

CS2100

Searching &
Sorting



Recap:

- HW due today - via git
 - Lab due today
 - Extra credit due Monday
 - Posted 1st HW
 - (due Sunday March 18?)
- I am traveling
(get me questions next week)

Searching:

Given a structure S , output true if x is in S .

Often also want an iterator to the value, or an index (if array-based).

Two ways:

- binary search
 - ↳ fast, but needs sorting
- linear search
 - ↳ look at everything

Coding + runtimes:

Linear Search:

- You've actually done the code for this (or nearly have) in both `SLinkedList` & `Vector`!

A simple loop to run through the data!

- return true if ever found
(or iterator / location)

- return false if not found

→ tricky bit is avoid seg fault

Run time:

- Lists
- Vectors

]
 $O(n)$

Binary Search:

- Check middle entry, val. ↙

{ If $x < \text{val}$,
Search right half ↙
Else Search left half ↙

(if equal, report "true")

Note: Need to be careful!

Issues: Recursive can
be problematic - don't want
 $O(n)$ time copy

Need: left + right index

Runtime:

$$B(n) = 5 + B\left(\frac{n}{2}\right)$$

Vectors: $O(\log n)$

Lists: $O(n)$ ← BAD
(b/c of operator [])

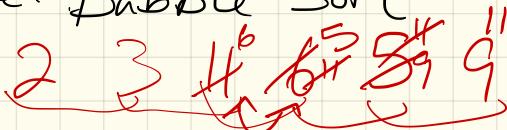
Next: Sorting!

Algorithms?

- Bubble Sort
 - Merge Sort
 - Insertion Sort
 - Quick Sort
 - Radix Sort
 - Heap sort
- ⋮

An easy one: Bubble Sort

Idea:



for $i = 1$ to n
for $j = 1$ to $n - (i-1)$
if $A[j-1] > A[j]$
Swap them

Details:

- linked structure — dec
w/ pointers &
move iterators around
- versions of this go
from n to i &
swap "down"

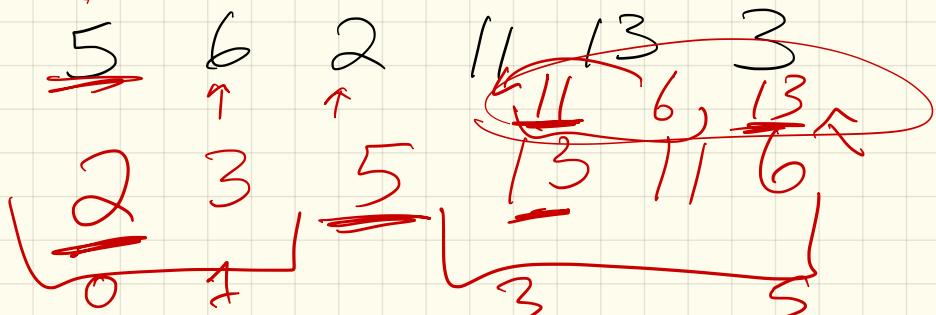
Runtime: $O(n^2)$

$$\sum_{i=1}^n \sum_{j=1}^i 4 = \sum_{i=1}^n 4i$$

$$= 4 \sum_{i=1}^n i = 4 \frac{n(n+1)}{2} = O(n^2)$$

Quick Sort :

Idea : Choose "pivot" + divide array



Then repeat on each side. If > 1 .

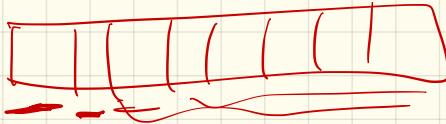
recursively
quicksort both sides

Issues :

Use reference + pass entire list

- Need left + right index of current sublist

"Code":



Quick Sort (list A , length n)

for ($i = 2$ to n)

if $A[i] > A[i-1]$

else move $A[i]$ to front ↗
move $A[i]$ to back ↗

QuickSort (first "half")

QuickSort (second "half")



Details:

linked vs vector

easy for this alg!

need to track indices

Runtimes

Worst case $O(n^2)$

Expected: $O(n \log n)$

Merge Sort :

if length of A is > 2

divide in half
MergeSort (left)
MergeSort (right)

Merge (left + right)

return list

else // (list of length 0 or 1)

→ Merge (left, right)

create empty list L

$i \leftarrow 1, j \leftarrow 1$

while ($i <$ or j)

Ex: 5 11 3 2 6 8 7 4

5 11

3 2

5 11

3 2
1 3

2 3

5 10

2 3

5

10

6 7

8

2 3 4 5 6 7 8

Runtimes:

Quicksort:

Mergesort:

Others: