

# Find the Safest Path in a Grid

You are given a **0-indexed** 2D matrix `grid` of size  $n \times n$ , where  $(r, c)$  represents:

- A cell containing a thief if `grid[r][c] = 1`
- An empty cell if `grid[r][c] = 0`

You are initially positioned at cell  $(0, 0)$ . In one move, you can move to any adjacent cell in the grid, including cells containing thieves.

The **safeness factor** of a path on the grid is defined as the **minimum** manhattan distance from any cell in the path to any thief in the grid.

Return the **maximum safeness factor** of all paths leading to cell  $(n - 1, n - 1)$ .

An **adjacent** cell of cell  $(r, c)$ , is one of the cells  $(r, c + 1)$ ,  $(r, c - 1)$ ,  $(r + 1, c)$  and  $(r - 1, c)$  if it exists.

The **Manhattan distance** between two cells  $(a, b)$  and  $(x, y)$  is equal to  $|a - x| + |b - y|$ , where  $|val|$  denotes the absolute value of  $val$ .

**Example 1:**

1	0	0
0	0	0
0	0	1

**Input:** `grid = [[1,0,0],[0,0,0],[0,0,1]]`

**Output:** `0`

**Explanation:** All paths from  $(0, 0)$  to  $(n - 1, n - 1)$  go through the thieves in cells  $(0, 0)$  and  $(n - 1, n - 1)$ .

**Example 2:**

0	0	1
0	0	0
0	0	0

**Input:** `grid = [[0,0,1],[0,0,0],[0,0,0]]`

**Output:** 2

**Explanation:** The path depicted in the picture above has a safeness factor of 2 since:

- The closest cell of the path to the thief at cell (0, 2) is cell (0, 0). The distance between them is  $|0 - 0| + |0 - 2| = 2$ .

It can be shown that there are no other paths with a higher safeness factor.

**Example 3:**

0	0	0	1
0	0	0	0
0	0	0	0
1	0	0	0

**Input:** `grid = [[0,0,0,1],[0,0,0,0],[0,0,0,0],[1,0,0,0]]`

**Output:** 2

**Explanation:** The path depicted in the picture above has a safeness factor of 2 since:

- The closest cell of the path to the thief at cell (0, 3) is cell (1, 2). The distance between them is  $|0 - 1| + |3 - 2| = 2$ .
- The closest cell of the path to the thief at cell (3, 0) is cell (3, 2). The distance between them is  $|3 - 3| + |0 - 2| = 2$ .

It can be shown that there are no other paths with a higher safeness factor.

**Constraints:**

- `1 <= grid.length == n <= 400`
- `grid[i].length == n`

- `grid[i][j]` is either `0` or `1`.
- There is at least one thief in the `grid`.