```
// coord-iterative.cpp
// Brooklyn College CISC3130 M. Lowenthal - Bonus Assignment
// Robert Wagner
// 2016-02-25
//
// iterative verion of the bonus assignment
// takes advantage of the fact that a multivariate function A(a1,a2,a3, \ldots a_n) is
// bijective with a single dimensional B(b) with b = \{ 0 ... product(a1,a2,...a_n) \}
// using modular aritmatic. this works as long as the product(a1..a n) does not
// overflow the variable data type used.
//
// to compile: g++ coord-iterative.cpp -o coord-iterative
//
      to run: ./coord-iterative <# of dims> <size1> <size2> ...
//
          eg: ./coord-iterative 3 4 5 6
#include <iostream>
#include <stdlib.h>
using namespace std;
int main(int argc, char* argv[]) {
   if (argc < 3) { cout << "must pass at least two integers." << endl; return -1; }
   int mods[argc-2];
   int divs[argc-2];
   int max, mod, div, index;
   // first, intialize what we know we can initialize
   int dim = atoi(argv[1]);
   if (argc - 2 != dim) { cout << "invalid number of parameters." << endl; return -1; }
   mods[0] = atoi(argv[2]);
   divs[0] = dim;
   \max = \overline{mods[0]}^* \dim;
   for (int n = 0; n < max; n++) { // the only loop
       // if we are still within our parameter list, continue to initialize
       if (n < argc - 3) {
           mods[n + 1] = atoi(argv[n + 3]);
           divs[n + 1] = divs[n] * mods[n];
           max = max * mods[n + 1];
       index = n \% dim;
       // if there should be an opening parenthesis, print it
       if (index == 0) cout << "(";
       // print the actual number
       mod = mods[index];
       div = divs[index];
       cout << 1 + (n / div) % mod;
       // print closing parenthesis or just a comma or both
                                cout << ")" << endl;
       if
               (n+1 >= max)
       else if ((n+1) % dim != 0) cout << ", ";
                                cout << "), ":
       else
   }
}
```

```
// coord-recurse.cpp
// Brooklyn College CISC3130 M. Lowenthal - Bonus Assignment
// Robert Wagner
// 2016-03-08
// recursive version of the bonus assignment
// builds a global variable finalString and recurses through the possible permutations
// of the dimension sizes, and only adds coordinates if it hasn't been added already
//
// to compile: q++ coordinates.cpp -o coordinates
//
      to run: ./coordinates <# of dims> <size1> <size2> ...
//
          eg: ./coordinates 3 4 5 6
#include <iostream>
#include <stdlib.h>
#include <string>
#include <sstream>
using namespace std;
string finalString = "";
void recurse(int N, int values[]) {
   ostringstream SS;
   SS << "(";
   for (int i = 0; i < N; i++) { // the only loop in the recursion
       SS << values[i];
       if (i < N - 1)^{-}SS << ", ";
       if (values[i] > 1) {
           values[i] -= 1;
           recurse(N, values);
           values[i] += 1;
       }
   SS << "), ";
   string s = SS.str();
   // only add it if its not already added
   if (finalString.find(s) == string::npos)
        finalString.append(s);
}
int main(int argc, char* argv[]) {
   if (argc < 3) { cout << "must pass at least two integers." << endl; return -1; }
   int vals[argc-2];
   // first, intialize what we know we can initialize
   int dim = atoi(argv[1]);
   if (argc - 2 != dim) { cout << "invalid number of parameters." << endl; return -1; }
   // this loop only acts to fill the input array with the passed parameter values
   for (int i = 0; i < dim; i++) vals[i] = atoi(argv[i + 2]);
   // do the work
   recurse(dim, vals);
   // now global string finalString contains the final output with a trailing ',' to
remove
   finalString = finalString.substr(0, finalString.length() - 2);
   cout << finalString << endl;</pre>
}
```

```
robert@C720:~/courses/CISC3130/bonus$ g++ coord-iterative.cpp -o coord-iterative
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 5 4 3 2 1 2
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robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 1 1
(1)
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 3 4 5 6
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robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 2 2 2
(1, 1), (2, 1), (1, 2), (2, 2)
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 5 1 1 1 1 5
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robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 3 8 4 5
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robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 7 1 1 1 2 1 1 4
(1, 1, 1, 1, 1, 1), (1, 1, 1, 2, 1, 1, 1), (1, 1, 1, 1, 1, 1, 2), (1, 1, 1, 2, 1, 1, 2), (1, 1,
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robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 2 12 12
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(12, 10), (1, 11), (2, 11), (3, 11), (4, 11), (5, 11), (6, 11), (7, 11), (8, 11), (9, 11), (10, 11), (11, 11), (12, 11), (1, 12), (2, 12), (3, 12), (4, 12), (5, 12), (6, 12), (7, 12), (8, 12), (9, 12),
```

(10, 12), (11, 12), (12, 12)

```
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 3 5 4 1
(1, 1, 1), (2, 1, 1), (3, 1, 1), (4, 1, 1), (5, 1, 1), (1, 2, 1), (2, 2, 1), (3, 2, 1), (4, 2, 1), (5, 2, 1), (1, 3, 1), (2, 3, 1), (3, 3, 1), (4, 3, 1), (5, 3, 1), (1, 4, 1), (2, 4, 1), (3, 4, 1),
(4, 4, 1), (5, 4, 1)
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 0
must pass at least two integers.
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 0 1
invalid number of parameters.
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 1 0
robert@C720:~/courses/CISC3130/bonus$ ./coord-iterative 1 7
(1), (2), (3), (4), (5), (6), (7)
robert@C720:~/courses/CISC3130/bonus$ g++ coord-recurse.cpp -o coord-recursive
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 2 2 2
(1, 1), (1, 2), (2, 1), (2, 2)
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 1 1
(1)
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 1 8
(1), (2), (3), (4), (5), (6), (7), (8)
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 3 5 4 1
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(5, 3, 1), (5, 4, 1)
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 7 1 1 1 2 1 1 4
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robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 2 12 12
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(12, 10), (12, 11), (12, 12)
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 5 4 3 2 1 2
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2, 1, 1), (4, 3, 2, 1, 2)
robert@C720:~/courses/CISC3130/bonus$ ./coord-recursive 3 8 4 5
(1, 1, 1), (1, 1, 2), (1, 1, 3), (1, 1, 4), (1, 1, 5), (1, 2, 1), (1, 2, 2), (1, 2, 3), (1, 2, 4),
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(8, 3, 4), (8, 3, 5), (8, 4, 1), (8, 4, 2), (8, 4, 3), (8, 4, 4), (8, 4, 5)
robert@C720:~/courses/CISC3130/bonus$
```

```
robert@C720:~/courses/CISC3130/bonus$ g++ coord-iterative.cpp -o coord-iterative
robert@C720:~/courses/CISC3130/bonus$ g++ coord-recurse.cpp -o coord-recursive
robert@C720:~/courses/CISC3130/bonus$ time ./coord-recursive 5 5 5 5 5 5 /dev/null
ΛС
      4m57.059s
real
user
      4m56.940s
      0m0.012s
sys
robert@C720:~/courses/CISC3130/bonus$ time ./coord-iterative 5 5 5 5 5 5 /dev/null
      0m0.028s
real
      0m0.008s
user
sys
      0m0.000s
robert@C720:~/courses/CISC3130/bonus$ time ./coord-recursive 2 50 50 > /dev/null
real
      3m12.837s
      3m12.784s
user
      0m0.000s
sys
robert@C720:~/courses/CISC3130/bonus$ time ./coord-iterative 2 50 50 > /dev/null
      0m0.021s
real
user
      0m0.004s
      0m0.000s
Sys
robert@C720:~/courses/CISC3130/bonus$ time ./coord-recursive 2 5 5 > /dev/null
real
      0m0.015s
user
      0m0.000s
      0m0.004s
SYS
robert@C720:~/courses/CISC3130/bonus$ time ./coord-iterative 2 5 5 > /dev/null
      0m0.020s
real
      0m0.004s
user
      0m0.000s
sys
robert@C720:~/courses/CISC3130/bonus$ time ./coord-recursive 2 10 10 > /dev/null
      0m0.322s
real
user
      0m0.308s
sys
      0m0.000s
robert@C720:~/courses/CISC3130/bonus$ time ./coord-iterative 2 10 10 > /dev/null
real
      0m0.023s
      0m0.000s
user
sys
      0m0.004s
robert@C720:~/courses/CISC3130/bonus$ time ./coord-recursive 2 20 20 > /dev/null
real
      5m0.097s
user
      5m0.032s
      0m0.004s
sys
robert@C720:~/courses/CISC3130/bonus$ time ./coord-iterative 2 20 20 > /dev/null
real
      0m0.021s
      0m0.000s
user
      0m0.008s
sys
robert@C720:~/courses/CISC3130/bonus$
```