

# Quiz

## Topological Gates

**Q1.** How do you write the following braiding sequence as a Python list for the course's simulator?

$$\sigma_1 \sigma_2^{-1} \sigma_1^{-1} \sigma_2$$

1. `[[2, 1], [1, -1], [2, -1], [1, 1]]` (True)
2. `[[1, 1], [2, -1], [1, -1], [2, 1]]`
3. `[[1, 2], [1, 1], [-1, 2], [1, 1]]`
4. `[[1, 1], [1, 2], [-1, 1], [1, 2]]`

**Q2.** What is the inverse of this braiding sequence?

$$\sigma_1 \sigma_2^{-1} \sigma_1^{-1} \sigma_2$$

1.  $\sigma_2^{-1} \sigma_1 \sigma_2 \sigma_1^{-1}$  (True)
2.  $\sigma_1 \sigma_2^{-1} \sigma_1^{-1} \sigma_2$
3.  $\sigma_1^{-1} \sigma_2 \sigma_1 \sigma_2^{-1}$
4.  $\sigma_1 \sigma_2 \sigma_1 \sigma_2$

**Q3.**  $\sigma_1$  is:

1. the braiding between anyon 1 and anyon 2 in the clockwise direction. (True)
2. the braiding between anyon 1 and anyon 2 in the counterclockwise direction.
3. the braiding between anyon 2 and anyon 3 in the clockwise direction.
4. the braiding between anyon 2 and anyon 3 in the counterclockwise direction.

**Q4.**  $\sigma_3^{-1}$  is:

1. the braiding between anyon 3 and anyon 4 in the counterclockwise direction. (True)
2. the braiding between anyon 3 and anyon 4 in the clockwise direction.
3. the braiding between anyon 2 and anyon 3 in the clockwise direction.
4. the braiding between anyon 2 and anyon 3 in the counterclockwise direction.

**Q5.** What could we say about braiding operations?  
(Check The correct statements)

1. Braiding operator can be represented as a unitary matrix. (True)
2. It is possible to braid anyon 1 with anyon 3.
3. Braiding operators are self-adjoint matrices ( $\sigma_i = \sigma_i^\dagger$ ).
4. Given 4 anyons, there are 6 elementary braiding operations. (True)

**Q6.** Check The correct statements:

1. Fibonacci braiding operations are universal. (True)
2. We can approximate a Hadamard gate using 3 Fibonacci anyons. (True)
3. We cannot approximate T gate using 3 Fibonacci anyons.
4. We cannot approximate the F matrix using 3 Fibonacci anyons.

**Q7.** Which one of these relations is the Yang-Baxter relation?

1.  $\sigma_1\sigma_2\sigma_1 = \sigma_2\sigma_1\sigma_2$  (True)
2.  $\sigma_1\sigma_2 = \sigma_2\sigma_1$
3.  $\sigma_1 = F\sigma_2F^\dagger$
4.  $\sigma_1^{10} = 1$

**Q8.** What is the periodicity of Fibonacci braiding operations?

1.  $\sigma_1^{10} = \sigma_2^{10} = I$  (True)
2.  $\sigma_1^5 = \sigma_2^5 = I$
3.  $\sigma_1^2 = \sigma_2^2 = I$
4.  $\sigma_1^9 = \sigma_2^9 = I$

**Q9.** Which one of these algorithms can approximate a quantum gate in a polylogarithmic time:  $O(\log^c(1/\epsilon))$ ?

1. Solovay-Kitaev algorithm. (True)
2. Brute-force algorithm.
3. Machine Learning algorithm.
4. Systematic algorithm.

**Q10.**  $\sigma_1\sigma_2\sigma_1^2\sigma_2\sigma_1 =$

1.  $\sigma_2\sigma_1\sigma_2^2\sigma_1\sigma_2$ . (True)
2.  $\sigma_1^{-1}\sigma_2^{-1}\sigma_1^{-2}\sigma_2^{-1}\sigma_1^{-1}$ .
3.  $(\sigma_1\sigma_2\sigma_1^2\sigma_2\sigma_1)^{10}$
4.  $\sigma_1\sigma_2\sigma_1\sigma_2\sigma_1$

**Q11.**  $\sigma_1\sigma_2\sigma_1\sigma_2 =$

1.  $F\sigma_2\sigma_1\sigma_2\sigma_1F^\dagger$ . (True)
2.  $\sigma_2\sigma_1\sigma_2\sigma_1$ .
3.  $(\sigma_1\sigma_2\sigma_1\sigma_2)^{10}$
4.  $(\sigma_1\sigma_2)^2$

**Q12.** Check The correct statements:

1. Weaving sequence is another name for braiding sequence.
2. Weaving sequences are universal, just like braiding sequences. (True)
3. Given 3 anyons, a weaving sequence is a combination of  $\sigma_1^2$ ,  $\sigma_2^2$  and their inverses. (True)
4. Weaving sequences are easier to implement in experiment than braiding sequences. (True)