Tests if a DFA is minimal

Return type bool

# minimalIncremental(minimal\_test=False)

Minimizes the DFA with an incremental method using the Union-Find algorithm and memoized non-equivalence intermediate results

**Parameters minimal\_test** (*bool*) – starts by verifying that the automaton is not minimal?

Returns equivalent minimal DFA

## Return type DFA

#### See also:

13.Almeida and N. Moreira and R. Reis.Incremental DFA minimisation. CIAA 2010. LNCS 6482. pp 39-48. 2010

#### minimalIncrementalP()

Tests if a DFA is minimal

Return type bool

#### minimalMoore()

Evaluates the equivalent minimal automata with Moore's algorithm

#### See also:

John E. Hopcroft and Jeffrey D. Ullman, Introduction to Automata Theory, Languages, and Computation, AW, 1979

Returns minimal complete DFA

Return type DFA

# minimalMooreSq()

Evaluates the equivalent minimal complete DFA using Moore's (quadratic) algorithm

#### See also:

John E. Hopcroft and Jeffrey D. Ullman, Introduction to Automata Theory, Languages, and Computation, AW, 1979

Returns equivalent minimal DFA

Return type DFA

# ${\tt minimalMooreSqP}\;(\;)$

Tests if a DFA is minimal using the quadratic version of Moore's algorithm

Return type bool

# minimalNCompleteP()

Tests if a non necessarely complete DFA is minimal, i.e., if the DFA is non complete, if the minimal complete has only one more state.

Returns True if not minimal

Return type bool

Attention: obsolete: use minimalP

#### minimalNotEquivP()

Tests if the DFA is minimal by computing the set of distinguishable (not equivalent) pairs of states

Return type bool

# minimalP (method='minimalHopcroft')

Tests if the DFA is minimal

Parameters method – the minimization algorithm to be used

Return type bool

..note: if DFA non complete test if complete minimal has one more state

#### minimalWatson (test\_only=False)

Evaluates the equivalent minimal complete DFA using Waton's incremental algorithm

```
Parameters test_only (bool) – is it only to test minimality
```

Returns equivalent minimal DFA

Return type DFA

Raises DFAnotComplete if automaton is not complete

..attention:: automaton must be complete

# minimalWatsonP()

Tests if a DFA is minimal using Watson's incremental algorithm

Return type bool

# notequal(other)

Test non equivalence of two DFAs

**Parameters other** (*DFA*) – the other DFA

Return type bool

#### pairGraph()

Returns pair graph

Return type DiGraphVM

#### See also:

A graph theoretic approach to automata minimality. Antonio Restivo and Roberto Vaglica. Theoretical Computer Science, 429 (2012) 282-291. doi:10.1016/j.tcs.2011.12.049 Theoretical Computer Science, 2012 vol. 429 (C) pp. 282-291. http://dx.doi.org/10.1016/j.tcs.2011.12.049

#### pref()

Returns a dfa that recognizes pref(L(self))

# Return type DFA

New in version 1.1.

#### print\_data(data)

Prints table of compatibility (in the context of the minimalization algorithm).

Parameters data - data to print

# product (other, complete=True)

Returns a DFA resulting of the simultaneous execution of two DFA. No final states set.

## **Parameters**

- other the other DFA
- complete (bool) evaluate product as a complete DFA

Return type DFA

# regexp()

Returns a regexp for the current DFA considering the recursive method. Very inefficent.

**Returns** a regexp equivalent to the current DFA

**Return type** regexp

#### reorder (dicti)

Reorders states according to given dictionary. Given a dictionary (not necessarily complete)... reorders states accordingly.

:param dicti :type dicti: dictionary

# reverseTransitions(rev)

Evaluate reverse transition function.

```
Parameters rev (DFA) – DFA in which the reverse function will be stored
```

#### sMonoid()

Evaluation of the syntactic monoid of a DFA

Returns the semigroup

Return type SSemiGroup

## sSemigroup()

Evaluation of the syntactic semigroup of a DFA

**Returns** the semigroup

Return type SSemiGroup

shuffle (other, strict=False)

Shuffle of two languages: L1 W L2

#### **Parameters**

- other (DFA) second automaton
- **strict** (*bool*) should the alphabets be necessary equal?

Return type DFA

#### See also:

C. Câmpeanu, K. Salomaa and S. Yu, *Tight lower bound for the state complexity of shuffle of regular languages*. J. Autom. Lang. Comb. 7 (2002) 303–310.

## simDiff(other)

Symetrical difference

Parameters other -

Returns

# sop (other)

Strange operation

**Parameters other** (*DFA*) – the other automaton

Return type DFA

New in version 1.2b2.

### star(flag=False)

Star of a DFA. If the DFA is not complete, it is completed.

..versionchanged: 0.9.6

Parameters flag (bool) – plus instead of star

Returns the result of the star

Return type DFA

#### starI()

Star of an incomplete DFA.

Returns the Kleene closure DFA

Return type DFA

# stateChildren(state, strict=False)

Set of children of a state

#### **Parameters**

- strict (bool) if not strict a state is never its own child even if a self loop is in place
- state (int) state id queried

```
Returns map children -> multiplicity
         Return type dictionary
subword()
         Returns a dfa that recognizes subword(L(self))
         Return type dfa
     New in version 1.1.
succintTransitions()
     Collects the transition information in a compact way suitable for graphical representation. :rtype: list
     of tupples
     New in version 0.9.8.
suff()
     Returns a dfa that recognizes suff(L(self))
         Return type DFA
     New in version 0.9.8.
syncPower()
     Evaluates the power automata for the action of each symbol
         Returns The power automata being the set of all states the initial state and all singleton
             states final.
         Return type DFA
syncWords()
     Evaluates the regular expression corresponding to the synchronizing pwords of the automata.
         Returns a regular expression of the sync words of the automata
         Return type regexp
toADFA()
    Try to convert DFA to ADFA
         Returns the same automaton as a ADFA
         Return type ADFA
         Raises notAcyclic if this is not an acyclic DFA
     New in version 1.2.
toDFA()
     Dummy function. It is already a DFA
         Returns a self deep copy
         Return type DFA
toGFA()
     Creates a GFA equivalent to DFA
         Returns GFA deep copy
         Return type GFA
toNFA()
     Migrates a DFA to a NFA as dup()
         Returns DFA seen as new NFA
         Return type NFA
```

#### uniqueRepr()

Normalise unique string for the string icdfa's representation.

#### See also:

TCS 387(2):93-102, 2007 http://www.ncc.up.pt/~nam/publica/tcsamr06.pdf

**Returns** normalised representation

Return type list

Raises DFAnotComplete if DFA is not complete

#### unmark()

Unmarked NFA that corresponds to a marked DFA: in which each alfabetic symbol is a tuple (symbol, index)

Returns a NFA

Return type NFA

## usefulStates (initial\_states=None)

Set of states reacheable from the given initial state(s) that have a path to a final state.

Parameters initial\_states (iterable of int) – starting states

**Returns** set of state indexes

Return type set of int

#### static vDescription()

Generation of Verso interface description

New in version 0.9.5.

**Returns** the interface list

#### witness()

Witness of non emptyness

Returns word

Return type str

## witnessDiff(other)

Returns a witness for the difference of two DFAs and:

0 if the witness belongs to the **other** language 1 if the witness belongs to the **self** language

**Parameters other** (*DFA*) – the other DFA

Returns a witness word

Return type list of symbols

Raises DFA equivalent if automata are equivalent

# 2.5 Class NFA (Nondeterministic Finite Automata)

#### class fa.NFA

Bases: fa.OFA

Class for Non-deterministic Finite Automata (epsilon-transitions allowed).



#### addEpsilonLoops()

Add epsilon loops to every state :return: self

Attention: in-place modification

New in version 1.0.

#### addInitial(stateindex)

Add a new state to the set of initial states.

**Parameters stateindex** (*int*) – index of new initial state

## addTransition (sti1, sym, sti2)

Adds a new transition. Transition is from stil to stil consuming symbol sym. stil is a unique state, not a set of them.

#### **Parameters**

- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- sym (str) symbol consumed

# addTransitionQ (srcI, dest, symb, qfuture, qpast)

Add transition to the new transducer instance.

#### **Parameters**

- **qpast** (*set*) past queue
- **qfuture** (*set*) future queue
- symb symbol
- dest destination state
- **srcI** (*int*) source state

New in version 1.0.

# autobisimulation()

Largest right invariant equivalence between states of the NFA

**Returns** Incomplete equivalence relation (transitivity, and reflexivity not calculated) as a set of unordered pairs of states

Return type Set of frozensets

#### See also:

Ilie&Yu, 2003

# autobisimulation2()

Alternative space-efficient definition of NFA.autobisimulation.

**Returns** Incomplete equivalence relation (reflexivity, symmetry, and transitivity not calculated) as a set of pairs of states

Return type list of tuples

#### closeEpsilon(st)

Add all non epsilon transitions from the states in the epsilon closure of given state to given state.

**Parameters st** (*int*) – state index

#### concat (other, middle='middle')

Concatenation of NFA

#### **Parameters**

- middle (str) glue state name
- other (NFA|DFA) the other NFA

**Returns** the result of the concatenation

Return type NFA

# countTransitions()

Number of transitions of a NFA

# Return type int

#### **delTransition** (*sti1*, *sym*, *sti2*, \_*no*\_*check*=*False*)

Remove a transition if existing and perform cleanup on the transition function's internal data structure.

#### **Parameters**

- **sti1** (*int*) state index of departure
- sti2 (int) state index of arrival
- sym (str) symbol consumed
- \_no\_check (bool) dismiss secure code

Note: unused alphabet symbols will be discarded from Sigma.

#### deleteStates (del\_states)

Delete given iterable collection of states from the automaton.

Parameters del\_states (set|list) - collection of int representing states

**Note:** delta function will always be rebuilt, regardless of whether the states list to remove is a suffix, or a sublist, of the automaton's states list.

#### deterministicP()

Verify whether this NFA is actually deterministic

#### Return type bool

```
dotFormat (size='20, 20', direction='LR', sep='n')
```

A dot representation :arg direction: direction of drawing :arg size: size of image :arg sep: line separator :return: the dot representation type sep: str :type direction: str :type size: str :rtype: str

New in version 0.9.6.

Changed in version 0.9.8.

#### dup()

Duplicate the basic structure into a new NFA. Basically a copy.deep.

# Return type NFA

# elimEpsilon()

Eliminate epsilon-transitions from this automaton.

:rtype: NFA

**Attention:** performs in place modification of automaton

Changed in version 1.1.1.

#### eliminateEpsilonTransitions()

Eliminates all epslilon-transitions with no state addition

**Attention:** in-place modification

#### eliminateTSymbol(symbol)

Delete all trasitions through a given symbol

**Parameters symbol** (*str*) – the symbol to be excluded from delta

**Attention:** in place alteration of the automata

New in version 0.9.6.

#### enumNFA(n=None)

returns the set of words of words of length up to n accepted by self :param n: highest length or all words if finite :type n: int

**Return type** list of strings or None

# epsilonClosure(st)

Returns the set of states epsilon-connected to from given state or set of states.

**Parameters st** (*int*|*set*) – state index or set of state indexes

Returns the list of state indexes epsilon connected to st

Return type set of int

Attention: st must exist.

#### epsilonP()

Whether this NFA has epsilon-transitions

Return type bool

# epsilonPaths (start, end)

All states in all paths (DFS) through empty words from a given starting state to a given ending state.

# **Parameters**

- start (int) start state
- **end** (*int*) end state

**Returns** states in epsilon paths from start to end

Return type set of states

#### equivReduced (equiv\_classes)

Equivalent NFA reduced according to given equivalence classes.

Parameters equiv\_classes (UnionFind) – Equivalence classes

Returns Equivalent NFA

Return type NFA

# evalSymbol(stil, sym)

Set of states reacheable from given states through given symbol and epsilon closure.

**Parameters** 

- stil (set|list) set of current states
- sym (str) symbol to be consumed

**Returns** set of reached state indexes

**Return type** set[int]

Raises DFAsymbolUnknown if symbol is not in alphabet

#### evalWordP (word)

Verify if the NFA recognises given word.

**Parameters word** (str) – word to be recognised

Return type bool

# finalCompP(s)

Verify whether there is a final state in strongly connected component containing given state.

Parameters s (int) – state index

Returns :: bool

#### half()

Half operation

New in version 0.9.6.

#### hasTransitionP (state, symbol=None, target=None)

Whether there's a transition from given state, optionally through given symbol, and optionally to a specific target.

#### **Parameters**

- state (int) source state
- **symbol** (*str*) optional transition symbol
- target (int) optional target state

**Returns** if there is a transition

Return type bool

#### homogenousP(x)

Whether this NFA is homogenous; that is, for all states, whether all incoming transitions to that state are through the same symbol.

**Parameters** x – dummy parameter to agree with the method in DFAr

Return type bool

# initialComp()

Evaluate the connected component starting at the initial state.

**Returns** list of state indexes in the component

Return type list of int

# lEquivNFA()

Equivalent NFA obtained from merging equivalent states from autobisimulation of this NFA's reversal.

Return type NFA

**Note:** returns copy of self if autobisimulation renders no equivalent states.

#### lrEquivNFA()

Equivalent NFA obtained from merging equivalent states from autobisimulation of this NFA, and from autobisimulation of its reversal; i.e., merges all states that are equivalent w.r.t. the largest right invariant and largest left invariant equivalence relations.

#### Return type NFA

**Note:** returns copy of self if autobisimulations render no equivalent states.

#### minimal()

Evaluates the equivalent minimal DFA

Returns equivalent minimal DFA

Return type DFA

#### minimalDFA()

Evaluates the equivalent minimal complete DFA

Returns equivalent minimal DFA

Return type DFA

#### product (other)

Returns a NFA (skeletom) resulting of the simultaneous execution of two DFA.

**Parameters other** (NFA) – the other automata

Return type NFA

Note: No final states are set.

#### **Attention:**

- •the name EmptySet is used in a unique special state name
- •the method uses 3 internal functions for simplicity of code (really!)

#### rEquivNFA()

Equivalent NFA obtained from merging equivalent states from autobisimulation of this NFA.

Return type NFA

**Note:** returns copy of self if autobisimulation renders no equivalent states.

#### reorder (dicti)

Reorder states indexes according to given dictionary.

Parameters dicti (dictionary) – state name reorder

Note: dictionary does not have to be complete

#### reversal()

Returns a NFA that recognizes the reversal of the language

Returns NFA recognizing reversal language

Return type NFA

# reverseTransitions (rev)

Evaluate reverse transition function.

Parameters rev (NFA) - NFA in which the reverse function will be stored

# setInitial(statelist)

Sets the initial states of an NFA

**Parameters statelist** (*set\list\lint*) – an iterable of initial state indexes

# $\verb|shuffle|(other)|$

Shuffle of a NFA

**Parameters other** (FA) – an FA

```
Returns the resulting NFA
         Return type NFA
star (flag=False)
     Kleene star of a NFA
         Parameters flag (Boolean) – plus instead of star
         Returns the resulting NFA
         Return type NFA
stateChildren (state, strict=False)
     Set of children of a state
         Parameters
             • strict (bool) – if not strict a state is never its own child even if a self loop is in place
             • state (int) – state id queried
         Returns children states
         Return type Set of int
stronglyConnectedComponents()
     Strong components
         Return type list
     New in version 1.0.
subword()
     returns a nfa that recognizes subword(L(self))
         Return type nfa
succintTransitions()
     Collects the transition information in a concat way suitable for graphical representation. :rtype: list
toDFA()
     Construct a DFA equivalent to this NFA, by the subset construction method.
         Return type DFA
     Note: valid to epsilon-NFA
toGFA()
     Creates a GFA equivalent to NFA
         Returns a GFA deep copy
         Return type GFA
toNFA()
    Dummy identity function
         Return type NFA
toNFAr()
     NFA with the reverse mapping of the delta function.
         Returns shallow copy with reverse delta function added
```

**usefulStates** (*initial\_states=None*)
Set of states reacheable from the given initial state(s) that have a path to a final state.

Return type NFAr

uniqueRepr()

Dummy representation. Used DFA.uniqueRepr():rtype: tuple

Parameters initial\_states (set of int or list of int) – set of initial states

**Returns** set of state indexes

Return type set of int

#### static vDescription()

Generation of Verso interface description

New in version 0.9.5.

**Returns** the interface list

#### witness()

Witness of non emptyness

Returns word

Return type str

#### wordImage (word, ist=None)

Evaluates the set of states reached consuming given word

#### **Parameters**

- word (list of stings) the word
- **ist** (*int*) starting state index (or set of)

**Returns** the set of ending states

Return type Set of int

# 2.6 Class NFAr (Nondeterministic Finite Automata w/ reverse transition f.)

#### class fa.NFAr

Bases: fa.NFA

Class for Non-deterministic Finite Automata with reverse delta function added by construction.



Variables deltaReverse – the reversed transition function

Note: Includes efficient methods for merging states.

# addTransition (sti1, sym, sti2)

Adds a new transition. Transition is from stil to stil consuming symbol sym. stil is a unique state, not a set of them. Reversed transition function is also computed

#### **Parameters**

- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- **sym** (*str*) symbol consumed

### delTransition (sti1, sym, sti2, \_no\_check=False)

Remove a transition if existing and perform cleanup on the transition function's internal data structure and in the reversal transition function

#### **Parameters**

- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- sym (str) symbol consumed
- no check (bool) dismiss secure code

#### deleteStates (del\_states)

Delete given iterable collection of states from the automaton. Performe deletion in the transition function and its reversal.

**Parameters del\_states** (set or list of int) – collection of int representing states

### elimEpsilonO()

Eliminate epsilon-transitions from this automaton, with reduction of states through elimination of epsilon-cycles, and single epsilon-transition cases.

Returns itself

Return type

Attention: performs inplace modification of automaton

### homogenousP (inplace=False)

Checks is the automaton is homogenous, i.e.the transitions that reaches a state have all the same label.

**Parameters inplace** (bool) – if True performs epsilon transitions elimination

Returns True if homogenous

Return type bool

### mergeStates(f, t)

Merge the first given state into the second. If first state is an initial or final state, the second becomes respectively an initial or final state.

### **Parameters**

- **f** (*int*) index of state to be absorbed
- **t** (*int*) index of remaining state

**Attention:** It is up to the caller to remove the disconnected state. This can be achieved with `trim().

### mergeStatesSet (tomerge, target=None)

Merge a set of states with a target merge state. If the states in the set have transitions among them, those transitions will be directly merged into the target state.

#### **Parameters**

- tomerge (Set of initegers) set of states to merge with target
- target (int) optional target state

**Note:** if target state is not given, the minimal index with be considered.

**Attention:** The states of the list will become unreacheable, but won't be removed. It is up to the caller to remove them. That can be achieved with trim().

#### toNFA()

Turn into an instance of NFA, and remove the reverse mapping of the delta function.

**Returns** shallow copy without reverse delta function

Return type NFA

### unlinkSoleIncoming(state)

If given state has only one incoming transition (indegree is one), and it's through epsilon, then remove such transition and return the source state.

**Parameters state** (*int*) – state to check

Returns source state

**Return type** int or None

Note: if conditions aren't met, returned source state is None, and automaton remains unmodified.

#### unlinkSoleOutgoing(state)

If given state has only one outgoing transition (outdegree is one), and it's through epsilon, then remove such transition and return the target state.

Parameters state (int) – state to check

Returns target state

Return type int or None

Note: if conditions aren't met, returned target state is None, and automaton remains unmodified.

## 2.7 Class GFA (Generalized Finite Automata)

#### class fa.GFA

Bases: fa.OFA

Class for Generalized Finite Automata: NFA with a unique initial state and transitions are labeled with regexp.



DFS (io)

Depth first search

Parameters io -

addTransition(sti1, sym, sti2)

Adds a new transition from stil to stil consuming symbol sym. Label of the transition function is a regexp.

### **Parameters**

- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- sym (str) symbol consumed

### Raises DFAepsilonRedefenition if sym is Epsilon

### assignLow(st)

Parameters st -

assignNum(st)

Parameters st -

#### completeDelta()

Adds empty set transitions between the automatons final and initial states in order to make it complete. It's only meant to be used in the final stage of SEA...

#### deleteState(sti)

deletes a state from the GFA :param sti:

dfs\_visit(s, visited, io)

#### **Parameters**

- **s** state
- visited list od states visited
- io -

### dup()

Returns a copy of a GFA

Return type GFA

#### eliminate(st)

Eliminate a state.

Parameters st (int) – state to be eliminated

### eliminateAll(lr)

Eliminate a list of states.

**Parameters** Ir (*list*) – list of states indexes

### eliminateState(st)

Deletes a state and updates the automaton

Parameters st (state index) – the state to be deleted

### normalize()

Create a single initial and final state with Epsilon transitions.

Attention: works in place

#### reorder (dictio)

Reorder states indexes according to given dictionary.

Parameters dictio (dictionary) – order

Note: dictionary does not have to be complete

### stateChildren (state, strict=False)

Set of children of a state

#### **Parameters**

- strict (bool) a state is never its own children even if a self loop is in place
- state (int) state id queried

Returns map: children -> alphabetic length

### Return type dictionary

#### weight (state)

Calculates the weight of a state based on a heuristic

Parameters state (int) – state

Returns the weight of the state

Return type int

weightWithCycles (state, cycles)

#### **Parameters**

- state -
- cycles -

Returns

# 2.8 Class SSemiGroup (Syntactic SemiGroup)

### class fa.SSemiGroup

Bases: object

Class support for the Syntactic SemiGroup.

#### Variables

- **elements** list of tuples representing the transformations
- words a list of pairs (index of the prefix transformation, index of the suffix char)
- gen a list of the max index of each generation
- **Sigma** set of symbols

### WordI(i)

Representative of an element given as index

Parameters i (int) – index of the element

Returns the first word originating the element

Return type str

WordPS (pref, sym)

Representative of an element given as prefix symb

### **Parameters**

- **pref** (*int*) prefix index
- **sym** (*int*) symbol index

Returns word

Return type str

add (tr, pref, sym, tmpLists)

Try to add a new transformation to the monoid

### **Parameters**

- **tr** (*tuple of int*) transformation
- **pref** (*int or None*) prefix of the generating word
- **sym** (*int*) suffix symbol
- tmpLists (pairs of lists as (elements, words)) this generation lists

### addGen (tmpLists)

Add a new generation to the monoid

Parameters tmpLists (pair of lists as (elements, words)) – the new generation data

# 2.9 Class EnumL (Language Enumeration)

### class fa.EnumL (aut, store=False)

Bases: object

Class for enumerate FA languages

### Variables

- aut Automaton of the language
- tmin table for minimal words for each s in aut.States
- Words list of words (if stored)
- Sigma alphabet

New in version 0.9.8.

#### See also:

Efficient enumeration of words in regular languages, M. Ackerman and J. Shallit, Theor. Comput. Sci. 410, 37, pp 3461-3470. 2009. http://dx.doi.org/10.1016/j.tcs.2009.03.018

#### enum(m)

Enumerates the first m words of L(A) according to the lexicographic order if there are at least m words. Otherwise, enumerates all words accepted by A.

Parameters m (int) -

### ${\tt enumCrossSection}\,(n)$

Enumerates the nth cross-section of L(A)

Parameters n (int) – nonnegative integer

### fillStack(w)

Abstract method :param w: :type w: str

### $\verb|iCompleteP|(i,q)$

Tests if state q is i-complete

### **Parameters**

- **i** (*int*) int
- q (int) state index

### initStack()

Abstract method

### minWord(m)

Computes the minimal word of length m accepted by the automaton :param m: :type m: int

### minWordT(n)

Abstract method :param n: :type n: int

#### nextWord(w)

Abstract method :param w: :type w: str

## 2.10 Functions

### fa.saveToString(aut, sep='&')

Finite automata definition as a string using the input format.

New in version 0.9.5.

Changed in version 0.9.6: Names are now used instead of indexes.

Changed in version 0.9.7: New format with quotes and alphabet

#### **Parameters**

- aut (FA) the FA
- **sep** (*str*) separation between *lines*

**Returns** the representation

Return type str

### fa.stringToDFA(s, f, n, k)

Converts a string icdfa's representation to dfa.

### **Parameters**

- $\mathbf{s}$  (*list*) canonical string representation
- **f** (*list*) bit map of final states
- **n** (*int*) number of states
- **k** (*int*) number of symbols

**Returns** a complete dfa with Sigma [k], States [n]

### Return type DFA

Changed in version 0.9.8: symbols are converted to str

CHAPTER

**THREE** 

# MODULE: COMMON DEFINITIONS ("COMMON")

**Common definitions for FAdo files** 

# 3.1 Class Word

```
class common.Word(it=[])
Bases: object
```

Class to implement generic words as iterables with pretty-print

Basically a unified way to deal with words with caracters of of sizes different of one with no much fuss

# **MODULE: FADO IO FUNCTIONS ("FIO")**

#### In/Out.

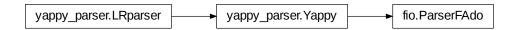
FAdo IO.

# 4.1 Class ParserFAdo (Yappy parser for FAdo FA files)

class fio.ParserFAdo (no\_table=1, table='.tableFAdo')

Bases: yappy\_parser.Yappy

A parser for FAdo standard automata descriptions



## 4.2 Functions

#### fio.readFromFile(FileName)

Reads list of finite automata definition from a file.

**Parameters FileName** (str) – file name

Return type list

The format of these files must be the as simple as possible:

- •# begins a comment
- •@DFA or @NFA begin a new automata (and determines its type) and must be followed by the list of the final states separated by blanks
- $\bullet fields$  are separated by a blank and transitions by a CR: state  ${\tt symbol}$  new  ${\tt state}$
- •in case of a NFA declaration, the "symbol" @epsilon is interpreted as a epsilon-transition
- •the source state of the first transition is the initial state
- •in the case of a NFA, its declaration @NFA can, after the declaration of the final states, have a  $\star$  followed by the list of initial states
- •both, NFA and DFA, may have a declaration of alphabet starting with a \$ followed by the symbols of the alphabet
- •a line with a sigle name, decrares a state

```
FAdo ::= FA | FA CR FAdo
```

FA ::= DFA | NFA | Transducer

```
DFA
                "@DFA" LsStates Alphabet CR dTrans
           ::=
NFA
           ::=
                "@NFA" LsStates Initials Alphabet CR nTrans
Transducer ::= "@Transducer" LsStates Initials Alphabet Output CR tTrans
Initials ::= "*" LsStates | \epsilon
Alphabet ::= "$" LsSymbols | \epsilon
          ::= "$" LsSymbols | \epsilon
Output
nSymbol
          ::= symbol | "@epsilon"
LsStates
           ∷= stateid | stateid , LsStates
LsSymbols ::= symbol | symbol , LsSymbols
dTrans
       ::= stateid symbol stateid |
              | stateid symbol stateid CR dTrans
nTrans
           ::= stateid nSymbol stateid |
               | stateid nSymbol stateid CR nTrans
tTrans
           ::=
               stateid nSymbol nSymbol stateid |
               | stateid nSymbol nSymbol stateid CR nTrans
```

**Note:** If an error occur, either syntactic or because of a violation of the declared automata type, an exception is raised

Changed in version 0.9.6.

Changed in version 1.0.

### fio.saveToFile(FileName, fa, mode='a')

Saves a list finite automata definition to a file using the input format

Changed in version 0.9.5.

Changed in version 0.9.6.

Changed in version 0.9.7: New format with quotes and alphabet

### **Parameters**

- **FileName** (*str*) file name
- fa (list of FA) the FA
- **mode** (*str*) writing mode

# MODULE: REGULAR EXPRESSIONS (REEX)

### Regular expressions manipulation

Regular expression classes and manipulation

# 5.1 Class regexp (regular expression)

class reex.regexp(val, sigma=None)

Bases: object

Base class for regular expressions.

Used directly to represent a symbol. The type of the symbol is arbitrary.

#### Variables

- Sigma alphabet set of strings
- val the actual symbol

reex.regexp

Constructor of a regular expression symbol.

Parameters val – the actual symbol

**PD**()

Closure of partial derivatives of the regular expression in relation to all words.

**Returns** set of regular expressions

Return type set

See also:

Antimirov, 95

### alphabeticLength()

Number of occurrences of alphabet symbols in the regular expression.

Return type integer

Attention: Doesn't include the empty word.

```
compare (r, cmp_method='compareMinimalDFA', nfa_method='nfaPosition')
```

Compare with another regular expression for equivalence. :param r: :param cmp\_method: :param nfa\_method:

### compareMinimalDFA (r, nfa\_method='nfaPosition')

Compare with another regular expression for equivalence through minimal DFAs. :param r: :param nfa method:

#### derivative (sigma)

Derivative of the regular expression in relation to the given symbol.

**Parameters sigma** – an arbitrary symbol.

Return type regular expression

**Note:** whether the symbols belong to the expression's alphabet goes unchecked. The given symbol will be matched against the string representation of the regular expression's symbol.

#### See also:

10. (a)Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)

#### dfaPosition()

Deterministic position automaton of a regular expression.

**Returns** position DFA

Return type DFA

Raises common.DFAnotNFAFAdo if not DFA

**Note:** If this expression is not linear (cf. linearP()), exception may be raised on non-deterministic transitions.

### emptyP()

Whether the regular expression is the empty set.

Return type Boolean

### epsilonLength()

Number of occurrences of the empty word in the regular expression.

Return type integer

### epsilonP()

Whether the regular expression is the empty word.

**Return type** Boolean

### equivalentP(other)

Tests equivalence

Parameters other -

Return type bool

### evalWordP (word)

Verifies if a word is a member of the language represented by the regular expression.

Parameters word (str) – the word

Return type bool

### ewp()

Whether the empty word property holds for this regular expression's language.

Return type Boolean

#### first (parent\_first=None)

List of possible symbols matching the first symbol of a string in the language of the regular expression.

#### Parameters parent first -

**Returns** list of symbols

#### followLists(lists=None)

Map of each symbol's follow list in the regular expression.

Parameters lists -

**Returns** map of symbols' follow lists **Return type** {symbol: list of symbols}

**Attention:** For first() and last() return lists, the follow list for certain symbols might have repetitions in the case of follow maps calculated from star operators. The union of last(), first() and follow() sets are always disjoint when the regular expression is in star normal form (Brüggemann-Klein, 92), therefore FAdo implements them as lists. You should order exclusively, or take a set from a list in order to resolve repetitions.

#### followListsD (lists=None)

Map of each symbol's follow list in the regular expression.

Parameters lists -

**Returns** map of symbols' follow lists **Return type** {symbol: list of symbols}

**Attention:** For first() and last() return lists, the follow list for certain symbols might have repetitions in the case of follow maps calculated from star operators. The union of last(), first() and follow() sets are always disjoint

### See also:

Sabine Broda, António Machiavelo, Nelma Moreira, and Rogério Reis. On the average size of glushkov and partial derivative automata. International Journal of Foundations of Computer Science, 23(5):969-984, 2012.

### followListsStar(lists=None)

Map of each symbol's follow list in the regular expression under a star.

Parameters lists -

**Returns** map of symbols' follow lists **Return type** {symbol: list of symbols}

## last (parent\_last=None)

List of possible symbols matching the last symbol of a string in the language of the regular expression.

Parameters parent\_last -

**Returns** list of symbols

Return type list

#### linearForm()

Linear form of the regular expression, as a mapping from heads to sets of tails, so that each pair (head, tail) is a monomial in the set of linear forms.

Returns dictionary mapping heads to sets of tails

**Return type** {symbol: set([regular expressions])}

#### See also:

Antimirov, 95

#### linearP()

Whether the regular expression is linear; i.e., the occurrence of a symbol in the expression is unique.

### Return type boolean

#### marked()

Regular expression in which every alphabetic symbol is marked with its position.

The kind of regular expression returned is known, depending on the literary source, as marked, linear or restricted regular expression.

**Returns** linear regular expression

Return type regexp

### See also:

R. McNaughton and H. Yamada, Regular Expressions and State Graphs for Automata, IEEE Transactions on Electronic Computers, V.9 pp:39-47, 1960

..attention: mark and unmark do not preserve the alphabet, neither set the new alphabet

### measure (from\_parent=None)

A list with four measures for regular expressions.

### Parameters from\_parent -

**Return type** [int,int,int,int]

[alphabeticLength, treeLength, epsilonLength, starHeight]

1.alphabeticLength: number of occurences of symbols of the alphabet;

2.treeLength: number of functors in the regular expression, including constants.

3.epsilonLength: number of occurrences of the empty word.

4.starHeight: highest level of nested Kleene stars, starting at one for one star occurrence.

**Attention:** Methods for each of the measures are implemented independently. This is the most effective for obtaining more than one measure.

#### nfaFollow()

NFA that accepts the regular expression's language, whose structure, and construction.

### Return type NFA

## See also:

Ilie & Yu (Follow Automata, 03)

#### nfaFollowEpsilon(trim=True)

Epsilon-NFA constructed with Ilie and Yu's method () that accepts the regular expression's language.

### Parameters trim -

**Returns** NFA possibly with epsilon transitions

Return type NFAe

#### See also:

Ilie & Yu, Follow automta, Inf. Comp., v. 186 (1),140-162,2003

### nfaGlushkov()

Position or Glushkov automaton of the regular expression. Recursive method.

**Returns** NFA

#### nfaNaiveFollow()

NFA that accepts the regular expression's language, and is equal in structure to the follow automaton.

### Return type NFA

**Note:** Included for testing purposes.

### See also:

Ilie & Yu (Follow Automata, 2003)

#### nfaPD()

**NFA that accepts the regular expression's language,** and which is constructed from the expression's partial derivatives.

**Returns** partial derivatives [or equation] automaton

Return type NFA

#### See also:

V. M. Antimirov, Partial Derivatives of Regular Expressions and Finite Automaton Constructions .Theor. Comput. Sci.155(2): 291-319 (1996)

#### nfaPDO()

NFA that accepts the regular expression's language, and which is constructed from the expression's partial derivatives.

Note: optimized version

**Returns** partial derivatives [or equation] automaton

Return type NFA

### nfaPSNF()

Position or Glushkov automaton of the regular expression constructed from the expression's star normal form.

Returns position automaton

Return type NFA

### nfaPosition (lstar=True)

Position automaton of the regular expression.

Parameters Istar (boolean) – if not None followlists are computed dijunct

**Returns** position NFA

Return type NFA

#### nfaThompson()

Epsilon-NFA constructed with Thompson's method that accepts the regular expression's language.

**Return type** NFA

### See also:

11. Thompson. Regular Expression Search Algorithm. CACM 11(6), 419-422 (1968)

### partialDerivatives (sigma)

Set of partial derivatives of the regular expression in relation to given symbol.

Parameters sigma – symbol in relation to which the derivative will be calculated.

```
Returns set of regular expressions
```

#### See also:

Antimirov, 95

### reduced (hasEpsilon=False)

Equivalent regular expression with the following cases simplified:

- 1.Epsilon.RE = RE.Epsilon = RE
- 2.EmptySet.RE = RE.EmptySet = EmptySet
- 3.EmptySet + RE = RE + EmptySet = RE
- 4.Epsilon + RE = RE + Epsilon = RE, where Epsilon is in L(RE)
- $5.RE^{**} = RE^{*}$
- 6.EmptySet\* = Epsilon\* = Epsilon

**Parameters hasEpsilon** – used internally to indicate that the language of which this term is a subterm has the empty word.

Returns regular expression

**Attention:** Returned structure isn't strictly a duplicate. Use \_\_copy\_\_() for that purpose.

#### reversal()

Reversal of regexp

#### Return type regexp

#### rpn()

RPN representation :return: printable RPN representation

### setOfSymbols()

Set of symbols that occur in a regular expression..

**Returns** set of symbols

Return type set of symbols

### setSigma (symbolSet, strict=False)

Set the alphabet for a regular expression and all its nodes

### **Parameters**

- symbolSet (list or set of str) accepted symbols. If None, alphabet is unset.
- strict (bool) if True checks if setOfSymbols is included in symbolSet

..attention: Normally this attribute is not defined in a regexp()

### snf (hollowdot=False)

Star Normal Form (SNF) of the regular expression.

### Parameters hollowdot -

Returns regular expression in star normal form

### starHeight()

Maximum level of nested regular expressions with a star operation applied.

For instance, starHeight(((a\*b)\*+b\*)\*) is 3.

### Return type integer

### stringLength()

Length of the string representation of the regular expression.

### Return type integer

### support()

'Support of a regular expression.

Returns set of regular expressions

Return type set

#### See also:

Champarnaud, J.M., Ziadi, D.: From Mirkin's prebases to Antimirov's word partial derivative. Fundam. Inform. 45(3), 195-205 (2001)

#### toDFA()

DFA that accepts the regular expression's language

#### toNFA (nfa\_method='nfaPD')

NFA that accepts the regular expression's language. :param nfa\_method:

### treeLength()

Number of nodes of the regular expression's syntactical tree.

Return type integer

### unmarked()

The unmarked form of the regular expression. Each leaf in its syntactical tree becomes a regexp(), the epsilon() or the emptyset().

Return type (general) regular expression

### wordDerivative (word)

**Derivative of the regular expression in relation to the given word,** which is represented by a list of symbols.

**Parameters word** – list of arbitrary symbols.

Return type regular expression

### See also:

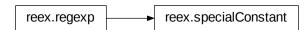
10. (a)Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)

# 5.2 Class specialConstant

class reex.specialConstant(sigma=None)

Bases: reex.regexp

Base class for Epsilon and EmptySet



Parameters sigma -

alphabeticLength()

Returns

```
derivative (sigma)
        Parameters sigma -
        Returns
first (parent_first=None)
        Parameters parent_first -
        Returns
followLists(lists=None)
        Parameters lists -
        Returns
followListsD (lists=None)
        Parameters lists -
        Returns
followListsStar(lists=None)
        Parameters lists -
        Returns
last (parent_last=None)
        Parameters parent_last -
        Returns
linearForm()
        Returns
reversal()
    Reversal of regexp
        Return type regexp
setOfSymbols()
        Returns
support()
        Returns
unmarked()
    The unmarked form of the regular expression. Each leaf in its syntactical tree becomes a regexp(), the
    epsilon() or the emptyset().
        Return type (general) regular expression
wordDerivative(word)
        Parameters word -
        Returns
```

# 5.3 Class epsilon

```
class reex.epsilon (sigma=None)
    Bases: reex.specialConstant
    Class that represents the empty word.
```



```
Parameters sigma -
epsilonLength()
        Return type int
epsilonP()
        Return type bool
ewp()
        Return type bool
measure (from_parent=None)
        Parameters from_parent -
        Returns measures
nfaThompson()
        Return type NFA
partialDerivatives (sigma)
        Parameters sigma -
        Returns
rpn()
        Returns str
snf (_hollowdot=False)
        Parameters _hollowdot -
        Returns
```

# 5.4 Class emptyset

```
class reex.emptyset (sigma=None)
    Bases: reex.specialConstant
    Class that represents the empty set.
```



Parameters sigma -

```
emptyP()
    Returns
epsilonLength()
    Returns
epsilonP()
    Returns
ewp()
    Returns
measure(from_parent=None)
    Parameters from_parent -
    Returns
rpn()
    Returns
```

# 5.5 Class connective

```
class reex.connective (arg1, arg2, sigma=None)
    Bases: reex.regexp
```

Base class for concatenation, and disjunction operations.



## 5.6 Class star

```
class reex.star(arg, sigma=None)
    Bases: reex.regexp
```

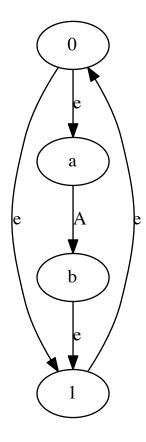
Class for iteration operation (aka Kleene star, or Kleene closure) on regular expressions.



```
nfaThompson()
```

Returns a NFA that accepts the RE.

Return type NFA



### reversal()

Reversal of regexp

Return type regexp

## 5.7 Class concat

class reex.concat (arg1, arg2, sigma=None)

 $Bases: \verb"reex.connective"$ 

Class for catenation operation on regular expressions.



### reversal()

Reversal of regexp :rtype: regexp

5.7. Class concat

# 5.8 Class disj

class reex.disj(arg1, arg2, sigma=None)

Bases: reex.connective

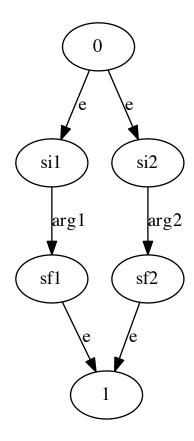
Class for disjuction operation on regular expressions.



### nfaThompson()

Returns an NFA (Thompson) that accepts the RE.

### Return type NFA



### reversal()

Reversal of regexp :rtype: regexp

# 5.9 Class position

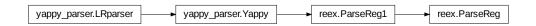
```
class reex.position((sym, pos), sigma=None)
    Bases: reex.regexp
```

Class for marked regular expression symbols.



# 5.10 Class ParseReg

class reex.ParseReg(no\_table=0, table='tableambreg')
 Bases: reex.ParseReg1



A parser for regular expressions with ambiguous rules: not working

## 5.11 Functions

reex.str2regexp(s, parser=<class 'reex.ParseReg1'>, no\_table=1, sigma=None, strict=False)
Reads a regexp from string.

### **Parameters**

- $\mathbf{s}$  (string) the string representation of the regular expression
- **parser** (*Yappy*) a parser generator for regexps
- no\_table (integer) -
- sigma (list or set of symbols) alphabet of the regular expression
- **strict** (*boolean*) if True tests if the symbols of the regular expression are included in the sigma

Return type regexp

reex.rpn2regexp (s, sigma=None, strict=False)
Reads a regexp from a RPN representation

Parameters s (string) – RPN representation

5.11. Functions 55

## Return type regexp

**Note:** This method uses python stack... thus depdth limitations apply

# MODULE: EXTENDED REGULAR EXPRESSIONS (XRE)

### **Extended regular expressions manipulation**

Extended regular expression classes and its manipulation

New in version 0.9.8.

# 6.1 Class xre (extended regular expression)

```
class xre.xre(val, sigma=None)
```

Bases: reex.regexp

Base class for extended regular expressions, used directly to represent a symbol.

Variables val – the actual symbol

Constructor of a regular expression symbol.

Parameters val – the actual symbol

**PD**()

Closure of partial derivatives of the regular expression in relation to all words.

**Returns** set of regular expressions

Return type set

compare (r, cmp\_method='equivP', nfa\_method=None)

Compare with another regular expression for equivalence. :param r: :param cmp\_method: :param nfa\_method:

#### concatenation(r)

Computes the concatenation of two regular expressions.

**Parameters**  $\mathbf{r}$  (*xre*) – a regular expression

Return type xre

derivative (sigma)

Derivative of the regular expression in relation to the given symbol.

**Parameters** sigma – an arbitrary symbol.

Return type regular expression

**Note:** whether the symbols belong to the expression's alphabet goes unchecked. The given symbol will be matched against the string representation of the regular expression's symbol.

#### See also:

10. (a)Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)

```
dfaDerivatives()
     Word derivatives automaton of the regular expression
         Returns word derivatives automaton
         Return type DFA
     See also:
       10. (a)Brzozowski, Derivatives of Regular Expressions. J. ACM 11(4): 481-494 (1964)
dfs()
     Minimal DFA of an extended regular expression :return: minimal DFA :rtype: DFA
equivP(reg)
     Verifies if two regular expressions are equivalent.
         Parameters reg – regular expression
         Return type bool
intersection(sx)
     Computes the intersection of two regular expressions.
         Parameters \mathbf{sx} (xre) – a regular expression
         Return type xre
linearForm()
     Linear form of the extended regular expression, as a mapping from heads to sets of tails, so
         that each pair (head,tail) is a monomial in the set of linear forms.
         Returns dictionary mapping heads to sets of tails
         Return type {symbol: set([regular expressions])}
     See also:
     Antimirov, 95
nfaPD()
     NFA that accepts the regular expression's language, and which is constructed from the expression's partial
         derivatives.
         Returns partial derivatives [or equation] automaton
         Return type NFA
     See also:
     V. M. Antimirov, Partial Derivatives of Regular Expressions and Finite Automaton Constructions.
     Theor. Comput. Sci.155(2): 291-319 (1996)
     ..attention why different from reex.nfaPD
partialDerivativeC (sigma)
         Parameters sigma -
         Return type xre
support()
     'Support of a regular expression.
         Returns set of regular expressions
         Return type set
```

#### See also:

Champarnaud, J.M., Ziadi, D.: From Mirkin's prebases to Antimirov's word partial derivative. Fundam. Inform. 45(3), 195-205 (2001)

```
toDFA (dfa_method='dfaDerivatives')
```

DFA that accepts the regular expression's language. :param dfa\_method:

```
toNFA (nfa_method='nfaPD')
```

NFA that accepts the regular expression's language. :param nfa\_method:

### unionSigma(reg)

Returns the union of two alphabets

Parameters reg - xre

Return type set

## 6.2 Functions

```
xre.to_x (reg)
```

Reads xre from FAdo regexp.

### **Parameters**

- **reg** (*regexp*) –
- re the FAdo representation regexp for a regular expression.

Return type xre

6.2. Functions 59

# MODULE: TRANSDUCERS (TRANSDUCERS)

### **Finite Tranducer Support**

Transducer manipulation.

New in version 1.0.

## 7.1 Class Transducer

class transducers. Transducer

Bases: fa.NFA

Base class for Transducers



setOutput (listOfSymbols)

Set Output

**Parameters listOfSymbols** (*set\list*) – output symbols

#### succintTransitions()

Collects the transition information in a concat way suitable for graphical representation. :rtype: list of tupples

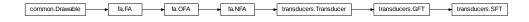
# 7.2 Class SFT (Standard Form Transducers)

class transducers.SFT

 $Bases: \verb|transducers.GFT| \\$ 

Standard Form Tranducer

Variables Output (set) – output alphabet



### addEpsilonLoops()

Add a loop transition with epsilon input and output to every state in the transducer.

### addOutput (sym)

Add a new symbol to the output alphabet

There is no problem with duplicate symbols because Output is a Set. No symbol Epsilon can be added

Parameters sym (str) – symbol or regular expression to be added

```
addTransition (stsrc, symi, symo, sti2)
```

Adds a new transition

#### **Parameters**

- stsrc (int) state index of departure
- sti2 (int) state index of arrival
- symi (str) symbol consumed
- **symo** (*str*) symbol output

## addTransitionQ (src, dest, sym, out, futQ, pastQ)

Add transition to the new transducer instance.

#### **Parameters**

- src source state
- **dest** destination state
- sym symbol
- out output
- **futQ** (*set*) queue for later
- pastQ (set) past queue

### composition (other)

Composition operation of a transducer with a transducer.

**Parameters other** (SFT) – the second transducer

**Return type** SFT

### concat (other)

Concatenation of transducers

**Parameters other** (SFT) – the other operand

Return type SFT

### ${\tt delTransition}~(sti1, sym, symo, sti2, \_no\_check = False)$

Remove a transition if existing and perform cleanup on the transition function's internal data structure.

### **Parameters**

- **symo** symbol output
- sti1 (int) state index of departure
- sti2 (int) state index of arrival
- sym symbol consumed
- \_no\_check (bool) dismiss secure code

### deleteState(sti)

Remove given state and transitions related with that state.

**Parameters sti** (*int*) – index of the state to be removed

Raises DFAstateUnknown if state index does not exist

### deleteStates (lstates)

Delete given iterable collection of states from the automaton.

### Parameters lstates (set|list) – collection of int representing states

### dup()

Duplicate of itself: rtype: SFT

Attention: only duplicates the initially connected component

#### emptyP()

Tests if the relation realized the empty transducer

### Return type bool

#### epsilonOutP()

Tests if epsilon occurs in transition outputs

### Return type bool

### epsilonP()

Test whether this transducer has input epsilon-transitions

### Return type bool

#### evalWordP (wp)

Tests whether the transducer returns the second word using the first one as input

Parameters wp (tuple) – pair of words

Return type bool

### functionalP()

Tests if a transducer is functional using Allauzer & Mohri and Béal&Carton&Prieur&Sakarovitch algorithms.

### Return type bool

### See also:

Cyril Allauzer and Mehryar Mohri, Journal of Automata Languages and Combinatorics, Efficient Algorithms for Testing the Twins Property, 8(2): 117-144, 2003.

### See also:

M.P. Béal, O. Carton, C. Prieur and J. Sakarovitch. Squaring transducers: An efficient procedure for deciding functionality and sequentiality. Theoret. Computer Science 292:1 (2003), 45-63.

**Note:** This is implemented using nonFunctionalW()

### inIntersection(other)

Conjunction of transducer and automata: X & Y.

**Parameters other** (*DFA*|*NFA*) – the automata needs to be operated.

Return type SFT

### inverse()

Switch the input label with the output label.

No initial or final state changed.

Returns Transducer with transitions switched.

**Return type** SFT

### nonEmptyW()

Witness of non emptyness

Returns pair (in-word, out-word)

Return type tuple

```
nonFunctionalW()
     Returns a witness of non funcionality (if is that the case) or a None filled triple
         Returns witness
         Return type tuple
outIntersection (other)
     Conjunction of transducer and automaton: X & Y using output intersect operation.
         Parameters other (DFA|NFA) – the automaton used as a filter of the output
         Return type SFT
outIntersectionDerived(other)
     Naive version of outIntersection
         Parameters other (DFA|NFA) – the automaton used as a filter of the output
         Return type SFT
outputS(s)
     Output label coming out of the state i
         Parameters s (int) – index state
         Return type set
productInput (other)
     Returns a transducer (skeleton) resulting from the execution of the transducer with the automaton as
     filter on the input.
         Parameters other (NFA) – the automaton used as filter
         Return type SFT
reversal()
     Returns a transducer that recognizes the reversal of the relation.
         Returns Transducer recognizing reversal language
         Return type SFT
runOnNFA (nfa)
     Result of applying a transducer to an automaton
         Parameters nfa (DFA|NFA) – input language to transducer
         Returns resulting language
         Return type NFA
runOnWord (word)
     Returns the automaton accepting the outup of the transducer on the input word
         Parameters word - the word
         Return type NFA
setInitial(sts)
     Sets the initial state of a Transducer
         Parameters sts (list) – list of states
square()
```

Conjunction of transducer with itself (Fast Version)

Return type NFA

Conjunction of transducer with itself

**Return type** NFA

square\_fv()

```
star (flag=False)
```

Kleene star

Parameters flag (bool) – plus instead of star

Returns the resulting Transducer

Return type SFT

### toInNFA()

Delete the output labels in the transducer. Translate it into an NFA

Return type NFA

### toNFT()

Transformation into Nomal Form Transducer

Return type NFT

### toOutNFA()

Returns the result of considering the output symbols of the transducer as input symbols of a NFA (ignoring the input symbol, thus)

Returns the NFA

Return type NFA

### toSFT()

Pacifying rule

Return type SFT

#### trim()

Remove states that do not lead to a final state, or, inclusively, that can't be reached from the initial state. Only useful states remain.

Attention: in place transformation

### union (other)

Union of the two transducers

**Parameters other** (SFT) – the other operand

Return type SFT

## 7.3 Functions

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# MODULE: FINITE LANGUAGES (FL)

Finite languages and related automata manipulation

Finite languages manipulation

## 8.1 Class FL (Finite Language)

```
class fl.FL(wordsList=None, Sigma=set([]))
    Bases: object
```

Finite Language Class

### **Variables**

- Words the elements of the language
- Sigma the alphabet

### addWords (wList)

Adds a list of words to a FL

Parameters wList (list) – words to add

### diff(other)

Difference of FL: a - b

Parameters other (FL) – right hand operand

Return type FL

Raises FAdoGeneralError if both arguments are not FL

### filter(automata)

Separates a language in two other using a DFA of NFA as a filter

Parameters automata (DFA|NFA) – the automata to be used as a filter

Returns the accepted/unaccepted pair of languages

Return type tuple of FL

### intersection (other)

Intersection of FL: a & b

Parameters other (FL) – right hand operand

Raises FAdoGeneralError if both arguments are not FL

#### multiLineAutomaton()

Generates the trivial linear ANFA equivalent to this language

Return type ANFA

### reunion(other)

Reunion of FL: a | b

**Parameters other** (FL) – right hand operand

Return type FL

Raises FAdoGeneralError if both arguments are not FL

setSigma (Sigma, Strict=False)

Sets the alphabet of a FL

#### **Parameters**

- **Sigma** (*set*) alphabet
- Strict (bool) behaviour

**Attention:** Unless Strict flag is set to True, alphabet can only be enlarged. The resulting alphabet is in fact the union of the former alphabet with the new one. If flag is set to True, the alphabet is simply replaced.

### suffixClosedP()

Tests if a language is suffix closed

Return type bool

#### toDFA()

Generates a DFA recognizing the language

**Return type** ADFA

New in version 1.2.

### toNFA()

Generates a NFA recognizing the language

Return type ANFA

New in version 1.2.

### trieFA()

Generates the trie automaton that recognises this language

**Returns** the trie automaton

Return type ADFA

# 8.2 Class DCFA (Deterministic Cover Finite Automata)

### class fl.DCFA

Bases: fa.DFA

Deterministic Cover Automata class



### length

**Returns** size of the longest word

Return type int

# 8.3 Class AFA (Acyclic Finite Automata)

### class fl.AFA

Bases: object

Base class for Acyclic Finite Automata

fl.AFA

Note: This is just a container for some common methods. Not to be used directly!!

#### addState()

Return type int

### directRank()

Compute rank function

**Returns** ranf map

Return type dict

## ensureDead()

Ensures that a state is defined as dead

# ${\tt evalRank}$ ()

Evaluates the rank map of a automaton

Returns pair of sets of states by rank map, reverse delta accessability map

Return type tuple

## getLeaves()

The set of leaves, i.e. final states for last symbols of language words

Returns set of leaves

Return type set

# ordered()

Orders states names in its topological order

**Returns** ordered list of state indexes

Return type list of int

**Note:** one could use the FA.toposort() method, but special care must be taken with the dead state for the algorithms related with cover automata.

### setDeadState (sti)

Identifies the dead state

Parameters sti (int) – index of the dead state

Attention: nothing is done to ensure that the state given is legitimate

Note: without dead state identified, most of the methods for acyclic automata can not be applied

# 8.4 Class ADFA (Acyclic Deterministic Finite Automata)

### class fl.ADFA

Bases: fa.DFA, fl.AFA

Acyclic Deterministic Finite Automata class



### complete (dead=None)

Make the ADFA complete

Parameters dead (int) – a state to be identified as dead state if one was not identified yet

Return type ADFA

**Attention:** The object is modified in place

## dup()

Duplicate the basic structure into a new ADFA. Basically a copy.deep.

## Return type ADFA

### forceToDCFA()

Conversion to DCFA

# Return type DFA

# level()

Computes the level for each state

Returns levels of states

Return type dict

New in version 0.9.8.

#### minDFCA()

Generates a minimal deterministic cover automata from a DFA

## Return type DCFA

New in version 0.9.8.

### See also:

Cezar Campeanu, Andrei Päun, and Sheng Yu, An efficient algorithm for constructing minimal cover automata for finite languages, IJFCS

#### minimal()

Finds the minimal equivalent ADFA

#### See also:

[TCS 92 pp 181-189] Minimisation of acyclic deterministic automata in linear time, Dominique Revuz

Returns the minimal equivalent ADFA

Return type ADFA

#### minimalP (method=None)

Tests if the DFA is minimal

**Parameters method** – minimization algorithm (here void)

Return type bool

# toANFA()

Converts the ADFA in a equivalent ANFA

Return type ANFA

### toNFA()

Converts the ADFA in a equivalent NFA

Return type ANFA

New in version 1.2.

### trim()

Remove states that do not lead to a final state, or, inclusively, that can't be reached from the initial state. Only useful states remain.

**Attention:** in place transformation

### wordGenerator()

Creates a random word generator

Returns the random word generator

Return type RndWGen

New in version 1.2.

# 8.5 Class ANFA (Acyclic Non-deterministic Finite Automata)

#### class fl.ANFA

Bases: fa.NFA, fl.AFA

Acyclic Nondeterministic Finite Automata class



# mergeInitial()

Merge initial states

Attention: object is modified in place

## mergeLeaves()

Merge leaves

Attention: object is modified in place

#### mergeStates (s1, s2)

Merge state s2 into state s1

#### **Parameters**

- **s1** (*int*) state
- **s2** (*int*) state

**Note:** no attempt is made to check if the merging preserves the language of teh automaton

Attention: the object is modified in place

#### moveFinal(st, stf)

Unsets a set as final transfering transition to another final :param int st: the state to be 'moved' :param int stf: the destination final state

**Note:** stf must be a 'last' final state, i.e., must have no out transitions to anywhere but to a possible dead state

Attention: the object is modified in place

# 8.6 Class RndWGen (Random Word Generator)

## class fl.RndWGen(aut)

Bases: object

Word random generator class

New in version 1.2.

Parameters aut (ADFA) – automata recognizing the language

next()

Next word

**Returns** a new random word

# 8.7 Functions

# fl.sigmaInitialSegment(Sigma, l, exact=False)

Generates the ADFA recognizing Sigma^i for i<=l :param set Sigma: the alphabet :param int l: length :param bool exact: only the words with exactly that length? :returns: the automaton :rtype: ADFA

## fl.genRndTrieBalanced(maxL, Sigma, safe=True)

Generates a random trie automaton for a binary language of balanced words of a given leght for max word :param int maxL: length of the max word :param set Sigma: alphabet to be used :param bool safe: should a word of size maxl be present in every language? :return: the generated trie automaton :rtype: ADFA

# fl.genRndTrieUnbalanced(maxL, Sigma, ratio, safe=True)

Generates a random trie automaton for a binary language of balanced words of a given length for max word

## **Parameters**

• maxL (int) – length of the max word

- Sigma (set) alphabet to be used
- ratio (int) the ratio of the unbalance
- safe (bool) should a word of size maxl be present in every language?

**Returns** the generated trie automaton

Return type ADFA

# fl.genRandomTrie (maxL, Sigma, safe=True)

Generates a random trie automaton for a finite language with a given length for max word :param int maxL: length of the max word :param set Sigma: alphabet to be used :param bool safe: should a word of size maxl be present in every language? :return: the generated trie automaton :rtype: ADFA

### fl.genRndTriePrefix (maxL, Sigma, ClosedP=False, safe=True)

Generates a random trie automaton for a finite (either prefix free or prefix closed) language with a given length for max word :param int maxL: length of the max word :param set Sigma: alphabet to be used :param bool ClosedP: should it be a prefix closed language? :param bool safe: should a word of size maxl be present in every language? :return: the generated trie automaton :rtype: ADFA

#### fl.DFAtoADFA(aut)

Transforms an acyclic DFA into a ADFA

**Parameters aut** (*DFA*) – the automaton to be transformed

Raises notAcyclic if the DFA is not acyclic

Returns the converted automaton

Return type ADFA

#### fl.stringToADFA(s)

Convert a canonical string representation of a ADFA to a ADFA :param list s: the string in its canonical order :returns: the ADFA :rtype: ADFA

#### See also:

Marco Almeida, Nelma Moreira, and Rogério Reis. Exact generation of minimal acyclic deterministic finite automata. International Journal of Foundations of Computer Science, 19(4):751-765, August 2008.

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# **MODULE: GRAPHS (GRAPH CREATION AND MANIPULATION)**

# **Graph support**

Basic Graph object support and manipulation

class graphs. Graph

Bases: common.Drawable

Graph base class

#### **Variables**

- **Vertices** (*list*) Vertices' names
- Edges (set) set of pairs (always sorted)



# addEdge (v1, v2)

Adds an edge :param int v1: vertex 1 index :param int v2: vertex 2 index :raises GraphError: if edge is loop

# addVertex(vname)

Adds a vertex (by name)

Parameters vname – vertex name

Returns vertex index

Return type int

Raises DuplicateName if vname already exists

vertexIndex (vname, autoCreate=False)

Return vertex index

### **Parameters**

- autoCreate (bool) auto creation of non existing states
- vname vertex name

Return type int

Raises GraphError if vname not found

class graphs.DiGraph

Bases: graphs.Graph

Directed graph base class



addEdge (v1, v2)

Adds an edge

# **Parameters**

- **v1** (*int*) vertex 1 index
- **v2** (*int*) vertex 2 index

static dotDrawEdge (st1, st2, sep='n')

Draw a transition in Dot Format

## **Parameters**

- **st1** (*str*) starting state
- st2 (str) ending state
- **sep** (*str*) separator

### Return type str

dotDrawVertex (sti, sep='n')

Draw a Vertex in Dot Format

#### **Parameters**

- sti (int) index of the state
- **sep** (*str*) separator

# Return type str

dotFormat (size='20, 20', direction='LR', sep='n')

A dot representation

## **Parameters**

- **direction** (*str*) direction of drawing
- **size** (*str*) size of image
- **sep** (*str*) line separator

Returns the dot representation

# Return type str

New in version 0.9.6.

Changed in version 0.9.8.

# inverse()

Inverse of a digraph

# class graphs.DiGraphVm

 $Bases: \verb"graphs.DiGraph"$ 

Directed graph with marked vertices

**Variables MarkedV** (set) – set of marked vertices



# $\mathbf{markVertex}\,(v)$

Mark vertex v

Parameters v(int) – vertex

# MODULE: CONTEXT FREE GRAMMARS MANIPULATION (CFG)

# **Context Free Grammars Manipulation.**

Basic context-free grammars manipulation for building uniform random generetors

# 10.1 Class CFGrammar (Context Free Grammar)

```
class cfg.CFGrammar(gram)
```

Bases: object

Class for context-free grammars

#### **Variables**

- Rules grammar rules
- Terminals terminals symbols
- Nonterminals nonterminals symbols
- Start start symbol
- ntr dictionary of rules for each nonterminal

#### Initialization

**Parameters gram** – is a list for productions; each production is a tuple (LeftHandside, RightHandside) with LeftHandside nonterminal, RightHandside list of symbols, First production is for start symbol

## NULLABLE ()

Determines which nonterminals  $X \rightarrow *[]$ 

# makenonterminals()

Extracts C{nonterminals} from grammar rules.

# maketerminals()

Extracts C{terminals} from the rules. Nonterminals must already exist

# 10.2 Class CNF

```
class cfg.CNF (gram, mark='A@')
    Bases: cfg.CFGrammar
```

No useless nonterminals or epsilon rules are ALLOWED... Given a CFG grammar description generates one in CNF Then its possible to random generate words of a given size. Before some pre-calculations are nedded.

## Chomsky()

Transform to CNF

```
elim_unitary()
```

Elimination of unitary rules

# 10.3 Class cfgGenerator

class cfg.cfgGenerator(cfgr, size)

Bases: object

CFG uniform genetaror

Object initialization :param cfgr: grammar for the random objects :type cfgr: CNF :param size: size of objects :type size: integer

generate()

Generates a new random object generated from the start symbol

Returns object

Return type string

# 10.4 Class reStringRGenerator (Reg Exp Generator)

Bases: cfg.cfgGenerator

Uniform random Generator for reStrings

Uniform random generator for regular expressions. Used without arguments generates an uncollapsible re over {a,b} with size 10. For generate an arbitary re over an alphabet of 10 symbols of size 100: reStringR-Generator (small\_alphabet(10),100,reStringRGenerator.g\_regular\_base)

#### **Parameters**

- **Sigma** (*list or set*) re alphabet (that will be the set of grammar terminals)
- **size** (*integer*) word size
- cfgr base grammar
- epsilon if not None is added to a grammar terminals
- empty if not None is added to a grammar terminals

Note: the grammar can have already this symbols

```
generate()
```

Generates a new random RE string

# 10.5 Functions

cfg.gRules(rules\_list, rulesym='->', rhssep=None, rulesep='|')

Transforms a list of rules into a grammar description.

### **Parameters**

- rules\_list is a list of rule where rule is a string of the form: Word rulesym Word1 ... Word2 or Word rulesym []
- rulesym LHS and RHS rule separator
- **rhssep** RHS values separator (None for white chars)

# Returns a grammar description

cfg.**smallAlphabet** (*k*, *sigma\_base='a'*)
Easy way to have small alphabets

# **Parameters**

- **k** alphabet size (must be less than 52)
- **sigma\_base** initial symbol

Returns alphabet

Return type list

10.5. Functions

# MODULE: RANDOM DFA GENERATOR (RNDFA)

# **Random DFA generation**

ICDFA Random generation binding

Changed in version 0.9.4: Interface python to the C code

Changed in version 0.9.6: Working with incomplete automata

Changed in version 0.9.8: distinct classes for complete and incomplete ICDFA

# 11.1 Class ICDFArgen (Generator container)

# class rndfa. ICDFArgen

Bases: object

Generic ICDFA random generator class

#### See also:

Marco Almeida, Nelma Moreira, and Rogério Reis. Enumeration and generation with a string automata representation. Theoretical Computer Science, 387(2):93-102, 2007

### next()

Get the next generated DFA

Returns a random generated ICDFA

Return type DFA

# 11.2 Class ICDFArnd (Complete ICDFA random generator)

class rndfa.ICDFArnd(n, k)

Bases: rndfa.ICDFArgen

Complete ICDFA random generator class

This is the class for the uniform random generator for Initially Connected DFAs

# Variables

- **n** number of states
- $\mathbf{k}$  size of the alphabet

**Note:** This is an abstract class, not to be used directly

# 11.3 Class ICDFArndIncomple (Incomplete ICDFA generator)

 ${f class}$  rndfa.  ${f iconstant}$  rndfa.  ${f iconstant}$  rndfa.  ${f iconstant}$ 

Bases: rndfa.ICDFArgen

Incomplete ICDFA random generator class

# Variables

- $\mathbf{n}$  number of states
- k size of alphabet
- bias how often must the gost sink state appear (default None)

Raises IllegalBias if a bias >=1 or <=0 is provided

# MODULE: COMBO OPERATIONS (COMBOPERATIONS)

## Several combined operations for DFAs

Deterministic and non-deterministic automata manipulation, conversion and evaluation.

Authors: Rogério Reis & Nelma Moreira

This is part of FAdo project http://fado.dcc.fc.up.pt

Version: 0.9.5

Copyright: 1999-2012 Rogério Reis & Nelma Moreira {rvr,nam}@dcc.fc.up.pt

comboperations.starConcat (fa1, fa2, strict=False)

Star of concatenation of two languages: (L1.L2)\*

#### **Parameters**

- **fa1** (*DFA*) first automaton
- fa2 (DFA) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

# Return type DFA

### See also:

Yuan Gao, Kai Salomaa, and Sheng Yu. 'The state complexity of two combined operations: Star of catenation and star of reversal'. Fundamenta Informaticae, 83:75–89, Jan 2008.

```
comboperations.concatWStar(fal, fa2, strict=False)
```

Concatenation combined with star: (L1.L2\*)

# **Parameters**

- **fa1** (*DFA*) first automaton
- fa2 (DFA) second automaton
- **strict** (*bool*) should the alphabets be necessary equal?

# Return type DFA

# See also:

Bo Cui, Yuan Gao, Lila Kari, and Sheng Yu. 'State complexity of two combined operations: Reversal-catenation and star-catenation'. CoRR, abs/1006.4646, 2010.

```
comboperations.starWConcat (fa1, fa2, strict=False)
```

Star combined with concatenation: (L1\*.L2)

#### **Parameters**

- **fa1** (*DFA*) first automaton
- **fa2** (*DFA*) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

### Return type DFA

#### See also:

Bo Cui, Yuan Gao, Lila Kari, and Sheng Yu. 'State complexity of catenation combined with star and reversal'. CoRR, abs/1008.1648, 2010

```
comboperations.starDisj (fal, fa2, strict=False)
Star of Union of two DFAs: (L1 + L2)*
```

#### **Parameters**

- **fa1** (*DFA*) first automaton
- **fa2** (*DFA*) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

# Return type DFA

#### See also:

Arto Salomaa, Kai Salomaa, and Sheng Yu. 'State complexity of combined operations'. Theor. Comput. Sci., 383(2-3):140–152, 2007.

```
comboperations.starInter0 (fa1, fa2, strict=False) Star of Intersection of two DFAs: (L1 & L2)*
```

#### **Parameters**

- **fa1** (*DFA*) first automaton
- **fa2** (*DFA*) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

# Return type DFA

#### See also:

Arto Salomaa, Kai Salomaa, and Sheng Yu. 'State complexity of combined operations'. Theor. Comput. Sci., 383(2-3):140–152, 2007.

```
comboperations.starInter(fal, fa2, strict=False)
```

Star of Intersection of two DFAs: (L1 & L2)\*

# **Parameters**

- **fa1** (*DFA*) first automaton
- fa2 (DFA) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

# Return type DFA

```
comboperations.disjWStar (f1, f2, strict=True)
Union with star: (L1 + L2*)
```

### **Parameters**

- **f1** (*DFA*) first automaton
- **f2** (*DFA*) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

## Return type DFA

#### See also:

Yuan Gao and Sheng Yu. 'State complexity of union and intersection combined with star and reversal'. CoRR, abs/1006.3755, 2010.

 $\verb|comboperations.interWStar| (f1, f2, \textit{strict=True})|$ 

Intersection with star: (L1 & L2\*)

# **Parameters**

- **f1** (*DFA*) first automaton
- **f2** (*DFA*) second automaton
- **strict** (*Boolean*) should the alphabets be necessary equal?

# Return type DFA

# See also:

Yuan Gao and Sheng Yu. 'State complexity of union and intersection combined with star and reversal'. CoRR, abs/1006.3755, 2010.

**CHAPTER** 

# **THIRTEEN**

MODULE: CODES (CODES)

Code theory module

New in version 1.0.

# 13.1 Class CodeProperty

class codes.CodeProperty (name, alph)

Bases: object

### See also:

K. Dudzinski and S. Konstantinidis: Formal descriptions of code properties: decidability, complexity, implementation. International Journal of Foundations of Computer Science 23:1 (2012), 67–85.

Variables Sigma – the alphabet

# 13.2 Class TrajProp

class codes.TrajProp (aut, Sigma)

Bases: codes.IATProp

Class of trajectoty properties



Constructor

# **Parameters**

- aut (DFA|NFA) regular expression over {0,1}
- **Sigma** (*set*) the alphabet

static trajToTransducer(traj, Sigma)

Input Altering Tranducer corresponding to a Trajectory

# **Parameters**

- **traj** (NFA) trajectory language
- Sigma (set) alphabet

Return type SFT

# 13.3 Class IPTProp

## class codes.IPTProp (aut, name=None)

Bases: codes.CodeProperty

Input Preserving Transducer Property



#### **Variables**

- Aut (SFT) the transducer defining the property
- **Sigma** (*set*) alphabet

Constructor :param SFT aut: Input preserving transducer

maximalP (aut, U=None)

Tests if the language is maximal w.r.t. the property

#### **Parameters**

- aut (NFA) the automaton
- U (NFA) Universe of permitted words (Sigma^\* as default)

# Return type bool

## notMaximalW(aut, U=None)

Tests if the language is maximal w.r.t. the property

# **Parameters**

- aut (DFA|NFA) the automaton
- U (DFA|NFA) Universe of permitted words (Sigma^\* as default)

Return type bool

Raises PropertyNotSatisfied if not satisfied

# notSatisfiesW(aut)

Return a witness of non-satisfaction of the property by the automaton language

**Parameters aut** (DFA|NFA) – the automaton

Returns word witness pair

Return type tuple

## satisfiesP(aut)

Satisfaction of the property by the automaton language

**Parameters aut** (*DFA*|*NFA*) – the automaton

Return type bool

# 13.4 Class IATProp

class codes . IATProp (aut, name=None)

Bases: codes.IPTProp

Input Altering Transducer Property



Constructor :param SFT aut: Input preserving transducer

notSatisfiesW(aut)

Return a witness of non-satisfaction of the property by the automaton language

**Parameters aut** (DFA|NFA) – the automaton

Returns word witness pair

Return type tuple

# 13.5 Class PrefixProp

class codes.PrefixProp(t)

Bases: codes.TrajProp, codes.FixedProp

Prefix Property



satisfiesPrefixP(aut)

Satisfaction of property by the automaton language: faster than satisfiesP

**Parameters aut** (*DFA*|*NFA*) – the automaton

Return type bool

# 13.6 Class ErrDetectProp

codes.ErrDetectProp

alias of IPTProp

# 13.7 Class ErrCorrectProp

### ${f class} \ {f codes} \ . \ {f ErrCorrectProp} \ (t)$

Bases: codes.IPTProp

**Error Correcting Property** 



notMaximalW (aut, U=None)

Tests if the language is maximal w.r.t. the property

#### **Parameters**

- aut (DFA|NFA) the automaton
- U (DFA|NFA) Universe of permitted words (Sigma^\* as default)

Return type bool

notSatisfiesW(aut)

Satisfaction of the code property by the automaton language

**Parameters aut** (*DFA*|*NFA*) – the automaton

Return type tuple

satisfiesP(aut)

Satisfaction of the property by the automaton language

#### See also:

S. Konstantinidis: Transducers and the Properties of Error-Detection, Error-Correction and Finite-Delay Decodability. Journal Of Universal Computer Science 8 (2002), 278-291.

**Parameters aut** (DFA|NFA) – the automaton

Return type bool

# 13.8 Functions

codes.buildTrajPropS (regex, sigma)

Builds a TrajProp from a string regexp

## **Parameters**

- **regex** (*str*) the regular expression
- **sigma** (*set*) alphabet

Return type TrajProp

codes.buildIATPropF (fname)

Builds a IATProp from a FAdo SFT file

**Parameters fname** (*str*) – file name

Return type IATProp

#### codes.buildIPTPropF (fname)

Builds a IPTProp from a FAdo SFT file

**Parameters fname** (*str*) – file name

Return type IPTProp

### codes.buildIATPropS(s)

Builds a IATProp from a FAdo SFT string

**Parameters** s (str) – string containing SFT

**Return type** IATProp

#### codes.buildIPTPropS(s)

Builds a IPTProp from a FAdo SFT string

**Parameters** s(str) – file name

Return type IPTProp

### codes.buildErrorDetectPropF (fname)

**Builds an Error Detecting Property** 

**Parameters fname** (*str*) – file name

Return type ErrDetectProp

#### codes.buildErrorCorrectPropF (fname)

**Builds an Error Correcting Property** 

**Parameters fname** (*str*) – file name

Return type ErrCorrectProp

# codes.buildErrorDetectPropS(s)

Builds an Error Detecting Property from string

**Parameters** s(str) – transducer string

Return type ErrDetectProp

### codes.buildErrorCorrectPropS(s)

Builds an Error Correcting Property from string

Parameters s (str) – transducer string

Return type ErrCorrectProp

### codes.buildPrefixProperty(alphabet)

Builds a Prefix Code Property

**Parameters alphabet** (set) – alphabet

Return type PrefixProp

# codes.buildTrajPropS (regex, sigma)

Builds a TrajProp from a string regexp

## **Parameters**

- **regex** (*str*) the regular expression
- **sigma** (*set*) alphabet

Return type TrajProp

### codes.editDistanceW(auto)

Compute the edit distance of a given regular language accepted by the NFA via Input-altering transducer.

Attention: language should have at least two words

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#### See also:

Lila Kari, Stavros Konstantinidis, Steffen Kopecki, Meng Yang. An efficient algorithm for computing the edit distance of a regular language via input-altering transducers. arXiv:1406.1041 [cs.FL]

**Parameters auto** (NFA) – language recogniser

Returns The edit distance of the given regular language plus a witness pair

Return type tuple

# codes.exponentialDensityP (aut)

Checks if language density is exponential

Using breadth first search (BFS)

Attention: aut should not have Epsilon transitions

**Parameters aut** (NFA) – the representation of the language

Return type bool

# codes.createInputAlteringSIDTrans(n, sigmaSet)

Create an input-altering SID transducer based

### **Parameters**

- **n** (*int*) max number of errors
- **sigmaSet** (*set*) alphabet

**Returns** a transducer representing the SID channel

Return type SFT

# MODULE: GRAIL COMPATIBILITY (GRAIL)

# **GRAIL** support.

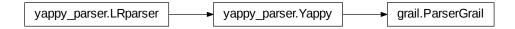
GRAIL formats support. This is an auxiliary module that sould be imported by fa.py New in version 0.9.4.

# 14.1 Class ParserGrail

class grail.ParserGrail (no\_table=1, table='.tableGrail')

Bases: yappy\_parser.Yappy

A parser form GRAIL standard automata descriptions



# 14.2 Class Grail

class grail.Grail

Bases: object

A class for Grail execution

Changed in version 0.9.8: tries to initialise execPath from fadorc

do (cmd, \*args)

Execute Grail command

#### **Parameters**

- cmd (string) name of the command
- **args** arguments

# Raises

- GrailCommandError if the syntax is not correct an exception is raised
- FAdoGeneralError if Grail fails to execute something

# setExecPath(path)

Sets the path to the Grail executables

**Parameters path** (*str*) – the path to Grail executables

# 14.3 Functions

# grail.exportToGrail (fileName, fa)

Saves a finite automatom definition to a file using Grail format

#### **Parameters**

- **fileName** (*string*) file name
- **fa** (*FA*) the FA

# grail.FAToGrail (f, fa)

Saves a finite automatom definition to an open file using Grail format

### **Parameters**

- **f** (*file*) opended file
- **fa** (*FA*) the FA

# grail.importFromGrailFile (fileName)

Imports a finite automaton from a file in GRAIL format

The type of the object returned depends on the transition definiion red as well as the number of initial states declared

Parameters fileName (str) – file name

Returns the automata red

Return type FA

# grail.FAFromGrail (buffer)

Imports a finite automaton from a buffer in GRAIL format

The type of the object returned depends on the transition definiion red as well as the number of initial states declared

**Parameters buffer** (*str*) – buffer file

**Returns** the automata red

Return type FA

# MODULE: VERSO LANGUAGE (VERSO)

# FAdo interface language and slave manager

Applications that want to use FAdo as a slave, just to process it objects should use this language to interface with it.

**Note:** Every object that is supposed to be available through this language, should be defined in objects and should have a method <code>vDescription</code>, returning the following list

- 0. A pair of descriptions, short and long, of the object
- 1. A list of pairs
- 1.0. A name of a format (names should be unique)
- 1.1. The function that returns the string representation of the object in that format
  - 2. A tuple for each method provided
- 2.0. Name of the command in verso
- 2.1. A pair, short/long, descriptions of the method
- 2.2. Number (n) of arguments of the method
- 2.2+i. The type of the ith argument
- 2.1+n. The return type None if does not return (in place transformation)
- 2.2+n. The function implementing the method having a list as arguments
  - 3. and so on...

class verso.ParserVerso(vsession, objects=None, no\_table=0, table='.tableVerso')

Bases: yappy\_parser.Yappy

A parser for FAdo standard automata descriptions

#### Variables

- vi virtual interaction session that knows how to communicate with the client
- **objects** the list of objects known
- **info** dictionary object -> (longdescription, [list of commands])
- **fun** dictionary command -> (arity, return type, function)
- format dictionary formatName -> function

# **Parameters**

- no\_table ignore the table if it exists
- table name of the table

# A SMALL TUTORIAL FOR FADO

FAdo system is a set tools for regular languages manipulation.

Regular languages can be represented by regular expressions (regexp) or finite automata, among other formalisms. Finite automata may be deterministic (DFA) or non-deterministic (NFA). In FAdo these representations are implemented as Python classes. A full documentation of all classes and methods is here.

To work with FAdo, after installation, import the following modules on a Python interpreter:

```
>>> from FAdo.fa import *
>>> from FAdo.reex import *
>>> from FAdo.fio import *
```

The module fa implements the classes for finite automata and the module reex the classes for regular expressions. The module fio implements methods for IO of automata and related models.

#### General conventions

Methods which name ends in P test if the object verifies a given property and return True or False.

#### Finite Automata

The top class for finite automata is the class FA, which has two main subclasses: OFA for one way finite automata and the class TFA for two-way finite automata. The class OFA implements the basic structure of a finite automaton shared by DFAs and NFAs. This class defines the following attributes:

Sigma: the input alphabet (set)

States: the list of states. It is a list such that each state is referred by its index whenever it is used (transitions, Final, etc).

Initial:the initial state (or a set of initial states for NFA). It is an index or list of indexes.

Final: the set of final states. It is a list of indexes.

In general, one should not create instances (objects) of class OFA. The class DFA and NFA implement DFAs and NFAs, respectively. The class GFA implements generalized NFAs that are used in the conversion between finite automata and regular expressions. All three classes inherit from class OFA.

For each class there are special methods for add/delete/modify alphabet symbols, states and transitions.

## **DFAs**

The following example shows how to build a DFA that accepts the words of  $\{0,1\}^*$  that are multiples of 3.

```
>>> m3= DFA()
>>> m3.setSigma(['0','1'])
>>> m3.addState('s1')
>>> m3.addState('s2')
>>> m3.addState('s3')
>>> m3.setInitial(0)
>>> m3.addFinal(0)
>>> m3.addTransition(0, '0', 0)
>>> m3.addTransition(0, '1', 1)
>>> m3.addTransition(1, '0', 2)
```

```
>>> m3.addTransition(1, '1', 0)
>>> m3.addTransition(2, '0', 1)
>>> m3.addTransition(2, '1', 2)
```

It is now possible, for instance, to see the structure of the automaton or to test if a word is accepted by it.

```
>>> m3
DFA((['s1', 's2', 's3'], ['1', '0'], 's1', ['s1'], "[('s1', '1', 's2'), ('s1', '0', 's1'), ('s2',
>>> m3.evalWordP("011")
True
>>> m3.evalWordP("1011")
False
```

If graphviz is installed it is also possible to display the diagram of an automaton as follows:

```
>>>m3.display()
```

Instead of constructing the DFA directly we can load (and save) it in a simple text format. For the previous automaton the description will be:

Then, if this description is saved in file mul3.fa, we have

```
>>> m3=readFromFile("mul3.fa")[0]
```

As the set of states is represented by a Python list, the list method len can be used to determine the number of states of a FA:

```
>>> len(m3.States)
```

For the number of Transitions the countTransitions() method must be used

```
>>> m3.countTransitions()
6
```

To minimize a DFA any of the minimization algorithms implemented can be used:

```
>>> min=m3.minimalHopcroft()
```

In this case, the DFA was already minimal so min has the same number of states as m3.

Several (regularity preserving) operations of DFAs are implemented in FAdo: boolean (union (l or \_\_or\_\_), intersection (& or \_\_and\_\_) and complementation (~ or \_\_invert\_\_)), concatenation (concat), reversal (reversal) and star (star).

```
>>> u = m3 | ~m3
>>> u
DFA(([(1, 1), (0, 0), (2, 2)], set(['1', '0']), 0, set([0, 1, 2]), {0: {'1': 1, '0': 0}, 1: {'1':
>>> m = u.minimal()
>>> m
DFA((['(1, 1)'], ['1', '0'], '(1, 1)', ['(1, 1)'], "[('(1, 1)', '1', '(1, 1)'), ('(1, 1)', '0', ')])
```

State names can be renamed in-place using:

```
>>> m.renameStates(range(len(m)))

DFA((['0'], ['1', '0'], '0', ['0'], "[(0, '1', 0), (0, '0', 0)]"))
```

Notice that m recognize all words over the alphabet  $\{0.1\}$ .

It is possible to generate a word recognisable by an automata (witness)

```
>>> u.witness()
'@epsilon'
```

In this case this allows to ensure that u recognizes the empty word.

This method is also useful for obtain a witness for the difference of two DFAs (witnessDiff).

To test if two DFAs are equivalent the operator == (equivalenceP) can be used.

#### **NFAs**

NFAs can be built and manipulated in a similar way. There is no distinction between NFAs with and without epsilon-transitions. But it is possible to test if a NFA has epsilon-transitions and convert between a NFA with epsilon-transitions to a (equivalent) NFA without them.

Converting between NFAs and DFAs

The method toDFA allows to convert a NFA to an equivalent DFA by the subset construction method. The method toNFA migrates trivially a DFA to a NFA.

## **Regular Expressions**

A regular expression can be a symbol of the alphabet, the empty set (@epmtyset), the empty word (@epsilon) or the concatenation or the union (+) or the Kleene star (\*) of a regular expression. Examples of regular expressions are a+b, (a+ba)\*, and (@epsilon+ a)(ba+ab+@emptyset).

The class regexp is the base class for regular expressions and is used to represent an alphabet symbol. The classes epsilon and emptyset are the subclasses used for the empty set and empty word, respectively. Complex regular expressions are concat, disj, and star.

As for DFAs (and NFAs) we can build directly a regular expressions as a Python class:

```
>>> r = star(disj(regexp("a"),concat(regexp("b"),regexp("a"))))
>>> print r
(a + (b a))*
```

But we can convert a string to a regexp class or subclass, using the method str2regexp.

```
>>> r = str2regexp("(a+ba)*")
>>> print r
(a + (b a))*
```

For regular expressions there are several measures available: alphabetic size, (parse) tree size, string length, number of epsilons and star height. It is also possible to explicitly associate an alphabet to regular expression (even if some symbols do not appear in it) (setSigma)

There are several algebraic properties that can be used to obtain equivalent regular expressions of a smaller size. The method reduced transforms a regular expression into one equivalent without some obvious unnecessary epsilons, emptysets or stars.

Several methods that allows the manipulation of derivatives (or partial derivatives) by a symbol or by a word are implemented. However, the class regexp does not deal with regular expressions module ACI properties (associativity, commutativity and idempotence of the union) (see class xre), a so it is not possible to obtain all word derivatives of a given regular expression. This is not the case for partial derivatives.

To test if two regular expressions are equivalent the method compare can be used.

```
>>> r.compare(str2regexp(\"(a*(ba)*a*)*\"))
True
>>>
```

Converting Finite Automata to Regular Expressions

For pedagogical purposes, it is implemented a recursive method that constructs a regular expression equivalent to a given DFA (regexp).

```
>>> print m3.regexp()
((0 + ((@epsilon + 0) (0* (@epsilon + 0)))) + ((1 + ((@epsilon + 0) (0* 1))) ((1 (0* 1))* (1 + (1
```

Methods based on state elimination techniques are usually more efficient, and produces much smaller regular expressions. We have implemented several heuristics for the elimination order.

```
>>> print m3.reCG()
((0 + (1 1)) + (((1 0) (1 + (0 0))*) (0 1)))*
```

Converting Regular Expressions to Finite Automata

Several methods to convert between regular expressions and NFAs are implemented. With the Thompson construction a NFA with epsilon transitions is obtained (nfaThompson). Epsilon free NFAs can be obtained by the Glushkov method (Position automata) (nfaPosition,) the partial derivatives method (nfaPD) or by the follow method (nfaFollow). The two last methods usually allows to obtain smaller NFAs.

# General Example

Considering the several methods described before it is possible to convert between the different equivalent representations of regular languages, as well to perform several regularity preserving operations.

```
>>> r.nfaPosition().toDFA().minimal(complete=False)
DFA((['0', '2'], ['a', 'b'], '0', ['0'], "[('0', 'a', '0'), ('0', 'b', '2'), ('2', 'a', '0')]"))
>>> m3 == m3.reCG().nfaPD().toDFA().minimal()
True
>>>
```

More classes and modules

Several other classes and modules are also available, including:

class ICDFArnd (module rndfa.py): Random DFA generation

class FL (module fl.py): special methods for finite languages

class xre (module xre.py): extended regular expressions

module comboperations.py: implementation of several algorithms for several combined operations with DFAs and NFAs

module grail.py: compatibility with GRAIL

module transducers.py: several classes and methods for transducers

# **CHAPTER**

# **SEVENTEEN**

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