

Rational Exponents & Radicals

SWBAT simplify exponential expressions by properly using properties of exponents.

SWBAT simplify radical expressions by factoring out primes of the radicand.

SWBAT simplify radical expressions using properties of radicals.

SWBAT convert from radical form to rational exponent form.

SWBAT simplify rational exponents using properties of exponents

SWBAT evaluate rational exponential expressions by breaking them apart into the product property.

SWBAT solve a square root equation.

SWBAT solve a radical equation with index > 2 .

SWBAT identify extraneous solutions of radical equations.

SWBAT solve an equation that has an exponent by using the reciprocal exponent as the inverse function.

SWBAT identify exponential functions, and differentiate between exponential and power functions.

SWBAT graph exponential functions by using a t-chart.

SWBAT graph exponential functions without using a t-chart.

SWBAT determine the end behavior of an exponential function.

SWBAT identify translations of the exponential graph by identifying key parts of the equation.

SWBAT calculate compound interest given the interest rate, number of years, and number of times per year, and the principal.

SWBAT use the number e as an exponential base for continuously compounded interest.

Standards

Real Number System

N-RN.1

Explain how the definition of the meaning of rational exponents follows from extending the properties of integer exponents to those values, allowing for a notation for radicals in terms of rational exponents. For example, we define $5^{\frac{1}{3}}$ to be the cube root of 5 because we want $\left(5^{\frac{1}{3}}\right)^3 = \left(5^{\frac{1}{3}}\right)^3$ to hold, so $\left(5^{\frac{1}{3}}\right)^3$ must equal 5.

2. Rewrite expressions involving radicals and rational exponents using the properties of exponents.

Creating Equations A -CED Create equations that describe numbers or relationships

1. Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear and quadratic functions, and simple rational and exponential functions.

Interpreting Functions F-IF Analyze functions using different representations

7. Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.

e. Graph exponential and logarithmic functions, showing intercepts and end behavior, and trigonometric functions, showing period, midline, and amplitude.

Pre-Assessment

To introduce our topic of exponential functions the students will begin by learning properties of exponents. The students should have already encountered this before, but since this information is necessary for our topic we will review the content and make sure that there are absolutely no misconceptions.

Assessments

Homework will be graded, there will be a lab, and test on this material.

Before & After

Before the students learned about creating algebraic expressions that represent a rule. This lesson prepares students for the extension of those that we just learned in our first unit. While we were learning about arithmetic functions before, we are now moving towards exponential functions.

After we will be learning how to solve for an exponential expression. This requires knowledge of the properties of exponents and rational exponents. From there we will analyze and model exponential functions.

Connections

Pre-Assessment

Properties of Exponents

1. **Product Property:** $a^m \cdot a^n = a^{m+n}$ **and** $(xy)^m = x^m \cdot y^m$

Example: $2^6 \cdot 2^8 = 2^{14}$ **and** $(2x)^5 = 2^5 \cdot x^5$

2. **Power Property:** $(a^m)^n = a^{(m \cdot n)}$

Example: $(g^2)^3 = g^6$

3. **Quotient Property:** $\frac{a^m}{a^n} = a^{m-n}$

Example: $\frac{k^7}{k^4} = k^3$ and $\frac{k^2}{k^8} = k^{-6}$

4. **Negative Property:** $a^{-n} = \frac{1}{a^n}$ and $\frac{1}{a^{-n}} = a^n$

Example: $2^{-1} = \frac{1}{2}$ **and** $\left(\frac{1}{2}\right)^{-1} = 2$ **and** $\left(\frac{2}{3}\right)^{-1} = \frac{3}{2}$

5. **Zero Property:** $a^0 = 1$

Example: $555,987,123,987,123^0 = 1$

6. **Power of a Quotient Property:** $\left(\frac{a}{b}\right)^n = \frac{a^n}{b^n}$

Example: $\left(\frac{2}{3}\right)^3 = \frac{2^3}{3^3} = \frac{8}{27}$

Properties of Exponents – Notes

1. Product Property:

Example:

2. Power Property:

Example:

3. Quotient Property:

Example:

4. Negative Property:

Example:

5. Zero Property:

Example:

6. Power of a Quotient Property:

Example:

Board Work

Simplify each expression.

1. $f^3 \cdot f^5 =$

2. $7^3 \cdot 7^7 =$

3. $(bc)^5 =$

4. $(2g)^3 =$

5. $(u^9)^{10} =$

6. $(4^2)^5 =$

7. $\frac{v^8}{v^2} =$

8. $\frac{v^2}{v^8} =$

9. $\left(\frac{2}{3}\right)^4 =$

10. $q^{-1} =$

11. $6^{-3} =$

Challenge problem: $\frac{9x^2y^3z^2}{3xy^{-5}z^6} =$

You Try: Partner Work

Section 1: Multiplication– Simplify each product of exponents. Leave answers in exponential form.

Example 1: $x^5 \cdot x^2 = x^7$

1. $y^6 \cdot y^4 =$ _____

3. $5^3 \cdot (5n)^2 =$ _____

2. $(7h)^3 =$ _____

4. $(2n)^3 \cdot 2^2 =$ _____

Section 2: Fractions & division – Simplify each expression. Make sure there are no negative exponents. Leave answers in exponential form.

5. $\left(\frac{1}{n}\right)^3 =$ _____

7. $\frac{h^9}{h^{12}} =$ _____

6. $\frac{p^6}{p^3} =$ _____

8. $\left(\frac{2^2 m^3 n^2}{2mn^2}\right) =$ _____

Section 3: Negative and Zero Exponents – Simplify each expression so that there are no negative exponents. Leave answers in exponential form.

9. $6^{-2} =$ _____

11. $\left(\frac{1}{10}\right)^{-3} =$ _____

10. $(bagillion)^0 =$ _____

12. $\left(\frac{7}{2}\right)^2 =$ _____

Section 4: Powers of exponents– Simplify so that there is only one level of exponent (e.g. **don't** write 2^{2^2} as an answer). Leave answers in exponential form.

13. $(2^2)^2 =$ _____

15. $\left(\frac{1}{2}\right)^{10} =$ _____

14. $(c^5)^7 =$ _____

16. $\left(\left(\frac{3}{4}\right)^{-1}\right)^{-1} =$ _____

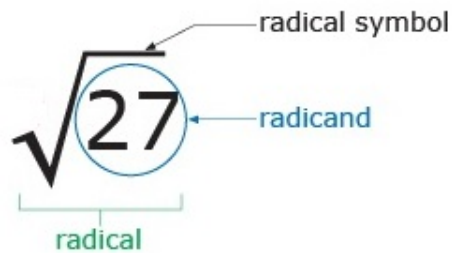
Square Roots

Square Roots are the opposite of squares (exponent of 2). This is also called an *inverse*.

$$\sqrt{a^2} = a$$

There are 2 parts to a squareroot.

1. the *RADICAL*
2. the *RADICAND*

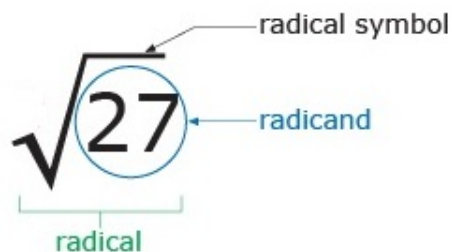


The *radical* tells us that we're looking for identical factors.

the *radicand* is a number that needs to be factored so we can pull out the identical ones.

Example: $\sqrt{25} = \sqrt{5 \cdot 5} \implies$ since there are 2 5's $\implies \sqrt{5 \cdot 5} = 5$

Simplifying Square Root Expressions



To simplify radical expressions follow these steps

Step 1: factor the radicand

Step 2: pull out factors that a repeated twice.

Step 3: all other factors stay inside the radical

Examples: Simplify the square root.

We try:

1. $\sqrt{36}$

2. $\sqrt{50}$

3. $\sqrt{27}$

4. $\sqrt{27x^2}$

You Try:

5. $\sqrt{120}$

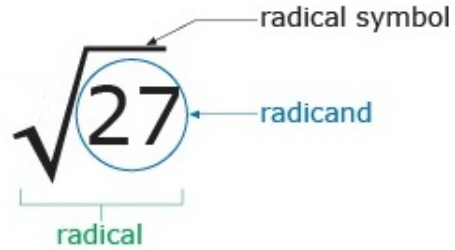
6. $\sqrt{52y^4}$

7. $\sqrt{16}$

8. $\sqrt{160n^7}$

Challenge Problem: $\sqrt[5]{800h^{11}}$

Simplifying Square Root Expressions– Guided Notes



To simplify radical expressions follow these steps

Step 1:

Step 2:

Step 3:

Examples: Simplify the square root.

We try:

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2. $\sqrt{50}$

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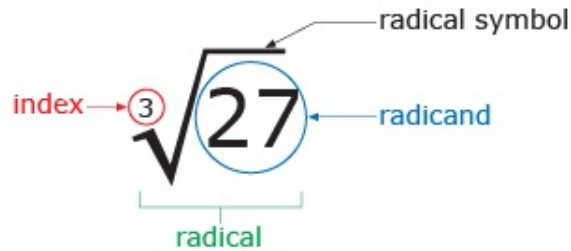
Other Roots

Roots are the opposite of exponents. This is also called an *inverse*.

$$\sqrt[n]{a^n} = a$$

There are *actually* 3 parts to a radical. Square-roots don't have an index because we assume it's 2.

1. the *RADICAL*
2. the *RADICAND*
3. the *INDEX*



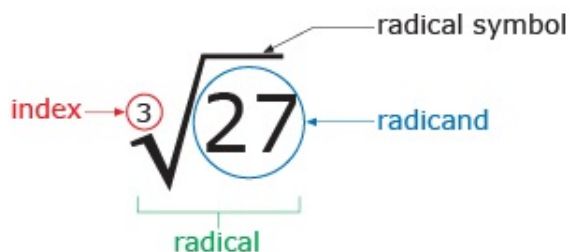
The **radical** tells us that we're looking for identical factors.

The **index** tells us how many identical factors we're looking for.

the **radicand** is a number that needs to be factored so we can pull out the identical ones.

Example: $\sqrt[3]{125} = \sqrt[3]{5 \cdot 5 \cdot 5} \implies$ since the index is 3, and there are 3- 5's $\implies \sqrt[3]{5 \cdot 5 \cdot 5} = 5$

Simplifying Radical Expressions



To simplify radical expressions follow these steps

Step 1: determine the index

Step 2: factor the radicand

Step 3: pull out repeated factors of the amount of the index

Step 4: all other factors stay inside the radical

Examples: Simplify the radical, keep track of the index

We try:

You Try:

1. $\sqrt[3]{8}$

5. $\sqrt[3]{120}$

2. $\sqrt[4]{48}$

6. $\sqrt[4]{162y^4}$

3. $\sqrt[3]{27}$

7. $\sqrt[4]{32}$

4. $\sqrt[3]{27x^5}$

8. $\sqrt[3]{162n^7}$

Challenge Problem: $\sqrt[5]{800h^{11}}$

Other Roots– Guided Notes

Roots are the opposite of exponents. This is also called an *inverse*.

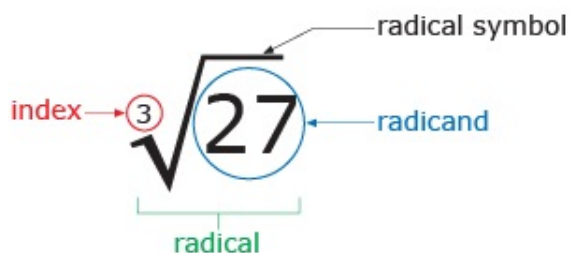
$$\sqrt[n]{a^n} = a$$

There are *actually* 3 parts to a radical. Square-roots don't have an index because we assume it's 2.

1. the

2. the

3. the



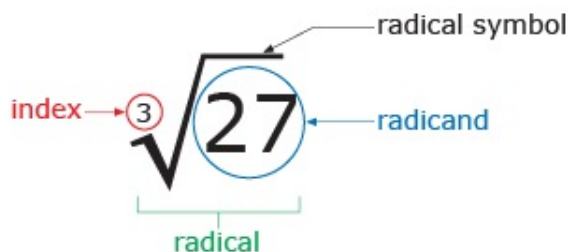
The **radical**

The

the

Example: $\sqrt[3]{125} =$

Simplifying Radical Expressions – Guided Notes



To simplify radical expressions follow these steps

Step 1:

Step 2:

Step 3:

Step 4:

Examples: Simplify the radical, keep track of the index

We try:

You Try:

1. $\sqrt[3]{8}$

5. $\sqrt[3]{120}$

2. $\sqrt[4]{48}$

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3. $\sqrt[3]{27}$

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Challenge Problem: $\sqrt[5]{800h^{11}}$

Add & Subtract Radical Expressions

When adding and subtracting radical expressions, treat the radical like a variable whenever possible.

$$\sqrt{a} + \sqrt{a} = 2\sqrt{a}$$

The roots need to be exactly the same (i.e. same index, same radicand) to be able to add or subtract.

Example 1: $5\sqrt{7} - 3\sqrt{7} = 2\sqrt{7}$

Sometimes the radical needs to be simplified before adding or subtracting.

Example 2: $\sqrt{3} + \sqrt{12} =$

You Try:

1. $8\sqrt{h} + 9\sqrt{h} =$

2. $2\sqrt{x} - \sqrt{x} =$

3. $6\sqrt{p} - 10\sqrt{p} =$

4. $\sqrt[3]{81} + \sqrt[3]{3} =$

5. $\sqrt{8} + \sqrt{32} - \sqrt{2} =$

Multiplication & Division with Radical Expressions

If two roots (with the same index) are multiplied, just multiply the inside numbers.

$$\sqrt{a} \cdot \sqrt{b} = \sqrt{a \cdot b}$$

$$\sqrt{a \cdot b} = \sqrt{a} \cdot \sqrt{b}$$

Example 1: $\sqrt[5]{8} \cdot \sqrt[5]{4} =$

Example 2: $3\sqrt{5} \cdot 4\sqrt{6} =$

Example 3: $(2 + \sqrt{h})(5 + \sqrt{h}) =$

Dividing is just as easy. The square-root symbol can be either broken or put together to the top and bottom.

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

Example 3: $\sqrt{\frac{16}{25}} =$

Example 4: $\sqrt{\frac{8}{100}} =$

You Try:

1. $\sqrt{10} \cdot \sqrt{10} =$

4. $\sqrt{\frac{3}{4}} =$

2. $\sqrt{12} \cdot \sqrt{4} =$

5. $\sqrt{\frac{9}{4}} =$

3. $(-1 + \sqrt{3})(8 - \sqrt{6}) =$

6. $\sqrt{\frac{25}{75}} =$

Add & Subtract Radical Expressions – Guided Notes

When adding and subtracting radical expressions, treat the radical like a variable whenever possible.

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Multiplication & Division with Radical Expressions – Guided Notes

If two roots (with the same index) are multiplied, just multiply the inside numbers.

$$\sqrt{a} \cdot \sqrt{b} =$$

$$\sqrt{a \cdot b} =$$

Example 1: $\sqrt[5]{8} \cdot \sqrt[5]{4} =$

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Example 3: $\sqrt{\frac{16}{25}} =$

Example 4: $\sqrt{\frac{8}{100}} =$

You Try:

1. $\sqrt{10} \cdot \sqrt{10} =$

4. $\sqrt{\frac{3}{4}} =$

2. $\sqrt{12} \cdot \sqrt{4} =$

5. $\sqrt{\frac{9}{4}} =$

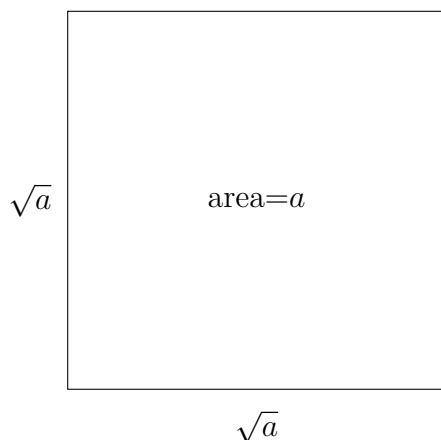
3. $(-1 + \sqrt{3})(8 - \sqrt{6}) =$

6. $\sqrt{\frac{25}{75}} =$

Rational Exponents

Rational = Fraction

What does it mean to have a fraction in the exponent?



Area of a square = (side length)².

This makes sense because $a = \sqrt{a}\sqrt{a} = \sqrt{a^2}$

(or $a = \sqrt{a}\sqrt{a} = (\sqrt{a})^2$ they're both the same.)

Using our **product property of exponents**, which power, when added to itself is 1?

$$a = a^{\frac{1}{2}} \cdot a^{\frac{1}{2}} = \left(a^{\frac{1}{2}}\right)^2$$

since we add the exponents. From here we learn that $\sqrt{a} = a^{\frac{1}{2}}$

Having a fraction in the exponent is called a **RATIONAL EXPONENT**. A *rational exponent* is just another way to write a root.

$$\sqrt{n} = n^{\frac{1}{2}}$$

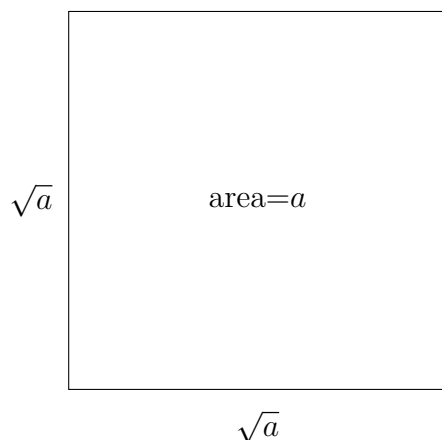
or more generically, for any index a

$$\sqrt[a]{n^b} = n^{\frac{b}{a}}$$

Rational Exponents – Guided Notes

Rational = Fraction

What does it mean to have a fraction in the exponent?



Area of a square = (side length)².

This makes sense because $a =$

(or $a =$ they're both the same.)

Using our **product property of exponents**, which power, when added to itself is 1?

$$a =$$

Having a fraction in the exponent is called a **RATIONAL EXPONENT**. A *rational exponent* is just another way to write a root.

$$\sqrt{n} =$$

or more generically, for any index a

$$\sqrt{\quad} = n$$

OMG that looks scary...

Rational Exponents – What’s the point?

1. It’s more natural given what we know about roots and their inverses.
2. For the sake of exponential functions.
3. Sometimes calculators have an exponent button, but no root button *index* > 3.
4. Intentionally left blank for student response.

Board Work: Convert the following from radical form into rational exponent form.

1. $\sqrt[3]{9^2} =$
2. $\sqrt[6]{j^5} =$
3. $\sqrt[10]{3^3 \cdot k^7} =$

You Try: Convert the following radical expressions into rational exponent expressions.

- | | |
|-------------------|-------------------------|
| 1. $\sqrt{7} =$ | 3. $\sqrt[3]{27j^3} =$ |
| 2. $\sqrt{h^3} =$ | 4. $\sqrt[5]{k^{10}} =$ |

You Try: Convert the rational exponent into a radical – You don’t need to simplify

- | | |
|------------------------|------------------------------|
| 5. $8^{\frac{1}{2}} =$ | 7. $(5h)^{\frac{3}{2}} =$ |
| 6. $3^{\frac{7}{8}} =$ | 8. $(10k^2)^{\frac{1}{3}} =$ |

You Try: Create your own rational exponent conversion. Make there is a number base and a variable base with and index > 1, and an exponent > 1.

Simplifying Rational Exponential Expressions

Use the properties of exponents to convert, and simplify the radicals and rational exponents.

The Product Property: $a^m \cdot a^n = a^{(m+n)}$

$$8^{\frac{1}{2}} \cdot 8^{\frac{3}{2}} =$$

The Product Property 2: $(a \cdot b)^m = a^m \cdot b^m$

$$(5x)^{\frac{3}{2}} =$$

The Power Property: $(a^m)^n = a^{(m \cdot n)}$

$$\left(h^{\frac{5}{7}}\right)^{\frac{6}{5}} =$$

The Quotient Property: $\frac{a^m}{a^n} = a^{m-n}$

$$\left(\frac{3^{\frac{3}{2}}}{3^{\frac{1}{2}}}\right) =$$

The Negative Property: $a^{-b} = \frac{1}{a^b}$ or $\frac{1}{a^{-b}} = a^b$

$$(81)^{-\frac{1}{2}} =$$

Power of a Quotient Property: $\left(\frac{a}{b}\right)^c = \frac{a^c}{b^c}$

$$\left(\frac{9}{4}\right)^{\frac{1}{2}} =$$

Evaluating Rational Exponents

3-Step process for evaluating rational exponential expressions. $a^{\frac{m}{n}}$

1. Factor the base of the exponent
2. Determine the ratio of bases $\frac{m}{n}$
3. Pull out the ratio amount of the bases.

Example: $(216)^{\frac{2}{3}}$

1. $(216)^{\frac{2}{3}} = (2 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 3)^{\frac{2}{3}}$
2. Ratio = $\frac{2}{3}$
3. Pull out $\frac{2}{3}$ of each factor – $(2 \cdot 2 \cdot 2 \cdot 3 \cdot 3 \cdot 3)^{\frac{2}{3}} = 2 \cdot 2 \cdot 3 \cdot 3 = 36$

You Try: Evaluate the rational exponential expressions. Keep an eye out for properties of exponents.

1. $25^{\frac{1}{2}}$

5. $32^{\frac{3}{5}}$

2. $1000^{\frac{2}{3}}$

6. $16^{-\frac{5}{2}}$

3. $121^{\frac{3}{2}}$

7. $0.04^{\frac{1}{2}}$

4. $49^{-\frac{1}{2}}$

8. $\left(\frac{1}{125}\right)^{-\frac{1}{3}}$

Simplifying Rational Exponential Expressions

Use the properties of exponents to convert, and simplify the radicals and rational exponents.

The Product Property: $a^m \cdot a^n = a^{(m+n)}$

$$8^{\frac{1}{2}} \cdot 8^{\frac{3}{2}} =$$

The Product Property 2: $(a \cdot b)^m = a^m \cdot b^m$

$$(5x)^{\frac{3}{2}} =$$

The Power Property: $(a^m)^n = a^{(m \cdot n)}$

$$\left(h^{\frac{5}{7}}\right)^{\frac{6}{5}} =$$

The Quotient Property: $\frac{a^m}{a^n} = a^{m-n}$

$$\left(\frac{3^{\frac{3}{2}}}{3^{\frac{1}{2}}}\right) =$$

The Negative Property: $a^{-b} = \frac{1}{a^b}$ or $\frac{1}{a^{-b}} = a^b$

$$(81)^{-\frac{1}{2}} =$$

Power of a Quotient Property: $\left(\frac{a}{b}\right)^c = \frac{a^c}{b^c}$

$$\left(\frac{9}{4}\right)^{\frac{1}{2}} =$$

Evaluating Rational Exponents – Notes

3-Step process for evaluating rational exponential expressions. $a^{\frac{m}{n}}$

1.

2.

3.

Example: $(216)^{\frac{2}{3}}$

1. $(216)^{\frac{2}{3}} =$

2. Ratio =

3. Pull out _____ of each factor

You Try: Evaluate the rational exponential expressions. Keep an eye out for properties of exponents.

1. $25^{\frac{1}{2}}$

5. $32^{\frac{3}{5}}$

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3. $121^{\frac{3}{2}}$

7. $0.04^{\frac{1}{2}}$

4. $49^{-\frac{1}{2}}$

8. $\left(\frac{1}{125}\right)^{-\frac{1}{3}}$

Review

Properties of Exponents: Use the properties of exponents to simplify the exponential expressions. Make sure there are no negative exponents.

1. $f^3 \cdot f^6$

5. $\frac{k^2}{k^6}$

2. $(5h)^4 =$

6. $109745^0 =$

3. $(m^4)^8 =$

7. $\left(\frac{2}{9}\right)^6 =$

4. $\frac{t^6}{t^4}$

8. $2^{-4} =$

Radical Expressions: Simplify the radical expressions by factoring.

9. $\sqrt{9}$

12. $\sqrt[3]{81}$

10. $\sqrt{50}$

13. $\sqrt{25m^3}$

11. $\sqrt[3]{27}$

14. $\sqrt[3]{54h^6}$

Operations with Radicals: Use properties of radicals to simplify the expressions.

15. $5\sqrt{3} + 3\sqrt{3}$

18. $\sqrt{8m} \cdot \sqrt{2m}$

16. $9\sqrt[3]{9} - 11\sqrt[3]{9}$

19. $\sqrt[5]{2^6 j^8} \cdot \sqrt[5]{2j^2}$

17. $\sqrt{2} \cdot \sqrt{3}$

20. $\sqrt{\frac{64}{81}}$

Rational Exponents: Convert the radical into a rational exponent.

21. $\sqrt{2}$

24. $\sqrt[10]{m^7}$

22. $\sqrt{5^2}$

25. $\sqrt[4]{h^3b^5}$

23. $\sqrt[3]{k^3}$

26. $\sqrt[3]{p}$

Properties of Exponents on Rational Exponents: Use the properties of exponents to simplify the rational exponents.

27. $h^{\frac{2}{3}} \cdot h^{\frac{2}{3}}$

29. $(m^6)^{\frac{5}{4}}$

28. $(8g)^{\frac{7}{12}}$

30. $\left(\frac{9}{16}\right)^{\frac{1}{2}}$

Evaluating Rational Exponential Expressions: Evaluate the rational exponential Expression.

31. $9^{\frac{3}{2}}$

32. $27^{\frac{2}{3}}$

33. $64^{\frac{2}{3}}$

34. $216^{\frac{2}{3}}$

35. $32^{\frac{6}{5}}$

Exponents & Radicals Test Review

Mr. Wolf
Pre-Calculus
MC²High
2015-2016

NAME: _____

DATE: _____

Simplify the exponential expression using properties of exponents (1 point each)

1. $j^5 \cdot j^8 = j^{13}$

5. $6^{-4} =$

2. $(k^2m)^8 = k^{16}m^8$

6. $\frac{7}{8}^{-2} =$

3. $\left(\frac{h}{k}\right)^6 = \frac{h^6}{k^6}$

7. $9^0 =$

4. $(g^5)^8 = g^{40}$

8. $0^0 =$

Simplify the radicals (2 points each)

9. $\sqrt{16}$

11. $\sqrt[3]{16}$

10. $\sqrt{18}$

12. $\sqrt[3]{72}$

Simplify the radical expressions using properties of radicals (1 point each)

13. $\sqrt{2} \cdot \sqrt{32}$

15. $\sqrt{2} + \sqrt{2}$

14. $\sqrt[3]{2} \cdot \sqrt[4]{32}$

16. $12\sqrt{10} - 17\sqrt{10}$

Convert from radical to rational exponent (2 points each)

17. $\sqrt{8}$

19. $\sqrt[5]{k^3}$

18. $\sqrt[3]{7^2}$

20. $\sqrt[4]{2^5 m^9}$

Simplify the expressions using properties of exponents and rational exponents
(2 points each)

21. $(5^3)^{\frac{1}{8}}$

24. $p^{\frac{2}{7}} \cdot p^{\frac{3}{7}}$

22. $(3k)^{\frac{1}{2}}$

25. $\left(\frac{3}{2}\right)^{-\frac{5}{4}}$

23. $\left(\frac{9}{2}\right)^{\frac{3}{2}}$

26. $\left(7^{\frac{1}{2}} d\right)^{\frac{1}{3}}$

Evaluate the exponential expression (2 points each)

27. $16^{\frac{1}{2}}$

29. $100^{\frac{5}{2}}$

28. $25^{\frac{3}{2}}$

30. $32^{\frac{2}{5}}$

Pre-assessment: This place will be extra credit on the real test.

The function $f(x) = 2^x$ is an exponential function. What happens to the y value as x increases? What happens to the y value as x decreases?

Will the graph go below 0? If not how can we change it to go below 0?

Exponents & Radicals Test Review

Mr. Wolf
Pre-Calculus
MC²High
2015-2016

NAME: _____

DATE: _____

Simplify the exponential expression using properties of exponents (1 point each)

1. $j^5 \cdot j^8 =$

5. $6^{-4} =$

2. $(k^2m)^8 =$

6. $\frac{7}{8}^{-2} =$

3. $\left(\frac{h}{k}\right)^6 =$

7. $9^0 =$

4. $(g^5)^8 =$

8. $0^0 =$

Simplify the radicals (2 points each)

9. $\sqrt{16} =$

11. $\sqrt[3]{16} =$

10. $\sqrt{18} =$

12. $\sqrt[3]{72} =$

Simplify the radical expressions using properties of radicals (1 point each)

13. $\sqrt{2} \cdot \sqrt{32} =$

15. $\sqrt{2} + \sqrt{2} =$

14. $\sqrt[3]{2} \cdot \sqrt[4]{32} =$

16. $12\sqrt{10} - 17\sqrt{10} =$

Convert from radical to rational exponent (2 points each)

17. $\sqrt{8} =$

19. $\sqrt[5]{k^3} =$

18. $\sqrt[3]{7^2} =$

20. $\sqrt[4]{2^5 m^9} =$

Simplify the expressions using properties of exponents and rational exponents
(2 points each)

21. $(5^3)^{\frac{1}{8}} =$

24. $p^{\frac{2}{7}} \cdot p^{\frac{3}{7}} =$

22. $(3k)^{\frac{1}{2}} =$

25. $\left(\frac{3}{2}\right)^{-\frac{5}{4}} =$

23. $\left(\frac{9}{2}\right)^{\frac{3}{2}} =$

26. $\left(7^{\frac{1}{2}} d\right)^{\frac{1}{3}} =$

Evaluate the exponential expression (2 points each)

27. $16^{\frac{1}{2}} =$

29. $100^{\frac{5}{2}} =$

28. $25^{\frac{3}{2}} =$

30. $32^{\frac{2}{5}} =$

Pre-assessment: This place will be extra credit on the real test.

The function $f(x) = 2^x$ is an exponential function. What happens to the y value as x increases? What happens to the y value as x decreases?

Will the graph go below 0? If not how can we change it to go below 0?

Rational Exponents & Radicals Test

Mr. Wolf
Pre-Calculus
MC²High
2015-2016

NAME: _____

DATE: _____

Simplify the exponential expression using properties of exponents (2 point each)

1. $j^4 \cdot j^7 =$

5. $b^{-5} =$

2. $(k^3m)^9 =$

6. $\left(\frac{9}{10}\right)^{-8} =$

3. $\left(\frac{2h}{k}\right)^5 =$

7. $100^0 =$

4. $(g^4)^7 =$

8. $(-14)^0 =$

Simplify the radicals (4 points each)

9. $\sqrt{32}$

11. $\sqrt[3]{32}$

10. $\sqrt{48}$

12. $\sqrt[3]{48}$

Simplify the radical expressions using properties of radicals (2 point each)

13. $\sqrt{3} \cdot \sqrt{27}$

15. $\sqrt{5} + 2\sqrt{5}$

14. $\sqrt[3]{3} \cdot \sqrt[3]{27}$

16. $\sqrt{8} - 9\sqrt{8}$

Convert from radical to rational exponent (4 points each)

17. $\sqrt{7}$

19. $\sqrt[5]{m^{12}}$

18. $\sqrt[3]{h^4}$

20. $\sqrt[4]{2^{10}p}$

Simplify the expressions using properties of exponents and rational exponents
(4 points each)

21. $(p^4)^{\frac{1}{8}}$

24. $g^{\frac{3}{8}} \cdot g^{\frac{1}{2}}$

22. $(4k)^{\frac{1}{4}}$

25. $\left(\frac{2}{3}\right)^{-\frac{9}{4}}$

23. $\left(\frac{5}{4}\right)^{\frac{5}{4}}$

26. $\left(8^{\frac{3}{2}}d\right)^{\frac{2}{3}}$

Evaluate the exponential expression (4 points each)

27. $49^{\frac{1}{2}}$

29. $100^{\frac{3}{2}}$

28. $25^{\frac{5}{2}}$

30. $32^{\frac{3}{5}}$

EXTRA CREDIT: Simplify the expression (10 points) – Must be completely correct.

$$\left(\frac{2xy^2z^{-5}}{5z^{-2}y^7}\right) \cdot \left(\frac{2z^5y^{-23}}{5x^{-1}y^{-18}z^8}\right)^{-1}$$

Rational Exponents & Radicals Make-up Test

Mr. Wolf
Pre-Calculus
MC²High
2015-2016

NAME: _____

DATE: _____

Simplify the exponential expression using properties of exponents (2 point each)

1. $j^9 \cdot j^5 =$

5. $b^{-8} =$

2. $(k^4m)^{10} =$

6. $\left(\frac{11}{13}\right)^{-7} =$

3. $\left(\frac{2h}{k}\right)^8 =$

7. $6^0 =$

4. $(g^8)^2 =$

8. $(-9)^0 =$

Simplify the radicals (4 points each)

9. $\sqrt{40}$

11. $\sqrt[3]{40}$

10. $\sqrt{189}$

12. $\sqrt[3]{189}$

Simplify the radical expressions using properties of radicals (2 point each)

13. $\sqrt{4} \cdot \sqrt{16}$

15. $4\sqrt{3} + 2\sqrt{3}$

14. $\sqrt[3]{6} \cdot \sqrt[3]{36}$

16. $7\sqrt{7} - 5\sqrt{7}$

Convert from radical to rational exponent (4 points each)

17. $\sqrt{2}$

19. $\sqrt[5]{m^3}$

18. $\sqrt[3]{h^6}$

20. $\sqrt[4]{2^4 p}$

Simplify the expressions using properties of exponents and rational exponents
(4 points each)

21. $(p^{11})^{\frac{3}{11}}$

24. $g^{\frac{11}{8}} \cdot g^{\frac{4}{2}}$

22. $(4k)^{\frac{1}{6}}$

25. $\left(\frac{2}{3}\right)^{-\frac{2}{5}}$

23. $\left(\frac{5}{3}\right)^{\frac{5}{4}}$

26. $\left(8^{\frac{3}{10}} d\right)^{\frac{2}{12}}$

Evaluate the exponential expression (4 points each)

27. $36^{\frac{1}{2}}$

29. $49^{\frac{3}{2}}$

28. $16^{\frac{5}{2}}$

30. $81^{\frac{5}{4}}$

EXTRA CREDIT: Simplify the expression (10 points) – Must be completely correct.

$$\left(\frac{2}{x^2}\right) \cdot \left(\frac{y^2}{x}\right)^{-\frac{1}{2}} \cdot \left(\frac{x^{\frac{1}{2}}}{y}\right)$$

Solving Radicals and Exponential Equations

Solve the equations for the variable.

1. $5x = 60$

2. $b - 12 = 5$

3. $p + 17 = 20$

4. $\frac{h}{3} = 9$

5. $\frac{5}{h} = \frac{20}{12}$

Question: How did you solve these problems?

Answer: By using the inverse operation.

Exponential expressions also have inverse operations, so we can solve for an exponential expression by using the inverse operation.

4-step process

1. Isolate the radical/exponent
2. Use inverse operation
3. Solve for the variable
4. Check your answer

Example: Solve for the variable

$$\sqrt{g} + 5 = 14$$

$$\sqrt{2x} + 7 = 19$$

$$\sqrt{g} = 9$$

$$\sqrt{2x} = 12$$

$$g = 9^2$$

$$2x = 12^2$$

$$2x = 144$$

$$g = 81$$

$$x = 72$$

Use the 4-step process to solve for the variable.

1. $\sqrt{x} + 3 = 5$

2. $16 - \sqrt{y} = 8$

Keep using the 4-step process. – These look a lot scarier than they really are

3. $3\sqrt{2x - 3} - 4 = 2$

4. $\sqrt{8x + 5} - 3 = 2$

Bell Work

1. $2\sqrt{x} = 16$

2. $3\sqrt{y-1} = 30$

3. $7\sqrt{2d+1} = 35$

Indices > 2

The inverse operation of a square root is a square (power of 2). The index of a square root is 2, so the inverse operation is the second power.

Similarly, if there is any other root greater than 2, the inverse operation will be a power that is the same number as the root's index. The 4-step process still applies.

Example 1: $\sqrt[3]{x} = 5$

$$\begin{aligned}(\sqrt[3]{x})^3 &= 5^3 \\ x &= 125\end{aligned}$$

Example 2: $\sqrt[5]{b+12} = 2$

You Try: Solve the radical equations

1. $\sqrt[3]{2h-4} = 6$

4. $3\sqrt[3]{4d+8} = 6$

2. $\sqrt[4]{5b} = 10$

5. $2\sqrt[3]{2k-4} + 7 = 47$

3. $10\sqrt[5]{9x} = 30$

6. $\sqrt[5]{2r} = -2$

Extraneous Solutions

In order to understand *extraneous solutions* we need to understand a fundamental idea of the nature of negative numbers.

Powers of 2 VS. powers of -2

$2^2 = 4$	$(-2)^2 = 4$
$2^3 = 8$	$(-2)^3 = -8$
$2^4 = 16$	$(-2)^4 = 16$
$2^5 = 32$	$(-2)^5 = -32$
\vdots	\vdots

Powers of 3 VS. powers of -3

$3^2 = 9$	$(-3)^2 = 9$
$3^3 = 27$	$(-3)^3 = -27$
$3^4 = 81$	$(-3)^4 = 81$
$3^5 = 243$	$(-3)^5 = -243$
\vdots	\vdots

hmmm... even powers of negative numbers will result in positive numbers, while the odd powers of negative numbers will result in odd numbers.

Let's see what this means practically. Use the 4-step process on the following problem.

$$\sqrt{x} + 18 = 9$$

When the solution is plugged back into the original, we get an untrue statement.

Big Rule: The solution to a square root problem (or any even index) can't be a negative number!

These are called *EXTRANEIOUS SOLUTIONS*. They are solutions you get while doing correct math, but they don't fit back into the equation. The proper way to answer the equation is to find the answer, then state that it is an extraneous solution.

Bell Work

Solve the radical expression. Use the 4-step process.

1. $\sqrt[3]{2x+5} = 5$

2. $\sqrt[4]{4t-4} = 4$

3. $\sqrt[3]{3k+3} - 3 = 3$

4. $\sqrt{w+12} = \sqrt{2x}$

Equations with Rational Exponents

This is why rational exponents are so much cooler than radicals

Same basic process as above:

1. Isolate the exponent
2. Use inverse (reciprocal) operation
3. Solve for variable
4. Check answer

Use the reciprocal of the rational exponent to find the answer.

Example:

$$p^{\frac{3}{2}} - 2 = 6$$

$$(w - 10)^{\frac{4}{5}} + 7 = 23$$

$$p^{\frac{3}{2}} = 8$$

$$(w - 10)^{\frac{4}{5}} = 16$$

$$p = 8^{\frac{2}{3}}$$

$$(w - 10) = 16^{\frac{5}{4}}$$

$$w - 10 = 32$$

$$p = 4$$

$$w = 42$$

You Try: Solve the exponential expressions using the 4-step process.

1. $x^{\frac{1}{2}} + 3 = 5$

4. $d^{\frac{2}{5}} = 4$

2. $16 - y^{\frac{1}{2}} = 8$

5. $(t - 7)^{\frac{1}{3}} = 5$

3. $c^{\frac{3}{2}} = 27$

6. $2(12p + 4)^{\frac{5}{2}} = 200,000$

Solving Radicals Quiz Review

Mr. Wolf
Pre-Calculus
MC²High
2015-2016

NAME: _____

DATE: _____

Solve the radical equations: Use the 4-step process to solve the square-root equation.

1. $\sqrt{3p-2} = 10$

2. $\sqrt{6f} = 12$

3. $5\sqrt{9y+4} = 125$

4. $7\sqrt{r} - 6 = 43$

5. $8\sqrt{11s} = 88$

Solve the radical equations: Use the 4-step process to solve the radical equations. These **ALL** have an index greater than 2.

6. $\sqrt[3]{8t} = 4$

7. $\sqrt[3]{2x+15} = 5$

8. $\sqrt[4]{4t} + 2 = 4$

9. $\sqrt[3]{6k+3} - 3 = 3$

10. $\sqrt[4]{w+12} = 2$

Solve the rational exponential equations: Use the 4-step process to solve.

11. $x^{\frac{1}{2}} + 3 = 6$

12. $2y^{\frac{1}{2}} = 8$

13. $2c^{\frac{3}{2}} = 16$

14. $d^{\frac{3}{5}} = 64$

15. $(t - 7)^{\frac{1}{3}} = 6$

Solving Radicals QUIZ – Open Note

Mr. Wolf
Pre-Calculus
MC²High
2015-2016

NAME: _____

DATE: _____

Solve the radical equations: Use the 4-step process to solve the square-root equation.

1. $\sqrt{3p - 18} = 9$

2. $\sqrt{5f} = 10$

3. $5\sqrt{2y - 1} = 35$

4. $7\sqrt{r} = 42$

5. $11\sqrt{16s} = 88$

Solve the radical equations: Use the 4-step process to solve the radical equations. These **ALL** have an index greater than 2.

6. $\sqrt[3]{t} = 1$

7. $\sqrt[3]{2x} = 10$

8. $\sqrt[4]{9t} + 12 = 15$

9. $\sqrt[3]{6k + 6} - 3 = 3$

10. $\sqrt[4]{w - 3} = 2$

Solve the rational exponential equations: Use the 4-step process to solve.

11. $x^{\frac{1}{2}} + 3 = 7$

12. $2y^{\frac{1}{2}} = 10$

13. $2c^{\frac{2}{3}} = 18$

14. $d^{\frac{5}{3}} = 32$

15. $(t - 7)^{\frac{1}{3}} = 5$

List of Powers

$2^2 = 4$

$2^3 = 8$

$2^4 = 16$

$3^2 = 9$

$3^3 = 27$

$3^4 = 81$

$4^2 = 16$

$4^3 = 64$

$4^4 = 256$

$5^2 = 25$

$5^3 = 125$

$5^4 = 625$

$6^2 = 36$

$6^3 = 216$

$6^4 = 1296$

$7^2 = 49$

$7^3 = 343$

$7^4 = 2401$

$8^2 = 64$

$8^3 = 512$

$8^4 = 4096$

$9^2 = 81$

$9^3 = 729$

$9^4 = 6561$

$10^2 = 100$

$10^3 = 1000$

$10^4 = 10000$

Introduction to Exponential Functions

Properties of Exponential functions –

1. Variable in the exponent.
2. Increase by multiplying by a constant.
3. Do **not** graph to a straight line.

Compare Linear vs. Exponential functions

Linear		Exponential	
x	$y = 2x$	x	$y = 2^x$
0	0	0	1
1	2	1	2
2	4	2	4
3	6	3	8
4	8	4	16
5	10	5	32
\vdots	\vdots	\vdots	\vdots

Example 2: Determine which each chart represents: linear, power, or exponential.

x	$y = 2x^3$	x	$y = 2x - 3$	x	$y = 2 \cdot 3^x$
-2	-16	-2	-7	-2	$\frac{2}{9}$
-1	-2	-1	-5	-1	$\frac{2}{3}$
0	0	0	-3	0	2
1	2	1	-1	1	6
2	16	2	1	2	18
\vdots	\vdots	\vdots	\vdots	\vdots	\vdots

Determine an Exponential Function from a Chart

x	-1	0	1	2	3	...
y	$\frac{1}{10}$	1	10	100	1000	...

The rule for this chart is easy to determine. Since each x increases the y value by multiplying 10, the equation is therefore

$$y = 10^x$$

But what about this...

x	-1	0	1	2	3	...
y	$\frac{11}{10}$	2	11	101	1001	...

The pattern goes away! There is no number to multiply by to get the next term. For this one we need to look at the first chart from $y = 10^x$. Notice that the y term for the second chart is always 1 more than the y value of the first chart. Besides that everything is the same.

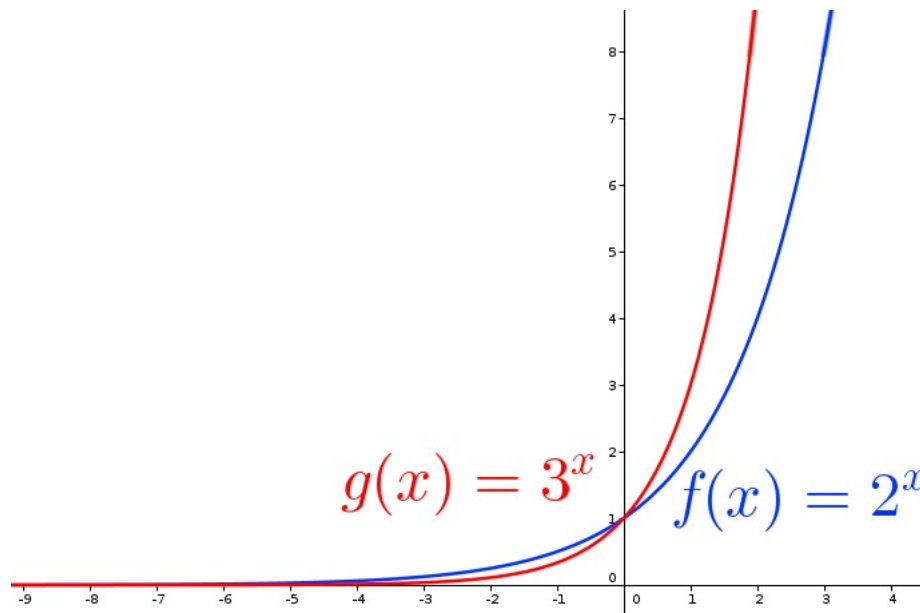
Graphing Exponential Functions

$$a \cdot b^{x-h} + k$$

The size of the base affects the vertical stretch of the function.

Compare $f(x) = 2^x$ and $g(x) = 3^x$

x	$f(x) = 2^x$		$g(x) = 3^x$
-2	$\frac{1}{4}$		$\frac{1}{9}$
-1	$\frac{1}{2}$		$\frac{1}{3}$
0	1		1
1	2		3
2	4		9
3	8		27
4	16		81
5	32		243
6	64		729
\vdots	\vdots		\vdots



The two functions overlap at (0, 1).

The two graphs will not go below the line $y = 0$. This is called an **ASYMPTOTE**. It is a way of describing the end behavior of the function. As the functions move towards negative infinity they will get smaller and smaller, but they will never actually reach 0.

Translations

A translation is when a function is moved around the graph. To move the graph up or down, add or subtract from the function.

If there is no $+h$ on the back of the function, then the asymptote is at $y = 0$. In these cases the h 's are $+2$ and -1 .

If there is a $+h$ or $-h$ then the asymptote is at $\pm h$

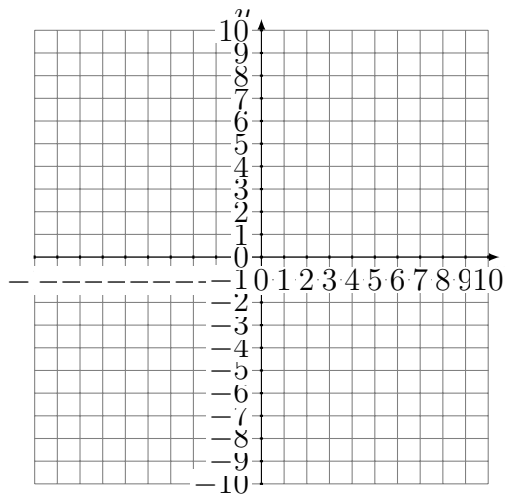
To move the function side to side add or subtract from the exponent. Be careful because it goes in the opposite direction of the sign. Notice the asymptote doesn't move

Method for Graphing

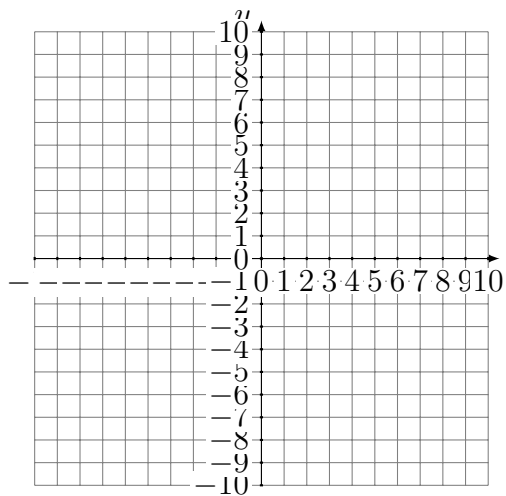
Graph exponential equations. Easy method.

1. Identify the asymptote. It's always the \pm at the *end* of the function
2. Set the exponent equal to 0
3. Find the y value when the exponent is equal to zero. Graph that point.
4. Follow the asymptote until it passes through the point, and graph the exponentiality.

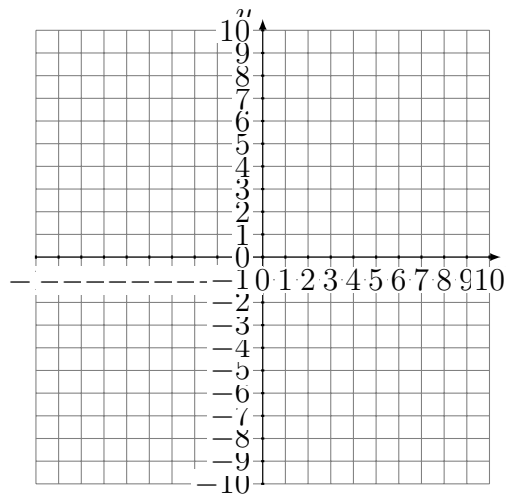
Example 1: graph $y = 2^{x-2} + 3$



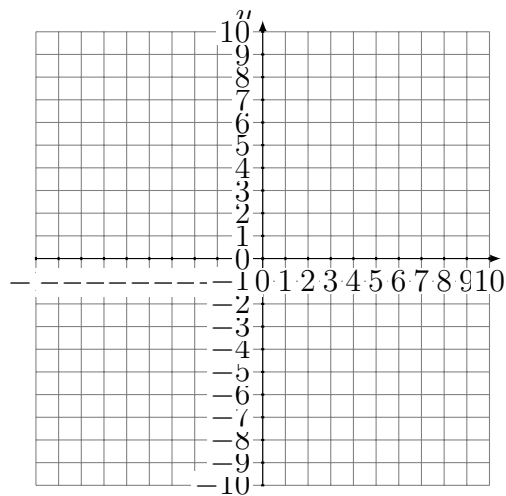
Example 2: graph $y = \left(\frac{1}{2}\right)^x - 7$



Example 3: graph $y = -2^{x-2} + 3$

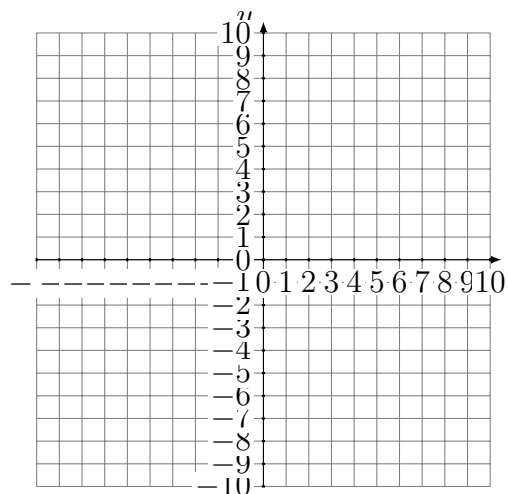


Example 4: graph $y = 2^{-x} - 7$

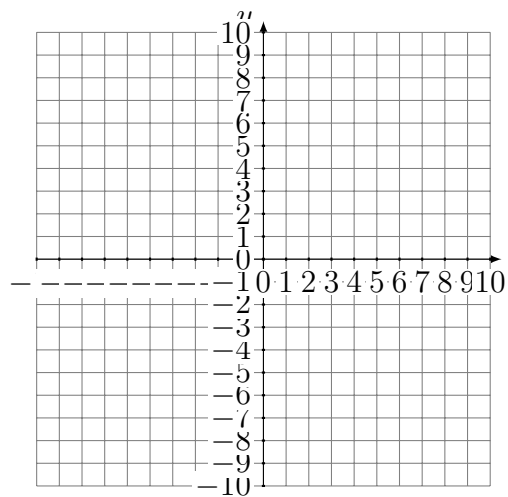


You Try: Graph the exponential Functions

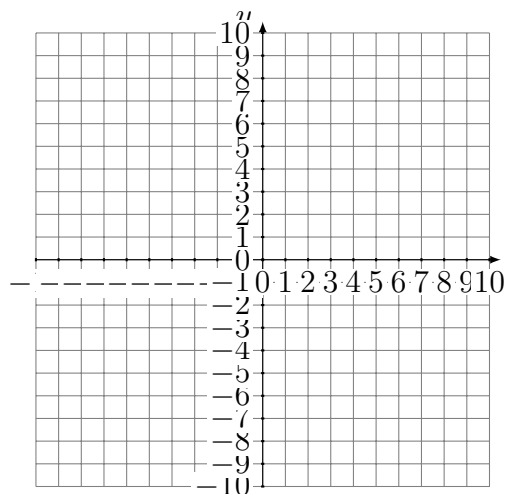
$$y = 3^x - 5$$



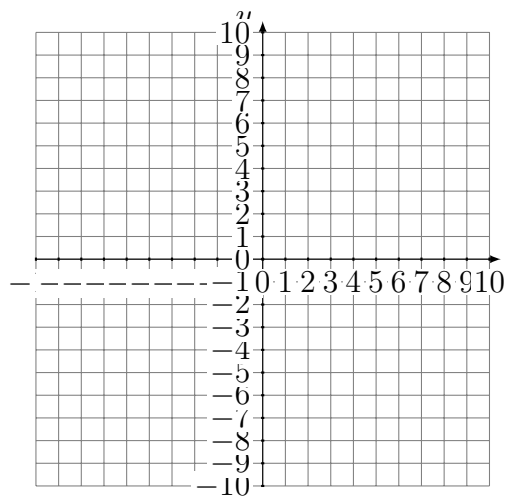
$$y = \left(\frac{1}{3}\right)^{x+4} + 1$$



$$y = (-2)3^{x-1} + 6$$



$$y = 3^{-x}$$



Exponential Growth

Compounding interest is an exponential expression because the exponent changes as time goes on.

$$A = P(1 + r)^t \qquad A = P \left(1 + \frac{r}{n} \right)^{nt}$$

A = Actual amount – what you'll end up with

P = Principle – original amount

r = rate – as a decimal, not as a fraction

t = time

The *independent* variable is t the amount of time that goes by. The *dependent* variable is A , the actual amount. This is because the actual amount depends on how much time goes by. If we set this up as a relationship between t and A , we would get an exponential function.

Example 1: How much will you have after investing \$500,000.00 compounded at 3% for 12 years?

Example 2:

Bacteria can multiply at an enormous rate when each cell doubles. If you get 3 bacteria cells on your hamburger and they double every hour, how much will be on your hamburger after 24 hours?

Example 3 – You Try:

In 1985, there were 102 cell phone subscribers in the small town of Stemville. The number of subscribers increased by 55% per year after 1985. How many cell phone subscribers were in Stemville in 1994?

Exponential (radioactive) Decay

Exponential decay is the same as exponential growth except for a minus sign.

$$A = P(1 - r)^t \qquad A = P \left(1 - \frac{r}{n}\right)^{nt}$$

We use this when something is decreasing in value.

Example 4:

Each year the local country club sponsors a tennis tournament. Play starts with 128 participants. During each round, half of the players are eliminated. How many players remain after 5 rounds?

Example 5:

A radioactive isotope has a half-life of 1 day. If there was an original amount of 32 kilos of this isotope, how much would be left over after 15 days?

Example 6 – You try:

DDT is a toxic pesticide that was used in the 1970's. It is suspected to cause cancer in humans. The half-life of DDT is about 15 years. Half-life is the amount of time it takes for half of the amount of a substance to decay. If there was 100 grams of DDT on a certain plot of land, how much would be left over after 75 years?

Exponential Growth – NOTES

Compounding interest is an exponential expression because the exponent changes as time goes on.

$A =$

$P =$

$r =$

$t =$

The *independent* variable is _____ the amount of time that goes by. The *dependent* variable is _____. This is because the actual amount _____ on how much time goes by.

If we set this up as a relationship between t and A , we would get an exponential function.

Example 1:

How much will you have after investing \$500,000.00 compounded at 3% for 12 years?

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Exponential (radioactive) Decay – NOTES

Exponential decay is the same as exponential growth except for a _____.

$A =$

We use this when something is _____ in value.

Example 4:

Each year the local country club sponsors a tennis tournament. Play starts with 128 participants. During each round, half of the players are eliminated. How many players remain after 5 rounds?

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The Number e

e is an irrational number discovered by Leonhard Euler (pronounced oiler). It is commonly called Euler's Number, but more commonly as the natural base. $e \approx 2.7182818\dots$ It is used as the base for many exponential functions, and has many applications in calculus.

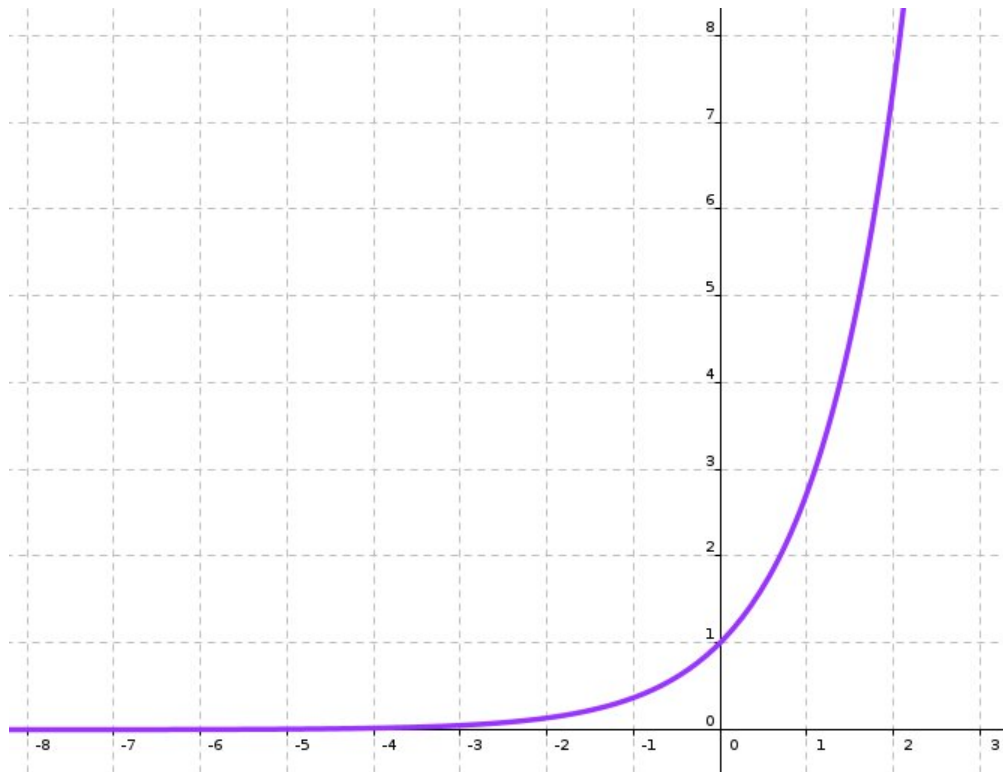
e is calculated by the following expression as n gets larger and larger

$$\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n}\right)^n \approx 2.7182818$$

I hope this expression looks a little familiar.

e can be used as a regular exponential base.

So we can graph $y = e^x$

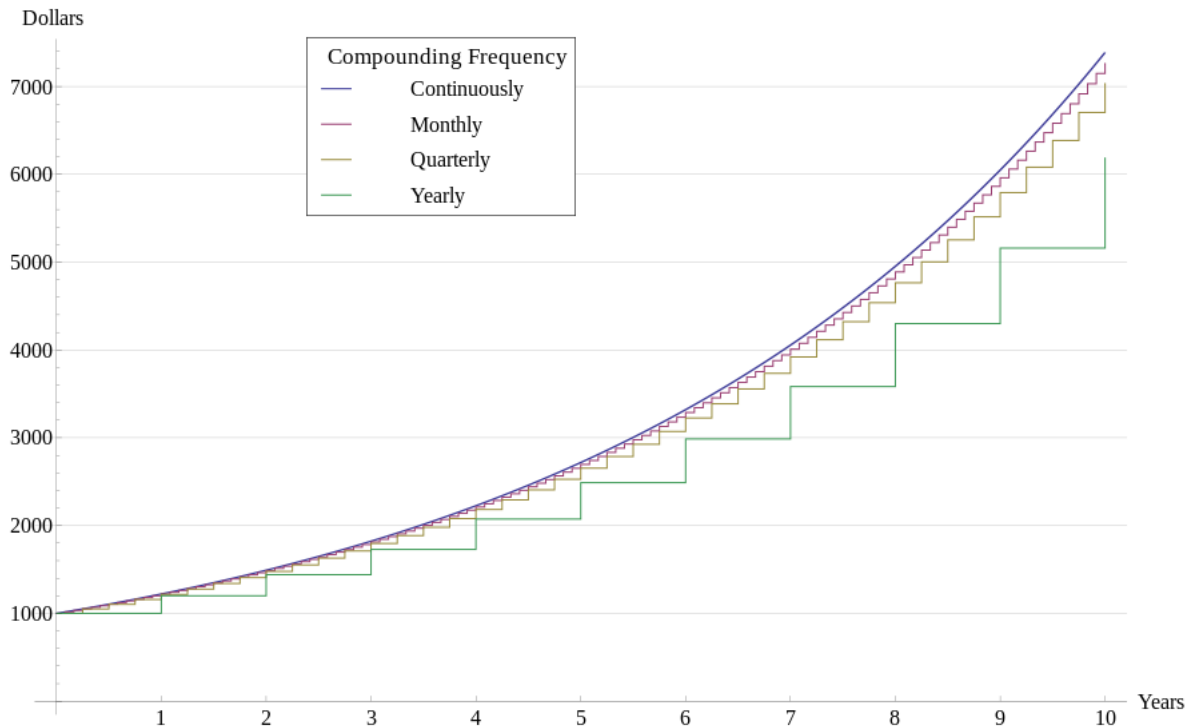


What it comes down to is that e is a number just like any other, and we can use it as such.

So what's so special about this number e ?

Continuously Compounded Interest

What is so special about e is that we can compound interest continuously. The nice thing about that is that I get more money when interest is compounded more frequently.



The graph above shows the same interest rate, but when the interest is compounded more often there are more significant gains made.

To calculate continuously compound interest we use the formula

$$A = Pe^{rt}$$

Where

A = Actualized amount

P = Principal

r = rate

t = time

So basically all the letters are the same (remember e is a number, not a variable), and it's a much tighter, neater package.

Example: You deposit \$1500.00 in an account compound continuously at 3%. How much will you have after 3 years?

How much will you have after 10 years?

How does this compare to compounded semi-annually (twice a year) for 10 years?

Example 2: How much will you have after investing \$2.00 compounded continuously since the year 1776?

Quiz Review

Mr. Wolf
wolf-math.com

NAME: _____

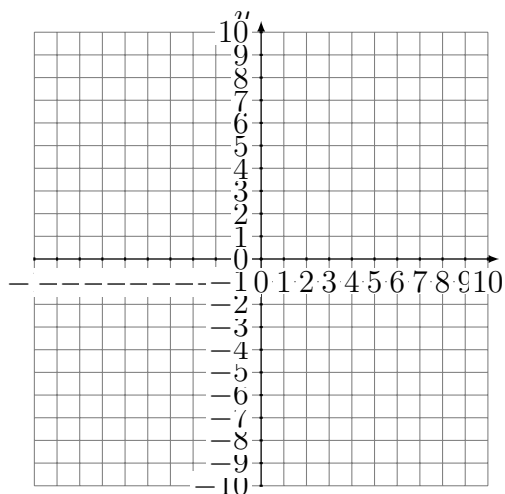
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Graphing Exponentials & Exponential Growth

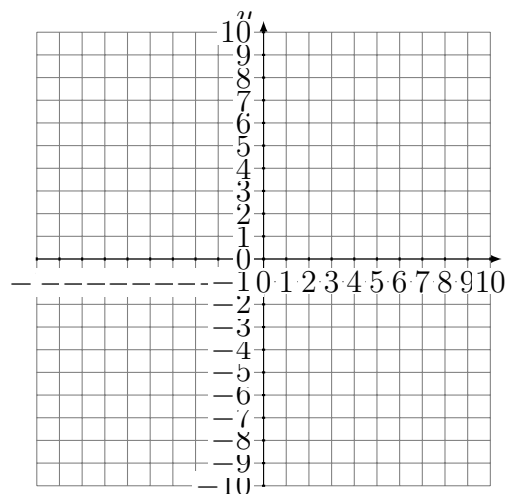
Due Monday 2014-10-13

Graph the exponential function

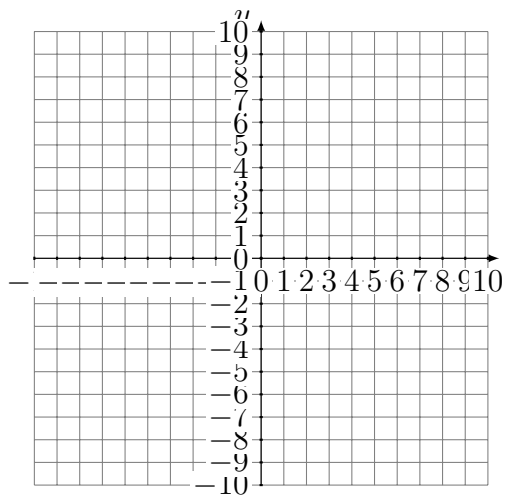
5. graph $y = 2^{x-2} + 3$



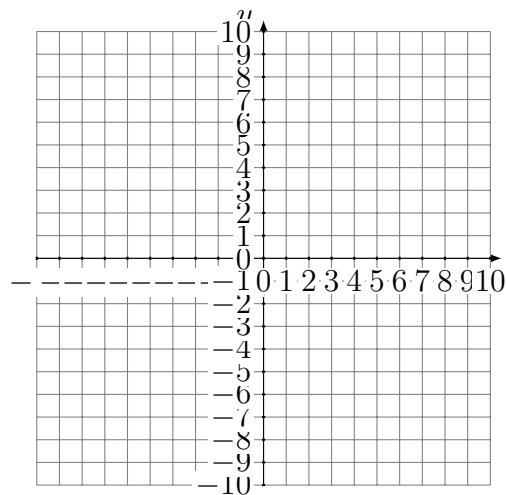
7. graph $y = -2^{x-2} + 3$



6. graph $y = \left(\frac{1}{2}\right)^x - 7$



8. graph $y = 2^{-x} - 7$



Compound the Interest

$$A = P \left(1 + \frac{r}{n} \right)^{n \cdot t}$$

9. How much money would you have after investing \$17 compounded daily at 10% for 25 years?
10. (Population Growth) A rabbit population increases at 60% compounded quarterly. If there were 20 rabbits to start with, how many rabbits will there be after 10 years?
11. (a) How much would you have after investing \$400 compounded monthly at 5% for 10 years?

(b) How much would you have after investing \$400 compounded monthly at 5% for 20 years?

(c) Even though twice as much time went by between (a) and (b), was twice as much money made?

Continuously Compound Interest

$$A = Pe^{rt}$$

12. How much money will you have after investing \$600 compounded continuously at 4% for 8 years?
13. (a) How much money will you have if you invest \$500 compounded continuously at 12% for 10 years?

(b) What's the difference between (a) and if you compounded twice per year for 10 years.

Quiz

Mr. Wolf
wolf-math.com

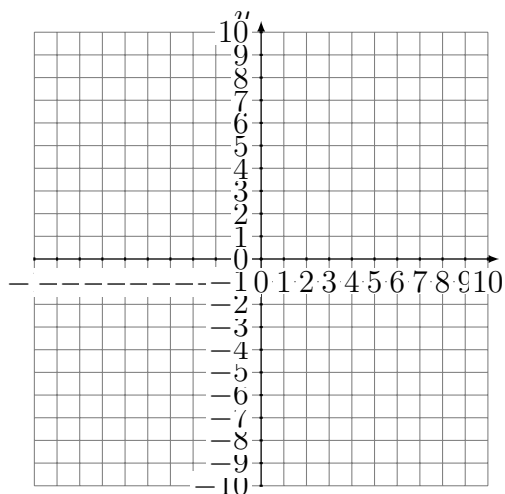
NAME: _____

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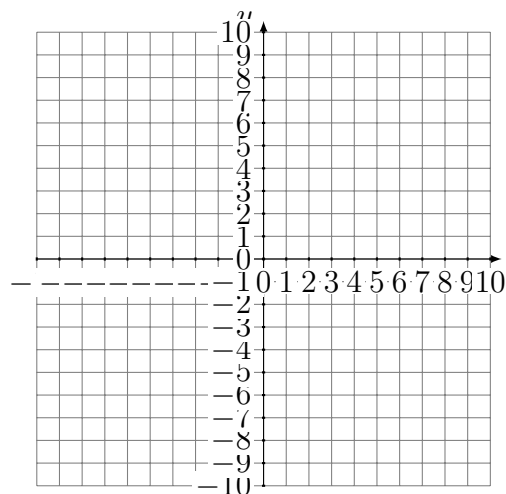
Graphing Exponentials & Exponential Growth OPEN NOTE

Graph the exponential function

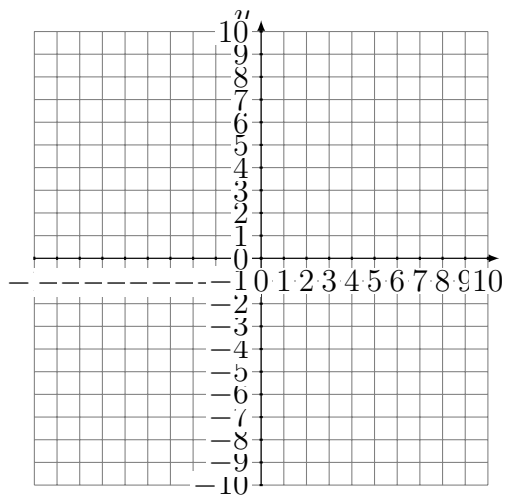
14. graph $y = 2^{x+2} - 3$



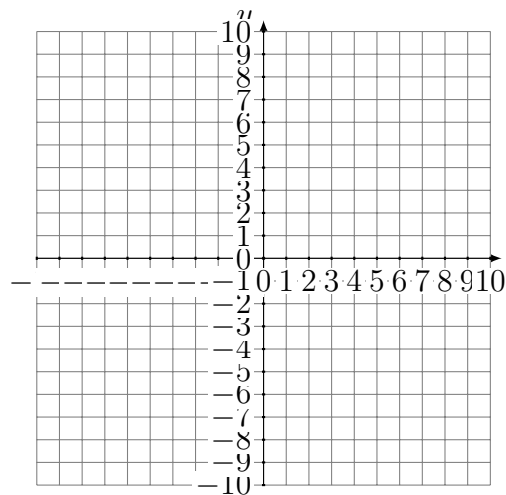
16. graph $y = -2^{x+5} - 3$



15. graph $y = \left(\frac{1}{2}\right)^x - 8$



17. graph $y = 2^{-x} + 5$



Compound the Interest

$$A = P \left(1 + \frac{r}{n} \right)^{n \cdot t}$$

18. How much money would you have after investing \$17 compounded daily at 10% for 25 years?
19. (Population Growth) A rabbit population increases at 60% compounded quarterly. If there were 20 rabbits to start with, how many rabbits will there be after 10 years?
20. (a) How much would you have after investing \$1000 compounded monthly at 6% for 10 years?

(b) How much would you have after investing \$1000 compounded monthly at 6% for 30 years?

(c) Even though triple the time went by between (a) and (b), was triple the money made?

Continuously Compound Interest

$$A = Pe^{rt}$$

21. How much money will you have after investing \$800 compounded continuously at 4% for 6 years?
22. (a) How much money will you have if you invest \$1200 compounded continuously at 10% for 14 years?

(b) What's the difference between (a) and compounded twice per year for 14 years.

**Now you're done :-)