# DRAFT: The factorial function in Clarity

Part 4

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#### Abstract

Clarity forbids recursion or unbounded iteration. So computing 'naturally recursive' functions in Clarity is interesting.

### 1 Classic Recursive Factorial

Factorials are classical. The factorial function is a classic example of recursion. For instance,

$$n! = \begin{cases} 1 & \text{if } n = 0, \\ n \cdot (n-1)! & \text{otherwise.} \end{cases}$$

Basic factorials are 0! = 1,  $1! = 1 \times 0!$ ,  $2! = 2 \times 1! = 2$ ,  $3! = 3 \times 2! = 6$ ,  $4! = 4 \times 3! = 24$ , and in full detail 5! is

$$5! = 5 * 4!$$

$$= 5 * 4 * 3!$$

$$= 5 * 4 * 3 * 2!$$

$$= 5 * 4 * 3 * 2 * 1!$$

$$= 5 * 4 * 3 * 2 * 1 * 0!$$

$$= 120$$

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Many programming languages use the factorial function to illustrate recursion, see [1]. The recursive Scheme factorial function in Listing 1 cannot be directly implemented in Clarity since Clarity forbids recursion.

Listing 1: Scheme factorial function

```
(define (factorial n)
  (cond
    ((= n 0) 1)
    (else
        (* n (factorial (- n 1))))))
```

To its credit, the recursive nature of a standard factorial definition is cleanly and clearly implemented using recursion. The factorial function in Listing 1 builds a stack as seen in Listing 2. At the end when all arguments are fully evaluated, the expression (\* 5 4 3 2 1 1) is evaluated.

Listing 2: Recursive factorial substitution

```
(factorial 5)
(* 5 (factorial 4))
(* 5 4 (factorial 3))
(* 5 4 3 (factorial 2))
(* 5 4 3 2 (factorial 1))
(* 5 4 3 2 1 (factorial 0))
(* 5 4 3 2 1 1)
```

Clarity has the following restructions,

- 1. Recursion is illegal
- 2. Looping can only be done using map, filter, or fold.

So, how can we implement the factorial function in Clarity? Central objectives include,

- 1. Correctness
- 2. Elegance

The value of correctness is self-evident. The value of elegance comes from several places

- 1. Elegant things are easy to remember
- 2. Revisiting elegant things is a pleasure so we will do it more

Of course, efficiency plays a role as well. Efficiency is also related to elegance.

## 2 Factorial in Clarity

### 2.1 The map function

Listing 3: The Clarity map function

```
(map f lst)
```

Consider the definition,

(define-constant 1st (list u1 u2 u3 u4 u5)).

```
(define-private (psquare (num uint))
          (* num num))

(define-public (square-numbers (numbers (list 10 uint)))
          (ok (map psquare numbers)))
```

The fold function takes three arguments. The first argument is a binary function, the second argument is an iterable item, and the last argument is the first value for the binary function application.

Listing 4: The Clarity fold function

```
(fold f lst base)
```

which means f is applied to base and 1st.

```
(f base lst )
```

#### 2.2 The filter function

Executing this in the Clarinet console,

#### Listing 5: The Clarity filter function

```
(contract-call? .c1 filter-even-numbers (list u1 u2 u3 u4 u5))
```

### 2.3 The map function

Listing 6: The Clarity map function

```
(map f lst)

Consider the definition,

(define-constant lst (list 1 2 3 4 5)).
```

## 2.4 The map function

Listing 7: The Clarity map function

```
(map f lst)

Consider the definition,

(define-constant lst (list 1 2 3 4 5)).

Given lst, how can 5! be computed?
```

Listing 8: A start of a factorial function in a Clarity contract c1

```
;;
;;
;(define-constant lst (list 1 2 3 4 5))
;;
;;
;;
(define-public (factorial-5 (v int))
;;
```

For example, we desire,

```
>> (contract-call? .c1 factorial-5 1)
>> (ok 120)
```

A version without an argument is,

```
(define-public (fact-1)
   ;;
```

Also giving,

```
>> (contract-call? .c1 fact-1)
>> (ok 120)
```

## 3 Exercises

1. The Fibonacci sequence is

$$f(n) = \begin{cases} f(n-1) + f(n-2) & \text{if n in } 1, \\ 0 & \text{if } n \leq 1. \end{cases}$$

How can we generate elements of the Fibonacci sequence in Clarity?

2. A recursive function may have k different recursive invocations in its definition. For example, the code in Listing 1 has one recursive invocation in its definition. The Fibonacci function has two recursive invocations in its definition.

In Clarity, how might we code a function that has k recursive invocation in its definition?

## References

- [1] Harold Abelson, Gerald Jay Sussman, with Julie Sussman: Structure and Interpretation of Computer Programs, Second Edition, MIT Press, 1996.
- [2] Clarity Book, https://book.clarity-lang.org/ 2023-04-11.