

1. BASIC DEFINITIONS

Let $f : \{0, 1\}^n \rightarrow \{0, 1\}$ be a Boolean function. For any input $x \in \{0, 1\}^n$, let $x^{(i)}$ be x with i^{th} bit flipped. Then the i^{th} bit is said to be *sensitive* for f if $f(x) \neq f(x^{(i)})$. The sensitivity of f on an input x , denoted by $s(f, x)$ is the number of sensitive bits for f on x .

Definition 1.1. The *sensitivity* of a Boolean function f , denoted by $s(f)$ is the maximum of $s(f, x)$ over all $x \in \{0, 1\}^n$.

Similarly, given $x \in \{0, 1\}^n$ and $B \subset [n]$, let x^B be x with i^{th} bit flipped for any $i \in B$. Then the "block" B is sensitive for f on x if $f(x) \neq f(x^B)$. And the *block sensitivity* of f on x , denoted by $bs(f, x)$ is the maximum number of *pairwise disjoint* sensitive blocks of f on x .

Definition 1.2. The *block sensitivity* of a Boolean function f , denoted by $bs(f)$ is the maximum of $bs(f, x)$ over all $x \in \{0, 1\}^n$.

Obviously, for any Boolean function f , we have

$$bs(f) \geq s(f).$$

Definition 1.3. A Boolean function $f : \{0, 1\}^{\binom{v}{2}} \rightarrow \{0, 1\}$ is called a *graph property* if for every input $x = (x_{(1,2)}, \dots, x_{(n-1,n)})$ and every permutation $\sigma \in S_v$, we have

$$f(x_{(1,2)}, \dots, x_{(n-1,n)}) = f(x_{(\sigma(1),\sigma(2))}, \dots, x_{(\sigma(n-1),\sigma(n))}).$$

Similarly, we can define k -uniform hypergraph property.

Definition 1.4. A Boolean function $f : \{0, 1\}^{\binom{v}{k}} \rightarrow \{0, 1\}$ is called a *k -uniform hypergraph property* if for every input $x = (x_{(1,2,\dots,k)}, \dots, x_{(n-k+1,\dots,n-1,n)})$ and every permutation $\sigma \in S_v$, we have

$$f(x_{(1,2,\dots,k)}, \dots, x_{(n-k+1,\dots,n-1,n)}) = f(x_{(\sigma(1),\sigma(2),\dots,\sigma(k))}, \dots, x_{(\sigma(n-k+1),\dots,\sigma(n-1),\sigma(n))}).$$