

Approach

Intuition

By maximizing the number of set bits in the most significant bit positions, we can achieve maximum possible score.

Approach: Greedy + Toggling

Here's how the approach works:

1. **Initial Score Initialization:** We initially assume that all the bits in the most significant position are set bits, meaning first column contains all 1s, which can be done by multiplying the number of rows n with the value represented by the most significant bit ($1 \ll (m - 1)$).
2. **Column Toggling:** We then iterate over the remaining columns (from the second column to the last column) to determine whether toggling (flipping) the entire column would increase the score or not.
3. **Value of the Current Column:** We then calculate a value val for each column j represented by that column's bit position ($1 \ll (m - 1 - j)$).
4. **Counting Matching Rows:** We then count the number of rows represented by set, where the value in the current column j matches the value in the first column (0 or 1) by iterating over all rows and comparing $grid[i][j]$ with $grid[i][0]$.
5. **To Toggle or Not:** If the number of rows set is greater than or equal to $n/2$ (half the number of rows), it's beneficial for us to not toggle (flip) the column. Otherwise, it's better to toggle (flip) the entire column to increase the score.
6. **Updating the Score:** We then update the res score by adding the maximum value between $set * val$ (if the column is kept unchanged) and $(n - set) * val$ (if the column is toggled), ensuring that the score is maximized by either keeping the current column unchanged or toggling it.
7. **Resulting Score:** After iterating through all columns, we return the maximum score res .

This approach works because toggling a row or a column affects all the bits in that row or column simultaneously. By ensuring that the most significant bits are set to 1 in as many rows as possible, and then adjusting the remaining columns based on the majority values, we can maximize the score of the matrix.

Dry - Run

Given Input:

grid =

[0, 0, 1, 1]

[1, 0, 1, 0]

[1, 1, 0, 0]

- Initialize variables:
 - $n = 3$ (number of rows)
 - $m = 4$ (number of columns)
 - $res = (1 \ll (m - 1)) * n = (1 \ll 3) * 3 = 8 * 3 = 24$
 - $[1, 1, 0, 0]$
 - $[1, 0, 1, 0]$

$[1, 1, 0, 0]$

since our 1st row's 1st element is 0 and we have to make all the elements in our 1st column as 1s to maximize our score, we'll toggle our first row

- Iterate through columns ($j = 1$ to $m - 1$):
 - $j = 1$:
 - $val = 1 \ll (m - 1 - j) = 1 \ll 2 = 4$
 - $set = 2$ (since $grid[0][1] == grid[0][0]$ and $grid[2][1] == grid[2][0]$)
 - $res += Math.max(set, n - set) * val$
 $= Math.max(2, 1) * 4$
 $= 2 * 4 = 8$
 - $res = 24 + 8 = 32$
 - no need to toggle this column
 - $j = 2$:
 - $val = 1 \ll (m - 1 - j) = 1 \ll 1 = 2$
 - $set = 2$ (since $grid[1][2] == grid[1][0]$ and $grid[2][2] == grid[2][0]$)
 - $res += Math.max(set, n - set) * val$
 $= Math.max(2, 1) * 2$
 $= 2 * 2 = 4$
 - $res = 32 + 4 = 36$
 - $[1, 1, 1, 0]$
 - $[1, 0, 0, 0]$

$[1, 1, 1, 0]$

- $j = 3$:
 - $val = 1 \ll (m - 1 - j) = 1 \ll 0 = 1$

- `set = 0` (since `grid[0][3] != grid[0][0]`, `grid[1][3] != grid[1][0]`, and `grid[2][3] != grid[2][0]`)
- `res += Math.max(set, n - set) * val`
`= Math.max(0, 3) * 1`
`= 3 * 1 = 3`
- `res = 36 + 3 = 39`
- `[1,1,1,1]`
- `[1,0,1,1]`

`[1,1,1,1]`

- Return the final result:
 - `return res = 39`

Complexity

- Time complexity: $O(n * m)$
- Space complexity: $O(1)$