

## KEY WORDS

Data: Any Observations that have been collected

Statistics: Collect, Analyze, Summarize, Interpret, Draw conclusion

Population: The complete set of elements being studied.

Samples: Some subset of a population.

Census: Collecting from every member of a population.

\* If you collect a sample, it must be collected random.

## Types of Data:

P-P Parameter: A characteristic of a population

S-S Statistic: A characteristic of a sample

Qualitative: Non-numeric

(Categorical) & mathematical are meaningless

Quantitative: Numeric

↳ Discrete, Continuous

## 4 Levels of Measurement

Nominal: Categories not ordered (Religion)

Ordinal: Can be ordered (Differences are meaningless)

Interval: Ordered, Differences are meaningful,

No "Nature Zero". Like temperature

Ratio: Just like Interval, But with a Nature Zero  
"Amount of money"

# Design of Experiments/Observations

## OBS VS EXP

Measures specific traits, but does not modify subjects. Apply a treatment and then measure the effect on the subjects.

## Random

Each member of a population has an equal chance of being selected in the sample.

## 4 Common Sampling Techniques.

1. Convenience Sample: Use the results that are easy to get (Not Random)
2. Systematic Sampling: Put a Pop in some order and select every " $k^{th}$ " Member.
3. Stratified Sample: Break pop into subgroups based on some characteristic then sample each group.
4. Cluster Sample: Divide pop into "Clusters" (Regardless of characteristic), Randomly select A certain # of clusters, and then collect data from the entire cluster.

## Describing Data

5 characteristics:

1. center

(In order)  
mean, median, mode

2. variation

how the data is spread

3. distribution

4. outliers

5. changes over time

$n = \#$  of items in a sample       $\bar{X} = \frac{\sum x}{n}$  Sample mean  
 $N = \#$  of items in a population       $\mu = \frac{\sum x}{N}$  Population mean

Variation:

Ways to measure.

1. Range (does not consider all values)

2. Standard deviation ( $s^2, \sigma^2$ )

Greatly affected by outliers

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$$

$$\text{or } s = \sqrt{\frac{n \sum (x^2) - (\sum x)^2}{n(n-1)}}$$

Normal Distribution. Empirical Rule

• 68% w

• 95% will fall w/in 2 std. dev "usual"

• 99.7% . . . 3 . . .

Measures of relative standing

Z-score: The # of std dev. A data value ( $x$ ) is away from the mean.

Sample

$$z = \frac{x - \bar{x}}{s}$$

Pop

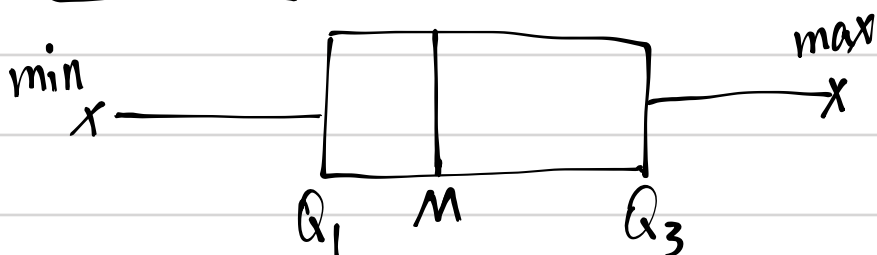
$$z = \frac{x - \mu}{\sigma}$$

Quartiles    Percentiles  $\rightarrow$  100 Parts

Box Plot

minimum    maximum  
 $Q_1$                        $Q_3$

Median



"At least one" means one or more

$$P(\text{"At least one"}) = 1 - P(\text{"None"})$$

Rules for Permutations

1.  $n$ : different items
2.  $r$ : the # of items to be arranged out of  $n$
3. Arrangement and order matters.

$${}_nP_r = \frac{n!}{(n-r)!}$$

For non-distinct items

$$\frac{n!}{n_1! n_2! n_3! \dots}$$

$n_1, n_2, \dots$  are non-distinct items

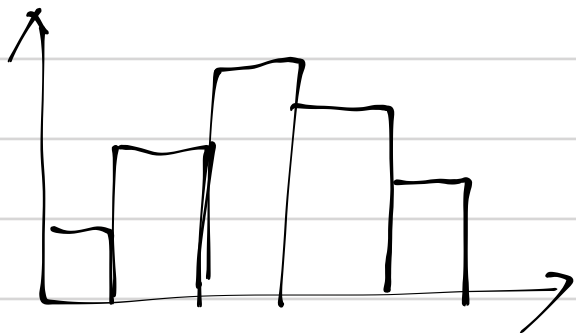
Sometimes order doesn't matter.

Combinations:

1.  $n$ . distinct items
2. select  $r$  items
3. Arrangement doesn't matter.

$${}_nC_r = \frac{n!}{(n-r)! r!}$$

Histogram form probability distribution



(Expected Value)

$$\text{Mean: } \mu = \frac{\sum (x \cdot f)}{N} = \sum [x \cdot P(x)]$$

Variance:

$$\sigma^2 = \sum [x^2 \cdot P(x)] - \mu^2$$