

# Design and Performance Analysis of a New STBC-MIMO LoRa System

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**Abstract**—LoRa is a modulation technology for low power wide area networks (LPWAN) with enormous potential in 5G era. However, the performance of LoRa system deteriorates seriously in fading-channel environments. To tackle this problem, in this paper we introduce multiple-input-multiple-output (MIMO) configuration employing space-time block coding (STBC) schemes into the LoRa system to formulate an STBC-MIMO LoRa system. Then, we investigate the theoretical performance of the proposed system over Rayleigh fading channels. To this end, we derive the distribution of the decision metric for the demodulator in the proposed system. Based on the above distribution, we propose a closed-form approximate BER expression of the proposed system when perfect and imperfect channel state information (CSI) are considered. Furthermore, we analyze the diversity order and the throughput of the proposed system. The results of the diversity analysis demonstrate that the diversity order of the system in the imperfect CSI scenario with fixed channel estimate error variance is zero. However, in the imperfect CSI scenario with a decreasing channel estimate error variance and the perfect CSI scenario, the system can achieve full diversity. In addition, the results of the throughput analysis show that the throughput of the proposed system is little affected by CSI conditions. Simulation results verify the accuracy of the theoretical analysis and the excellent performance of the proposed system. Due to such superiority, the proposed STBC-MIMO LoRa system can be considered as a good scheme for LPWAN.

**Index Terms**—Internet of Things (IoT), LoRa, bit error rate (BER), space-time block coding (STBC), multiple-input-multiple-output (MIMO), diversity order, Rayleigh fading channel.

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## I. INTRODUCTION

WITH the continuous update and improvement of Internet of things (IoT) and 5G technologies, massive connectivity has become one of the most important backbones of current world development. By providing real-time information, analysis and decision-making, the IoT in the 5G era is greatly changing the previous business models and lifestyles of people, such as driverless cars, unmanned aerial vehicle, smart appliances, and automated factories, thereby bringing unlimited possibilities for the future development of society. The widely promoted low power wide area network (LPWAN) plays an important role in 5G networks in recent years [1], because it can complement traditional cellular and short-range wireless technologies to address the different requirements of IoT applications. It is estimated that in 2022, the number of compatible nodes for LPWAN will reach 350 million [2].

For LPWAN, several communication technologies have been proposed, such as NB-IoT [3], Sigfox [4], and LoRa [5], [6]. Compared with NB-IoT- and Sigfox-based LPWAN, LoRa-based LPWAN has some unique advantages such as being highly open and flexible. Furthermore, LoRa-based LPWAN can be deployed in a private network and the operating cost of this LPWAN is low. As a modulation scheme of LPWAN, LoRa has gained considerable commercial traction and its specifications are maintained by the LoRa Alliance.<sup>1</sup> LoRa is a low-power, low-speed, and long-range modulation based on chirp spread-spectrum (CSS) technology [7]. In the LoRa modulation, cyclic shifts of chirp signal with linearly increased frequency form a multidimensional space for LoRa symbols, and the signals of different LoRa symbols are orthogonal to each other [8]. The coverage of LoRa is determined by the spreading factor. Increasing the spreading factor can provide wider coverage but reduce the data rate [9].

With the expansion of the market share occupied by LoRa in LPWAN, the number of countries deploying LoRa-based solutions has grown rapidly, which has reached 142 [6]. Accordingly, LoRa has also attracted more and more attention from academia. To explore various performance indicators of the LoRa modulation, researchers have carried out a lot of experimental-based works in the real world. In [10]–[13], the coverage capability of LoRa has been studied. In different scenarios, the coverage of LoRa ranges from 100m to 30km. In [12], the coverage of LoRa in an outdoor scenario has been evaluated by deploying a LoRa base station on a mountain.

<sup>1</sup><https://lora-alliance.org>

The results of the study indicate that the LoRa base station at an altitude of 470m can cover an area of 1380 square kilometers. In [13], it has been observed that the available communication distances of LoRa are 15km in the ground environment and 30km in the water environment.

After some pioneering work based on experiments, research on LoRa networks has attracted growing interest. With the increasing density of IoT applications, some work has considered the scalability and capacity of LoRa. In [14], mathematical tools have been utilized to simulate the uplink coverage of the single gateway LoRa network and it reveals the unique physical layer characteristics of the LoRa network. In [15], scalability performance has been conducted on a LoRa network with multiple gateways, and the impact of confirmed and unconfirmed messages on the traffic of a large-scale LoRa network has been analyzed. In addition, theoretical LoRa capacity has been explored in [16]–[18], where ALOHA network model is utilized to characterize LoRa-based LPWAN. In [19], a more practical model considering capture effect has been adopted to analyze LoRa capacity. Moreover, some recent research works have been studied to design multi-hop and multi-relay schemes for improving reliability of LoRa networks, e.g., concurrent transmission multi-hop LoRa network [20], multi-hop LoRa network with tree-based spreading factor clustering algorithm [21], and cooperative LoRa networks [22], [23].

While the LoRa physical layer is protected by patent [24], the study on such a modulation has become more active recently due to the implementation of reverse engineering [25], [26]. A rigorous mathematical description of the LoRa modulation and demodulation process has been developed in [8], and subsequently the waveform and spectral characteristics of the LoRa modulation have been investigated in [27]. In addition, bit-error-rate (BER) performance analysis of the LoRa modulation has been performed in [28], [29]. The analytical results show that the poor performance of the LoRa system might not sustain long-range communication in the fading environment. For this reason, some improved modulation schemes based on the physical layer of LoRa have been proposed, such as phase-shift-keying (PSK) LoRa [30], interleaved chirp spreading LoRa [31], and dual orthogonal LoRa [32]. All of these schemes aim at enhancing the capacity of the LoRa network.

Multiple-input-multiple-output (MIMO) technology is a desirable solution to improve the reliability of wireless communication systems [33]. In particular, by employing space-time block coding (STBC), an MIMO system can be easily realized to achieve considerable transmit and receive diversity over wireless channels. The STBC for two transmit antennas has been first proposed by Alamouti [34], and has subsequently been generalized to the scenario of more than two transmit antennas [35], [36]. On the basis of these schemes, a variety of the enhanced STBCs have been conceived for different application scenarios [37]–[39]. Thanks to the appealing advantages, MIMO technology has been introduced into spread-spectrum communication systems [40]–[43]. More recently, researchers have endeavored to apply such technology to LoRa systems. A LoRa-aided binary PSK MIMO system has been presented in [44]. However, the LoRa

signal in this system is only utilized to spread the spectrum of the BPSK baseband signal rather than carrying information, which leads to severe data-rate loss. In [45], a system offering joint localization and range extensions for LPWANs has been proposed. In such a system, MIMO technique is utilized in LoRa end devices and LoRa gateways to achieve a higher signal-to-noise ratio (SNR) with limited additional cost. The experimental results of this system can be found in [46].

With the above motivation, we propose a STBC-MIMO scheme with the LoRa modulation (i.e., STBC-MIMO LoRa system) in this paper. Taking into account the low-complexity requirements for the LoRa system, the Alamouti code in [34] and the STBC in [35], [36] are adopted for designing the proposed STBC-MIMO LoRa system. The contributions of this paper are summarized as follows:

- 1) An STBC-MIMO LoRa system with  $M$  transmit antennas and  $N$  receive antennas is put forward. The proposed system can greatly improve BER performance, thereby enhancing the reliability of LoRa networks in fading-channel environments.
- 2) The theoretical BER performance of the proposed system is carefully analyzed over Rayleigh fading channels. Based on the principle of the STBC-MIMO scheme, the theoretical model of the proposed system is established, then the distribution of the decision metric for the demodulator of the proposed system is derived. According to the above distribution, the closed-form approximate BER expression of the proposed system is presented for both perfect and imperfect channel state information (CSI). In particular, two common channel estimation error models (CEEMs) are considered in the analysis.
- 3) The asymptotic BER performance is investigated to analyze the diversity order of the proposed system. The results indicate that for the fixed channel estimation error variance, the system reaches zero diversity order, while for the perfect CSI and channel estimation error variance being a decreasing function of average SNR, the system can achieve full diversity  $d = MN$ . In addition, the throughput of the proposed system is further analyzed.
- 4) Simulation results not only verify the accuracy of the approximate BER expressions and diversity order analysis of the proposed STBC-MIMO LoRa system, but also demonstrate the superior BER performance. Furthermore, we present some design insight for the proposed STBC-MIMO LoRa system.

The remainder of the paper is organized as follows. In Section II, we provide the detailed descriptions of the LoRa modulation/demodulation process and the proposed STBC-MIMO LoRa system. In Section III, we present the closed-form approximate BER expressions of the proposed system for perfect and imperfect CSIs. We also analyze the diversity order and the throughput of the proposed system in the same Section. In Section IV, we present various simulation results with some discussions. Finally, Section V concludes the paper.

## II. SYSTEM MODEL

### A. LoRa Modulation

LoRa is a frequency shift CSS based modulation scheme. In the LoRa modulation, the frequency of the baseband signal varies linearly in a symbol duration and the bandwidth of the LoRa signal is  $B_w$ . There are  $2^{SF}$  chips in each LoRa symbol, where  $SF \in \{7, 8, \dots, 12\}$  is the spreading factor of LoRa [18], [28]. For a LoRa symbol  $x_o$ , it can carry  $SF$  bits, and assuming that the  $o^{th}$  transmitted symbol is  $s_o = p \in \{0, 1, \dots, 2^{SF} - 1\}$ . The frequency of  $x_o$  varies linearly from the starting frequency  $f_s = \frac{B_w \cdot p}{2^{SF}}$  to  $B_w$  and then folds to 0, in the remaining symbol duration, the frequency continues to change linearly from 0 to  $f_s$  [18]. Specifically, the frequency of each chip increases by  $\frac{B_w}{2^{SF}}$ . Therefore, the discrete-time baseband signal of the LoRa symbol  $x_o$  can be expressed as [18]

$$\begin{aligned} w_o(\kappa T_c) &= \sqrt{E_s} \bar{w}_p(\kappa T_c) \\ &= \sqrt{\frac{E_s}{2^{SF}}} \exp \left[ j2\pi \left( \frac{((p + \kappa) \bmod 2^{SF})^2}{2^{SF+1}} \right) \right], \end{aligned} \quad (1)$$

where  $T_c = \frac{1}{B_w}$  is the sample interval,  $\kappa$  denotes the index of the sample at time  $\kappa T_c$ ,  $E_s$  is the symbol energy, and  $\bar{w}_p(\kappa T_c)$  is the basis function of  $w_o(\kappa T_c)$ . As seen from Eq. (1), the LoRa signal transmitting the symbol  $p$  can be considered as a cyclic shift of  $pT_c$  for the basis CSS signal [18], [28].<sup>2</sup> Since chirp signals with different offsets are mutually orthogonal, for the LoRa signal of the symbol  $s_o$ , when it correlates with  $2^{SF}$  possible LoRa signals, it has the following properties [28]

$$\Lambda_i = \sum_{\kappa=0}^{2^{SF}-1} w_o(\kappa T_c) \cdot \bar{w}_i^*(\kappa T_c) = \begin{cases} \sqrt{E_s}, & i = p \\ 0, & i \neq p \end{cases}, \quad (2)$$

where  $0 \leq i \leq 2^{SF} - 1$  and  $*$  is the complex conjugate operation. The demodulation of the LoRa signal can be performed based on the above properties. For a received signal  $r_o(\kappa T_c)$  of the LoRa symbol  $x_o$  after transmission over a frequency-flat and time-invariant channel, the output of the correlator in the LoRa demodulator is written as [28]

$$\begin{aligned} \dot{\Lambda}_i &= \sum_{\kappa=0}^{2^{SF}-1} r_o(\kappa T_c) \cdot \bar{w}_i^*(\kappa T_c) \\ &= \sum_{\kappa=0}^{2^{SF}-1} \left( \sqrt{h_c} w_o(\kappa T_c) + w_n(\kappa T_c) \right) \cdot \bar{w}_i^*(\kappa T_c) \\ &= \begin{cases} \sqrt{h_c E_s} + w_{n,i}, & i = p \\ w_{n,i}, & i \neq p \end{cases}, \end{aligned} \quad (3)$$

where  $\sqrt{h_c}$  is the magnitude of fading channel coefficient [28], [30],  $w_n(\kappa T_c)$  is the complex additive white Gaussian noise (AWGN), and  $w_{n,i}$  is the corresponding complex Gaussian noise process [31]. Hence, the symbol  $s_o$  can be estimated as

$$\hat{s}_o = \arg \max_{i=0, \dots, 2^{SF}-1} \left( |\dot{\Lambda}_i| \right), \quad (4)$$

where  $|\cdot|$  denotes absolute operation. In addition, another equivalent low complexity method can also be utilized for

<sup>2</sup>The basic CSS signal can also be called as the *upchirp* signal, and its frequency varies linearly from 0 to  $B_w$  in a symbol duration.

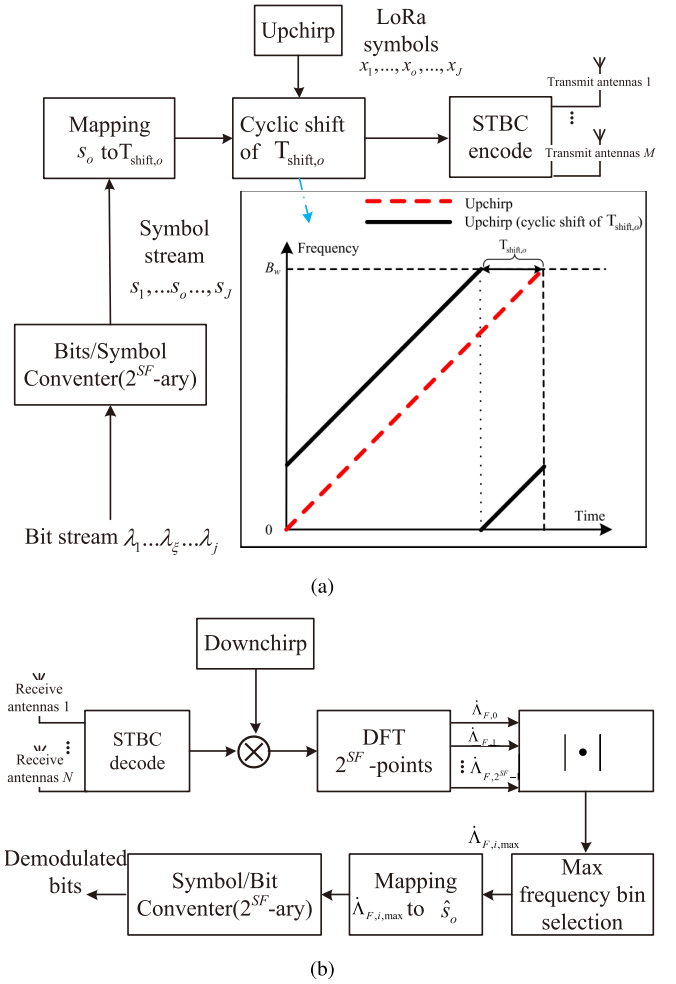


Fig. 1. Illustration of one possible realization of (a) transmitter and (b) receiver for the proposed STBC-MIMO LoRa system.

demodulation. First, the received signal is multiplied with downchirp  $\bar{w}_{down}(\kappa T_c)$  (this step is called a *dechirping*) [18], where  $\bar{w}_{down}(\kappa T_c)$  can be expressed as

$$\bar{w}_{down}(\kappa T_c) = \sqrt{\frac{1}{2^{SF}}} \exp \left( -j2\pi \frac{\kappa^2}{2^{SF+1}} \right). \quad (5)$$

Afterwards, the  $2^{SF}$  - point discrete Fourier transform (DFT) is performed on the dechirped signal, thus one can obtain as

$$\dot{\Lambda}_F = \text{DFT}(\mathbf{r}_o \odot \bar{\mathbf{w}}_{down}), \quad (6)$$

where  $\dot{\Lambda}_F = [\dot{\Lambda}_{F,0}, \dots, \dot{\Lambda}_{F,i}, \dots, \dot{\Lambda}_{F,2^{SF}-1}]$ ,  $\mathbf{r}_o = [r_o(0), r_o(T_c), \dots, r_o((2^{SF}-1)T_c)]$ ,  $\bar{\mathbf{w}}_{down} = [\bar{w}_{down}(0), \bar{w}_{down}(T_c), \dots, \bar{w}_{down}((2^{SF}-1)T_c)]$ , and  $\odot$  is the Hadamard product operator [47]. Next, the LoRa symbol is estimated by selecting the index of the frequency bin with the maximum magnitude, given by

$$\hat{s}_o = \arg \max_{i=0, \dots, 2^{SF}-1} \left( |\dot{\Lambda}_{F,i}| \right). \quad (7)$$

### B. The Proposed STBC-MIMO LoRa System

In this paper, we consider a wireless MIMO system with  $M$  ( $M \geq 2$ ) transmit antennas and  $N$  receive antennas that operates over a flat and quasi-static Rayleigh fading



channel,<sup>3</sup> therefore the path gains remain constant in a frame of  $J$  symbols and varies from a frame to another [50], [51]. We represent the MIMO channel as an  $M \times N$  matrix,  $\mathbf{H} = \{h_{m,n}\}$ , where  $h_{m,n}$  denotes the complex channel gain from the  $m^{\text{th}}$  transmit antenna to the  $n^{\text{th}}$  receive antenna.  $h_{m,n}$  are independent random variables that follow complex Gaussian distribution with zero mean and variance 0.5 per dimension. Fig. 1 illustrates one possible realization on the transmitter and receiver of the proposed STBC-MIMO LoRa system. In order to be compatible with the LoRa MAC protocol [52], the proposed STBC-MIMO LoRa system utilizes the preamble in the LoRa packet for channel estimation. Here we take the STBC-MIMO LoRa system with two transmitting antennas and two receiving antennas as an example to introduce. It is worth noting that the channel estimator is in the STBC decoder structure. The transmitter first sends  $L_p$  preambles through the transmit antenna 1, and the receiver obtains  $\hat{h}_{1,1}$  and  $\hat{h}_{1,2}$  by the channel estimator. Then, the transmitter sends  $L_p$  preambles through the transmit antenna 2, and the receiver obtains  $\hat{h}_{2,1}$  and  $\hat{h}_{2,2}$  by the channel estimator.

A complex orthogonal STBC transmission matrix  $\mathbf{G}$  is represented by a  $U \times M$  transmission matrix, where the entries are linear combinations of transmitted symbols  $g_1, g_2, \dots, g_J$  and their conjugates. Moreover, matrix  $\mathbf{G}$  satisfies complex orthogonality  $\mathbf{G}^H \mathbf{G} = u_{\text{cons}} (|g_1|^2 + \dots + |g_J|^2) \mathbf{I}_M$  [36], [53], where  $\mathbf{I}_M$  is an  $M \times M$  identity matrix and  $u_{\text{cons}}$  is a constant that depends on the STBC transmission matrix [54]. Matrix  $\mathbf{G}$  is utilized to encode  $J$  ( $J \geq 2$ ) input symbols into an  $M$ -dimensional vector sequence of  $U$  time slots (i.e., to control the symbol transmission of  $M$  transmitting antennas in each slot). Consequently, the transmission rate of STBC is  $r = J/U$ .

In this paper, the channel estimation matrix at the receiver is modeled as [55]–[57]

$$\hat{\mathbf{H}} = \mathbf{H} + \mathbf{E}_h, \quad (8)$$

where  $\mathbf{E}_h = \{e_{m,n}\}$  is an  $M \times N$  error matrix independent of  $\mathbf{H}$ ,  $e_{m,n}$  are complex Gaussian independent random variables with zero mean and variance  $\sigma_e^2$ , where  $\sigma_e^2$  reflects the accuracy of the channel estimation. Accordingly, the variance of the estimated channel gain is  $\sigma_{\hat{h}}^2 = \sigma_h^2 + \sigma_e^2$ . In particular, when  $\sigma_e^2 = 0$ , it can be considered that perfect channel estimation is performed at the receiver (i.e., the receiver knows perfect CSI). In this paper, two types of channel estimation error variance are considered: one is that  $\sigma_e^2$  is fixed and independent of the average SNR, and the other is that  $\sigma_e^2$  is a decreasing function of the average SNR. These two types of error variance correspond to CEEMs I and II, respectively. For the proposed STBC-MIMO LoRa system, when the channel estimation error occurs at the receiver, it causes inter-antenna interference (IAI). Here, we take the STBC  $\mathbf{G}_2$  in [58] as an example and apply it to an STBC-MIMO LoRa system

<sup>3</sup>The proposed system can be applied for uplink and downlink transmission. Generally, in a MIMO IoT network, the base station is equipped with multiple antennas, while the IoT nodes are equipped with fewer or even one antenna [45], [48], [49]. For general analysis, a wireless system with  $M$  transmit antennas and  $N$  receive antennas is considered in this paper.

TABLE I

THE ENCODING AND TRANSMISSION SEQUENCE FOR THE PROPOSED STBC-MIMO LoRa SYSTEM WITH TWO TRANSMIT ANTENNAS

	Transmit antenna 1	Transmit antenna 2
Time $t_s$	$x_1$	$x_2$
Time $t_s + 2^{SF}T_c$	$-x_2^*$	$x_1^*$

TABLE II

THE NOTATION FOR THE RECEIVED SIGNAL AT THE TWO RECEIVE ANTENNAS

	Receive antenna 1	Receive antenna 2
Time $t_s$	$r_1$	$r_3$
Time $t_s + 2^{SF}T_c$	$r_2$	$r_4$

with two receive antennas to illustrate the encoding/decoding process in the proposed system. Code  $\mathbf{G}_2$  is given by [34]

$$\mathbf{G}_2 = \begin{pmatrix} g_1 & g_2 \\ -g_2^* & g_1^* \end{pmatrix}. \quad (9)$$

Utilizing  $\mathbf{G}_2$ , we can encode the LoRa symbol in space and time. Taking the encoding of the first two LoRa symbols  $x_1$  (the symbol transmitted by  $x_1$  is  $s_1 = p$ ) and  $x_2$  (the symbol transmitted by  $x_2$  is  $s_2 \neq p$ ) in the sequence as an example, this process is shown in Table I. Correspondingly, the notation for the received signal at the two receive antennas is defined in Table II, where

$$\begin{aligned} r_1 &= h_{1,1}x_1 + h_{2,1}x_2 + n_1 \\ r_2 &= -h_{1,1}x_2^* + h_{2,1}x_1^* + n_2 \\ r_3 &= h_{1,2}x_1 + h_{2,2}x_2 + n_3 \\ r_4 &= -h_{1,2}x_2^* + h_{2,2}x_1^* + n_4, \end{aligned} \quad (10)$$

and  $n_1, n_2, n_3$ , and  $n_4$  are the complex AWGN with variance  $N_0/2$  per dimension. Next, the maximum likelihood decoding of the STBC can be achieved by linear processing [58] in the STBC decoder at the receiver, thereby recovering the desired LoRa symbols. Without loss of generality, we take  $x_1$  as an example for illustration and following analysis. For the LoRa symbol  $x_1$ , the other LoRa symbol  $x_2$  (i.e., the transmitted symbol carried by  $x_2$  is not equal to  $p$ ) can be regarded as interference. After STBC decoding, the recovered LoRa symbol  $\tilde{x}_1$  can be expressed as

$$\begin{aligned} \tilde{x}_1 &= \hat{h}_{1,1}^* r_1 + \hat{h}_{2,1}^* r_2^* + \hat{h}_{1,2}^* r_3 + \hat{h}_{2,2}^* r_4^* \\ &= \underbrace{\left( |\hat{h}_{1,1}|^2 + |\hat{h}_{2,1}|^2 + |\hat{h}_{1,2}|^2 + |\hat{h}_{2,2}|^2 \right)}_{S_\alpha} x_1 \\ &\quad - \underbrace{\left( \hat{h}_{1,1}^* e_{1,1} - \hat{h}_{2,1}^* e_{2,1} - \hat{h}_{1,2}^* e_{1,2} - \hat{h}_{2,2}^* e_{2,2} \right)}_{S_\beta} x_2 \\ &\quad + \underbrace{\left( -\hat{h}_{1,1}^* e_{2,1} + \hat{h}_{2,1}^* e_{1,1}^* - \hat{h}_{1,2}^* e_{2,2} + \hat{h}_{2,2}^* e_{1,2}^* \right)}_{S_\beta} x_2 \\ &\quad + \underbrace{\left( \hat{h}_{1,1}^* n_1 + \hat{h}_{2,1}^* n_2^* + \hat{h}_{1,2}^* n_3 + \hat{h}_{2,2}^* n_4^* \right)}_{S_\tau}, \end{aligned} \quad (11)$$

where terms  $S_\alpha$ ,  $S_\beta$ , and  $S_\tau$  are the desired signal, IAI and noise, respectively.<sup>4</sup> Accordingly, referring to Eq. (3) and Eq. (4), the decision metric of  $\tilde{x}_1$  can be expressed as

$$Z_{\tilde{x}_1, i} = \left| \sum_{\kappa=0}^{2^{SF}-1} w_{\tilde{x}_1}(\kappa T_c) \cdot \tilde{w}_i^*(\kappa T_c) \right|$$

$$= \begin{cases} \sqrt{\frac{E_s}{2}} \left( \left| \hat{h}_{1,1} \right|^2 + \left| \hat{h}_{2,1} \right|^2 + \left| \hat{h}_{1,2} \right|^2 + \left| \hat{h}_{2,2} \right|^2 - \hat{h}_{1,1}^* e_{1,1} + \hat{h}_{2,1} e_{2,1}^* - \hat{h}_{1,2}^* e_{1,2} + \hat{h}_{2,2} e_{2,2}^* \right) + \hat{h}_{1,1}^* \phi_1 + \hat{h}_{2,1} \phi_2^* + \hat{h}_{1,2}^* \phi_3 + \hat{h}_{2,2} \phi_4^* \right|, & i = p \\ \sqrt{\frac{E_s}{2}} \left( -\hat{h}_{1,1}^* e_{2,1} + \hat{h}_{2,1} e_{1,1}^* - \hat{h}_{1,2}^* e_{2,2} + \hat{h}_{2,2} e_{1,2}^* \right) + \hat{h}_{1,1}^* \phi_1 + \hat{h}_{2,1} \phi_2^* + \hat{h}_{1,2}^* \phi_3 + \hat{h}_{2,2} \phi_4^* \right|, & i \neq p, i = s_2 \\ \left| \hat{h}_{1,1}^* \phi_1 + \hat{h}_{2,1} \phi_2^* + \hat{h}_{1,2}^* \phi_3 + \hat{h}_{2,2} \phi_4^* \right|, & i \neq p, i \neq s_2 \end{cases}, \quad (12)$$

where  $\phi_\varphi$  ( $\varphi = 1, 2, 3, 4$ ) is the complex Gaussian noise process caused by  $n_\varphi$  and  $w_{\tilde{x}_1}(\kappa T_c)$  is the discrete-time baseband signal of  $\tilde{x}_1$ . Then, the symbol  $s_1$  is estimated by

$$\hat{s}_1 = \arg \max_{i=0, \dots, 2^{SF}-1} (Z_{\tilde{x}_1, i}). \quad (13)$$

More generally, the encoding and decoding algorithms for the STBC-MIMO LoRa system are summarized in Algorithm 1 and Algorithm 2, respectively.

### C. Complexity Analysis

Here, we analyze the complexity of the proposed STBC-MIMO LoRa system. The main computational complexity of the proposed system comes from the channel estimation, STBC decoding and LoRa demodulation.<sup>5</sup> Due to the low-power consumption and low-complexity requirements of LoRa devices, the least-square method [60] is considered in the channel estimator of the proposed system. The complexities of channel estimation and STBC decoding of the proposed STBC-MIMO LoRa system are  $\mathcal{O}(MNL_p\Psi)$  and  $\mathcal{O}(JUN\Psi)$ , respectively. Where  $\Psi = 2^{SF}$ . The computational complexity of LoRa demodulation consists of four parts, i.e., dechirping  $\mathcal{O}(J\Psi)$ ,  $J$  times DFT  $\mathcal{O}(J\Psi^2)$ , performing absolute value operation on the result of DFT  $\mathcal{O}(J\Psi)$ , and argmax operation  $\mathcal{O}(J\Psi)$ . Therefore, the total computational complexity of the proposed STBC-MIMO LoRa system is required at an order of  $\mathcal{O}(\Psi^2)$ . Notably, the computational complexity of the single-input single-output (SISO) LoRa

### Algorithm 1 Encoding algorithm for the STBC-MIMO LoRa system

#### Initialization:

- 1: Initialize the number of transmit antennas  $M$ , spreading factor  $SF$ ;
- 2: Input the transmitted bit streams  $\lambda_1, \dots, \lambda_J$ ;
- 3: Bit/symbol converter:  $\lambda_1, \dots, \lambda_J \rightarrow s_1, \dots, s_J$ .

#### LoRa modulation:

- 4: The transmitted symbols  $s_1, \dots, s_J \rightarrow$  LoRa symbols  $x_1, \dots, x_J$  (Utilizing Eq. (1)).

#### STBC-aided encoding:

- 5: Choose a  $\mathbf{G}_M$  for STBC;
- 6: Initialize an  $U \times (M \cdot 2^{SF})$  zero matrix  $\mathfrak{S}$ ;
- 7: By utilizing  $\mathbf{G}_M$ , obtain the matrix  $\mathfrak{S}$  with entries linear combinations of  $x_1, \dots, x_J$  and their conjugates;
- 8: **for**  $u = 1 : 1 : U$  **do**
- 9:   **for**  $\theta = 1 : 1 : M$  **do**
- 10:     In the time slot  $u$ , the signals in the  $u^{th}$  row,  $[(\theta - 1) \cdot 2^{SF} + 1]^{th}$  column to  $(\theta \cdot 2^{SF})^{th}$  column in  $\mathfrak{S}$  are transmitted through the  $\theta^{th}$  antenna.
- 11:   **end for**
- 12: **end for**

### Algorithm 2 Decoding algorithm for the STBC-MIMO LoRa system

#### Initialization:

- 1: Initialize the number of transmit antennas  $N$ , spreading factor  $SF$ , and the signal  $\mathfrak{R}_{u, n_t}$  received by the  $n_t^{th}$  ( $1 \leq n_t \leq N$ ) receive antenna in the  $u^{th}$  time slot;
- 2: Utilize the channel estimator to get the estimated channel gain  $\hat{\mathbf{H}}$ .

#### STBC-aided decoding

- 3: **for**  $N_{sym} = 1 : 1 : J$  **do**
- 4:    $\mathbf{z}_{sym, N_{sym}} = [0, \dots, 0]_{1 \times 2^{SF}}$ ;
- 5:    $\mathbf{z}_{N\_temp} = [0, \dots, 0]_{1 \times 2^{SF}}$ ;
- 6:   **for**  $n_t = 1 : 1 : N$  **do**
- 7:      $\mathbf{z}_{slot, N_{sym}} = [0, \dots, 0]_{1 \times 2^{SF}}$ ;
- 8:     **for**  $u = 1 : 1 : U$  **do**
- 9:       According to  $\mathbf{G}_M$ ,  $\mathfrak{R}_{u, n_t}$  is processed with  $\hat{\mathbf{H}}$  (linear processing or conjugate operation) to obtain  $\hat{\mathfrak{R}}_{u, n_t}$ ;
- 10:        $\mathbf{z}_{slot\_temp} = \mathbf{z}_{slot\_temp} + \hat{\mathfrak{R}}_{u, n_t}$ ;
- 11:     **end for**
- 12:      $\mathbf{z}_{N\_temp} = \mathbf{z}_{N\_temp} + \mathbf{z}_{slot\_temp}$ ;
- 13:   **end for**
- 14:    $\tilde{\mathbf{z}}_{sym, N_{sym}} = \mathbf{z}_{N\_temp}$ ;
- 15: **end for**

#### LoRa demodulation:

- 16:  $\tilde{\mathbf{z}}_{sym, 1}, \dots, \tilde{\mathbf{z}}_{sym, J} \rightarrow \hat{s}_1, \dots, \hat{s}_J$  (Utilizing Eqs. (6) and (7)).
- 17: Symbol/bit converter:  $\hat{s}_1, \dots, \hat{s}_J \rightarrow \hat{\lambda}_1, \dots, \hat{\lambda}_J$ .

<sup>4</sup>Unlike the conventional-modulation-based (e.g.,  $\mathcal{M}$ -PSK and  $\mathcal{M}$ -QAM-based) STBC-MIMO systems, the IAI can be regarded as noise [54], [59]. However, in the STBC-MIMO LoRa system, IAI is the signal of the undesired symbol.

<sup>5</sup>Since the STBC encoding of the LoRa symbols in the transmitter only needs to perform linear processing [36] on the LoRa symbols, the computational complexity in the transmitter is very low.

system to transmit  $J$  information bits is  $\mathcal{O}(J\Psi^2) + 3\mathcal{O}(J\Psi)$ , which has the same order of computational complexity as the STBC-MIMO LoRa system. For the hardware complexity, like other IoT devices with multiple antennas [45], [48], [49], each

transmit and receive antenna needs to be equipped with a radio frequency chain.

*Remark 1:* Similar to the LoRa system in [45], the proposed STBC-MIMO LoRa system also requires channel estimation. Nevertheless, the LoRa packet structure in the proposed system does not need to be adjusted, hence the commonly utilized LoRa MAC protocol [52] can still be applied. In the conventional LoRa system, the preamble symbols in the LoRa packet are utilized for synchronization, while in the proposed STBC-MIMO LoRa system, the preamble symbols are utilized not only for synchronization, but also for channel estimation. Moreover, due to the low-power consumption and low-complexity requirements of LoRa devices, the least-square estimator [60] is considered in the proposed system. Although the proposed STBC-MIMO LoRa system introduces additional but limited computational complexity and hardware complexity, it can be observed from the results in Sect. IV that the proposed STBC-MIMO LoRa system has superior BER performance compared to SISO LoRa in fading-channel environments.

### III. PERFORMANCE ANALYSIS

In this section, the average BER expression of the proposed STBC-MIMO LoRa system is derived, then we analyze the throughput of the proposed system. We denote  $f_{Ray}(y; \sigma_y)$  and  $f_{Ri}(y; m_y, \sigma_y)$  as the probability density functions (PDFs) of the Rayleigh and Rice distributions, respectively, and we denote the cumulative distribution function (CDF) of Rayleigh distribution by  $F_{Ray}(y; \sigma_y)$ , where  $m_y$  and  $\sigma_y$  are the scale and location parameters of the variable  $y$  [61]. One can generalize from Eq. (12) that the distribution of the decision metric of  $x_1$  for an STBC-MIMO LoRa system with  $M$  transmit antennas and  $N$  receive antennas

$$Z_{\hat{x}_1, i} \sim \begin{cases} f_{Ri} \left( \alpha; \|\hat{\mathbf{H}}\|_F^2 \sqrt{\frac{E_s}{r^2 M}}, \sqrt{\frac{\|\hat{\mathbf{H}}\|_F^2}{2} \left( \frac{\sigma_e^2 E_s}{r^2 M} + \frac{N_0}{r} \right)} \right), & i = p \\ f_{Ray} \left( \beta; \sqrt{\frac{\|\hat{\mathbf{H}}\|_F^2}{2} \left( \frac{\sigma_e^2 E_s}{r^2 M} + \frac{N_0}{r} \right)} \right), & i \neq p, \\ & i = s_2, \dots, s_J \\ f_{Ray} \left( \tau; \sqrt{\frac{\|\hat{\mathbf{H}}\|_F^2 N_0}{2r}} \right), & i \neq p, s_2, \dots, s_J \end{cases}, \quad (14)$$

where  $\|\hat{\mathbf{H}}\|_F^2 = \sum_{m=1}^M \sum_{n=1}^N |\hat{h}_{m,n}|^2$  is the square of the Frobenius norm of  $\{\hat{h}_{m,n}\}$ . For convenience, we denote  $\|\hat{\mathbf{H}}\|_F^2$  by  $X$ . For a Rayleigh fading channel,  $X$  follows a chi-square distribution with  $MN$  degrees of freedom. Thus, the average BER of the proposed system can be expressed as

$$\begin{aligned} P_b &= \frac{2^{SF-1}}{2^{SF}-1} \Pr \left[ \max_{i, i \neq p} (Z_{\hat{x}_1, i}) > Z_{\hat{x}_1, p} \right] \\ &= \frac{2^{SF-1}}{2^{SF}-1} \int_0^\infty \left[ 1 - \Pr \left[ Z_{\hat{x}_1, p|X} > \max_{i, i \neq p} (Z_{\hat{x}_1, i|X}) \right] \right] \\ &\quad \times f_X(X) dX \end{aligned}$$

$$\begin{aligned} &= \frac{2^{SF-1}}{2^{SF}-1} \int_0^\infty \int_0^\infty \left[ 1 - [F_{Ray}(\alpha|X; \sigma_\beta)]^{J-1} \right. \\ &\quad \times [F_{Ray}(\alpha|X; \sigma_\tau)]^{2^{SF}-J} \left. \times f_{Ri}(\alpha|X; m_\alpha, \sigma_\alpha) \right] \\ &\quad \times f_X(X) d\alpha dX, \end{aligned} \quad (15)$$

where  $f_X(X)$  is the PDF of  $X$ . To simplify Eq. (15), another equivalent form is utilized to represent  $P_b$  [18], [62], in which the error probability is expressed in terms of the noise-driven probability and the IAI-driven probability, i.e.,

$$P_b = \frac{2^{SF-1}}{2^{SF}-1} [P_{err}^N + (1 - P_{err}^N) \times P_{err}^{IAI}], \quad (16)$$

where

$$\begin{aligned} P_{err}^N &= \int_0^\infty \left[ 1 - \Pr \left[ Z_{\hat{x}_1, p|X} > \max_{i, i \neq p, s_2, \dots, s_J} (Z_{\hat{x}_1, i|X}) \right] \right] \\ &\quad \times f_X(X) dX \\ &= \int_0^\infty \int_0^\infty \left[ 1 - [F_{Ray}(\alpha|X; \sigma_\tau)]^{2^{SF}-J} \right] \\ &\quad \times f_{Ri}(\alpha; m_\alpha, \sigma_\alpha) \times f_X(X) d\alpha dX, \end{aligned} \quad (17)$$

$$\begin{aligned} P_{err}^{IAI} &= \int_0^\infty \left[ 1 - \Pr \left[ Z_{\hat{x}_1, p|X} > \max_{i, i \neq p, i = s_2, \dots, s_J} (Z_{\hat{x}_1, i|X}) \right] \right] \\ &\quad \times f_X(X) dX \\ &= \int_0^\infty \int_0^\infty \left[ 1 - [F_{Ray}(\alpha|X; \sigma_\beta)]^{J-1} \right] \\ &\quad \times f_{Ri}(\alpha; m_\alpha, \sigma_\alpha) \times f_X(X) dX d\alpha. \end{aligned} \quad (18)$$

In Eqs. (17) and (18), because  $f_{Ri}(\alpha|X; m_\alpha, \sigma_\alpha)$  in the integrand contains a modified Bessel function [63], the overflow and accuracy problems will be faced when the numerical calculation is performed. Considering that when the Rice factor  $K$  is large, the Rice distribution can be well approximated as a Gaussian distribution [61], thus the Rice factor  $K_\alpha$  of  $f_{Ri}(\alpha|X; m_\alpha, \sigma_\alpha)$  is further analyzed, which can be expressed as

$$K_\alpha = \frac{m_\alpha^2}{2\sigma_\alpha^2} = \frac{X \cdot T \cdot 2^{SF}}{(\sigma_e^2 \cdot T \cdot 2^{SF} + rM)}, \quad (19)$$

where  $T = E_s/(N_0 \cdot 2^{SF})$  is the SNR in the LoRa communication [28]. It can be observed from Eq. (19) that since  $X$  is a random variable,  $K_\alpha$  is also a random variable related to  $X$ . Fig. 2 shows the PDF of  $K_\alpha$  by Monte Carlo simulation under different parameters (e.g.,  $r$ ,  $M$ ,  $N$ ,  $SF$ ,  $T$ , and  $\sigma_e^2$ ), where  $\sigma_e^2 = 0$  and  $\sigma_e^2 \neq 0$  correspond to the perfect CSI and the imperfect CSI scenarios, respectively, where  $L_p$  denotes the number of the preamble symbol utilized for channel estimation. When  $\sigma_e^2$  is nonzero and fixed, it corresponds to CEEM I, while when  $\sigma_e^2 = 1/(1 + L_p T_{eff})$ , it corresponds to CEEM II [59], [64].<sup>6</sup> It can be seen that  $K_\alpha$  is basically distributed in the region of  $K_\alpha \geq 10$  dB in both perfect CSI and imperfect CSI scenarios. Hence, the Rice random variable  $\alpha$  approximately follows a Gaussian distribution  $\mathcal{N}(m_\alpha, \sigma_\alpha^2)$  [61]. However, in the imperfect CSI scenario with CEEM I, it can be observed from Figs. 2(c) and 2(d) that  $K_\alpha$  hardly increases with the increase of SNR in high SNR region. Therefore, considering that in presence of

<sup>6</sup> $T_{eff} = 2^{SF} \cdot T$  is the effective SNR for the target symbol [28].

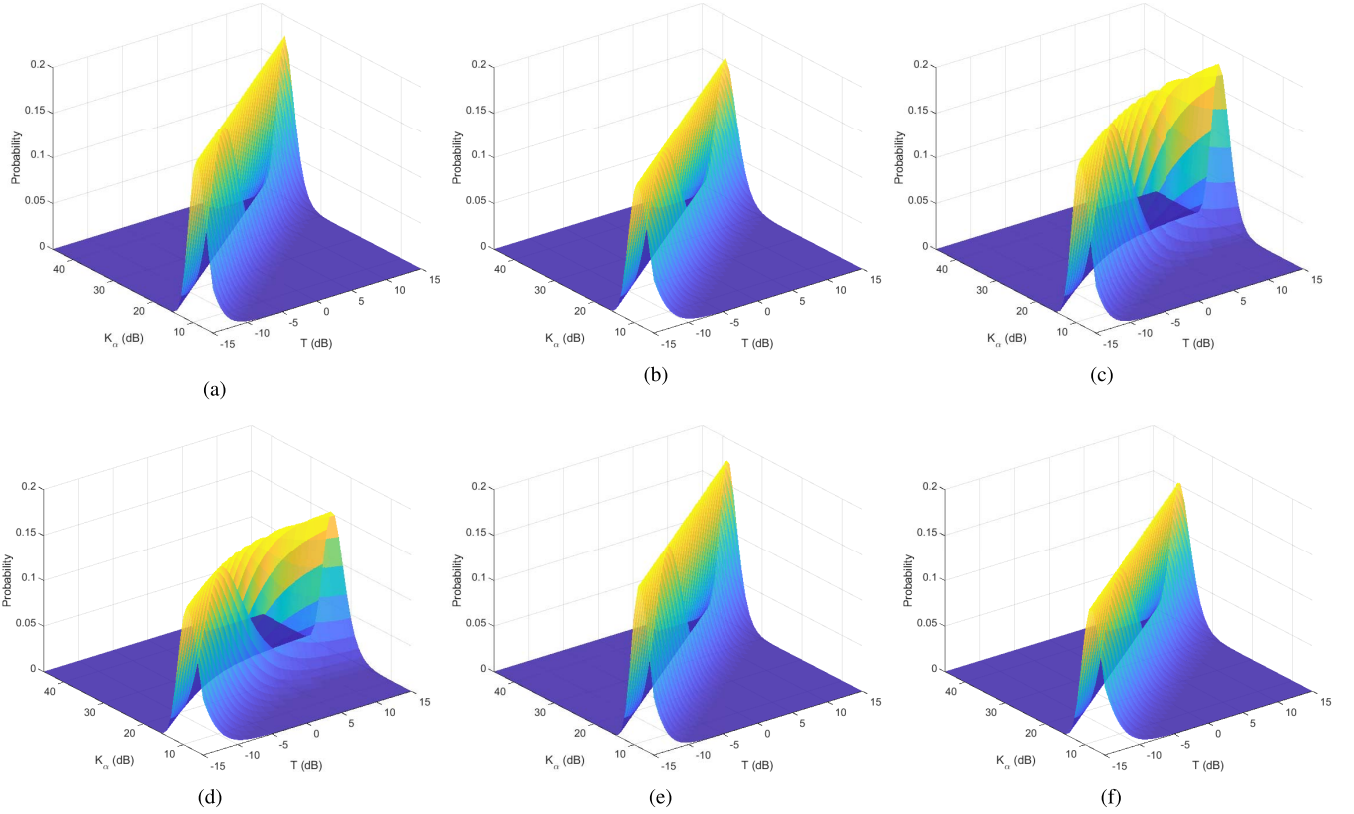


Fig. 2. The PDF of  $K_\alpha$  versus SNR with parameters  $\{r, M, N, SF, \sigma_e^2\} =$  (a)  $\{1, 2, 2, 7, 0\}$ , (b)  $\{0.5, 3, 1, 7, 0\}$ , (c)  $\{1, 2, 2, 7, 0.01\}$ , (d)  $\{0.5, 3, 1, 7, 0.01\}$ , (e)  $\{1, 2, 2, 7, 1/(1 + L_p T_{eff})\}$ , (f)  $\{0.5, 3, 1, 7, 1/(1 + L_p T_{eff})\}$ , where  $L_p$  is set to 4.

imperfect CSI,  $P_b$  in high SNR region is dominated by  $P_{err}^{IAI}$ , the Gaussian distribution will not be utilized to approximate the Rice distribution in the derivation of  $P_{err}^{IAI}$  in order to ensure the accuracy of the performance analysis in high SNR region (although this phenomenon does not occur under the CEEM II, for consistency of the derivation of  $P_{err}^{IAI}$  under the CEEM I and the CEEM II, the Gaussian distribution will not be utilized to approximate the Rice distribution in the entire derivation of  $P_{err}^{IAI}$ ).

In addition to the above numerical problems, since  $SF$  can be up to 12,  $[F_{Ray}(\alpha|X; \sigma_J)]^{2^{SF}-1}$  in Eq. (17) has a very high complexity. Here, let  $\tau_{\max} = \max_{i, i \neq p, s_2, \dots, s_J} (Z_{\tilde{x}_1, i})$ , and then refer to the procedure in [28] to approximate the distribution of variable  $\tau_{\max}$  by a Gaussian distribution  $\mathcal{N}(\mu_{\tau_{\max}}, \sigma_{\tau_{\max}}^2)$ . Specifically,  $\mu_{\tau_{\max}}$  and  $\sigma_{\tau_{\max}}^2$  are respectively given by

$$\mu_{\tau_{\max}} = \left[ X^2 \left( \frac{N_0^2 \cdot h_{2^{SF}-J}^2}{r^2} - \frac{N_0^2 \cdot \lambda_{2^{SF}-J}}{2r^2} \right) \right]^{\frac{1}{4}}, \quad (20)$$

$$\sigma_{\tau_{\max}}^2 = \frac{X^2}{r} \left( N_0 h_{2^{SF}-J} - \sqrt{N_0^2 h_{2^{SF}-J}^2 - \frac{N_0^2 \lambda_{2^{SF}-J}}{2}} \right), \quad (21)$$

where  $h_k = \sum_{q=1}^k \frac{1}{q}$  denotes the  $k^{th}$  harmonic number and  $\lambda_k = \sum_{q=1}^k \frac{1}{q^2}$ .

Based on the above approximation of the distribution of the random variables  $\alpha$  and  $\tau_{\max}$ ,  $P_{err}^N$  can be

approximated as

$$\begin{aligned} P_{err}^N &\approx \int_0^\infty Q \left( \frac{\mu_\alpha - \mu_{\tau_{\max}}}{\sqrt{\sigma_\alpha^2 + \sigma_{\tau_{\max}}^2}} \right) \cdot f_X(X) dX \\ &= \int_0^\infty Q \left( \left( \sqrt{\frac{X^2 E_s}{N_0 r M}} - \left( h_{2^{SF}-J}^2 - \frac{\lambda_{2^{SF}-J}}{2} \right)^{\frac{1}{4}} \right) \right. \\ &\quad \left. \div \sqrt{\left( \frac{\sigma_e^2 E_s}{2N_0 r M} + \frac{1}{2} \right) + h_{2^{SF}-J}^2 - \sqrt{h_{2^{SF}-J}^2 - \frac{\lambda_{2^{SF}-J}}{2}}} \right) \\ &\quad \times f_X(X) dX, \end{aligned} \quad (22)$$

where  $Q(\cdot)$  is the  $Q$ -function [65], [66]. Since  $SF \in \{7, \dots, 12\}$ ,  $h_{2^{SF}-J} \gg \frac{\lambda_{2^{SF}-J}}{2}$ . Hence, one can obtain

$$P_{err}^N \approx \int_0^\infty Q \left( \frac{A\sqrt{X} - B}{C} \right) \cdot DX^{MN-1} \cdot e^{-EX} dX, \quad (23)$$

where  $A = \sqrt{\frac{T \cdot 2^{SF}}{rM}}$ ,  $B = \sqrt{h_{2^{SF}-J}^2}$ ,  $C = \sqrt{\frac{\sigma_e^2 T \cdot 2^{SF}}{2rM} + \frac{1}{2}}$ ,  $D = \frac{1}{\Gamma(MN) \cdot (1 + \sigma_e^2)^{MN}}$ ,  $\Gamma(\cdot)$  denotes Gamma function [63], and  $E = -\frac{1}{1 + \sigma_e^2}$ . Next, further derivations of  $P_{err}^N$  and  $P_{err}^{IAI}$  are performed in the perfect CSI and the imperfect CSI scenarios.

#### A. Perfect CSI

Since there is no IAI in the perfect CSI scenario, the BER of the proposed STBC-MIMO LoRa system only depends on the



noise-driven error probability in this scenario. In order to evaluate Eq. (23), we need to approximate the  $Q$ -function. According to the relationship between the Gaussian  $Q$ -function and the complementary error function  $\text{erfc}(\cdot)$ , given by [67]

$$Q(x) = \frac{1}{2} \text{erfc}\left(\frac{x}{2}\right), \quad (24)$$

when  $\sigma_e^2 = 0$ , Eq. (23) can be rewritten as

$$P_{err}^N \approx \frac{1}{2} D \int_0^\infty \text{erfc}\left(A\sqrt{X} - B\right) \cdot X^{MN-1} e^{-X} dX. \quad (25)$$

According to [68], we can approximate  $\text{erfc}(y)$  quite well by utilizing

$$\text{erfc}(y) \approx \frac{1}{6} e^{-y^2} + \frac{1}{2} e^{-\frac{4}{3}y^2}. \quad (26)$$

Thus, one has

$$\begin{aligned} P_{err}^N &\approx P_{err,pcsi}^{N,Appr} = \frac{1}{2} D \int_0^\infty (I_1 + I_2) X^{MN-1} e^{-X} dX \\ &= \frac{1}{2} D \left( \underbrace{\int_0^\infty I_1 X^{MN-1} e^{-X} dX}_{R_1} + \underbrace{\int_0^\infty I_2 X^{MN-1} e^{-X} dX}_{R_2} \right), \end{aligned} \quad (27)$$

where

$$I_1 = \frac{1}{6} e^{-A^2 X + 2AB\sqrt{X} - B^2}, \quad (28)$$

$$I_2 = \frac{1}{2} e^{-\frac{4}{3}A^2 X + \frac{8}{3}AB\sqrt{X} - \frac{4}{3}B^2}. \quad (29)$$

Let  $t = \sqrt{X}$ ,  $R_1$  can be rewritten as

$$R_1 = \frac{1}{3} e^{-B^2} \int_0^\infty e^{[-(A^2+1)t^2 + 2ABt]} t^{2MN-1} dt. \quad (30)$$

Utilizing [63, Eq.(3.462.1)],  $R_1$  can be expressed as

$$\begin{aligned} R_1 &= \frac{1}{3(2A^2+2)^{MN}} \Gamma(2MN) e^{\left(\frac{A^2 B^2}{2A^2+2} - B^2\right)} \\ &\quad \times \Xi_{-2MN} \left( \frac{-2AB}{\sqrt{2A^2+2}} \right), \end{aligned} \quad (31)$$

where  $\Xi_{y_1}(y_2)$  is the parabolic cylinder function, defined as

$$\Xi_{y_1}(y_2) = 2^{\frac{y_2}{2}} e^{-\frac{y_2^2}{4}} \left[ \frac{\sqrt{\pi}}{\Gamma\left(\frac{1-y_1}{2}\right)} {}_1F_1\left(-\frac{y_1}{2}, \frac{1}{2}; \frac{y_2^2}{2}\right) - \frac{\sqrt{2\pi} y_2}{\Gamma\left(-\frac{y_1}{2}\right)} {}_1F_1\left(-\frac{1-y_1}{2}, \frac{3}{2}; \frac{y_2^2}{2}\right) \right], \quad (32)$$

and  ${}_1F_1(\cdot, \cdot; \cdot)$  is the confluent hypergeometric function [63]. Similarly,  $R_2$  can be expressed by

$$\begin{aligned} R_2 &= \left(\frac{8}{3}A^2 + 2\right)^{-MN} \Gamma(2MN) e^{\left(\frac{8A^2 B^2}{12A^2+9} - B^2\right)} \\ &\quad \times \Xi_{-2MN} \left( \frac{-8AB}{\sqrt{24A^2+18}} \right). \end{aligned} \quad (33)$$

Finally, combining Eqs. (27), (31), and (33), the closed-form approximate average BER expression of the proposed

STBC-MIMO LoRa system in the perfect scenario is obtained as

$$P_{b,pcsi} \approx \frac{2^{SF-1}}{2^{SF}-1} \cdot P_{err,pcsi}^{N,Appr}. \quad (34)$$

### B. Imperfect CSI

In the imperfect CSI scenario, the foregoing approximation method for the  $Q$ -function is not utilized in the derivation due to accuracy problem.<sup>7</sup> To obtain the closed-form expression for Eq. (23) in the imperfect scenario, the Gaussian-Hermite quadrature approach [69] is utilized to evaluate  $P_{err}^N$ , which can be expressed as

$$\int_{-\infty}^{+\infty} f(\xi) d\xi = \sum_{\vartheta=1}^{\rho} \omega_{\vartheta} f(\xi_{\vartheta}) e^{\xi_{\vartheta}^2} + O_{\rho}, \quad (35)$$

where  $\rho$  is the number of samples and it determines the accuracy of the approximation,  $\xi_{\vartheta}$  is the  $\vartheta^{th}$  zero point of the Hermite polynomial, and  $O_{\rho}$  is the remaining term (when  $\rho$  approaches infinity,  $O_{\rho}$  decreases to 0), and  $\omega_{\vartheta}$  is the  $\vartheta^{th}$  associated weight written as

$$\omega_{\vartheta} = \frac{2^{\rho} \rho! \sqrt{\pi}}{\rho^2 \Omega_{\rho-1}^2(\xi_{\vartheta})}. \quad (36)$$

To solve the integral in  $P_{err}^N$ , some mathematical processing needs to be performed first. Utilizing variable substitution  $\xi = \ln(X)$ ,  $P_{err}^N$  can be rewritten as

$$P_{err}^N = D \int_{-\infty}^{+\infty} Q\left(\frac{A\sqrt{e^{\xi}} - B}{C}\right) \cdot e^{(MN\xi + Ee^{\xi})} d\xi. \quad (37)$$

Therefore, by utilizing the Gaussian-Hermite approach given in Eq. (35),  $P_{err}^N$  in Eq. (23) can be approximated as

$$P_{err,icsi}^{N,Appr} \approx D \cdot \sum_{\vartheta=1}^{\rho} \omega_{\vartheta} Q\left(\frac{A\sqrt{e^{\xi_{\vartheta}}} - B}{C}\right) \cdot e^{(\xi_{\vartheta}^2 + MN\xi_{\vartheta} + Ee^{\xi_{\vartheta}})}. \quad (38)$$

Next, we focus on the derivation of the IAI-driven error probability as follow

$$\begin{aligned} P_{err}^{IAI} &= \int_0^\infty \int_0^\infty \left[ 1 - \left[ 1 - e^{\frac{-\alpha^2 + m_\alpha^2}{2\sigma_\alpha^2}} \right]^{J-1} \right] \\ &\quad \times \frac{\alpha}{\sigma_\alpha^2} I_0\left(\frac{m_\alpha \alpha}{\sigma_\alpha^2}\right) e^{\frac{-(\alpha^2 + m_\alpha^2)}{2\sigma_\alpha^2}} \\ &\quad \cdot DX^{(MN-1)} \times e^{EX} d\alpha dX \\ &= D \cdot \int_0^\infty \int_0^\infty \sum_{\ell=1}^{J-1} (-1)^{\ell+1} \binom{J-1}{\ell} \cdot e^{\frac{-\ell\alpha^2}{2\sigma_\alpha^2}} \\ &\quad \times \frac{\alpha}{\sigma_\alpha^2} I_0\left(\frac{m_\alpha \alpha}{\sigma_\alpha^2}\right) \cdot e^{\frac{-(\alpha^2 + m_\alpha^2)}{2\sigma_\alpha^2}} \\ &\quad \cdot X^{(MN-1)} \cdot e^{EX} d\alpha dX, \end{aligned} \quad (39)$$

where  $I_\eta(\cdot)$  is  $\eta^{th}$ -order modified Bessel function of the first kind [63] and  $\binom{R_1}{R_2} = \frac{R_1!}{R_2!(R_1-R_2)!}$ . Owing to  $\sigma_\alpha^2 = \sigma_\beta^2$ ,

<sup>7</sup>In the imperfect CSI scenario, the BER performance of the proposed system in low and middle SNR regions mainly depends on  $P_{err}^N$ . However, the exponential function based approximation method is usually not very accurate in low or middle SNR regions [59], [61].



Eq. (39) becomes

$$P_{err}^{IAI} = D \cdot \sum_{\ell=1}^{J-1} (-1)^\ell \binom{J-1}{\ell} \cdot e^{-\frac{\ell m_\alpha^2}{2(\ell+1)\sigma_\alpha^2}} \times \int_0^\infty \int_0^\infty \frac{\alpha}{\sigma_\alpha^2} I_0\left(\frac{m_\alpha \alpha}{\sigma_\alpha^2}\right) \cdot e^{-\frac{(\ell+1)\alpha^2 + \frac{m_\alpha^2}{(\ell+1)}}{2\sigma_\alpha^2}} \times X^{(MN-1)} \cdot e^{EX} d\alpha dX. \quad (40)$$

By introducing substitutions of variables  $m'_\alpha = \frac{m_\alpha}{\sqrt{\ell+1}}$  and  $\alpha' = \alpha\sqrt{\ell+1}$ , Eq. (40) can be rewritten as [29], [61]

$$P_{err}^{IAI} = D \cdot \sum_{\ell=1}^{J-1} (-1)^{\ell+1} \binom{J-1}{\ell} \cdot e^{-\frac{\ell m_\alpha^2}{2(\ell+1)\sigma_\alpha^2}} \times \frac{1}{\ell+1} \int_0^\infty \int_0^\infty \frac{\alpha'}{\sigma_\alpha^2} I_0\left(\frac{\alpha' m'_\alpha}{\sigma_\alpha^2}\right) \cdot e^{-\frac{\alpha'^2 + m'^2_\alpha}{2\sigma_\alpha^2}} \times X^{(MN-1)} \cdot e^{EX} d\alpha' dX \\ = D \cdot \sum_{\ell=1}^{J-1} \frac{(-1)^{\ell+1}}{\ell+1} \binom{J-1}{\ell} \times \int_0^\infty e^{-\left(\frac{\ell}{\ell+1} \cdot \frac{T \cdot 2^{SF}}{\sigma_e^2 \cdot T \cdot 2^{SF} + rM} - E\right)X} \cdot X^{(MN-1)} dX, \quad (41)$$

Then, utilizing [63, Eq.(3.351)], a closed-form expression of  $P_{err}^{IAI}$  is given by

$$P_{err,clo}^{IAI} = D \cdot \sum_{\ell=1}^{J-1} \frac{(-1)^{\ell+1}}{\ell+1} \binom{J-1}{\ell} (MN-1)! \times \left( \frac{\ell}{\ell+1} \cdot \frac{T \cdot 2^{SF}}{\sigma_e^2 \cdot T \cdot 2^{SF} + rM} - E \right)^{-MN}. \quad (42)$$

Finally, combining Eqs. (16), (38), and (42), the closed-form approximated average BER expression of the proposed STBC-MIMO LoRa system in the imperfect CSI scenario can be expressed as

$$P_{b,icsi} \approx \frac{2^{SF-1}}{2^{SF}-1} \left[ P_{err,icsi}^{N,Appr} + \left(1 - P_{err,icsi}^{N,Appr}\right) \times P_{err,clo}^{IAI} \right]. \quad (43)$$

### C. Analysis of Diversity Order

In this subsection, for gaining more insights from the BER analysis, we analyze the diversity order of the proposed STBC-MIMO LoRa system.<sup>8</sup> When  $T \rightarrow \infty$ ,  $R_1$  and  $R_2$  can be approximated as

$$R_1 \approx \frac{1}{3} \Gamma(2MN) e^{-\frac{B^2}{3}} \Xi_{-2MN} \left( -\frac{2B}{\sqrt{2}} \right) \times \left( \frac{2^{SF+1}}{rM} \right)^{-MN} \cdot T^{-MN} \\ \approx C_1 \cdot T^{-MN}, \quad (44)$$

<sup>8</sup>According to [70], the diversity order of the proposed STBC-MIMO LoRa system depends only on the behavior of the PDF  $f_X(X)$  around the origin  $X = 0$ . In the derivation of the approximate average BER expression, we utilize the exact  $f_X(X)$  rather than the approximation of  $f_X(X)$ . Hence, the diversity analysis based on the approximate BER expression can still characterize the behavior of  $f_X(X)$ .

$$R_2 \approx \Gamma(2MN) e^{-\frac{B^2}{3}} \Xi_{-2MN} \left( -\frac{4B}{\sqrt{6}} \right) \times \left( \frac{2^{SF+3}}{3rM} \right)^{-MN} \cdot T^{-MN} \\ \approx C_2 \cdot T^{-MN}. \quad (45)$$

Thus, combining Eqs. (27), (44), and (45),  $P_{b,pcsi}$  can be written as

$$P_{b,pcsi} \approx \frac{1}{2} D (C_1 + C_2) T^{-MN}. \quad (46)$$

From expression (46), we can conclude that the diversity order of the proposed system in the perfect CSI scenario is  $d = MN$ .

Next, we study the diversity order of the STBC-MIMO LoRa system in the imperfect CSI scenario. In this scenario,  $P_{b,icsi}$  can be expressed in terms of  $P_{err}^N$  and  $P_{err,clo}^{IAI}$ . For the CEEM I, when  $T$  approaches to infinity,  $P_{err,icsi}^N$  and  $P_{err,icsi}^{IAI}$  are approximately expressed respectively as

$$P_{err,icsi}^N \approx P_{err,icsi,s}^N = \frac{1}{\Gamma(MN) (1 + \sigma_e^2)^{MN}} \times \int_0^\infty Q\left(\frac{2}{\sigma_e^2} \cdot X\right) X^{MN-1} e^{-\frac{X}{1+\sigma_e^2}} dX, \quad (47) \\ P_{err,icsi}^{IAI} \approx P_{err,icsi,s}^{IAI} = D \cdot \sum_{\ell=1}^{J-1} \frac{(-1)^{\ell+1}}{\ell+1} \cdot \binom{J-1}{\ell} \cdot (MN-1)! \times \left( \frac{\ell}{\ell+1} \cdot \frac{1}{\sigma_e^2} - E \right)^{-MN}. \quad (48)$$

To solve the integral in Eq. (47), the following integral function can be employed [67, Eq. (5A.4a), (5A.4b)]

$$\int_0^\infty Q(\sqrt{\varpi x}) x^{\varphi-1} e^{-\frac{x}{\varsigma}} dx = \frac{1}{2} \varsigma^\varphi \Gamma(\varphi) \times \left( \frac{1-\mu}{2} \right)^\varphi \sum_{k=0}^{\varphi-1} \binom{\varphi-1+k}{k} \left( \frac{1+\mu}{2} \right)^k, \quad (49)$$

where  $\mu = \sqrt{(\varpi\varsigma)/(2+\varpi\varsigma)}$ . Then,  $P_{err,icsi,s}^N$  can be rewritten as

$$P_{err,icsi,s}^N = \frac{1}{2} \left[ \left( \frac{1-\mu_1}{2} \right)^{MN} \sum_{k=0}^{MN-1} \binom{MN-1+k}{k} \left( \frac{1+\mu_1}{2} \right)^k \right], \quad (50)$$

where  $\mu_1 = \sqrt{(1+\sigma_e^2)/(1+2\sigma_e^2)}$ . Since both  $P_{err,icsi,s}^N$  and  $P_{err,icsi,s}^{IAI}$  are constants, for CEEM I, the diversity order of the STBC-MIMO LoRa system is zero. Therefore, the error floor of BER appears in high SNR region, and one can get the expression of error floor, given by

$$P_{err,flo} = \frac{2^{SF-1}}{2^{SF}-1} \cdot \left[ P_{err,icsi,s}^N + \left(1 - P_{err,icsi,s}^N\right) \times P_{err,icsi,s}^{IAI} \right]. \quad (51)$$

According to Eq. (51), the error floor depends on parameters  $\{M, N, \sigma_e^2\}$ . For the CEEM II, as  $T$  trends to infinity,  $\sigma_e^2$

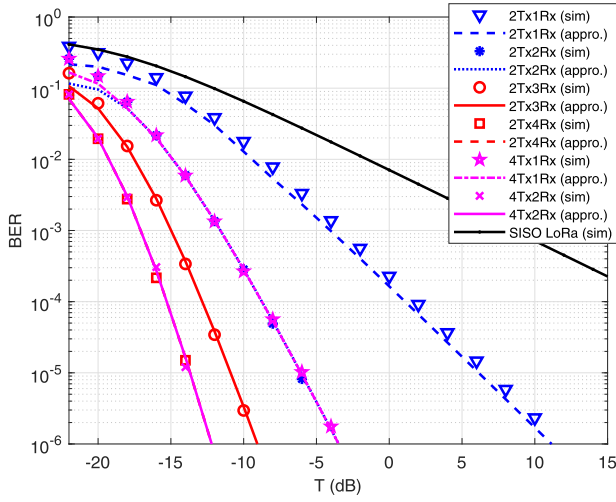


Fig. 3. Simulated and approximated BER results of the proposed STBC-MIMO LoRa system in the perfect CSI scenario. The simulated BER performance of the SISO LoRa system is shown with black solid line.

becomes zero. Hence, the diversity order of the proposed system for the CEEM II is the same as that in the perfect CSI scenario, which is verified by simulations.

#### D. Throughput

In a wireless communication system, the throughput is defined as the number of bits that correctly detected by the receiver, which can be expressed as [71]

$$\Upsilon = \frac{F_{pa} N_{bit} (1 - P_{pa})}{T_t}, \quad (52)$$

where  $F_{pa}$  is the number of the symbols in each packet,  $N_{bit} = SF$  is the number of bits in each symbol,  $T_t$  is the transmission time per packet, and  $P_{pa}$  is the packet error rate, which can be expressed as

$$P_{pa} = 1 - (1 - P_s)^{F_{pa}}, \quad (53)$$

where  $P_s = \frac{2^{SF}-1}{2^{SF}} P_{b,\Theta}$  ( $\Theta \in \{icsi, pcsi\}$ ) is the symbol error rate of the proposed system. Moreover,  $T_t = \frac{F_{pa} T_c \cdot 2^{SF}}{r}$  and  $T_t = F_{pa} T_c \cdot 2^{SF}$  for the proposed system and the SISO LoRa system, respectively. Without loss of generality, we set  $T_c = 1$ .

#### IV. SIMULATION RESULTS AND DISCUSSIONS

In this section, the performance of the proposed STBC-MIMO LoRa system with different space-time codes over a quasi-static flat Rayleigh fading channel is evaluated by simulations, and the simulation results are compared with the theoretical BER performance analysis results to verify the analysis in Sect. III. In addition,  $\mathcal{V}Tx$  and  $\mathcal{Y}Rx$  denote  $\mathcal{V}$  transmit antennas and  $\mathcal{Y}$  receive antennas, respectively. In the following simulations, STBCs  $\mathbf{G}_2$  and  $\mathbf{G}_4$  in [58] are employed for the system with 2Tx and 4Tx, respectively. Correspondingly, the code rates of 2Tx and 4Tx are 1 and 0.5, respectively. All numerical results and simulation results

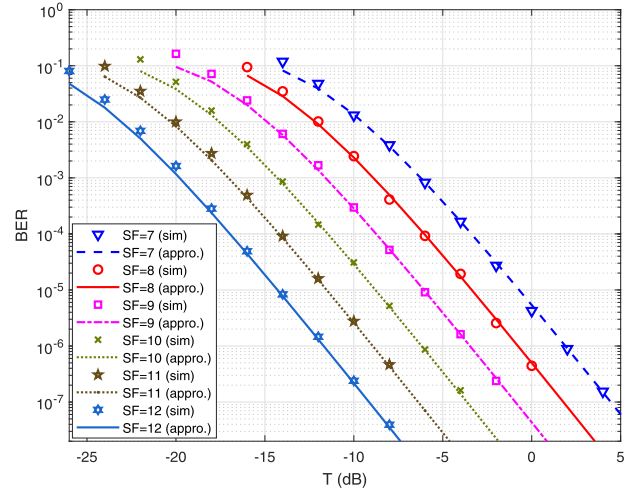


Fig. 4. Simulated and approximate BER results of the proposed STBC-MIMO LoRa system with 4Tx and 1Rx at different spreading factors in the perfect CSI scenario.

in this section are obtained utilizing MATLAB. A total of  $10^9$  Monte Carlo trials were performed to generate the BER curve.

In Fig. 3, we plot the approximate average BER curves and simulation results in the perfect CSI scenario, where  $SF$  is set to 9. From Fig. 3, the derived approximate BER results can well match with the simulated ones. Then, it can be seen from these figure that utilizing the STBC-MIMO scheme can significantly improve the diversity gain of the LoRa system. From the perspective of BER performance, taking the STBC-MIMO LoRa system with 2Tx1Rx as an instance, at a BER of  $10^{-4}$ , the proposed system has a 16-dB gain compared to the SISO system. In addition, it can be observed that the STBC-MIMO LoRa systems with 2Tx2Rx and 4Tx1Rx have the same BER performance in the perfect CSI scenario. However, the throughput performance of the STBC-MIMO LoRa systems with these two configurations is different, and the corresponding simulation results are shown later. Similarly, the relative performance between the STBC-MIMO LoRa systems with 2Tx4Rx and 4Tx2Rx, remain the same.

Fig. 4 presents the simulated and approximate BER results of the proposed STBC-MIMO LoRa system with 4Tx and 1Rx for all possible spreading factors  $SF \in \{7, \dots, 12\}$  in the perfect CSI scenario. It can be seen from the figure that the simulated results are consistent with the approximate ones. In addition, BER performance increases with the increase of  $SF$ . This law in the STBC-MIMO LoRa system is consistent with that in the SISO LoRa system [18].

Furthermore, two different channel estimation error models are utilized to evaluate the proposed STBC-MIMO LoRa system with imperfect CSI, i.e., CEEM I ( $\sigma_e^2$  is fixed) and CEEM II ( $\sigma_e^2 = 1/(1 + L_p T_{eff})$ ).  $L_p$  is set to 4. The simulated and approximate BER results of the proposed STBC-MIMO LoRa system in the imperfect CSI scenario with CEEM I are shown in Fig. 5. From this figure, it is observed that in the proposed system with the same number of the transmit and receive antenna, the error floor becomes higher as  $\sigma_e^2$  increases. For a fixed  $\sigma_e^2$ , increasing the number of the transmit or receive antenna can reduce the error floor.

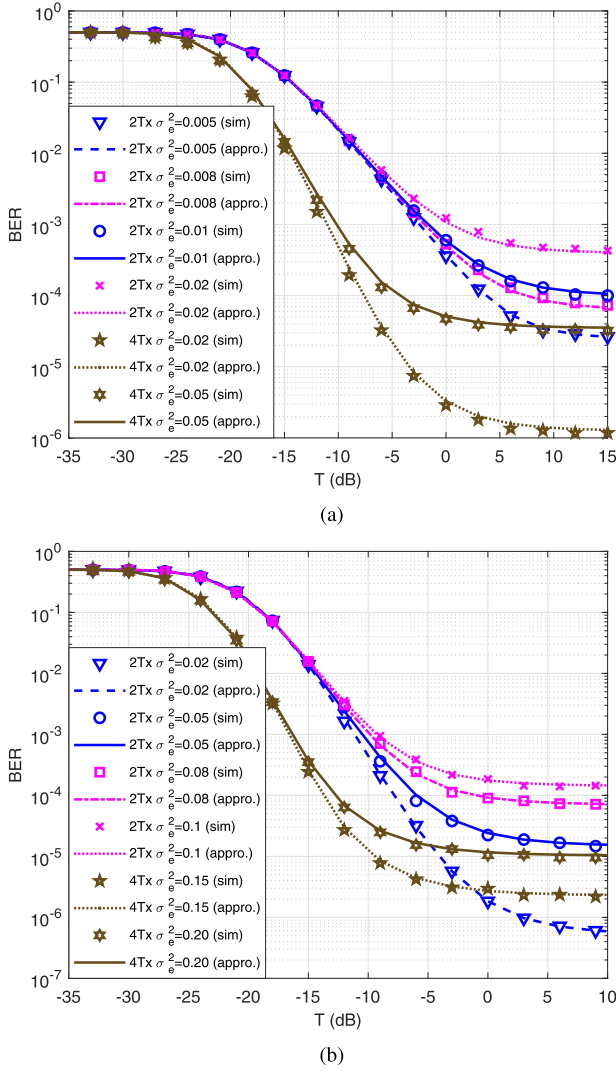


Fig. 5. Simulated and approximate BER results of the proposed STBC-MIMO LoRa system with (a) 1Rx and (b) 2Rx in the imperfect CSI scenario (CEEM I).

Fig. 6 presents the simulated and approximate BER results of the proposed STBC-MIMO LoRa system with 4Tx and 1Rx at different spreading factors in the imperfect CSI scenario with CEEM I, where  $SF \in \{7, \dots, 12\}$  and  $\sigma_e^2 = 0.05$ . As expected, for an STBC-MIMO LoRa systems with the same parameters  $\{M, N, \sigma_e^2\}$ , the change of  $SF$  does not affect the error floor of the BER. Then, Fig. 5 and Fig. 6 not only verify the accuracy of the derived approximate BER in the imperfect CSI scenario, but also show that the diversity order of the proposed STBC-MIMO LoRa system is zero under the CEEM I.

Fig. 7 shows the simulated and approximate BER results of the proposed STBC-MIMO LoRa system in the imperfect CSI scenario with CEEM II (i.e.,  $\sigma_e^2$  is a decreasing function of SNR). It can be seen from this figure that under the CEEM II, the diversity order of the proposed system is the same as that in the perfect CSI scenario, which verifies the conclusion obtained by the analysis of the diversity order in Sect. III-C. In high SNR region, BER performance of the proposed

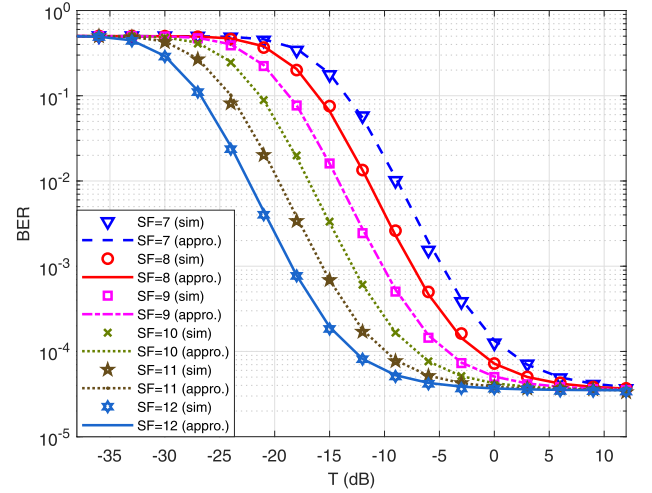


Fig. 6. Simulated and approximate BER results of the proposed STBC-MIMO LoRa system with 4Tx and 1Rx in the imperfect CSI scenario (CEEM I) at different spreading factors, where  $\sigma_e^2 = 0.05$ .

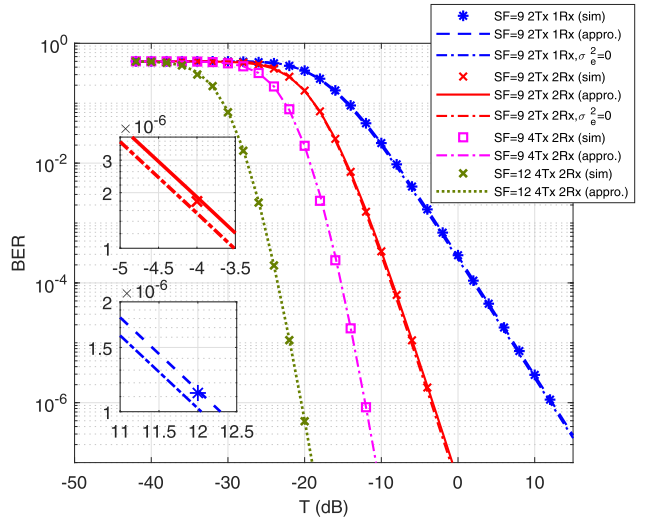


Fig. 7. Simulated and approximate BER results of the proposed STBC-MIMO LoRa system in the imperfect CSI scenario (CEEM II).

STBC-MIMO LoRa system under CEEM II is worse than that under perfect CSI, but the system performance in these two cases is very similar because  $\sigma_e^2$  is very small in high SNR region. Furthermore, the results also show that the derived approximate BER expression is valid for CEEM II.

Fig. 8 illustrates the throughput of the proposed STBC-MIMO LoRa system and the SISO LoRa system, where  $F_{pa}$  is set to 8. In the proposed system, the throughput depends on the  $SF$  and STBC utilized. Since the transmission rate of  $\mathbf{G}_2$  is twice that of  $\mathbf{G}_4$ , the throughput of the STBC-MIMO LoRa system with 2Tx2Rx is twice that of the STBC-MIMO LoRa system with 4Tx1Rx at the same  $SF$ . Compared to the SISO LoRa system, the STBC-MIMO LoRa system can achieve its maximum throughput at a lower SNR. Taking the STBC-MIMO LoRa system with 2Tx2Rx as an example, the SNR required by the system to achieve its maximum throughput is about 24 dB lower than that of the SISO LoRa

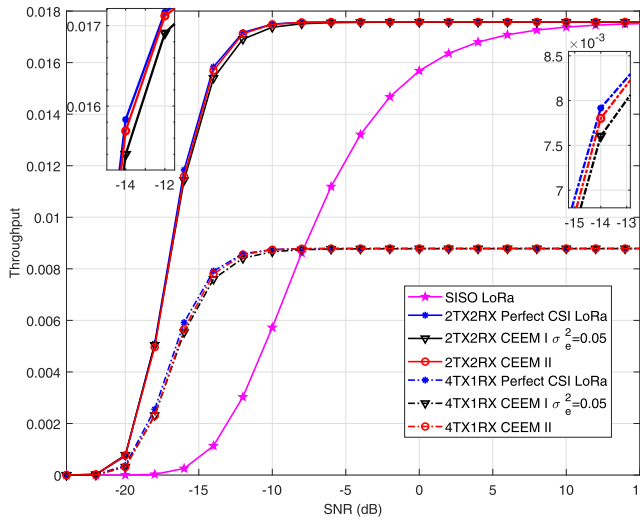


Fig. 8. Throughput of the STBC-MIMO LoRa system and the SISO LoRa system,  $SF$  is set to 9.

system. Moreover, in the middle SNR region, we observe that the throughput in the perfect CSI scenario is slightly higher than that in the imperfect CSI scenario for the STBC-MIMO LoRa systems with the same parameters. In the high SNR region, the STBC-MIMO LoRa system has almost the same throughput under different CSI conditions.

Based on the results of theoretical analysis and simulation, we can obtain some design insight for the proposed STBC-MIMO LoRa system. For LoRa-based LPWAN, in the entire transmission duration after LoRa node connect with the LoRa gateway, the uplink transmission occupies most of the time (e.g., class A of LoRaWAN protocol [14], [52]). This is because the main role of LoRa based LPWAN is to transmit the data of the LoRa nodes to the LoRa gateway. Therefore, how to transmit more data within the precious uplink transmission duration is particularly important. Considering the low power and low complexity requirements of LoRa nodes and the throughput performance of the system, equipping LoRa nodes with two antennas and utilizing  $G_2$  for transmission could be considered as an efficient solution (for complex STBC, only Alamouti code  $G_2$  can achieve  $r = 1$  [36]). In order to further improve the reliability of the system, more antennas can be equipped at the LoRa gateway to achieve higher diversity and reduce the impact of channel estimation error (see Fig. 5). Although this configuration will increase the hardware complexity and computational complexity of the LoRa gateway (refer to Sect. II-C), the LoRa gateway is generally not sensitive to the complexity and energy consumption in practice.

## V. CONCLUSION

In this paper, an STBC-MIMO LoRa system has been presented and its theoretical performance has been carefully studied. To be specific, the closed-form approximate BER expression of the proposed STBC-MIMO LoRa system for the perfect and imperfect CSI scenarios has been derived. As a further advance, the diversity order of the proposed system has

been analyzed. According to the analyzed results, the diversity order of the proposed system is zero in the imperfect CSI scenario with CEEM I, hence the error floor appears in high SNR region. In addition, full-diversity order  $d = MN$  can be achieved in the imperfect CSI scenario with CEEM II and the perfect CSI scenario. Afterward, the throughput analysis demonstrates that the STBC-MIMO LoRa system with the same parameters has almost the same throughput under different CSI conditions. Simulated BER results not only are in well agreement with the theoretical ones, but also verify the excellent performance and potential of the proposed STBC-MIMO LoRa system. From the perspective of BER performance, throughput, and complexity, configuring two antennas for the LoRa node and more antennas for the LoRa gateway can be regarded as an efficient solution in LoRa based LPWAN. Hence, the proposed system can be considered as a promising scheme for LPWAN.

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