piecewise reg

wonilChoi 2018년 1월 30일

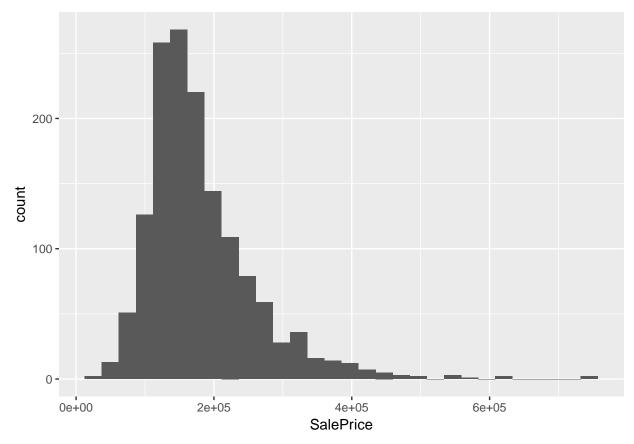
Season 0 - Preseason - Regression

```
library(data.table)

tr <- fread("train.csv", select=c("SalePrice", "SaleCondition", "MiscVal", "GarageCars", "Fireplaces", "Over
ts <- fread("test.csv")

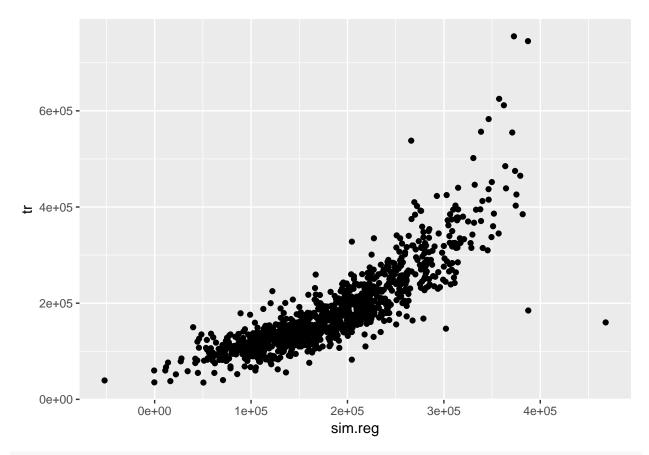
library(ggplot2)
base <- ggplot(data=tr)
base+geom_histogram(aes(x=SalePrice))</pre>
```

`stat_bin()` using `bins = 30`. Pick better value with `binwidth`.



```
tr <- na.omit(tr)

sim.reg <- lm(SalePrice~.,data=tr)
tr.err <- data.table(tr=tr$SalePrice)
tr.err$sim.reg <- sim.reg$fitted.values
qplot(data=tr.err,x=sim.reg,y=tr)</pre>
```



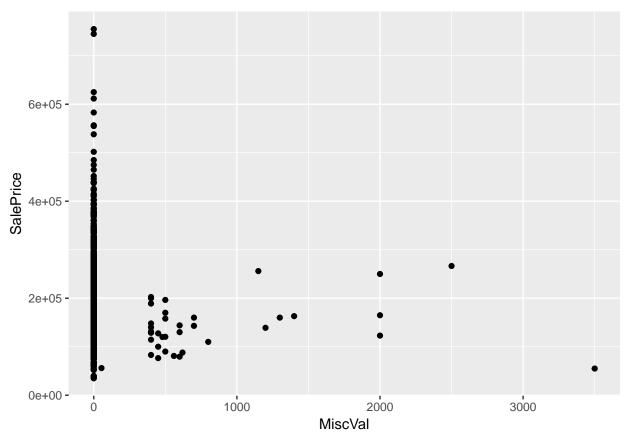
summary(sim.reg)

##

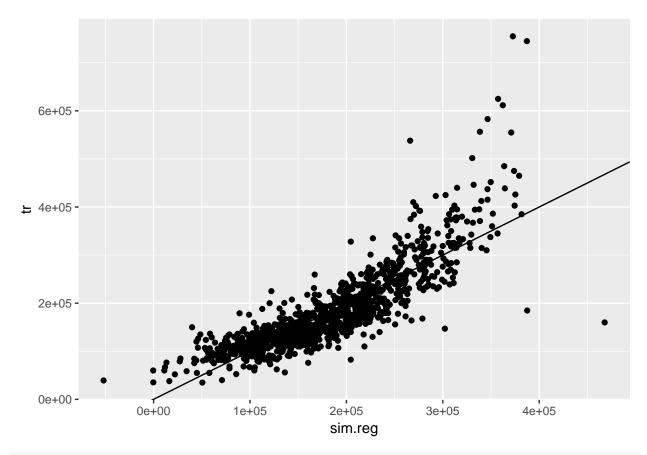
```
## lm(formula = SalePrice ~ ., data = tr)
##
## Residuals:
      Min
               1Q Median
##
                               3Q
                                      Max
## -307810 -25076
                   -3227
                            19524
                                   382357
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                       -1.126e+05 1.058e+04 -10.637 < 2e-16 ***
## SaleConditionAdjLand 1.767e+04 2.281e+04
                                               0.775
                                                       0.4388
## SaleConditionAlloca
                        5.774e+03
                                   1.489e+04
                                               0.388
                                                       0.6983
## SaleConditionFamily -1.656e+04
                                   1.153e+04 -1.436
                                                       0.1512
## SaleConditionNormal
                        3.576e+03
                                   5.102e+03
                                              0.701
                                                       0.4835
## SaleConditionPartial 2.946e+04
                                   6.626e+03
                                               4.446 9.55e-06 ***
## MiscVal
                        1.188e+00
                                   6.797e+00
                                              0.175
                                                       0.8613
## GarageCars
                        2.242e+04 2.184e+03 10.269 < 2e-16 ***
## Fireplaces
                        1.830e+04 2.311e+03
                                              7.918 5.49e-15 ***
## OverallCond
                                               1.718
                                                       0.0861 .
                        2.085e+03
                                   1.214e+03
## OverallQual
                        3.277e+04
                                   1.242e+03
                                              26.384 < 2e-16 ***
                                               6.431 1.84e-10 ***
## LotFrontage
                        3.612e+02 5.617e+01
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
```

```
##
## Residual standard error: 44300 on 1189 degrees of freedom
## Multiple R-squared: 0.7204, Adjusted R-squared: 0.7178
## F-statistic: 278.5 on 11 and 1189 DF, p-value: < 2.2e-16</pre>
```

qplot(data=tr,x=MiscVal,y=SalePrice)



```
tr <- tr[,!"MiscVal"]
sim.reg <- lm(SalePrice~.,data=tr)
tr.err$sim.reg <- sim.reg$fitted.values
qplot(data=tr.err,x=sim.reg,y=tr)+geom_abline(slope=1,intercept=0)</pre>
```

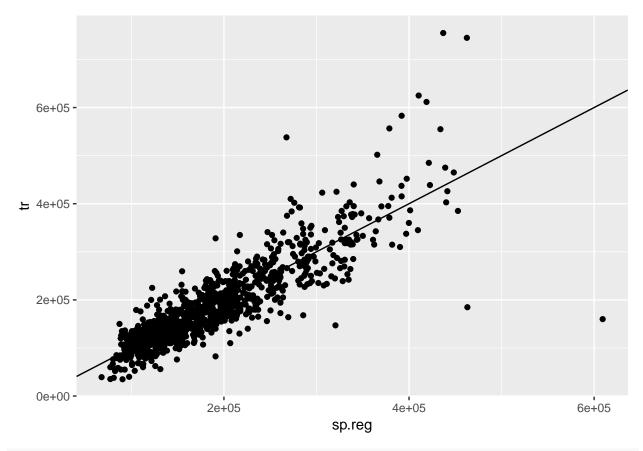


summary(sim.reg)

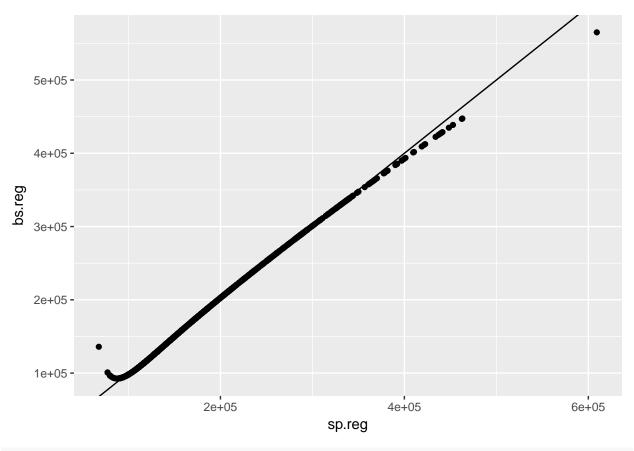
```
##
## lm(formula = SalePrice ~ ., data = tr)
##
## Residuals:
      Min
               1Q Median
##
                               3Q
                                      Max
## -307889 -25078 -3155
                            19474 382336
##
## Coefficients:
##
                         Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                    10580.49 -10.640 < 2e-16 ***
                       -112577.66
## SaleConditionAdjLand
                        17648.85
                                    22797.48
                                               0.774
                                                       0.4390
## SaleConditionAlloca
                                    14885.92
                                                       0.6982
                          5772.71
                                               0.388
## SaleConditionFamily
                        -16573.52
                                    11524.61 -1.438
                                                       0.1507
## SaleConditionNormal
                          3597.91
                                     5098.21
                                              0.706
                                                       0.4805
## SaleConditionPartial
                         29476.45
                                     6622.61
                                               4.451 9.35e-06 ***
## GarageCars
                         22411.54
                                     2181.64 10.273 < 2e-16 ***
## Fireplaces
                         18327.14
                                     2305.35
                                              7.950 4.31e-15 ***
## OverallCond
                         2097.25
                                     1211.21
                                              1.732
                                                       0.0836 .
## OverallQual
                         32758.78
                                     1239.73 26.424 < 2e-16 ***
## LotFrontage
                           361.38
                                       56.14 6.438 1.76e-10 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
```

```
## Residual standard error: 44280 on 1190 degrees of freedom
## Multiple R-squared: 0.7204, Adjusted R-squared: 0.7181
## F-statistic: 306.6 on 10 and 1190 DF, p-value: < 2.2e-16
library(splines)
sp.reg <- lm(data=tr.err, formula=tr~ns(tr.err$sim.reg, df=2))</pre>
bs.reg <- lm(data=tr.err, formula=tr~bs(tr.err$sim.reg, df=2))
## Warning in bs(tr.err$sim.reg, df = 2): 'df' was too small; have used 3
summary(sp.reg)
##
## Call:
## lm(formula = tr ~ ns(tr.err$sim.reg, df = 2), data = tr.err)
## Residuals:
##
      Min
               1Q Median
                               3Q
                                      Max
## -449231 -20131
                     -688
                            17235 318056
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                 67797
                                             9008
                                                    7.526 1.02e-13 ***
                                            16438 23.731 < 2e-16 ***
## ns(tr.err$sim.reg, df = 2)1
                                390100
## ns(tr.err$sim.reg, df = 2)2
                                523375
                                            10046 52.097 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 40560 on 1198 degrees of freedom
## Multiple R-squared: 0.7638, Adjusted R-squared: 0.7635
## F-statistic: 1937 on 2 and 1198 DF, p-value: < 2.2e-16
summary(bs.reg)
##
## Call:
## lm(formula = tr ~ bs(tr.err$sim.reg, df = 2), data = tr.err)
## Residuals:
##
                1Q Median
                               30
      Min
                                      Max
## -405063 -20631
                     -539
                            18128 330001
##
## Coefficients:
##
                              Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                                135892
                                            19312
                                                   7.037 3.31e-12 ***
                                            43097 -3.892 0.000105 ***
## bs(tr.errsim.reg, df = 2)1 -167725
## bs(tr.err$sim.reg, df = 2)2
                                188285
                                            17933 10.500 < 2e-16 ***
## bs(tr.err$sim.reg, df = 2)3
                                429172
                                            38092 11.267 < 2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 40730 on 1197 degrees of freedom
## Multiple R-squared: 0.762, Adjusted R-squared: 0.7614
## F-statistic: 1278 on 3 and 1197 DF, p-value: < 2.2e-16
```

```
tr.err$sp.reg <- sp.reg$fitted.values
tr.err$bs.reg <- bs.reg$fitted.values
base+geom_point(data=tr.err,aes(x=sp.reg,y=tr))+geom_abline(slope=1,intercept=0)</pre>
```



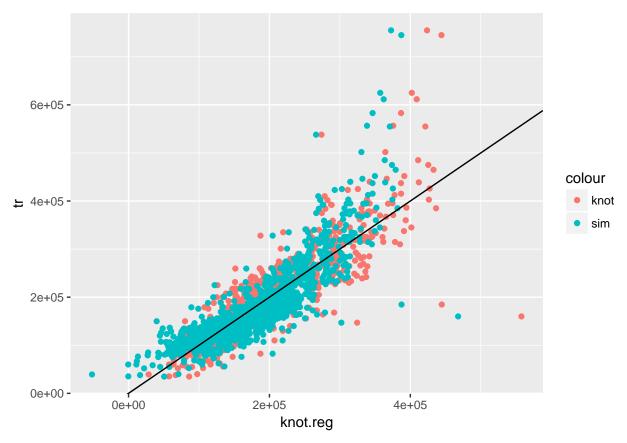
base+geom_point(data=tr.err,aes(x=sp.reg,y=bs.reg))+geom_abline(slope=1,intercept=0)



library(plotly)

```
##
## Attaching package: 'plotly'
## The following object is masked from 'package:ggplot2':
##
       last_plot
##
## The following object is masked from 'package:stats':
##
##
       filter
## The following object is masked from 'package:graphics':
##
##
       layout
plot_ly(data=tr.err,y=~tr,x=~sp.reg)%>% add_markers()%>%add_lines(x = ~tr, y = ~tr)
breaks <- with(tr.err, sim.reg[which(sim.reg >= 310*10^3 & sim.reg <= 370*10^3)])
mse <- numeric(length(breaks))</pre>
for(i in 1:length(breaks)){
    piecewise1 <- lm(tr ~ sim.reg*(sim.reg < breaks[i]) + sim.reg*(sim.reg>=breaks[i]),data=tr.err)
    mse[i] <- summary(piecewise1)[6]</pre>
mse <- as.numeric(mse)</pre>
breaks[which(mse==min(mse))]
## [1] 357298.6
```

```
# knot.reg <- lm(tr~sim.reg:(sim.reg>357298.6)+sim.reg:(sim.reg<=357298.6),data=tr.err)
library(SiZer)
## Warning: package 'SiZer' was built under R version 3.4.3
## Loading required package: boot
knot.reg <- with(tr.err,piecewise.linear(sim.reg, tr, middle = 1, CI = FALSE,</pre>
                 bootstrap.samples = 1000, sig.level = 0.05))
summary(knot.reg$model)
##
## Call:
## lm(formula = y \sim x + w)
##
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -397683 -19911 -987
                            16759 331259
## Coefficients:
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 5.767e+04 4.977e+03 11.59
                                             <2e-16 ***
              5.620e-01 3.331e-02 16.87
                                             <2e-16 ***
## x
              8.446e-01 5.581e-02 15.13 <2e-16 ***
## w
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## Residual standard error: 40430 on 1198 degrees of freedom
## Multiple R-squared: 0.7653, Adjusted R-squared: 0.7649
## F-statistic: 1953 on 2 and 1198 DF, p-value: < 2.2e-16
tr.err <- cbind(tr.err, knot.reg=knot.reg$model$fitted.values)</pre>
base+geom_point(data=tr.err,aes(x=knot.reg,y=tr, col='knot'))+
   geom_point(data=tr.err,aes(x=sim.reg,y=tr, col='sim'))+
   geom_abline(slope=1,intercept=0)
```



```
tr.err[,sim.reg.err2:=(tr-sim.reg)^2]
tr.err[,sp.reg.err2:=(tr-sp.reg)^2]
tr.err[,knot.reg.err2:=(tr-knot.reg)^2]
sort(apply(tr.err,2,mean))
##
                                                     bs.reg
                                                                 knot.reg
              tr
                       sim.reg
                                       sp.reg
        180770.5
                      180770.5
                                                   180770.5
                                                                 180770.5
##
                                     180770.5
## knot.reg.err2
                   sp.reg.err2 sim.reg.err2
   1630862017.5 1640811447.1 1942642595.3
library(psych)
##
## Attaching package: 'psych'
## The following object is masked from 'package:boot':
##
##
       logit
## The following objects are masked from 'package:ggplot2':
##
##
       %+%, alpha
describe(tr.err)
```

```
## bs.reg 4 1201
## knot.reg 5 1201
                               180770.5 7.279355e+04
                                                        163003.0
                               180770.5 7.294924e+04
                                                        156320.5
                                                                     170941.8
## sim.reg.err2 6 1201 1942642595.3 7.864007e+09 500363323.4 818547676.0 
## sp.reg.err2 7 1201 1640811447.1 8.087383e+09 349339962.1 620590980.5
## knot.reg.err2 8 1201 1630862017.5 7.392256e+09 339341870.2 623873313.4
##
                          mad
                                    min
                                                            range skew
                                                 max
## tr
                   58414.44 34900.00 7.550000e+05 7.201000e+05
## sim.reg
                   69558.14 -51860.33 4.678885e+05 5.197488e+05 0.37
## sp.reg
                    61852.80 67796.80 6.092315e+05 5.414347e+05 1.35
## bs.reg
                    65956.35 92503.29 5.650635e+05 4.725602e+05 1.21
## knot.reg
                     51920.45 28519.90 5.576828e+05 5.291629e+05 1.27
## sim.reg.err2 686715371.89 608.17 1.461810e+11 1.461810e+11 12.24
                 493052496.09 137.03 2.018089e+11 2.018089e+11 16.60
## sp.reg.err2
## knot.reg.err2 476085125.91 82.02 1.581516e+11 1.581516e+11 13.85
##
                 kurtosis
                                    se
## tr
                             2406.25
                     6.22
## sim.reg
                     0.04
                               2042.34
## sp.reg
                   2.14
                             2103.02
## bs.reg
                   1.40
                             2100.49
## knot.reg
                               2104.99
                    1.46
## sim.reg.err2 180.10 226919784.95
## sp.reg.err2 349.07 233365418.54
## knot.reg.err2 234.38 213307194.71
```