L.A. Traffic Collision Analysis



Presented to:

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I. Introduction

Car accidents happen every day with an alarmed increasing rate in California. According to the California Office of Traffic Safety (OTS), traffic fatalities increased 7% from 3,387 in 2015 to 3,623 in 2016. Below is a summary statistics for traffic collision in Los Angeles city in 2016 to give us some other perspectives:

TYPE OF COLLISION	VICTIMS KILLED & INJURED	OTS RANKING
Total Fatal and Injury	44207	4/15
Alcohol Involved	3546	4/15
Had Been Drinking Driver < 21	125	7/15
Had Been Drinking Driver 21 – 34	1137	5/15
Motorcycles	2441	5/15
Pedestrians	3487	5/15
Pedestrians < 15	293	6/15
Pedestrians 65+	430	4/15
Bicyclists	1980	10/15
Bicyclists < 15	74	11/15
Composite	22688	4/15

TYPE OF COLLISION	FATAL & INJURY COLLISIONS	OTS RANKING
Speed Related	8331	6/15
Nighttime (9:00pm – 2:59am)	4559	5/15
Hit and Run	4990	6/15

We want to provide a solution for LAPD (Los Angeles Police Department) and OTS to help create a safer city with fewer traffic collisions.

II. Questions of Interests and Descriptions of Variables

1. The Questions of Interests

There are four research interests that our research is based on:

- Which factor contributes to the accidents happening on the weekends or on holidays.
- Which factor predicts a DUI (driving under influence) and hit and run.
- Which cluster of variables identifies incidents violated traffic laws.
- Forecasting model for the next 3 months (September to November) of 2019.

These findings will give the insight to create a better policy and/or education program to lower the traffic collision rate, thus reduce, fatality rate.

2. The Dataset

Los Angeles (L.A.) is one of the busiest urban metropolitan cities where people with various modes of transportation are on the road. The dataset was retrieved from Kaggle.com which further directed us to the lacity.org website where a broad layer of information was available. The dataset includes records from 2010 to August 2019, when the data was pulled. There are total 18 attributes with 488,384 observations. The sample data of L.A. Traffic Collision data is provided below:

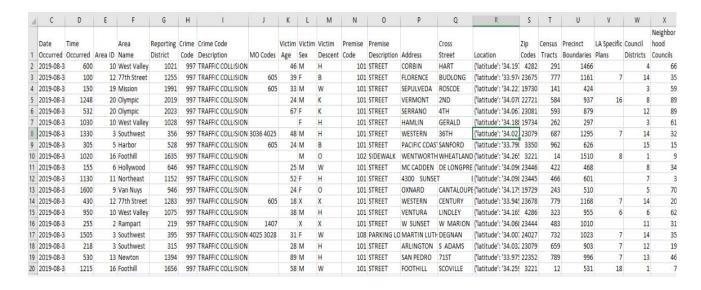


Exhibit 2.1:shows the sample data of L.A. Traffic Collision data.

3. The Descriptions of Variables

VARIABLE	FIELD DESCRIPTION	VARIABLE TY	ORDINAL/ NOMINAL
DR Number	Division of Records Number: Official file number made up of a 2	text	ordinal
Date Reported	MM/DD/YYYY	date time	ordinal
Date Occurred	MM/DD/YYYY	date time	ordinal
Time Occurred	In 24 hour military time	date time	ordinal
Area ID	The area code of each LAPD	number	nominal
Area Name	The name of each LAPD location depends on the name of the la	text	nominal
Reporting District	Reporting code of each LAPD, which helps to group data based	number	nominal
Crime Code	The code of committed crime	number	nominal
Crime Code Description	Description of crime code	text	nominal
MO Codes	Code of criminal activities	number	nominal
Description	Description of MO code (seperate file)	text	nominal
Victim Age		number	nominal
Victim Sex	Gender of victim	text	nominal
Victim Descent	Origin of victim	text	nominal
Premise Code	Code of the crime scene	number	nominal
Premise Description	Description of scene code	text	nominal
Address	The closest street to the crime scene, but still anonymous to eve	text	nominal
Cross Street	Cross street based on the round address	text	nominal
Location	The location of the crime but encrypted	text	nominal
Zip Code		number	nominal
Census Tracts	Statistical population	number	nominal
Precinct Boundaries	Crime district (for the uses of LAPD)	number	nominal
LA Specific Plans	Land use Policy by area	number	nominal
Council Districts	Council Districts of crime	number	nominal
Neighborhood Councils (Certified)	Neighborhood councils of crime	number	nominal

4. Data Exploration

Variable	Graph 1	Graph 2	Comment
DR Number	N/A	N/A	There is no missing value. 889 DR Number repeated 2 times, the rest showed only one time (MAX=2, MIN=1).
Date Reported		Total number of collisions reported Page 1 2010 2012 2014 2016 2018 Time	There is no missing value. From the graph, we can depict that the number of collisions was reported as the collision occurred. Note: 2019 is not considered as the data for the complete year is not available.
Date Occurred		Total number of collisions occurred Description Descr	There is no missing value. From the graph, it is evident that the number of collisions is increasing every year. Note: 2019 is not considered as the data for the complete year is not available.
Time Occurred	Time Occurred	Time Occurred 00095 00091 00091 00091 00091 00091 00091 00091 00091 00091 00091 00091 00091 00091	Through Graph 1, no outlier is indicated. There is no missing value. Graph 2 shows that there is a strong correlation between time occurred and the chance of the collision happened.

Area ID	Area ID 02 51 02 45 45 45 45 45 45 45 45 45 4	Area ID Occopy of the first of	Through Graph 1, no outlier is indicated. There is no missing value. There are 21 Area IDs.
Area Name		Area Name Area Name 77th Street Harbor N Holywood Pacific Topanga Wilshire Popular Area	There is no missing value. There are some major area names, such as 77th street, Habor, N Hollywood, Pacific, Topanga, and Wilshire.
Reportin g District	Reporting District	Reporting District	There are no missing values. There are no outliers.
Crime Code	N/A	N/A	There is only one constant value for this field. It will be deleted during data cleaning.
Crime Code Descripti on	N/A	N/A	There is only one constant value for this field. It will be deleted during data cleaning.
MO Codes		TOP 10 MO Codes 250000 - 2500000 - 250000 - 250000 - 250000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 250000 - 250000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 250000 - 250000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 250000 - 250000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 250000 - 250000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 250000 - 250000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 250000 - 250000 - 2500000 - 250000 - 2500000 - 25000000 - 2500000 - 2500000 - 2500000 - 2500000 - 2500000 - 250000	There are 85,096 missing values.

Victim Age	Victim Age	Victim Age Victim Age Victim Age	There are 77,907 missing values. The age of 85 or larger is indicated as an outlier from graph 1.
Victim Sex		Victim Sex 0000957 0000951 000095 0 F H M N X	There are 5,770 missing values and 5 categories as follow (there is no description for H and N categories. Moreover, these 2 categories don't have a lot of observations and it would not affect the analysis): F (female): 184,950 obs H: 133 obs M (male): 284,766 obs N: 11 obs X (unknown): 11,328 obs
Victim Descent		Victim Descent Victim Descent B D G I J L P U W Z Popular Victim Descent	There is no missing value, but there are 2 obs were represented by "-". There are some major descents, the 1st one is H - Hispanic/Latin/Mexican, following by W - White, O - Other, and B - Black.
Premise Code		Premise Code Set 10	There are 25 missing values.
Premise Descripti	N/A	N/A	There are 25 missing values. This variable is an

on			enumerated variable.
Address	N/A	N/A	There are no missing values and 11,472 unique values. This variable will be useful for geographic map analysis but will not be used in prediction models.
Cross Street		Cross Street 3500	There are 21,945 missing values. The most frequent location of collisions are at Vermont AV recorded as 3650.
Location	Location Counts 21748 21748 21748 21748 21748 21749		There is no missing values.
Zip Code	Zip Codes	Zip Codes Company Code Code	There are 396 missing values. Zip codes are usually 5-digit or 9-digit formats. However, there are 421,864 5-digit zip codes and 66,124 4-digit zip codes.
Census Tracts	#2 Pet Zeen	Census Tracts 000000 000000 000000 00000000000000	There are 6,591 missing values. There are few outliers as shown in graph 1.

Precinct Boundari es		Histogram of Precinct Boundaries Output	There are 3,114 missing values in this variable. Since these are area codes, outlier treatment will not be an appropriate step to explore.
LA Specific Plans	LA Specific Plans 8 9 9 9 9 9 9 9 9 9 9 9 9	LA Specific Plans 10	There are 308,578 missing values, which take about 63.18% of the observation. We will drop this variable in the preprocessing step.
Council Districts	Council Districts 7	Council Districts 00007 000000 00000 0000 0000 0000 000	Through Graph 1, no outlier is indicated. There is no missing value and there are 15 council districts.
Neighbor hood Councils (Certified)	Neighborhood Councils (Certified)	Neighborhood Councils (Certified)	Through Graph 1, no outlier is indicated. There are 24,381 missing values.

Exhibit 3.1: Exploratory Data Analysis of traffic collision variables

III. Data Preprocessing

1. Create a binary 'Day Off' variable:

Since we are interested in whether the accident happens on the weekend/holidays, we create a binary response variable based on 'Date Occurred' predictor combining with the US holiday/weekend calendar through manipulation in Excel.

2. Missing values:

When we deal with data preprocessing, we would first check whether values are missing from the dataset. Though missing data is common, it can cause huge problem to the study on the dataset. Missing values can lower the representativeness of the sample, which can mislead people about the population of the dataset. If the dataset has missing values, we have to eliminate those values, or carry forward the values of the previous records. When a predictor has a lot of missing data (more than 30%) and, thus, becomes irrelevant for our prediction models, we will delete that predictor.

3. Detect and delete outliers:

We check if the variables that have outliers in order to decide whether we should leave the outliers in the dataset or take them off the dataset. When a dataset has too many outliers, those outliers will affect other analytical results dramatically. We run boxplots to have a closer look at the outliers in each variable. Then, we calculate lower and upper whiskers of the boxplot to identify the values of outliers. Lower whisker is equal to the smallest value greater than Q1-1.5IQR (Interquartile Range). Lower whisker represents the lower bound of the dataset. Upper whisker is calculated is the greatest value smaller than Q3+1.5IQR. It indicates the upper bound of the dataset.

There are some outliers in Victim Age, Zip Code, and Census Tracts. Zip Code and Census Tracts's data is not in their right respective format. For example, the Zip Code should always have 5 digits, but our data have value less than 10000. As a result, we drop these two variables. On the other hand, Victim Age have outliers at 81 and above. People who have age 81 or higher are less likely to drive a vehicle. Therefore, we drop all the outliers for Victim Age.

4. Frequence table of categorical variables - combine values:

We run table function for all predictors to see if there is any category within each predictor has a small number of observations. Usually, we combine with predictor's categories that have similar patterns. Since there are a lot of values in 'Area Name', we combine the areas into 5 main territories (South LA, North LA, West LA, East LA, and Central LA). In contrast, we take a different approach for 'Victim Descent'. White and Hispanic descent have the highest number of observations in our data. Thus, we combine other descents into one category called 'Other Descent' within 'Victim Descent'.

5. Collinearity:

Multicollinearity occurs when your model includes multiple factors that are correlated not just to your response variable but also to each other. In other words, it results when you have factors that are a bit redundant. Serve multicollinearity is a major problem, because it increases the variance of the regression coefficients, making them unstable. The more variance they have, the more difficult it is to interpret the coefficients. If there is a strong indicator of collinearity between two predictors, we will

delete one that is less appropriate for our response variable. There is no collinearity in our data as shown below:

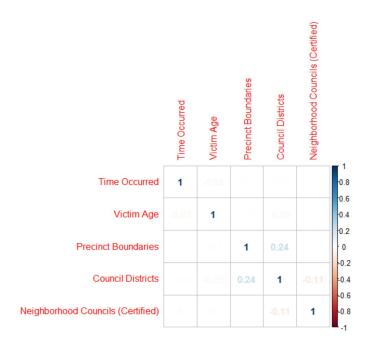


Exhibit 6.3: Classification three model

5. Data Reduction

We will partition data randomly into standard 60% for training and 40% for validation to test the accuracy of the model.

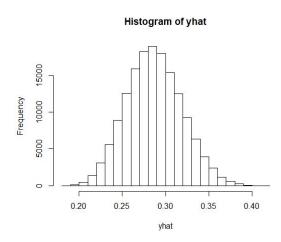
IV. Data Mining - Prediction Models

1. Logistic Regression

Logistic Regression is a statistical machine learning classification model used to predict the probability of a categorical dependent variable. In Logistic Regression, instead of using the dependent variable, it is expressed as a function of logit. In logistic regression, the output is modeled as a binary value (0 or 1) rather than a numeric value and the probability of the outcome lies between 0 and 1. The logit is modeled as a linear

function of the predictors, which reflects the probability. An example logistic regression equation can be written as:

y = e^(b0 + b1*x) / (1 + e^(b0 + b1*x)) where y is the predicted output, b0 is the bias or intercept term and b1 is the coefficient for the single input value (x). To implement logistic regression, all the categorical predictors are transformed into dummy variables (0/1). Dummy variables have been created for these categorical predictors - Area Name, Victim Sex, Victim Descent and Premise Description. The areas were categorized into South LA, North LA, Central LA, West LA and East LA. The sex of the victim was categorized into Male (M), Female (F) and Other (X). Majority of traffic collisions have occurred on the street and parking lot. Therefore, we have categorized Premise Description into Street, Parking Lot and Other Premises. Victim Descent was categorized into H, Other Descent and W. We divided our data into training data 60% and validation data 40%. There are 20 predictors or variables and the logit is modeled as a linear function of the predictors, which reflects the probability. The accuracy of the model is around 71.15 %.



```
call:
glm(formula = Day.Off ~ Time.Occurred + Area.Name_South.LA +
    Victim.Sex_F + Victim.Age + Victim.Descent_W + Area.Name_West.LA +
    Area.Name_East.LA + Neighborhood.Councils..Certified. + Victim.Descent_H
    Council.Districts + Premise.Description_PARKING.LOT + Area.Name_Central.L
    family = "binomial", data = dat.train)
Deviance Residuals:
                  Median
    Min
             10
                               3Q
                                       Max
-1.0162 -0.8393 -0.7895
                           1.4895
                                    1.8601
Coefficients:
                                   Estimate Std. Error z value Pr(>|z|)
(Intercept)
                                 -5.195e-01 2.383e-02 -21.796 < 2e-16
Time.Occurred
                                 -1.277e-04 7.879e-06 -16.208 < 2e-16
Area.Name_South.LA
                                  7.827e-02 2.379e-02
                                                         3.290
                                                                0.0010
                                 -1.404e-01 9.425e-03 -14.896 < 2e-16
Victim.Sex_F
                                 -3.393e-03 2.916e-04 -11.636 < 2e-16
Victim.Age
Victim.Descent_W
                                 -8.998e-02 1.236e-02 -7.280 3.35e-13
Area.Name_West.LA
                                 -1.028e-01 1.432e-02
                                                       -7.178 7.09e-13
Area.Name_East.LA
                                 -1.372e-01 2.351e-02
                                                       -5.834 5.42e-09
Neighborhood.Councils..Certified. -9.378e-04 1.790e-04
                                                       -5.239 1.61e-07
                                  4.620e-02 1.083e-02
                                                        4.265 2.00e-05
Victim.Descent_H
                                                         1.800
Council.Districts
                                  3.672e-03 2.040e-03
                                                                 0.0719
Premise.Description_PARKING.LOT
                                 7.738e-02 2.579e-02
                                                         3.000
                                                                 0.0027
Area.Name_Central.LA
                                  2.817e-02 1.600e-02
                                                         1.761
                                                                 0.0783
```

2. K-Nearest Neighbor

K-Nearest Neighbor (kNN) is an algorithm, which can be used for classification or prediction. kNN classification works best for categorical output and kNN prediction is more suitable for numerical response. In this project we applied both kNN prediction and kNN classification.

There are pros and cons when using kNN method. One of the pros of kNN is: no model-driven. kNN is data-driven. It means that users don't have to fit a data model like linear regression. Besides that, users don't have to make any assumptions about the data, which seems to be more objective. However, kNN does take a long time to calculate and produce k value.

We started kNN analysis process by selecting the variables which can be fitted in the kNN model and have great impacts on the prediction process, and normalizing those variables to avoid bias analysis results. The results of our kNN method is the majority of the car accidents in LA area happened on weekends or holidays. The accuracy of our kNN classification is approximately 70.7%.

3. Classification Tree

Classification tree is one of the most popular methods used for prediction. It's flexible and data-driven. It results in a set of rules by dividing observations into subgroups based on predictor values. The diagram below is a minimum error tree where the validation data will have the lowest error rate. If an accident occurs from midnight to 5:04 am, it is more likely happened on the weekend/holiday.

Min Error Tree

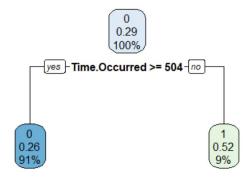


Exhibit 6.3: Classification tree model

4. Prediction results

We use accuracy rate to evaluate the performance of three prediction models. Logistic Regression, kNN, and classification have the accuracy of 71.5%, 70.7%, and

71.85%, respectively. Since the classification tree has the highest accuracy, it is our best prediction model. Compared to the other two models, the classification tree has only one variable, 'Time Occurred', which makes it even more preferable.

V. Forecasting

1. Data Transformation for forecasting

"It is likely that unlikely will happen. But, if you wait long enough, the unlikely will happen." (Aristotle, 2400 B.C). Hence, forecasting is a method that takes past values into consideration to predict the estimates of the future values. It helps to develop strategies to make a better decision. The question of interest is to forecast monthly collisions from September 2019 to November 2019. The variable "Date Occurred" is the daily date of the collision which was aggregated to monthly data. After the transformation, there are a total of 116 observations. A snapshot of the data can be viewed as followed:

Year/Months	January	February	March	April	May	June	July	August	September	October	November	December
2010	3721	3490	3899	3670	3809	3632	3758	3680	3583	4047	3725	4073
2011	3506	3602	3984	3657	3714	3647	3846	3929	3821	3998	3739	3833
2012	3719	3598	4179	3738	3764	3679	3686	3951	3794	4023	3612	3657
2013	3572	3360	3860	3739	3881	3578	3646	4031	3745	4127	3794	3700
2014	3586	3502	3879	3700	3887	3906	3839	4183	4111	4291	3882	4184
2015	4101	3915	4457	4217	4258	4183	4313	4705	4467	4813	4471	4585
2016	4178	4529	4688	4730	4625	4819	4672	4961	4838	4921	4633	4933
2017	4517	4312	5079	4681	4849	4762	4807	4987	4659	5284	4856	4929
2018	4592	4477	4925	4687	4579	4649	4917	5000	4696	5197	4772	4628
2019	4502	4404	4922	4522	4662	4479	4828	4466				

2. Model Criteria

We first identified the four components of the time series which are trend, seasonality, cyclical and random variations. Trend is a general tendency that increases or decreases in a predictable manner. Trend methods involves determining the speed and direction of data over

time. Seasonality is a characteristic of a time series in which the data experiences regular and predictable changes that recur every period (usually calendar year). While cyclical component indicates recurrent variation in the time series, a fluctuation in data that is caused by uncertain or random occurrences. Random variations or noise is unexplainable variability and it is something which does not fall under any of the above three described. Visual analysis will help us to understand the time-series and produce various forecasting methods to understand various components of the time-series in the given data.

We are going to select the best model based by evaluating performance measure. There are various accuracy measures like Mean Error (ME), Mean Absolute Error (MAE), Root Mean Square Error (RMSE), Mean Percentage Error (MPE), Mean Absolute Percentage Error (MAPE), Mean Absolute Scaled Error (MASE). However, we are focusing on MAPE as it is unit free, making the interpretation easier, as well as it is useful when comparing two entirely two different models. Lower the MAPE, better the model.

3. Time Series Analysis

Number of collisions occurred from 2010-2018

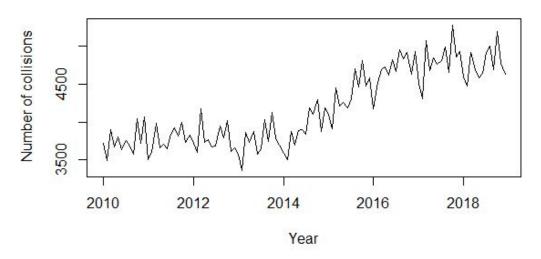


Exhibit 6.5: Time-series from January 2010 to August 2019.

From the exhibit 6.5 above, there seems to be an upper trend starting from 2014 and a seasonality in the data. Also, there seems to be a multiplicative seasonality as seasonal cycle seems to be growing over time. Multiplicative seasonality is when the seasonality influences increases or decreases with the increase and decrease in the level of the series. the seasonality. To confirm the presence of these components, we will decompose the time-series into its components as shown in Exhibit 6.6.

Decomposition of multiplicative time series

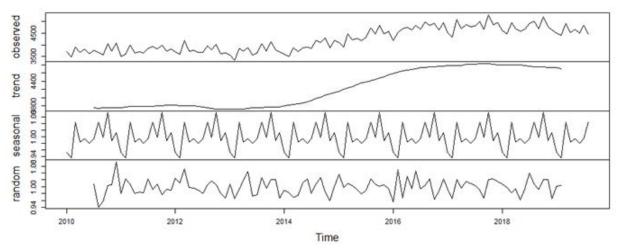


Exhibit 6.6 - Decomposition of time series

From Exhibit 6.6, we see that the time series has a gradual growing trend. Hence, it is not stationary. To understand the type of trend (linear, damped, exponential trend), we will cover in the next topic. The repetitive pattern in the seasonal variations confirms the presence of seasonal pattern. Seasonality is influenced by climate change, human behavior, holidays, etc.

De-trended time series

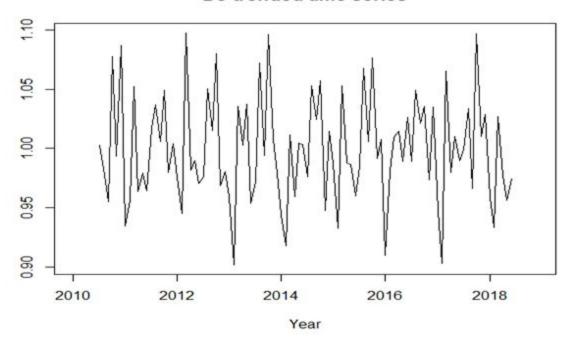


Exhibit 6.7: Detrended time series of the number of collisions from 2010 to 2019

This detrended time series forces its mean to zero and reduces overall variation. It helps removes any kind of distortion, provide a clear picture of the data as well as focus on other important factor(s) (if present).

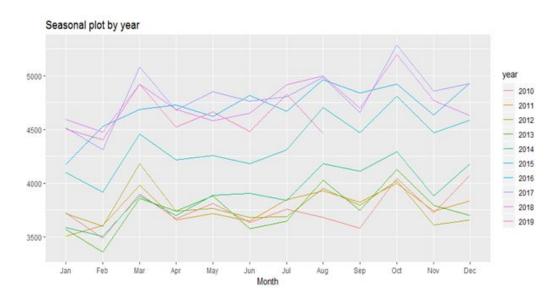


Exhibit 6.8: Seasonal plot of number of collisions by year

The above visualization graph (Exhibit 6.8) shows the seasonality by year starting from 2010 to August 2019. The line graph shows that the seasonality has increased from 2010 to 2019. Hence, this confirms the presence of multiplicative seasonality in the number of collisions. Also, to understand the concentration of accidents based on certain seasons, we focused on seasonal factor. A seasonal factor greater than 1 indicates that the number of collisions for that month was above yearly average. On the other hand, a seasonal factor below 1 indicates the number of collisions was below yearly average number of collisions. From the exhibit 6.9 and 6.10, October averaged the highest number of collisions. In fact, March and August had the second highest whereas January and February averaged the lowest rate. High number of collisions in October could be due to on-set of fall season. Weather conditions do play an important role in traffic conditions, hence rise and fall in the seasonal factor can be observed. Other factor such as holiday seasons, number of road trips/journeys made which also depend on the weather could be the contribution to fatal accidents.

Months	Seasonal Factor	Months	Seasonal Factor
Jan	0.9522	July	0.9945
Feb	0.9344	August	1.0444
March	1.044	September	0.9976
April	0.9835	October	1.0741
May	0.9943	November	0.9869
June	0.9804	December	1.0129

Exhibit 6.9: Seasonal factors by month

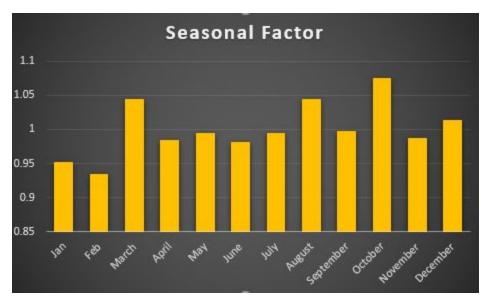


Exhibit 6.10: Bar chart of seasonal factors by month

4. Exponential smoothing models

Exponential Smoothing method is one of the forecasting methods. They use weighted averages of past observations to forecast new values. They give more importance to recent values in the time series. Thus, as observations get older (in time), the importance of these values get exponentially smaller.

For exponential smoothing model, we have again, considered the data from the year 2010 to 2019 (August). We will be forecasting for the next three months (i.e. September 2019, October 2019 and November 2019) giving more importance to the recent values over the older observations.

(a) Simple exponential smoothing model (SES): It assumes there is no trend and seasonality in the data. It requires only one parameter called alpha or smoothing factor which has a range from 0 to 1. Smoothing factor controls the rate at which the influence of the observations at prior time helps decay exponentially. A value close to 1 indicates the most recent values are weighted heavily related to older past observations whereas value close to 0 indicates the older observations influence the forecasts. The graph in Exhibit 4.8 shows that forecasted values are going to be the same for the next 3 months which can be confirmed by viewing the summary in this exhibit.

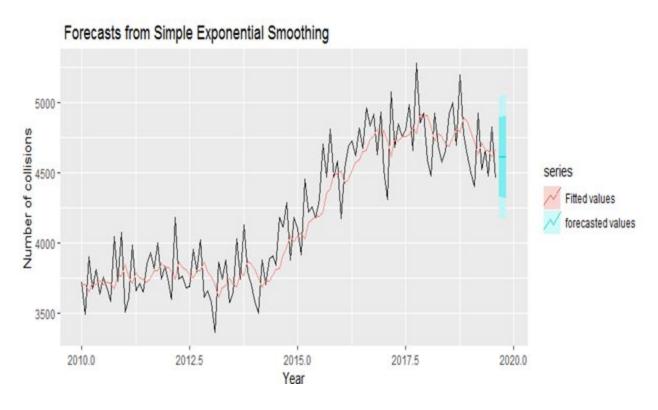


Exhibit 6.11: Graph and Summary of Simple Exponential Smoothing model

Forecast method: Simple exponential smoothing

Model Information:

Simple exponential smoothing

call:

 $ses(y = f_ts_2019, h = 3)$

Smoothing parameters:

alpha = 0.2718

Initial states:

1 = 3702.0724

sigma: 216.7458

AIC AICC BIC 1803.263 1803.478 1811.524

Error measures:

ME RMSE MAE MPE MAPE MASE ACF1
Training set 28.94056 214.8692 177.7408 0.4771262 4.198607 0.9084899 -0.1354741

Forecasts:

Point Forecast Lo 80 Hi 80 Lo 95 Hi 95 Sep 2019 4614.68 4336.909 4892.451 4189.866 5039.494 Oct 2019 4614.68 4326.828 4902.531 4174.449 5054.911 Nov 2019 4614.68 4317.089 4912.270 4159.554 5069.805 (b) Holt's Linear method: This method assumes that there is a presence of linear trend and there is no seasonality in the data. The forecasts from linear trend extrapolate the last estimate of the trend without limit. It involves two smoothing factors: alpha for the level and beta for the trend. The value of Beta also ranges from 0 to 1. The value of beta close to 0 reduces to simple exponential smoothing model.

```
Forecast method: Holt's method
Model Information:
Holt's method
call:
 holt(y = f_ts_2019, h = 3, PI = FALSE)
  Smoothing parameters:
    alpha = 0.0411
beta = 0.041
  Initial states:
    1 = 3657.8476
    b = 6.441
  sigma: 208.1949
     AIC
             AICC
1795.872 1796.417 1809.640
Error measures:
                                                  MPE
                                                          MAPE
                                                                     MASE
                                                                                  ACF1
                     ME
                            RMSE
                                      MAE
Training set -7.873892 204.5738 164.2864 -0.3341425 3.914891 0.8397203 -0.01030476
Forecasts:
                             Nov
          Sep
                   oct
2019 4579.458 4548.450 4517.442
```

Exhibit 6.12: Summary of Holt's Linear method

(c) Damped Holt's method: This method assumes that there is a damped trend and there is no seasonality. The forecast from damped trend starts almost linearly but dies off exponentially until they reach a constant level.

```
Forecast method: Damped Holt's method
Model Information:
Damped Holt's method
call:
 holt(y = f_ts_2019, h = 3, damped = TRUE, PI = FALSE)
  Smoothing parameters:
alpha = 0.0397
    beta = 0.0397
    phi
          = 0.9607
  Initial states:
    1 = 3673.9607
    b = 15.6954
  sigma: 208.851
             AICC
     ATC
                        BIC
1797.562 1798.332 1814.083
Error measures:
                      ME
                             RMSE
                                                   MPE
                                                            MAPE
                                                                      MASE
Training set -0.5514119 204.3004 162.3277 -0.1711181 3.871225 0.8297086 -0.008332423
          sep
                    Oct
                             Nov
2019 4602.544 4578.635 4555.665
```

Forecasts from Linear Holt method and Damped Holt method

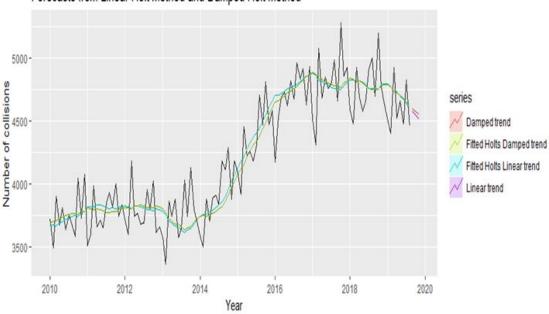


Exhibit 6.12: Summary of Damped Holt's method

(d) Holt-Winter's additive method: This model is an extension of Holt's exponential model. It assumes that there is a linear trend and an additive seasonality. There are three smoothing factors: alpha for level, beta for trend and gamma for seasonal adjustment. The value of gamma also ranges from 0 to 1.

```
Forecast method: Holt-Winters' additive method
Model Information:
Holt-Winters' additive method
call:
 hw(y = f_ts_2019, h = 3, seasonal = "additive")
  Smoothing parameters:
    alpha = 0.1699
    beta = 0.0462
    gamma = 1e-04
  Initial states:
    1 = 3756.5464
    b = 1.6114
    s = 54.5913 -49.6101 310.2622 -10.9417 189.5796 -17.8914
           -76.5225 -28.1312 -66.9449 183.2336 -276.48 -211.1449
  sigma: 130.6231
     AIC
             AICC
1698.577 1704.822 1745.388
Error measures:
                    ME
                           RMSE
                                     MAE
                                                MPE
                                                        MAPE
                                                                  MASE
                                                                              ACF1
Training set -5.041776 121.2805 95.52365 -0.1320246 2.278069 0.4882518 0.01303577
Forecasts:
                                    Hi 80
                                             Lo 95
         Point Forecast
                           LO 80
                                                      Hi 95
Sep 2019
               4551.562 4384.161 4718.962 4295.545 4807.578
Oct 2019
               4847.346 4676.081 5018.610 4585.420 5109.272
Nov 2019
               4462.046 4285.242 4638.850 4191.647 4732.445
```

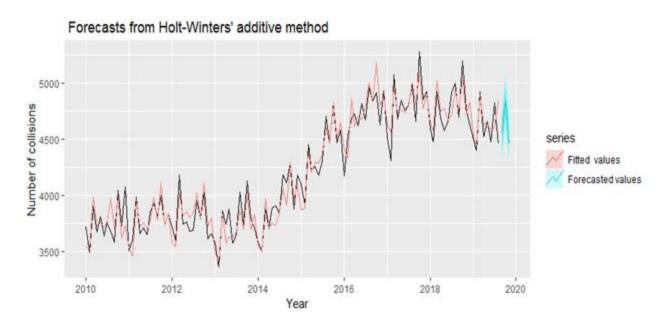


Exhibit 6.14: Graph and Summary of Holt-Winter's additive model

(e) Holt-Winter's Multiplicative model: It is similar to the above model. The only difference is it assumes that there is a linear trend and a multiplicative seasonality in the data.

```
Forecast method: Holt-Winters' multiplicative method
Model Information:
Holt-Winters' multiplicative method
hw(y = f_ts_2019, h = 3, seasonal = "multiplicative")
  Smoothing parameters:
    alpha = 0.1048
    beta = 0.0389
    gamma = 1e-04
  Initial states:
    1 = 3748.9489
    b = 5.4371
    s = 1.0156 0.99 1.0733 0.9925 1.0305 0.9994
           0.9793 1.0006 0.9869 1.0448 0.9325 0.9546
  sigma: 0.0312
     AIC
             AICC
1698.777 1705.022 1745.588
Error measures:
                    ME
                            RMSE
                                      MAE
                                                  MPE
                                                          MAPE
                                                                     MASE
                                                                               ACF1
Training set -6.354812 121.8239 94.59422 -0.1619321 2.257106 0.4835012 0.1022409
                                     Hi 80
                                               Lo 95
                                                        Hi 95
         Point Forecast
                            Lo 80
Sep 2019
               4555.057 4372.788 4737.326 4276.300 4833.814
oct 2019
               4901.055 4702.905 5099.206 4598.010 5204.101
Nov 2019
               4497.437 4312.595 4682.279 4214.746 4780.128
  5000
Number of collisions
```

4000

3500

2010

2012

2014

Year

2016

Exhibit 6.15: Graph and Summary of Holt-Winter's multiplicative model

2020

2018

series

Fitted values

Linear trend and multiplicative seasonality

(f) Damped Holt-Winter's additive method: This exponential model considers that there is a damp trend and additive seasonality in the time series.

Forecasts from Damped Holt-Winters' additive method

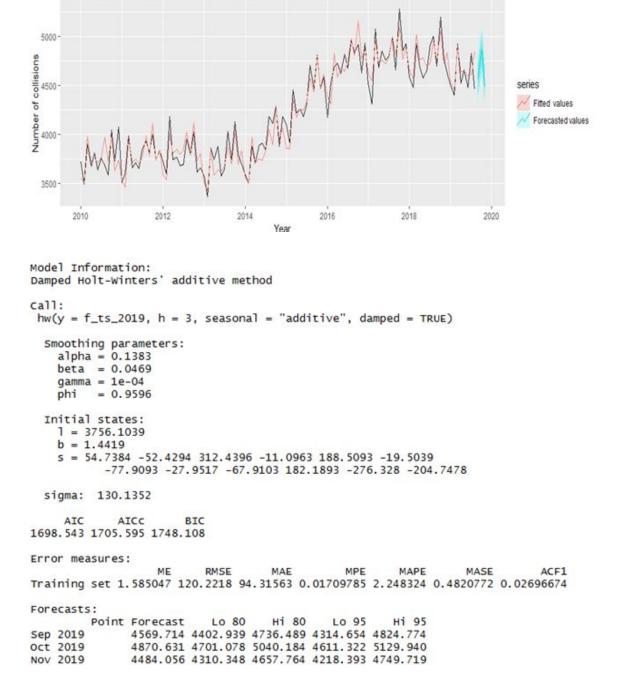


Exhibit 6.16 Graph and Summary of Damped Holt-Winter's additive model

(g) Damped Holt-Winter's Multiplicative method: This model assumes that there is a damped trend and multiplicative seasonality in the time series.

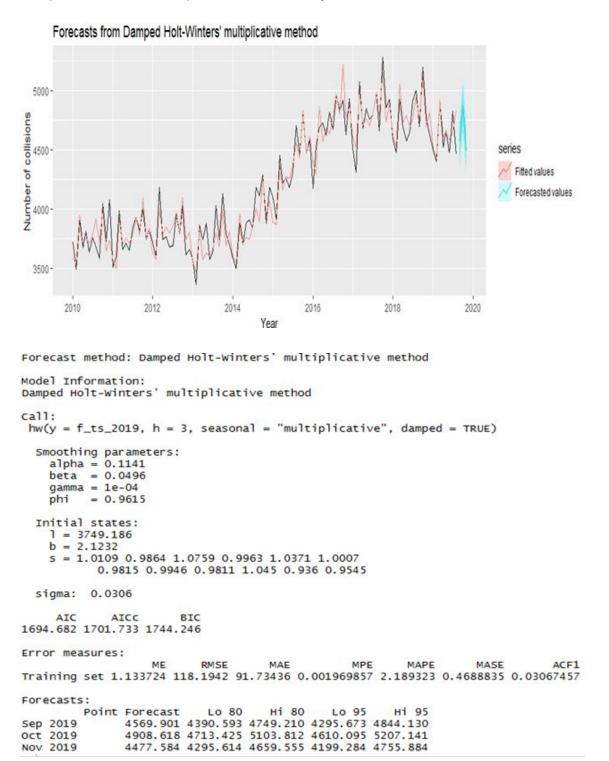
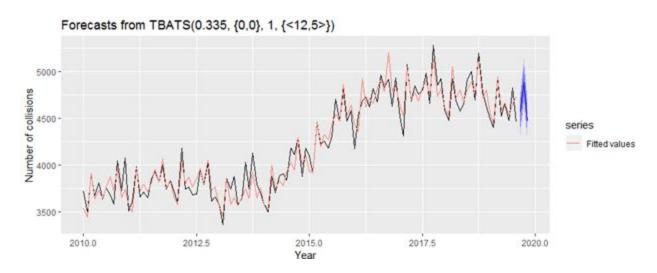


Exhibit 6.17 Graph and Summary of Damped Holt-Winters multiplicative model

(h) TBATS method: This method is completely automated method and it is a modified exponential smoothing state space model. TBATS stands for Trigonometric seasonality, Box-Cox transformations, ARMA models for residuals, Trend and Seasonality.



Sigma: 0.4466125 AIC: 1684.688

Error measures:

ME RMSE MAE MPE MAPE MASE ACF1
Training set -3.003907 114.9318 89.76503 -0.08426658 2.130709 0.4588177 0.04074475

Forecasts:

Point Forecast Lo 80 Hi 80 Lo 95 Hi 95 Sep 2019 4566.302 4412.843 4723.268 4333.013 4807.795 Oct 2019 4888.488 4726.856 5053.754 4642.750 5142.725 Nov 2019 4472.651 4319.205 4629.679 4239.412 4714.268

Exhibit 6.18 Graph and Summary of TBATS model

(i) ARIMA model: ARIMA models is technically sophisticated way of forecasting a time series variable by looking only at the past patterns of the time series. They do by exploiting the autocorrelation structure of the time series.

```
Forecast method: ARIMA(3,1,0)(2,1,0)[12]
Model Information:
Series: f_ts_2019
ARIMA(3,1,0)(2,1,0)[12]
coefficients:
          ar1
                   ar2
                             ar3
                                     sar1
                                               sar2
      -0.7302
               -0.3784
                         -0.1916
                                  -0.5621
                                           -0.2188
       0.1082
                0.1211
                          0.1040
                                   0.1093
sigma^2 estimated as 23208:
                              log likelihood=-663.59
AIC=1339.19
              AICC=1340.06
                              BIC=1355
Error measures:
                    ME
                            RMSE
                                                  MPE
                                                                                 ACF1
                                      MAE
                                                           MAPE
                                                                     MASE
Training set -2.969676 140.0253 107.1298 -0.06618339 2.528344 0.5475743 0.03136809
Forecasts:
         Point Forecast
                            Lo 80
                                     Hi 80
                                              Lo 95
Sep 2019
               4524.885 4329.650 4720.120 4226.298 4823.472
oct 2019
               4885.402 4683.185 5087.619 4576.138 5194.666
Nov 2019
               4531.072 4312.527 4749.617 4196.836 4865.307
```

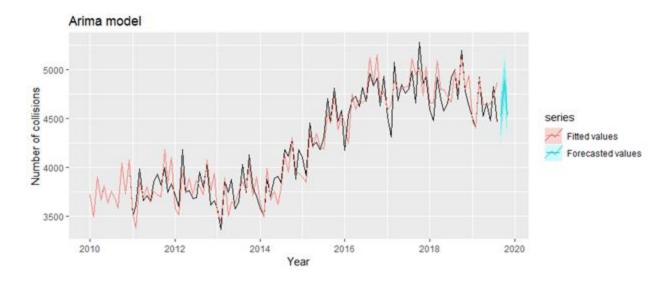


Exhibit 6.19 Graph and Summary of ARIMA model

5. Result from forecast:

Models		Holt's Linear	Holt's	additive	Multiplicative	Holt-Winter's	Damped Holt-Winter's Multiplicative method	ARIMA models	TBATS method
MAPE (%)	4.19%	3.91%	3.87%	2.27%	2.25%	2.24%	2.18%	2.52%	2.13%

Exhibit 6.20 Performance evaluations using MAPE of all forecasting models

In conclusion, TBAT model has the lowest MAPE. Thus, it is the best model for forecasting the number of collisions for next three months. This model makes sense because the frequencies of the seasonality increases over time in data. Also, this method works fine for short-term predictions.

VI. Predict DUI (Driving under influence)

1. Random forest

Random forest combines several trees for better performance, which is one of the ensemble methods. it uses bootstrap which draws multiple random samples with a replacement that selected data can be repeated, and fits each sample for separate model and compute (average) the predictions to obtain enhanced prediction result. For the classification, the final prediction selected with the majority vote among models. Unlike a single tree, the results from a random forest can not be displayed like a dendrogram; it only provides the variable importance scores which measure the relative contribution of different predictors.

The purpose of this test is to predict DUI (driving under influence) using MO Codes variable, which contains 3038 (DUI felony) and 3039 (DUI misdemeanor). Since there were only a few DUI cases (DUI 0.34% of total 332,182 data set), under-sampling was used for the test. If the original data used for the training, it may not detect y=1

(DUI) data well since y=0 (non-DUI) dominates the training data set. We split the selected independent variables, which are "Time Occurred", "Victim Age" in a range of 0, 20, 35, 50, 100 respectively, "Victim Sex", "Victim Descent" and "Council Districts". Among those independent variables, the "Time Occurred" variable was rescaled within a range from 0 to 1, and other ones were transformed into dummy variables.

	Reference	
	Y!=DUI	Y=DUI
Training	500	500
Validation	330,556	626

Exhibit 6.21: Frequency table of the output label, DUI or not.

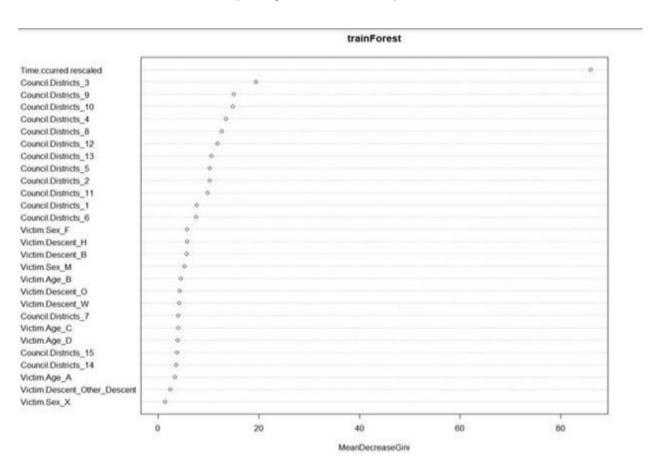


Exhibit 6.21: Significant variables from random forest

Validation results	Reference	
Prediction	FALSE	TRUE
FALSE	224,352	90
TRUE	106,205	535

Exhibit 6.22: Confusion Matrix from Random Forest Model

From the chart of Variable Importance, the "Time Occurred" variable dominated the data. The differences among other variables are not significant. The accuracy, sensitivity, and specificity of Random Forest are 67.90%, 85.60%, and 67.87% respectively.

2. Up sampling and SMOTE

Since my target data sample (1126, 0.34%) was very small compared to the whole data, we tried upsampling and SMOTE sampling to make larger training data. Up-sampling randomly replicates instances in the minority class. Synthetic minority sampling technique (SMOTE) decreases samples of the majority class and synthesizes new minority instances by interpolating between existing ones.

<u>Up-sampling:</u> Produced 9985 TRUE and selected 9818 FALSE data for training.

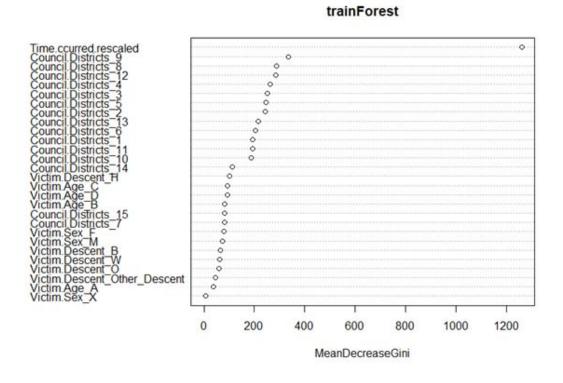


Exhibit 6.23: Significant variables from Up-Sampling

FALSE	TRUE
9918	9985

Exhibit 6.24: Frequency table from Up-Sampling

Validation results	Reference			
Prediction	FALSE	TRUE		
FALSE	97683	27		
TRUE	35061	102		
Sensitivity	0.790698			
Specificity	0.7358750			

Exhibit 6.25: Confusion Matrix and Statistics from Up-Sampling

The sensitivity rate for the of the up-sampling was 6.6% lower than the under-sampling model. There were 273 y=1 (DUI) in the original training data, and the size of y=1 data increased about 30 times the scale of the x-axis for the up-sampling increased nearly 14 times.

SMOTE: produced 819 TRUE data and selected 1092 FALSE data for training.

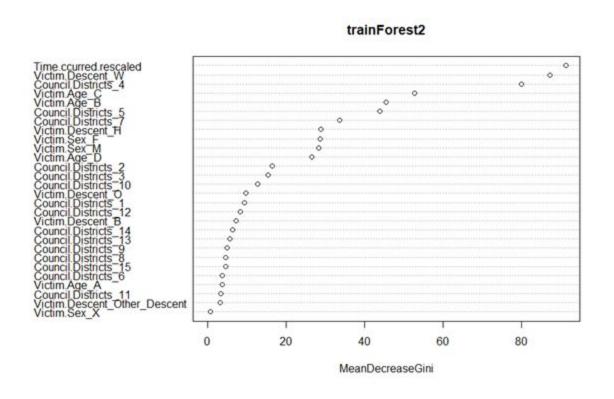


Exhibit 6.26: Significant variables from SMOTE

FALSE	TRUE
1092	819

Exhibit 6.26: Frequency table from training data for SMOTE

		Reference			
		FALSE	TRUE		
Prediction	FALSE	128536	113	Sensitivity	0.124031
Frediction	TRUE	4208	16	Specificity	0.9683

Exhibit 6.27: Confusion Matrix and Statistics from SMOTE

Even though the SMOTE increased specificity a lot from 67.87% (under-sampling) to 96.83%, the sensitivity of SMOTE was very low as 12.4%. Since the purpose of this research is to predict the target y=1, SMOTE is not recommended. From the importance chart, the pattern of the distribution became distorted than the up-sampling. It can be inferred that producing instances by interpolating between existing values produced more distortion than the up-sampling for this distortion for this case.

3. XGBoost

XGBoost is a type of Boosting model which gives higher selection probabilities to misclassified records. The most important feature of XGBoost is the capability of managing sparse data; it stores data without storing zeros that can save memory and time. It has a distributed weighted quantile sketch algorithm to effectively handle weighted data. And it can execute multiple threading that has the effect of running multiple machines. Finally, it can handle missing data and use for the regression as well.

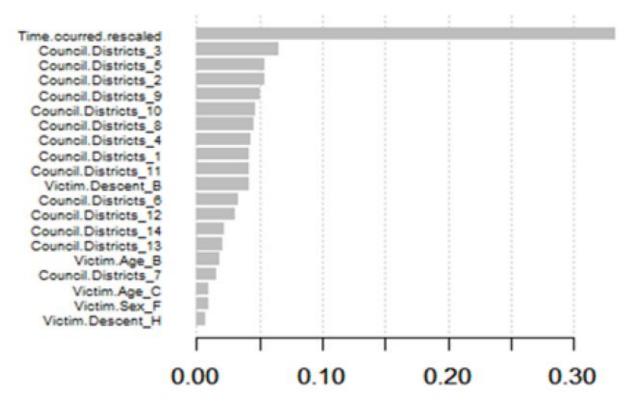


Exhibit 6.28: Significant variables from XGBoost

		Reference			
		FALSE	TRUE		
Prediction	FALSE	215,409	71		
	TRUE	115,148	554		

Exhibit 6.29: Confusion Matrix from XGBoost

The results of XGBoost are Accuracy 65.21%, Sensitivity 88.64%, Specificity 65.16%. The Variable Importance chart of XGBoost showed a very similar pattern with the random forest since it uses tree method as well. Because XGBoost is the most enhanced model among tree methods, it had a 3% higher sensitivity compared to random forest. However, XGBoost had a lower specificity of about 2.7% (8943 data

more False-true) than the random forest. Therefore, to choose the better model, if the LA transportation department thinks to search 8943 data (115,148 XGBoost False positive-106,205 random forest) more than the random forest model is worth searching 19 cases (554 XGBoost True positive -535 random forest) of DUI then they can select a XGBoost model to predict the DUI case.

From the importance variable chart, the time occurred, and locations such as district 3 are important factors. It can suggest that LA CITY can strengthen monitor of DUI for district 3 at late hours to prevent DUI cases.

4. Predict Hit and Run Felony

The purpose of this test is to predict Hi and Run Felony using MO Codes variable, the cleaned data set contained 3029 Hit and Run Felony. Since there were few Hit and Run Felony cases (29259, 8.8% of total 332,182 data set) in the data set, under-sampling was used for the test.

(a) Random forest (Predict Hit and Run Felony)

y='hit and run' 5000 and y! hit and run' 5000, 10000 data set in the training data.

UE
00
(

Exhibit 6.30: Frequency table from training data for Random Forest

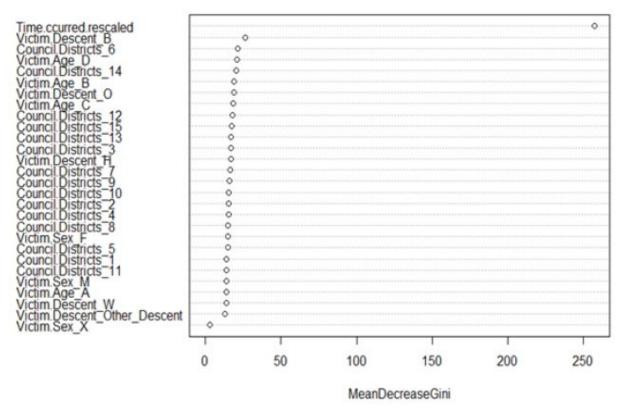


Exhibit 6.31: significant variables from Random Forest to predict hit and run

From the importance variable chart, time was the dominant factor, and the victim descent B was the second important variable for predicting hit and run felony prediction.

	test								
		0	1	0	1	0	1	0	1
2	Cut off	0.5		0.45		0.4		0.3	
y_predi	0	166107	10866	145637	9195	124599	7599	83311	4758
ct	1	131816	13393	152286	15064	173364	16660	214612	19501

Cut off	Sensitivity	Specificity
0.5	0.55208	0.55755
0.45	0.62097	0.48884
0.4	0.68676	0.41809
0.3	0.8039	0.2796

Exhibit 6.32: Confusion matrix, sensitivity and specificity with different cut-off values

Unlike to predict the DUI test, the sensitivity of "hit and run felony" was only 55% (compared to the sensitivity of random forest predicting DUI 85%). Therefore to predict hit and run felony's cut off 0.45 or 0.4 can be selected for random forest model.

(b) XGBoost (Predict Hit and Run Felony)

FALSE	TRUE
5000	5000

Exhibit 6.33: Frequency table from training data for XGBoost for hit and run

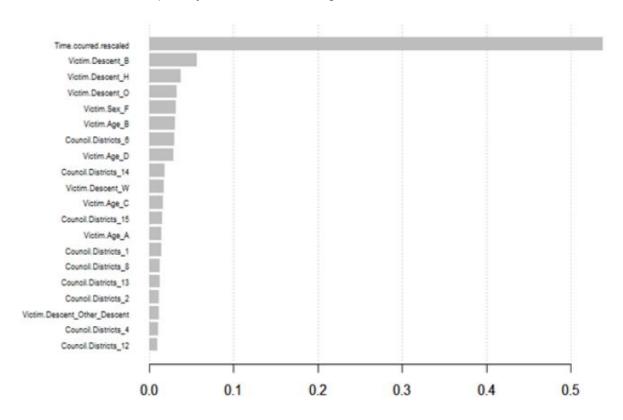


Exhibit 6.35: significant variables from XGBoost to predict hit and run.

From the Variable Importance chart, time was the dominant factor, and the victim descent B was the second important variable for predicting hit and run felony prediction similar to the random forest method. However, compared to the random forest, the council district ranked lower than the random forest model.

			test						/
		0	1	0	1	0	1	0	1
	Cut off	0.5		0.45		0.4		0.3	
y_predi	0	167086	10642	105788	6460	57678	3321	13496	719
ct	1	130837	13617	192135	17799	240245	20938	284427	23540

Cut off	Sensitivity	Specificity
0.5	0.56084	0.56132
0.45	0.73371	0.35509
0.4	0.8631	0.1936
0.3	0.97036	0.0453

Exhibit 6.36: Confusion matrix, sensitivity and specificity with different cut-off values.

Despite the XGBoost model return much higher sensitivity result random forest (at cut off 0.45 random forest 0.62, XGBoost 0.73), its specificity was much lower than the random forest. This means that to detect the true hit and run felony case, the XGBoost model should predict more cases for the hit and run felony for false positive. For 0.45 and 0.4, the test produced higher returns within the cutoff values. To prevent hit and run felony, LA transport department can emphasize education about the crime, especially for the upper ranked groups, which are Decent Black, Hispanic, and female, and age 20 to 35 range than other groups.

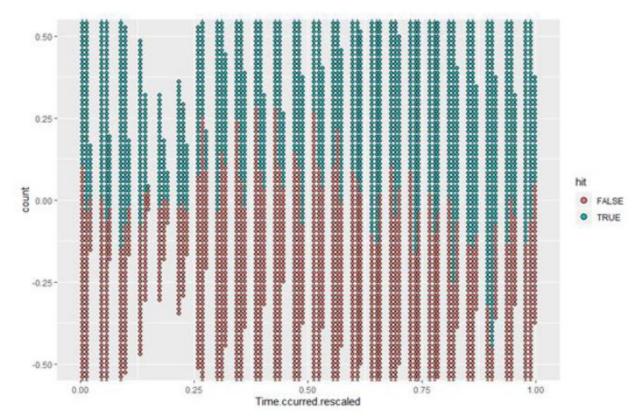


Exhibit 6.37: "Time Occurred' distribution

The hit and run felony was evenly spread across time; it can be explained why the sensitivity was lower using the time variable as a dominant factor. Since the dominant variable (time occurred rescaled) looked hard to split vertically for prediction, the tree-related method may not work well for this type of distribution.

VII. Clustering

Clustering is unsupervised learning (no answers are given). The goal of clustering is to segment the data into similar clusters to generate insight. Clustering is popular for business applications such as customer segmentation for industry analysis. For this test, the k-means method used to assign k clusters to minimize dispersion within the cluster using Euclidean distances.

The object of clustering research is to find the distinctive traffic law violations for each cluster group. First, it found that clustering five groups for the data set gives a reasonable sum of within-cluster distance. Second, it searched traffic law violations for each five groups. Last, it showed relative traffic law violations against population data set (% of law violation for the individual groups subtracted by % of law violation of total population). The variables for clustering were Victim.Sex, Victim.Age, Victim.Decsent, which contains demographic characteristics.

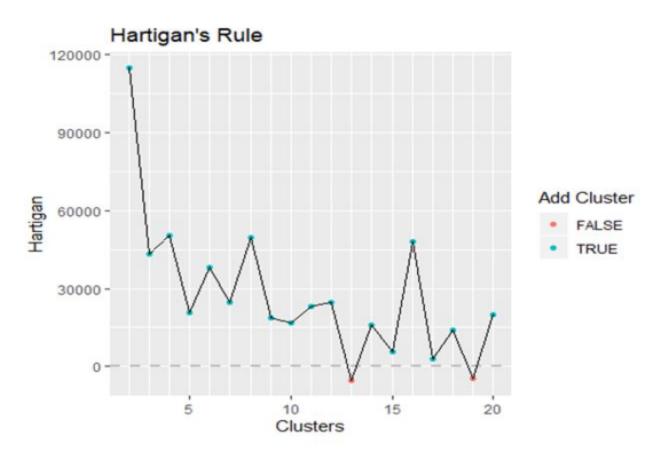


Exhibit 6.38: Graph of Hartigan's rule

Hartigan's rule compares the values of the within-cluster sum of squares for a clustering to 5 groups gives a reasonable low value of the within-cluster sum of squares.

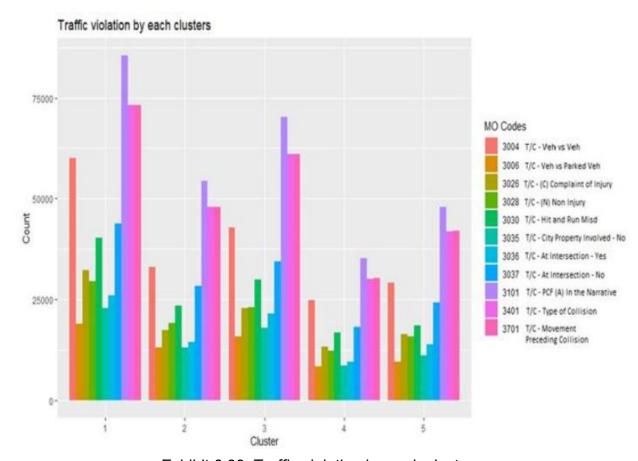
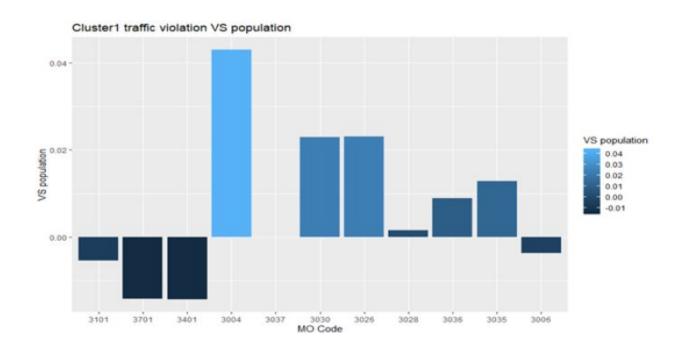
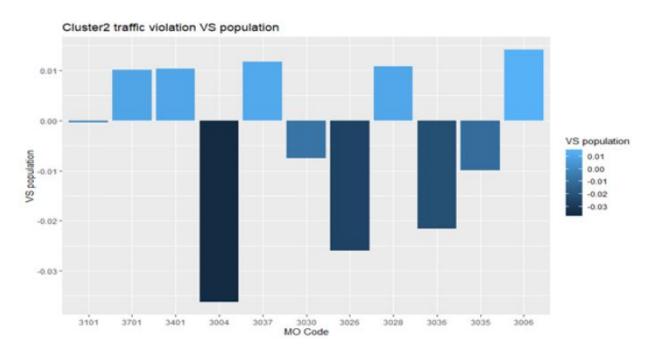
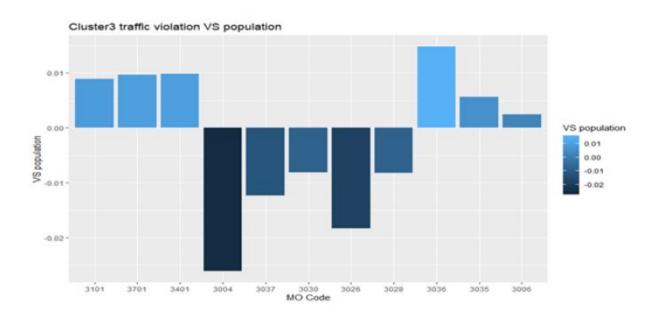


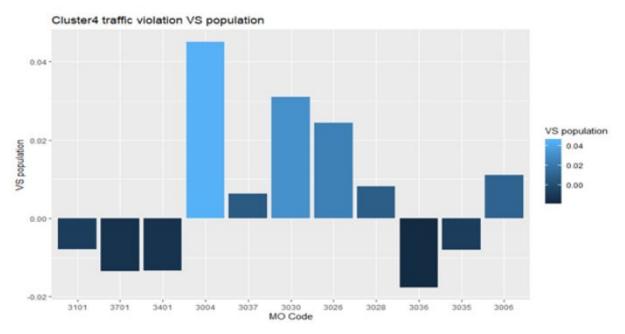
Exhibit 6.39: Traffic violation by each cluster

The 3004 (T/C vehicle vs vehicle), 3401(T/C type of Collision), 3701 (T/C Movement preceding Collision) were the most common traffic violations.









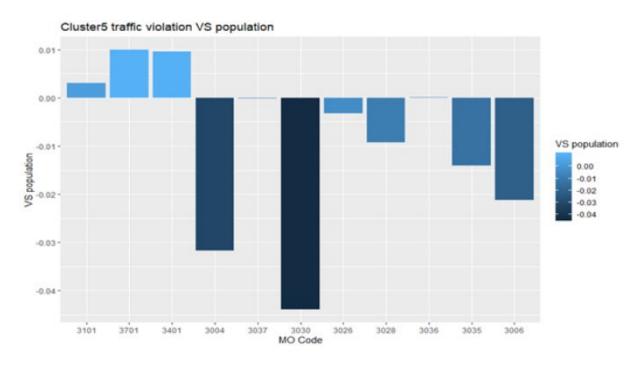


Exhibit 6.40: Various clusters for violation vs population

Percentage of traffic violation by cluster VS percentage of violation by population data set. The most frequently violated law versus population are as below:

- 1. Cluster 1: age 50-100, Female, Black 3004 (T/C Veh vs Veh)
- 2. Cluster 2: age 35-50, Male, Hispanic 3006 (T/C Veh vs Parked Veh)
- 3. Cluster 3: age 20-35, Male, Hispanic 3036 (T/C At Intersection Yes)
- 4. Cluster 4: age 35-50, Female, O (race-Unknown) 3004 (T/C Veh vs Veh)
- 5. Cluster 5: age 50-100, Male, White 3701 (T/C Movement Preceding Collision)

For example, the LA transportation department can give additional warning for driving in the parking lot to cluster 2 members who is the age range 35-50, Male, and Hispanic to prevent 3006 Vehicle versus parked vehicles.

For further research, separating a dataset into clusters is useful for improving performance of supervised methods by modeling each cluster separately. For instance, random forest and XGboost test in the previous section can proceed for each 5 cluster.

VIII. Conclusion

Our team has used three classification prediction models (Logistic Regression, kNN, and Classification Tree) to predict whether an accident will happen on a day off. Classification Tree provides the best accuracy rate with the simplest model. If the time is from midnight to 5:04 am, the accident is more likely to happen on a day off. The increase probability of accident occurrence at night on a day off happens because people usually go to party, drink alcohol, sleep late and/or their night vision is bad. The California Office of Traffic Safety (OTS) can inform people to not go out too late on the weekend.

For prediction, XGBoost was a better model for finding higher sensitivity. However, the specificity was lower than random forest means that it has more false-positive data. For data sampling, three methods used, under-sampling, up-sampling, and SMOTE, under-sampling returned the most precise prediction in the models. Clustering method used for grouping by demographic characteristics, there was much variation for the frequent accidents among groups, LA city can provide customized education by each cluster for preventing the accident effectively.

IX. References

Alice, Michy (2015, October 13). How to Perform a Logistic Regression in R.

Retrieved October 13, 2015, from https://datascienceplus.com,

https://datascienceplus.com/per

form-logistic-regression-in-r/

ALTERYX, INC. (2004 - 2019). Alteryx Designer (2019.1.4.57073). Retrieved from https://www.alteryx.com/why-alteryx/alteryx-for-good/students.

Bartlett. (2016). Better Decisions Demand Forecast Accuracy - Forecast Pro. Retrieved October 13, 2019, from Forecast Pro website: https://www.forecastpro.com/

Charpentier, Arthur (2013, September 26). Logistic Regression and Categorical Covariates. Retrieved from https://www.r-bloggers.com/logistic-regression-and-categorical-covariates/

ggplot2 package | R Documentation. (2019). Retrieved from Rdocumentation.org website: https://www.rdocumentation.org/packages/ggplot2/versions/3.2.1

glm function | R Documentation. (2019). Retrieved from Rdocumentation.org website: https://www.rdocumentation.org/packages/stats/versions/3.6.1/topics/glm

Hilbe, Joseph M., & Hilbe, Joseph M. (2009). Logistic regression models (A Chapman & Hall Book). Hoboken: CRC Press.

Hyndman, R. J., & Athanasopoulus, G. (2018, April). Forecasting: Principles and Practice. Retrieved from https://otexts.com/fpp2/.

James, G., Witten, D., Hastie, T., Tibshirani, R. (2017). Chapter 4.3: Logistic Regression. An Introduction to Statistical Learning with Application in R(1st ed., pp.130-138). New York: Springer Science+Business Media, LLC.

James, G., Witten, D., Hastie, T., Tibshirani, R. (2017). Chapter 4.6.5: K-Nearest Neighbors. An Introduction to Statistical Learning with Application in R(1st ed., pp.163-164). New York: Springer Science+Business Media, LLC.

James, G., Witten, D., Hastie, T., Tibshirani, R. (2017). Chapter 10.3: Clustering Methods. An Introduction to Statistical Learning with Application in R(1st ed., pp.385-401). New York: Springer Science+Business Media, LLC.

Kaggle (2010). Los Angeles Traffic Collision Data. Retrieved from Kaggle.com website: https://www.kaggle.com/cityofLA/los-angeles-traffic-collision-data

Le, James (2018, April 10). *Logistic Regression in R Tutorial*. Retrieved from https://www.datacamp.com/community/tutorials/logistic-regression

Los Angeles City (2017, June 8). Traffic Collision Data from 2010 to Present. Retrieved

October 13, from Lacity.org website: https://data.lacity.org/A-Safe-City/Traffic-Collision

-Data-from-2010-to-Present/d5tf-ez2w

National Center for Statistics and Analysis (2019, October). Estimate of motor vehicle traffic crash fatalities for the holiday periods of 2019. (Traffic Safety Facts Research Note. Report No. DOT HS 812 823). Washington, DC: National Highway Traffic Safety Administration.

Package Forecast. (2019, August 22). Retrieved from https://cran.r-project.org/web/ packages/forecast/forecast.pdf.

Shmueli, G., Patel, N. R., Bruce, P. C. (2010). Logistic Regression. *Data Mining for Business Intelligence: Concepts, Techniques, and Applications in Microsoft Office Excel with XLMiner* (2nd ed., pp. 347-365). Hoboken, NJ: John Wiley & Son Inc.

Shmueli, G., Patel, N. R., Bruce, P. C. (2010). Classification Tree. *Data Mining for Business Intelligence: Concepts, Techniques, and Applications in Microsoft Office Excel with XLMiner* (2nd ed., pp. 301-306). Hoboken, NJ: John Wiley & Son Inc.

Shmueli, G., Patel, N. R., Bruce, P. C. (2010). k-NN Classifier (categorical outcome). *Data Mining for Business Intelligence: Concepts, Techniques, and Applications in Microsoft Office Excel with XLMiner* (2nd ed., pp. 250-259). Hoboken, NJ: John Wiley & Son Inc.

Shmueli, G., Patel, N. R., Bruce, P. C. (2010). Chapter 14: Cluster Analysis. *Data Mining for Business Intelligence: Concepts, Techniques, and Applications in Microsoft*Office Excel with XLMiner (2nd ed., pp. 489-523). Hoboken, NJ: John Wiley & Son Inc.

Shumway, Robert & Stoffer, David (2011). *Time Series Analysis and Its Applications With R Examples*. (3rd Ed.). New York: Springer Science+Business Media, LLC.

RStudio.(2019). Retrieved October 13, 2019, from Rstudio.com website: https://rstudio.com/sqldf package | R Documentation. (2013). Retrieved October 13, 2019, from Rdocumentation.org website: https://www.rdocumentation.org/packages/sqldf/versions/0.4-11

Torgo, Luis (2010, October 1). *K-Nearest Neighbour Classification*. Retrieved October 1, 2010, from https://www.rdocumentation.org, https://www.rdocumentation.org/packages/DMwR/versions/0.4.1/topics/kNN

Wickham H., Retrieved from https://www.rdocumentation.org/packages/ggplot2/ versions3.2.1

Zhang, S., Li, X., Zong, M., Zhu, X., & Wang, R. (2018). Efficient kNN Classification With Different Numbers of Nearest Neighbors. *IEEE Transactions on Neural Networks and Learning Systems*, 29(5), 1774-1785.

https://www.ots.ca.gov/media-and-research/collision-rankings-results/?wpv-wpcf-year=2 016&wpv-wpcf-city county=Los+Angeles&wpv filter submit=Submit