

Matrix Chain Multiplication

Given a sequence of matrices, find the most efficient way to multiply these matrices together. The efficient way is the one that involves the least number of multiplications.

The dimensions of the matrices are given in an array **arr[]** of size **N** (such that $N = \text{number of matrices} + 1$) where the **ith** matrix has the dimensions (**arr[i-1] x arr[i]**).

Example 1:

Input: $N = 5$

$\text{arr} = \{40, 20, 30, 10, 30\}$

Output: 26000

Explanation: There are 4 matrices of dimension 40×20 , 20×30 , 30×10 , 10×30 . Say the matrices are named as A, B, C, D. Out of all possible combinations, the most efficient way is $(A * (B * C)) * D$.

The number of operations are -

$$20 * 30 * 10 + 40 * 20 * 10 + 40 * 10 * 30 = 26000.$$

Example 2:

Input: $N = 4$

$\text{arr} = \{10, 30, 5, 60\}$

Output: 4500

Explanation: The matrices have dimensions 10×30 , 30×5 , 5×60 . Say the matrices are A, B and C. Out of all possible combinations, the most efficient way is $(A * B) * C$. The

number of multiplications are -

$$10 * 30 * 5 + 10 * 5 * 60 = 4500.$$

Your Task:

You do not need to take input or print anything. Your task is to complete the function **matrixMultiplication()** which takes the value **N** and the array **arr[]** as input parameters and returns the minimum number of multiplication operations needed to be performed.

Expected Time Complexity: $O(N^3)$

Expected Auxiliary Space: $O(N^2)$

Constraints:

$$2 \leq N \leq 100$$

$$1 \leq \text{arr}[i] \leq 500$$