| SISO — | - Shortest Pa | th Algorithm | 11/28/2012 |
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Other graph algorithms dist BFS returns a "short" S-t in some sense. But won't work if graph has weights on the edges. which s-t path will be in BFS tre?

> IR which gives ea a weigh stance d(u,v) is the leng's a minimum weight patt Given a weighted graph of a vertex u, compute the shortest paths from u) to every other vertex.

Dijkstra's Algorithm
Essentally, a "weighted" BFS.
We'll teep a set of vertices whose shortest path is known. Want to add in the next closest vertex. Ken idea: This must give the shortest path to that votex.

Assume 6 is undirected a has What is the shortest path from stat? Suppose D[u] holds current best path from 5 to u (so far).

(Initially, D[s]=0 or D[u]=00 for all u's.) to update D labels via relaxation:

we update D[n].

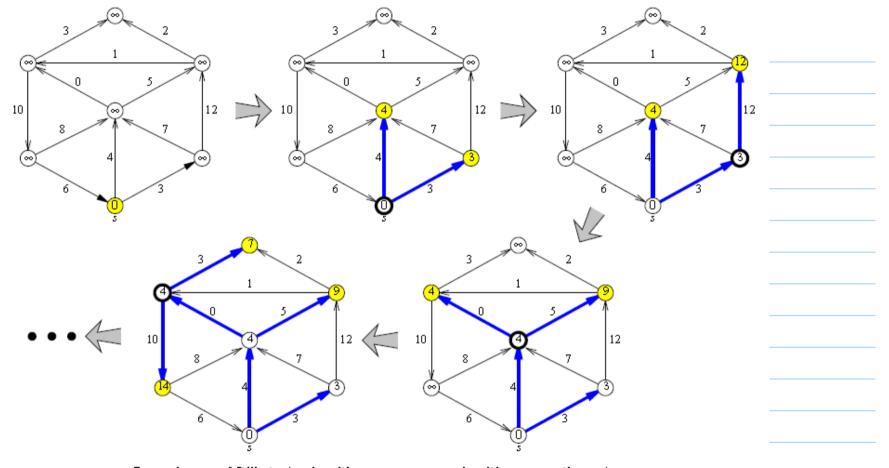
each edge (u, u)

if D[u] >> D[v] + w(v,u):

So at each phase, let S be set of "known" distances D[u]. Relax all neighbors of vertices Afterwards, can add the minimum of all the neighbors to S.

orthon: Given Gas: A Initalize D[8] = 0 For all u + s, set D[u]= 00 Create a heap H of add (DES), S While H is not empty
u= H. remove Min () for each neighbor v of u eby (if D[u]+w(u,v) < D[v]
eby
Add new (D[v],v] to

Ollog n updat

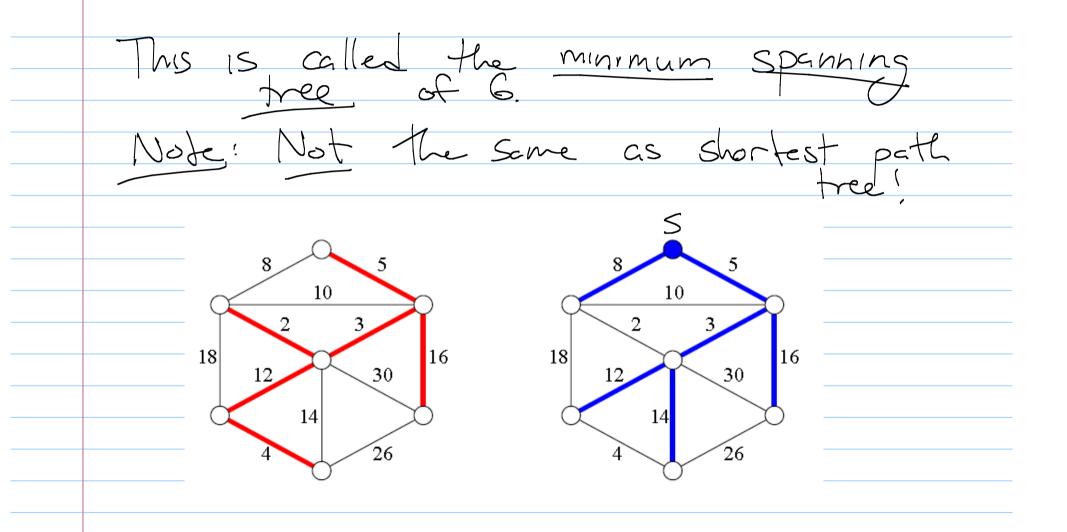


Four phases of Dijkstra's algorithm run on a graph with no negative edges.

At each phase, the shaded vertices are in the heap, and the bold vertex has just been scanned.

The bold edges describe the evolving shortest path tree.

· relaxation of each adjacent edge: Note: Need an adapatable priority queue, where priorities can of be updated in Ollog of time Uses? Goal: Connect every body while paying some waining manny



How to compute MST.