Chapter 1

Demo problem: Boundary-driven elastic deformation of a fish-shaped domain

Detailed documentation to be written. Here's a plot of the result and the already fairly well documented driver code...

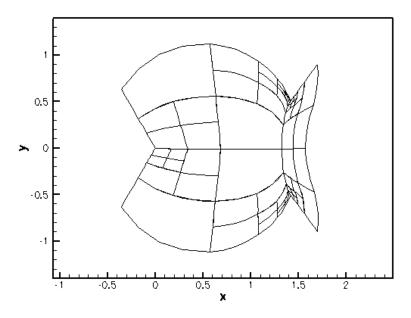


Figure 1.1 Boundary-driven elastic deformation of a fish-shaped domain.

```
//LIC// This file forms part of comph-lib, the object-oriented,
//LIC// multi-physics finite-element library, available
//LIC// at http://www.oomph-lib.org.
//LIC//
//LIC// Copyright (C) 2006-2024 Matthias Heil and Andrew Hazel
//LIC//
//LIC// This library is free software; you can redistribute it and/or
//LIC// modify it under the terms of the GNU Lesser General Public
//LIC// License as published by the Free Software Foundation; either
//LIC// version 2.1 of the License, or (at your option) any later version.
//LIC//
//LIC// This library is distributed in the hope that it will be useful,
//LIC// but WITHOUT ANY WARRANTY; without even the implied warranty of
//LIC// MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU
//LIC// Lesser General Public License for more details.
//LIC//
//LIC// You should have received a copy of the GNU Lesser General Public
```

```
//LIC// License along with this library; if not, write to the Free Software
//LIC// Foundation, Inc., 51 Franklin Street, Fifth Floor, Boston, MA //LIC// 02110-1301 USA.
//T.TC//
//LIC// The authors may be contacted at oomph-lib@maths.man.ac.uk.
//LIC//
//LIC//===
// Driver for elastic deformation of a fish-shaped domain with
// adaptivity -- deformation is driven by displacement of
// GeomObject-based boundary!
// Generic oomph-lib headers
#include "generic.h"
// Solid mechanics
#include "solid.h"
// The fish mesh
#include "meshes/fish_mesh.h"
using namespace std;
using namespace oomph;
//-----
/// Refineable fish mesh upgraded to become a solid mesh
template<class ELEMENT>
class ElasticFishMesh : public virtual RefineableFishMesh<ELEMENT>,
                        public virtual SolidMesh
public:
 /// Constructor: Build underlying adaptive fish mesh and then
 /// set current Eulerian coordinates to be the Lagrangian ones.
 /// Pass pointer to geometric objects that specify the /// fish's back in the "current" and "undeformed" configurations,
 /// and pointer to timestepper (defaults to Static)
 // Note: FishMesh is virtual base and its constructor is automatically
 // called first! --> this is where we need to build the mesh;
 // the constructors of the derived meshes don't call the
 \ensuremath{//} base constructor again and simply add the extra functionality.
 ElasticFishMesh(GeomObject* back_pt, GeomObject* undeformed_back_pt,
                TimeStepper* time_stepper_pt=&Mesh::Default_TimeStepper) :
  FishMesh<ELEMENT>(back_pt,time_stepper_pt),
  RefineableFishMesh<ELEMENT>(back_pt,time_stepper_pt)
   // Mesh has been built, adaptivity etc has been set up -->
   // assign the Lagrangian coordinates so that the current // configuration becomes the stress-free initial configuration
   set_lagrangian_nodal_coordinates();
   // Build "undeformed" domain: This is a "deep" copy of the
   // Domain that we used to create set the Eulerian coordinates // in the initial mesh -- the original domain (accessible via
   // the private member data Domain_pt) will be used to update
   // the position of the boundary nodes; the copy that we're
   // creating here will be used to determine the Lagrangian coordinates
   // of any newly created SolidNodes during mesh refinement
   double xi_nose = this->Domain_pt->xi_nose();
double xi_tail = this->Domain_pt->xi_tail();
   Undeformed_domain_pt=new FishDomain(undeformed_back_pt,xi_nose,xi_tail);
   // Loop over all elements and set the undeformed macro element pointer
   unsigned n_element=this->nelement();
   for (unsigned e=0;e<n_element;e++)</pre>
    {
     // Get pointer to full element type
     ELEMENT* el_pt=dynamic_cast<ELEMENT*>(this->element_pt(e));
     // Set pointer to macro element so the curvlinear boundaries
     // of the undeformed mesh/domain get picked up during adaptive
     // mesh refinement
     el_pt->set_undeformed_macro_elem_pt(
      Undeformed_domain_pt->macro_element_pt(e));
     // Use MacroElement representation for
     // Lagrangian coordinates of newly created
     // nodes
     el_pt->enable_use_of_undeformed_macro_element_for_new_lagrangian_coords();
```

```
}
/// Destructor: Kill "undeformed" Domain
virtual ~ElasticFishMesh()
  delete Undeformed_domain_pt;
private:
/// Pointer to "undeformed" Domain -- used to determine the
/// Lagrangian coordinates of any newly created SolidNodes during
 /// Mesh refinement
Domain* Undeformed_domain_pt;
};
//-----
/// Global variables
namespace Global_Physical_Variables
/// Pointer to strain energy function
StrainEnergyFunction* Strain_energy_function_pt;
 /// Pointer to constitutive law
ConstitutiveLaw* Constitutive_law_pt;
/// Elastic modulus
double E=1.0;
 /// Poisson's ratio
double Nu=0.3;
 /// "Mooney Rivlin" coefficient for generalised Mooney Rivlin law
double C1=1.3;
/// Body force
double Gravity=0.0;
 /// Body force vector: Vertically downwards with magnitude Gravity
Vector<double>& b)
 b[0]=0.0;
 b[1]=-Gravity;
}
/// Boundary-driven elastic deformation of fish-shaped domain.
template<class ELEMENT>
class ElasticFishProblem : public Problem
public:
/// Constructor:
ElasticFishProblem();
 /// Run simulation.
void run();
 /// Access function for the mesh
ElasticFishMesh<ELEMENT>* mesh_pt()
```

```
{return dynamic_cast<ElasticFishMesh<ELEMENT>*>(Problem::mesh_pt());}
 /// Doc the solution
void doc_solution(DocInfo& doc_info);
 /// Update function (empty)
void actions_after_newton_solve() {}
 /// Update before solve: We're dealing with a static problem so
 /// the nodal positions before the next solve merely serve as
 \ensuremath{///} initial conditions. For meshes that are very strongly refined
/// near the boundary, the update of the displacement boundary /// conditions (which only moves the SolidNodes \star on \star the boundary),
 /// can lead to strongly distorted meshes. This can cause the
 /// Newton method to fail --> the overall method is actually more robust
 /// if we use the nodal positions as determined by the Domain/MacroElement-
 /// based mesh update as initial guesses.
 void actions_before_newton_solve()
   bool update_all_solid_nodes=true;
   mesh_pt()->node_update(update_all_solid_nodes);
 /// Update after adapt: Pin all redundant pressure nodes (if required)
void actions_after_adapt()
   // Pin the redundant solid pressures (if any)
   PVDEquationsBase<2>::pin_redundant_nodal_solid_pressures(
   mesh_pt()->element_pt());
 // Geometric object that represents the deformable fish back
Circle* Fish_back_pt;
/// Constructor:
//=======
template<class ELEMENT>
ElasticFishProblem<ELEMENT>::ElasticFishProblem()
// Set coordinates and radius for the circle that will become the fish back
double x_c=0.5;
double y_c=0.0;
double r back=1.0;
 // Build geometric object that will become the deformable fish back
 // \texttt{GeomObject} \star \ \texttt{fish\_back\_pt=new ElasticFishBackElement} \ (\texttt{x\_c,y\_c,r\_back}) \ ;
Fish_back_pt=new Circle(x_c,y_c,r_back);
 // Build geometric object that specifies the fish back in the
 // undeformed configuration (basically a deep copy of the previous one)
GeomObject* undeformed_fish_back_pt=new Circle(x_c,y_c,r_back);
 // Build fish mesh with geometric objects that specify the deformable
 // and undeformed fish back
Problem::mesh_pt() = new ElasticFishMesh<ELEMENT>(Fish_back_pt,
                                                    undeformed_fish_back_pt);
 // Set error estimator
 Z2ErrorEstimator* error_estimator_pt=new Z2ErrorEstimator;
mesh_pt()->spatial_error_estimator_pt()=error_estimator_pt;
 // Change/doc targets for mesh adaptation
mesh_pt()->max_permitted_error()=0.05;
mesh_pt()->min_permitted_error()=0.005;
mesh_pt()->doc_adaptivity_targets(cout);
 // Pin all nodal positions apart from those on the tail
unsigned num_bound = mesh_pt()->nboundary();
 for (unsigned ibound=0; ibound<num_bound; ibound++)</pre>
  {
   if (ibound!=2)
     unsigned num_nod=mesh_pt()->nboundary_node(ibound);
     for (unsigned inod=0;inod<num_nod;inod++)</pre>
       for (unsigned i=0;i<2;i++)</pre>
         mesh_pt()->boundary_node_pt(ibound,inod)->pin_position(i);
        }
      }
```

```
}
 //Loop over the elements in the mesh to set parameters/function pointers
unsigned n_element =mesh_pt()->nelement();
 for (unsigned i=0;i<n_element;i++)</pre>
   //Cast to a solid element
  ELEMENT *el_pt = dynamic_cast<ELEMENT*>(mesh_pt()->element_pt(i));
   // Set the constitutive law
  el_pt->constitutive_law_pt() =
   Global_Physical_Variables::Constitutive_law_pt;
   // Set the body force
  el_pt->body_force_fct_pt() =Global_Physical_Variables::body_force;
 // Pin the redundant solid pressures (if any)
 PVDEquationsBase<2>::pin_redundant_nodal_solid_pressures(
 mesh_pt()->element_pt());
 //Attach the boundary conditions to the mesh
cout « assign_eqn_numbers() « std::endl;
 // Refine the problem uniformly (this automatically passes the
 // function pointers/parameters to the finer elements
 refine_uniformly();
 // The non-pinned positions of the newly SolidNodes will have been
 // determined by interpolation. Update all solid nodes based on
 // the Mesh's Domain/MacroElement representation.
bool update_all_solid_nodes=true;
mesh_pt()->node_update(update_all_solid_nodes);
 // Now set the Eulerian equal to the Lagrangian coordinates
mesh_pt()->set_lagrangian_nodal_coordinates();
/// Doc the solution
                      ______
template<class ELEMENT>
void ElasticFishProblem<ELEMENT>::doc_solution(DocInfo& doc_info)
ofstream some file:
char filename[100];
 // Number of plot points
unsigned npts = 5;
 // Output shape of deformed body
sprintf(filename, "%s/soln%i.dat", doc_info.directory().c_str(),
        doc_info.number());
 some_file.open(filename);
mesh_pt()->output(some_file,npts);
some_file.close();
// removed until Jacobi eigensolver is re-instated // // Output principal stress vectors at the centre of all elements
 // SolidHelpers::doc_2D_principal_stress<ELEMENT>(doc_info,mesh_pt());
//-----
/// Run the problem
template<class ELEMENT>
void ElasticFishProblem<ELEMENT>::run()
 // Output
DocInfo doc_info;
// Set output directory
doc_info.set_directory("RESLT");
 // Step number
doc_info.number()=0;
 // Initial parameter values
 // Gravity:
Global_Physical_Variables::Gravity=0.1;
 //Parameter incrementation
unsigned nstep=5:
```

```
for(unsigned i=0;i<nstep;i++)</pre>
    //Solve the problem with Newton's method, allowing for up to 5
    //{\tt rounds} of adaptation
   newton_solve(5);
    // Doc solution
    doc_solution(doc_info);
   doc_info.number()++;
    // Increment width
   Fish\_back\_pt->y\_c()+=0.03;
}
/// Driver for simple elastic problem
int main()
 // \\ Initialise \ physical \ parameters
Global_Physical_Variables::E = 2.1;
Global_Physical_Variables::Nu = 0.4;
Global_Physical_Variables::C1 = 1.3;
 // Define a strain energy function: Generalised Mooney Rivlin
 Global_Physical_Variables::Strain_energy_function_pt =
 new GeneralisedMooneyRivlin(&Global_Physical_Variables::Nu, &Global_Physical_Variables::C1, &Global_Physical_Variables::E);

// Define a constitutive law (based on strain energy function)
 Global_Physical_Variables::Constitutive_law_pt =
  {\tt new} \ {\tt IsotropicStrainEnergyFunctionConstitutiveLaw} \ (
    Global_Physical_Variables::Strain_energy_function_pt);
 //Set up the problem with pure displacement formulation
ElasticFishProblem<RefineableQPVDElement<2,3> > problem;
 problem.run();
}
```

1.1 PDF file

A pdf version of this document is available.