# Package 'svi'

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Type Package

Title SVI Implied Volatility Surface
Version 0.2.1
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<b>Description</b> A package for fitting the option-implied volatility surface, computing the risk-neutral density distribution and risk-neutral moments based on the Stochastic Volatility Inspired (SVI) equation.
License GPL-2   GPL-3
Encoding UTF-8
LazyData true
<b>Depends</b> Matrix
R topics documented:
axel durrleman geom rnd rnmoment sp500 svi svifit svifit svipar
Index 1
axel Axel-Vogt Parameters
Description  Loads the Axel-Vogt parameters, which are a typical example of arbitrage SVI surface.
Usage
axel()

2 durrleman

#### **Details**

The paramters are given as:

```
-0.041, 0.1331, 0.306, 0.3586, 0.4153
```

corresponding to (a, b, rho, m, sigma). When inspecting the Durrleman condition, one recognizes that this setting is not entirely positive.

#### Value

Loads the parameters par and shows the Durrleman/SVI plot.

#### Author(s)

Wolfgang Schadner

#### References

```
Schadner, W. (2023): Direct Fit for SVI Implied Volatilities
```

#### See Also

svi

# **Examples**

```
## Not run
# axel()
```

durrleman

Durrleman Condition

# Description

Calculates the the Durrleman condition of arbitrage.

# Usage

```
durrleman(x, par, Gs=FALSE)
```

# **Arguments**

Gs

x Vector of option's log moneyness. Preferably defined as

$$x = log(\frac{strike\ price}{forward\ price})$$

par Either the five SVI parameters  $(a, b, \rho, m, \sigma)$  or the conic coefficients z.

Returns additional values of  $G_{1\pm}$  and  $G_2$ , see Martini and Mingone (2022) for details.

geom 3

#### **Details**

The Durrleman function g(x) should be positive across all x for an abritrage free volatility surface. If g(x) is positive, then the risk-neutral density q(x) is also positive. Let y be the implied variance for the moneyness x, then the durrleman function is defined as:

$$g(x) := (1 - \frac{xy'}{2y})^2 - \frac{y'^2}{4}(\frac{1}{y} + \frac{1}{4}) + \frac{y''}{2}$$

Alternatively, this might be expressed as:

$$g(x) = G_1(x) + \frac{1}{2\sigma}G_2(x)$$

(cp. Martini and Mingone (2022)).

#### Value

Returns the values g of the Durrleman function.

# Author(s)

Wolfgang Schadner

#### References

Martini, C. and Mingone, A. (2022): No Arbitrage SVI, SIAM J. Financial Math., 13(1), pp. 227-261

#### See Also

svi

# **Examples**

```
## Not run
# axel()
# g <- durrleman(x, par)
# plot(x, g); abline(h=0)</pre>
```

geom

Geometric Properties

#### **Description**

Calculates the center and asymptotes of the SVI hyperbola.

# Usage

geom(par)

#### **Arguments**

par

Either the five SVI parameters, or the six z coefficients defining the conic.

4 rnd

#### **Details**

Calculates the center and asymptotes of the SVI hyperbola.

#### Value

Returns the values of the Durrleman function.

#### Author(s)

Wolfgang Schadner

#### References

```
Schadner, W. (2023): Direct Fit for SVI Implied Volatilities
```

#### See Also

svi

# **Examples**

```
## Not run
# load("sp500")
# df <- opt$`tau = 7 days`
# x <- df$k
# y <- df$ivol^2
# fit <- svifit(x, y)
# plot(x, y)
# lines(x, fit$yhat)</pre>
```

rnd

Risk-Neutral Density

# **Description**

Computes the risk-neutral density distribution for some SVI parameters par.

# Usage

```
rnd(x, par)
```

# Arguments

v

Vector of option's log moneyness. Preferably defined as

$$x = log(\frac{strike\ price}{forward\ price})$$

par

Either the five SVI parameters  $(a, b, \rho, m, \sigma)$  or the conic coefficients z.

# Value

Returns the risk-neutral density distribution.

rnmoment 5

#### Author(s)

Wolfgang Schadner

#### References

```
Schadner, W. (2023): Direct Fit for SVI Implied Volatilities
```

#### See Also

svi

#### **Examples**

```
## Not run
# axel()
# q <- rnd(x, par)
# plot(x, q)</pre>
```

rnmoment

Risk-Neutral Moments

#### **Description**

Computes the risk-neutral variance (rnvar), skewness (rnskew), kurtosis (rnkurt) or more generally a moment of certain order (rnmoment) for the risk-neutral density distribution as specified by the SVI parameters par.

# Usage

```
rnskew(par)
rnkurt(par)
rnmoment(par, order=2, absolute=FALSE, standardized=TRUE)
```

#### **Arguments**

par either the five SVI parameters  $(a, b, \rho, m, \sigma)$  or the conic coefficients z.

order of the moment to be computed, the default is to compute the second mo-

ment, i.e., the variance.

absolute a logical value indicating whether absolute moments are to be computed.

standardized a logical value indicating whether standardized moments are to be computed.

# Value

Returns the risk-neutral moment.

#### Author(s)

Wolfgang Schadner

# References

```
Schadner, W. (2023): Direct Fit for SVI Implied Volatilities
```

6 svi

#### See Also

```
svi, rnd
```

# **Examples**

```
## Not run
# data(sp500)
# df <- sp500$`tau = 7 days`
# x <- df$k
# y <- df$ivol^2
# mdl <- svifit(x,y)
# rnskew(mdl$par)
# rnmoment(mdl$par)</pre>
```

sp500

Example options of the S&P 500

# Description

This data set covers option data for the S&P 500 as observed on ....

# Usage

```
data(sp500)
```

# **Format**

A list of the options with different maturities and strikes.

# Source

OptionMetrics.

# References

•••

svi

Calculate SVI predicted values

# Description

Calculates the y values as predicted by SVI for some given x and parameter set.

# Usage

```
svi(x, par)
```

svifit 7

# **Arguments**

x Values of forward log moneyness. I.e., log(strike/forward).

par Either the five SVI parameters, or the six z coefficients defining the conic.

#### **Details**

•••

# Value

Returns the predicted y values.

# Author(s)

Wolfgang Schadner

#### References

```
Schadner, W. (2023): Direct Fit for SVI Implied Volatilities
```

#### See Also

svipar

# **Examples**

```
## Not run
# load("sp500")
# df <- opt$`tau = 7 days`
# x <- df$k
# y <- df$ivol^2
# fit <- svifit(x, y)
# plot(x, y)
# lines(x, fit$yhat)</pre>
```

svifit

Fitting SVI volatilities

# Description

Fits the Stochastic Volatility Inspired (SVI) equation to an implied volatility surface of given maturity. The input variable x represents the log-moneyness (logarithm of strike over forward-price) and y the implied variance (implied volatility squared).

# Usage

```
svifit(x, y, fit="direct", na.rm=TRUE, low_ecc=TRUE, W=NA, a=NA, init=c(0, 0.2))
```

8 svifit

#### **Arguments**

x Vector of option's log moneyness. Preferably defined as

$$x = log(\frac{strike\ price}{forward\ price})$$

y Vector of implied variances corresponding to x. That is, the squared implied

volatilities over x.

fit Fitting method to be used. Possible vbalues are:

• direct: direct least-squares

• direct\_UC: direct unconstrained least-squares

• vanish: vanishing wings, i.e. flat extrapolation

• QE: quasi-explicit fit, i.e. iterative routine

na.rm Removing NA's

low\_ecc Correction for the low eccentricity bias.

W (optional) Weighting vector for a weighted least-squares.

a (optional) For vanish fit: specify the y-level for the flat extrapolation.

init (optional) For QE fit: Starting values of m and  $\sigma$ .

#### **Details**

The method is implemented as described by Schadner (2023).

## Value

Returns a list of the following:

yhat Fitted y values.

 $\text{par} \qquad \qquad \text{The SVI parameters } a,b,\rho,m,\sigma.$ 

z The conic coefficients defining the hyperbola.

input The input data.

# Author(s)

Wolfgang Schadner

# References

Schadner, W. (2023): Direct Fit for SVI Implied Volatilities

# See Also

svipar

svipar 9

# **Examples**

```
## Not run
# library(svi)
# data(sp500)
# df <- sp500$`tau = 7 days`
# x <- df$k
# y <- df$ivol^2
# fit <- svifit(x, y)
# plot(x, y)
# lines(x, fit$yhat)
#
# # Risk-Neutral Density:
# q <- rnd(x, fit$par)
# plot(x, q)</pre>
```

svipar

Translating conic coefficients into SVI parameters, and vice versa

# **Description**

This function transforms the 6 conic coefficients z into the 5 SVI paramters, or other way around.

#### Usage

svipar(par)

#### **Arguments**

par

Either the six conic coefficients z, or the 5 SVI paramters:  $(ab\rho m\sigma)$ .

#### **Details**

A conic is generally defined as:

$$0 = Dz$$

for the coefficients z and the design matrix D

$$D = (x^2 x y y^2 x y 1)$$

. There exists a direct mapping between z and the 5 SVI parameters, see Schadner 2023.

# Value

Returns either the five SVI paramters:

$$par = (ab\rho m\sigma)$$

Or the z coefficients.

# Author(s)

Wolfgang Schadner

10 svipar

# References

Schadner, W. (2023): Direct Fit for SVI Implied Volatilities

# See Also

svipar

# **Examples**

```
## Not run
# TBD
```

# **Index**

```
* datasets
     sp500, 6
* svi, implied volatility
    axel, 1
    durrleman, 2
    geom, 3
    rnd, 4
    rnmoment, 5
    svi, 6
    svifit, 7
    svipar, 9
axel, 1
{\it durrleman}, {\color{red} 2}
geom, 3
rnd, 4, 6
rnkurt (rnmoment), 5
rnmoment, 5
rnskew (rnmoment), 5
rnvar (rnmoment), 5
sp500, 6
svi, 2-6, 6
svifit, 7
svipar, 7, 8, 9, 10
```