

Chapter 1

Introduction

1.1 The BeachBot Project

The BeachBot project was a “focus project” at ETH Zurich. During the last two semesters of the bachelor studies the team had the opportunity to develop a mobile and autonomous robot for creating sand drawings on beaches. In total 7 mechanical engineering students, one electrical engineering student and two industrial design students (from the Zürcher Hochschule der Künste) were working on the project. The result of the project is a 3 wheeled mobile robot that can drive autonomously. The key features are:

Localization The robot is able to reliably localize itself on the beach, using a laser range finder and 3 or more reflective poles. An localization accuracy of about 3 centimetres was achieved.

Driving speed and turning radius The top speed of the robot is about 0.4 metres per second and it can turn on the spot. Both back wheels are independently steerable. The front wheel is also actuated. This is done to reduce the risk of getting stuck in sand.

Rake The main drawing tool of the robot is a rake. The rake consists of seven pin-pairs which are individually liftable.

Controller The controller uses the output from the localization to steer the robot in a way that it follows a pre-defined trajectory. The trajectory generally is a text file with coordinates.

The robot was tested successfully at the beach.



Figure 1.1: Various images of the BeachBot

Chapter 2

Requirements and Inspiration

The BeachBot project itself was inspired by the images of sand artists like Peter Donnelly and Andres Amador, who create large scale sand art at beaches using a rake. Some of the imagery that we found online can be seen in Figure 2.1.

Since our goal was to create drawings similar to those of the artists, we derived our requirements from these sample images.

First of all, and probably the easiest, the BeachBot should be able to draw lines. But even more important is the support of filled areas. While driving lines or curves is straight forward, there is no easy solution how to derive the path for filled areas. Not only should the area be covered to the highest extent, the drawing process should look interesting and artistic to spectators as well (unlike, for example, a printer).

Derived from the pictures is also the requirement that the BeachBot should only be able to draw in two colors. Gradients or differently colored areas are not needed.

Crossing lines or filled areas should be prohibited as good as possible since the balloon wheels and also the front wheels leave visible marks on the raked sand (a humanoid has a huge advantage here, since it can jump over the drawn areas). The effect of driving over the drawing depends on the scale. If the drawing is very big, it does not matter much if part of the image is crossed out.

The input of the path generator should not only be computer readable, but also human editable. Typing in endless lists of coordinates would be tedious in the long run, and having a difficult format to work with would make it hard to collaborate with artists, for example. Therefore the requirement to be able to use a modern graphics editor tool to work with was set. To conform to this requirement we soon decided to use *Inkscape*¹, a popular open source vector graphics editor, as our input creation tool of choice. Further discussion about vector graphics as input and the steps to integrate a standardized vector graphics format into the path generator are explained in ?? and ?? respectively.

During the testing phase it was found out, that some of the generated paths needed some extra care by humans. To be able to easily edit the output of the generator program a graphical user interface should be created to work with the output of the generator program.

In the following sections it will be shown how these requirements were fulfilled and to which extent.

¹<http://inkscape.org>



(a) Sand drawing by Peter Donnelly. Source: <http://becky-garrett.blogspot.ch/2009/03/sand-dancer-peter-donnelly.html>



(b) Sand drawing by Andres Amador. Source: <http://sftimes.co/?id=25>



(c) Sand drawing by Andres Amador. Source: <http://sftimes.co/?id=25>

Figure 2.1: Various beach drawings by artists

Chapter 3

Path Planning Algorithms

3.1 Algorithm Overview

The output of the path generator should be a single trajectory that completely connects and covers all elements of the drawing.

This happens in three steps: First, the polygons that have to be filled are selected and the fill algorithm is separately executed for each of the polygons with polygon specific settings. In a second step all of the drawing elements are connected by an open tour and tries to minimize the traveled distance by applying a traveling salesman heuristic. As last step, connections with limited curvature are generated to complete the trajectory.

Each of those steps will be discussed in detail in this section.

3.2 Image Structure

Derived from the requirements, three different elements were identified as part of drawing (also shown in Figure 3.1):

Polyline A line consisting of 2 to n vertices

Polygon A closed line, consisting of 2 to n vertices, where the last segment is a closing one. So that vertex v_{n+1} equals v_0 .

Filled Polygon Defined in the same way as the polygon, except that the inner space should be filled by the generated trajectory. Another difference is that the filled polygon can also contain holes, which should not be covered and be excluded from the fill trajectory.

3.3 Polygon Filling

3.3.1 Related Work

Over time several surface coverage algorithms have been developed, and some distinctions can be made.

Coverage algorithms exist for applications like autonomous vacuum cleaners or autonomous lawn mowers, but also search and rescue robotic applications usually and they usually do not care if they visit the same spot twice. The target for those algorithms is rather to achieve complete coverage of an previously unknown terrain in sensible time. Usually, the complete surface coverage algorithms in are

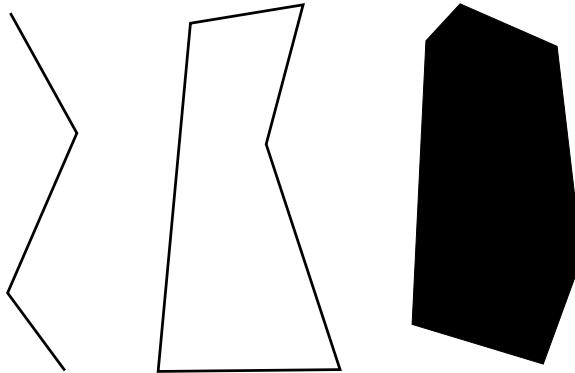


Figure 3.1: Polyline, polygon and filled polygon

also connected with online map generation techniques *SLAM*, whereas the path generation for the BeachBot should happen offline.

However, in agricultural applications some interesting algorithms have been found, which served as inspiration for the explorations presented in this thesis. Especially [1], who hinted at exploiting the straight skeleton algorithm to generate the inset polygons. An optimization strategy is employed to find the shortest trajectory through the field by repeatedly offsetting the remaining shape and traversing all possible ways off filling the shape. The algorithm is relatively computing intensive, what might be justified when using huge agricultural machines but what was not necessary for the goals of this thesis as the benefit of this optimization would be relatively small.

Another field where trajectories have to be generated is in *Computer Aided Manufacturing*. The process of removing layers of material from a block of metal is quite similar (though inverse, usually) to what is achieved in this thesis. Many publications deal with the problem of multi-axis milling machines which are far more complex and are also able to go over the machined surface without problem because they can lift the machining head – something that is not possible with the autonomous ground robot.

One interesting publication in the CAM field is [2] that presents a method to reduce gaps that are present when simply offsetting a polygon with spirals. The presented method could be a possible future improvement to the spiral fill algorithm of ??.

The OpenCAM library has also been inspected...

3.3.2 Spiral Filling

Straight Skeleton

To generate a spiral fill for the trajectory, we use the properties of the so called straight skeleton. The straight skeleton is defined as the topological skeleton of a polygon that is created by moving the edges inwards at a constant speed and observing the intersections of the vertices. It was first described by [3].

During the creation of the straight skeleton, two events can happen:

- Edge event: An edge shrinks to zero, making its neighboring edges adjacent now.
- Split event: An edge is split, i.e., a reflex vertex runs into this edge, thus splitting the whole polygon. New adjacencies occur between the split edge and each of the two edges incident to the reflex vertex.

(cited from [3]).

The straight skeleton is similar to the median axis of a polygon, but unlike the median axis it is not defined to have a constant distance to the polygon edges.

For the case of this thesis, the most interesting property of the straight skeleton is the ability to easily obtain inset polygons. The inset polygons are used to create a spiral fill for the polygons. The procedure is as follows:

- (0) The straight skeleton is generated
- (1) The inset polygon is created
- (2) If a split event has happened, then it is decided which polygon should be used to extend the current spiral (that is the one with the closer point to our current position). All the others are recursively filled in the same way. Additionally, a starting point to the spiral is passed, so that the beginning of the next spiral will be close to the current one. (The procedure restarts with the split polygon as input at (0)).
- (3) The $n + 1$ vertex of the inset polygon is appended to the current spiral
- (4) An inset polygon is generated with inset length divided by number of vertices. Through dividing the inset length (which is predefined, usually as one rake width) by the number of vertices in the polygon, we make sure that one revolution of the spiral will travel only one rake distance.

The algorithm is both displayed in pseudo code and graphically.

3.3.3 Back and Forth Filling

This fill method is quite straight forward: The polygon is filled by a number of lines that are parallel to each other and clipped at the polygon edges.

3.4 Path Generation

As already mentioned, to finally create a drawing all elements have to be connected by support trajectories where the rake is lifted. The supporting paths should have two properties: The total sum of all support paths should be as small as possible and the curvature of the connections should be limited.

As previously defined, a drawing consists of the three different types: Lines, polygons and filled polygons. Lines and polygons differ in the way they can be connected, as illustrated in ???. A line can be entered or exited on both ends and is traversed in a previously unknown direction. A polygon however can be entered at any vertex, but can only be exited at the same so that the polygon is closed. Filled polygons work the same as the regular polygon in that sense, since the spiral and the back and forth filling create a polyline that is inserted into the filled polygon.

3.4.1 Traveling Salesman Problem

The Traveling Salesman Problem (TSP) is the problem of finding the minimum-weight Hamiltonian Circuit in a weighted graph. A weighted graph is a graph where every edge between two vertices has a certain weight. The Hamiltonian Circuit is defined as a tour through the graph, that travels to every vertex exactly once. It is called salesman problem because in the historical context the vertices were cities and the salesman, seeking to minimize the distance traveled to visit all the cities in a given tour, would have liked to get a solution for this problem. However, one of

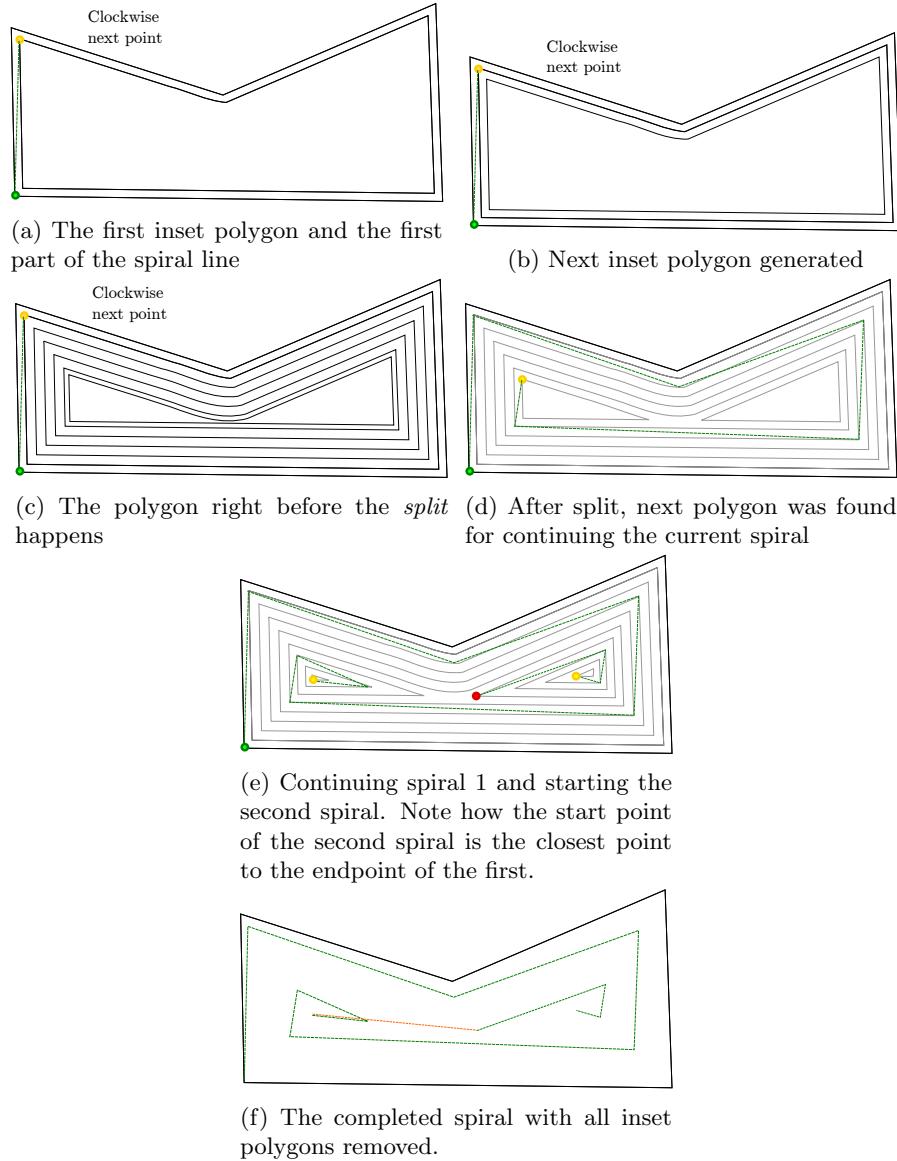


Figure 3.2: Generating the fill spiral. Note that this is only an example for illustration purposes. Of course, the density of inset polygons for a real application is much higher.

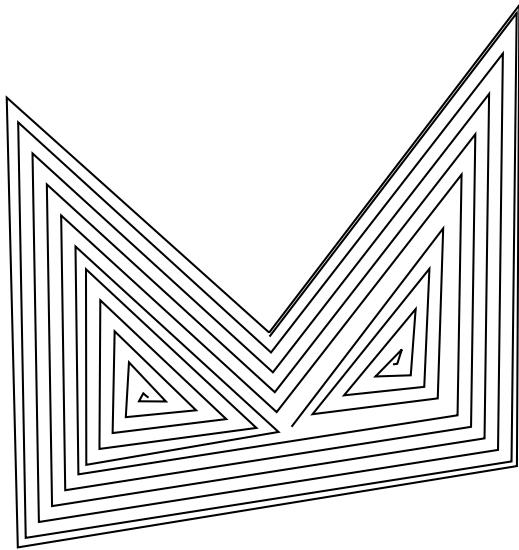


Figure 3.3: Generated spiral

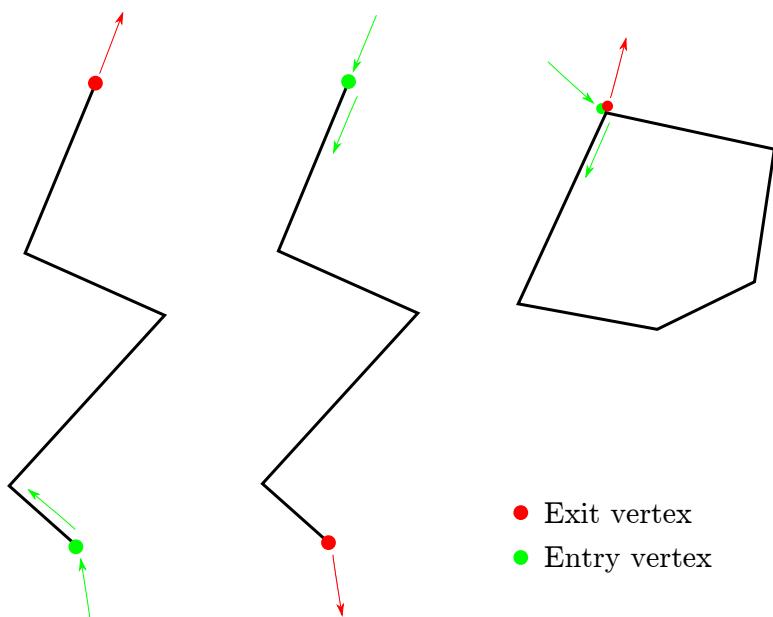


Figure 3.4: Possible entry- and exit vertices and direction of traversal for polylines and polygons. Note that the polygon could also be traversed in clockwise direction.

the properties that make this problem hard is that it is NP-hard. If no heuristic is used, the amount of solutions that have to be searched in order to test all available possibilities is $n!$.

The TSP can be subcategorized in three categories:

Symmetric A TSP is symmetric if all distances between every node pair are symmetric (equal) in both directions from $A \Leftrightarrow B$.

Metric In a metric traveling salesman problem, all distances conform to the triangle inequality $c \leq a + b$ which is, for example, true if all distances are calculated using the euclidean distance formula between two points: $d = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$

Asymmetric If the weights are different from $A \rightarrow B$ than from $B \rightarrow A$ then the TSP is assymetric. Of course, the triangle inequality cannot be fulfilled anymore.

The simplest heuristic to the TSP is the nearest neighbour search. From a given startpoint the nearest, unvisited vertex is searched and connected. This is done until no more unvisited elements exist. Positive about the nearest neighbour approach is that the complexity is only growing linear to the search size. However, the obtained solutions are often of unsatisfying quality.

Another popular heuristic is the branch and bound method. It works by splitting the set of possible solution into two halves and calculating a upper and lower bound for both. If the upper bound of the first is lower than the lower bound of the second, the second is discarded. During the course of this thesis a variant of the depth-first branch and bound search was implemented. First, the graph was traversed until a tour was completed. Afterwards, another tour (in order) was recursively started. As soon as the traveled distance of the entire tour in that branch got higher than the current minimum tour, the branch is discarded. While this already reduces the search space, the effect becomes relatively small on larger problems (e.g. the first 6 out of 15 nodes might only seldomly span a tour which distance is higher than the current minimum, and it gets only worse). It must be said, that the implementation was not very mature, and it actually produces an optimal tour in the current implementation, which is not desired in a heuristic. With more level-wise bounds it could have been a lot more efficient.

The final solution to the minimum connection problem was to use a state of the art TSP solver[4], which employs the Lin-Kernighan-Heuristic[5] to approximately solve the Traveling Salesman Problem.

3.4.2 Adaptation of Traveling Salesman Problem for the Algorithm

3.5 Smooth line connections

Bezir Splines

Spiro Splines

Chapter 4

Implementation

- 4.1 Input**
- 4.2 SVG Parser**
- 4.3 Tree Container**
- 4.4 Preprocessing**
- 4.5 Implementation of the Algorithms**
- 4.6 Postprocessing**
- 4.7 User Interface**

Chapter 5

Conclusion

Appendix A

Appendix

Bibliography

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