

LCA Pairs

You are given a connected tree of N nodes numbered from 0 to $N-1$ rooted at the 0^{th} node, where $p[i]$ is the parent of the i^{th} node and $p[0] = -1$ as the 0^{th} node is the root.

Calculate the numbers of pairs of nodes (a,b) $0 \leq a < N$, $a \leq b < N$ such that $LCA(a,b) = x$, for each x where $0 \leq x < N$.

The LCA or lowest common ancestor between two nodes a and b is defined as the lowest node in tree that has both a and b as descendants (where we allow a node to be a descendant of itself).

Example 1:

Input:

$N = 3$

$p[] = [-1, 0, 0]$

Output: $[4, 1, 1]$

Explanation: The structure of tree is :

```
    0
   / \
  1   2
```

For $LCA = 0$, we have 4 pairs $(0,0)$, $(0,1)$, $(0,2)$, $(1,2)$

For $LCA = 1$, we have only 1 pair $(1,1)$

For $LCA = 2$, we have only 1 pair $(2,2)$

Example 2:

Input:

$N = 5$

$p[] = [-1, 0, 0, 1, 1]$

Output: $[8, 4, 1, 1, 1]$

Explanation: The structure of tree is :



For LCA = 0, we have 8 pairs (0,0), (0,1),
(0,2), (0,3), (0,4), (1,2), (2,3), (2,4)

For LCA = 1, we have 4 pairs (1,1), (1,3),
(1,4), (3,4)

FOR LCA = 2, we have only 1 pair (2,2),

FOR LCA = 3, we have only 1 pair (3,3)

For LCA = 4, we have only 1 pair (4,4)

Your Task:

Your task is to complete the function **calcPairs()** which takes the integer **N** and a list **p[]** of size **N** as input parameters and returns a list of **N** elements a_0, a_1, \dots, a_{N-1}

where a_i is the the number of unordered pairs for which $\text{lca}(a,b) = i$, where $0 \leq a < N$, $a \leq b < N$

Constraints:

$$1 \leq N \leq 10^5$$

$$0 \leq p[i] < N \text{ where } 0 < i < N$$

$$p[0] = -1$$