

KEY WORDS

Data: Any Observations that have been collected

Statistics: Collect, Analyze, Summarize, Interpret, Draw conclusion

Population: The complete set of elements being studied.

Samples: Some subset of a population.

Census: Collecting from every member of a population.

* If you collect a sample, it must be selected random.

Types of Data:

P-P Parameter: A characteristic of a population

S-S Statistic: A characteristic of a sample

Qualitative: Non-numeric

(Categorical) as mathematical are meaningless

Quantitative: Numeric

↳ Discrete. Continuous

4 Levels of Measurement

Nominal: Categories not ordered (Religion)

Ordinal: Can be ordered (Differences are meaningless)

Interval: Ordered, Differences are meaningful,

No "Nature Zero". like temperature

Ratio: Just like Interval, But with a Nature Zero
"Amount of money"

Design of Experiments / Observations

OBS VS EXP

Measures specific traits, but does not modify subjects. Apply a treatment and then measure the effect on the subjects.

Random

Each member of a population has an equal chance of being selected in the sample.

4 Common Sampling Techniques.

1. Convenience Sample: Use the results that are easy to get
(Not Random)

2. Systematic Sampling: Put a Pop in some order and select every "kTH" Member.

3. Stratified Sample: Break pop into subgroups based on some characteristic. then sample each group.

4. Cluster Sample: Divide pop into "Clusters" (Regardless of characteristic), Randomly select A certain # of clusters, and then collect data from the entire cluster.

Describing Data

5 characteristics:

1. center

(In order)

mean, median, mode

2. variation

how the data is spread

3. distribution

4. outliers

5. changes over time

$$n = \# \text{ of items in a sample} \quad \bar{X} = \frac{\sum x}{n} \text{ Sample mean}$$

$$N = \# \text{ of items in a population} \quad \mu = \frac{\sum x}{N} \text{ Population mean}$$

Variation:

Ways to measure.

1. Range (does not consider all values)
2. Standard deviation (s^2, σ^2)

Greatly affected by outliers.

$$s = \sqrt{\frac{\sum (x - \bar{x})^2}{n-1}}$$

or

$$s = \sqrt{\frac{n \sum (x^2) - (\sum x)^2}{n(n-1)}}$$

Normal Distribution. Empirical Rule

- 68% w
- 95% will fall w/in 2 std dev "usual"
- 99.7% . . . 3 . . .

Measures of relative standing

Z-score: The # of std dev. A data value (x) is away from the mean.

Sample

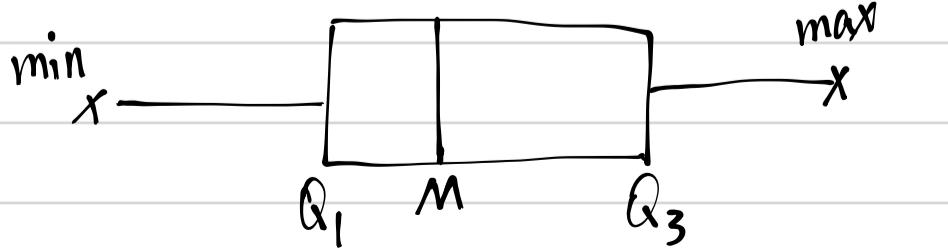
$$z = \frac{x - \bar{x}}{s}$$

Pop

$$z = \frac{x - \mu}{\sigma}$$

Quartiles Percentiles \rightarrow 100 Parts

Box Plot



minimum maximum
 Q_1 Q_3

Median

"At least one" means one or more

$$P(\text{"At least one"}) = 1 - P(\text{"None"})$$

Rules for Permutations

1. n : different items
2. r : the # of items to be arranged out of n
3. Arrangement and order matters.

$$P_r^n = \frac{n!}{(n-r)!}$$

For non-distinct items

$$\frac{n!}{n_1! n_2! n_3! \dots}$$

n_1, n_2, \dots are non-distinct items

Sometimes order doesn't matter.

Combinations:

1. n . distinct rides
2. select r items
3. Arrangement doesn't matter.

$$C_r^n = \frac{n!}{(n-r)! r!}$$

Histogram form probability distribution

(Expected Value)

$$\text{Mean: } \mu = \frac{\sum (x f)}{N} = \sum [x \cdot P(x)]$$

Variance:

$$\sigma^2 = \sum [x^2 \cdot P(x)] - \mu^2$$

