# Forecasting Hotel Arrivals and Occupancy Using Monte Carlo Simulation


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**Abstract**

Forecasting hotel arrivals and occupancy is an important component in hotel revenue management systems. In this paper we propose a new Monte Carlo simulation approach for the arrivals and occupancy forecasting problem. In this approach we simulate the hotel reservations process forward in time, and these future Monte Carlo paths will yield forecast densities. A key step for the faithful emulation of the reservations process is the accurate estimation of its parameters. We propose an approach for the estimation of these parameters from the historical data. Then, the reservations process will be simulated forward with all its constituent processes such as reservations arrivals, cancelations, length of stay, no shows, group reservations, seasonality, trend, etc. We considered as a case study the problem of forecasting room demand for Plaza Hotel, Alexandria, Egypt. The proposed model gives superior results compared to existing approaches.

# 1 Introduction

Revenue management is the science of managing a limited amount of supply to maximize revenue by dynamically controlling the price/quantity offered (Talluri and Van Ryzin (2005), Bitran and Caldentey (2003), and Ingold et al. (2003)). Revenue management systems have been widely adopted in the hotel industry. Because of the large number of existing hotels, any possible improvement in the technology will amount to potentially very large overall savings (see Chiang et al. (2007)). A key component of hotel room revenue management system is the forecasting of the daily hotel arrivals and occupancy. Inaccurate forecasts will significantly impact the performance of the revenue management system, because the forecast is the main driver of the pricing/room allocation decisions (see Lee (1990), and Weatherford and Kimes (2003) for discussions of this issue). In fact, Polt (1987) estimates that a 20% improvement in forecasting error translates into a 1% increase in revenue generated from the revenue management system. This will probably impact the net income in a much larger way, due to the small margins existing in the hotel industry.

In this paper we consider the problem of forecasting daily hotel arrivals and hotel occupancy. In the theory of forecasting there has been two competing philosophies. The first one is based on developing an empirical formula that relates the value to be forecasted with the recent history (for example ARIMA-type or exponential smoothing models). The other approach focuses on developing a model from first principles that relates the value in question with the available variables/parameters etc, and simulates that model forward to obtain the forecast. Because the majority of real-world systems are either intractable or very complex to model, most forecasting applications follow the first approach. In contrast, we follow here the second approach. In other words, the proposed model is based on simulating forward in time the actual process of reservations in a Monte Carlo fashion. What makes the modeling quite intricate is the existence of many often interrelated processes: reservations arrivals, cancelations, duration of stay, no shows, group reservations, seasonality, trend, etc. We propose methods that attempt to model all these processes as faithfully as possible. This is achieved by estimating the distributions of the different quantities from the actual data if feasible, and, if the data are insufficient, aggregating the data in reasonable ways so as they become sufficient for obtaining relatively accurate estimation. The advantage of such methodology is that it yields the density of forecasts. This is a very beneficial aspect from the point of view of revenue management. The revenue management problem can be formulated using a dynamic programming-type construction (Bitran and Mondschein (1995) and Liu et al. (2006)). It is desirable to have the density of the forecasts, rather than just point forecasts. This is due to the probabilistic nature of dynamic programming-type revenue management formulations. For example, the "value function" is typically computed using the probability transitions.

In this work we considered as a case study the problem of forecasting the arrivals and occupancy of Plaza Hotel, Alexandria, Egypt.

There are several distinct advantages of the proposed approach:

- It produces the density of the forecasts, and hence also confidence intervals.
- It allows for measuring other quantities of interest, for example the probability of reaching the hotel capacity limit or a certain fraction thereof.
- It allows for scenario analysis. For example one can examine the effect of overbooking on future arrivals. Another example, one can explore the effect of a cancelation penalty beyond some date before arrival.
- The sensitivity of the arrivals forecast and the occupancy forecast due to changes of some control variables can in many cases be estimated. This, of course is very useful to the revenue management aspect of the problem.
- It allows for forecasting unconstrained demand. This means the total demand that would have occurred, had the hotel not been limited by its room capacity and had it accepted every single reservation. This is an important quantity from the point of view of revenue management.
- The presented approach is very flexible in that it can accommodate any input from the hotel manager, or any judgemental information (for example some expected rise in reservations arrivals due to some anticipated future event such as a major convention or a sports event).

The paper is organized as follows: Next section, we briefly review other work on hotel arrivals and occupancy forecasting. Section 3 presents the problem description and definitions. Section 4 describes the proposed approach, specifically the estimation of the system components. Section 5 details how we put these components together to obtain the forecast. Section 6 discusses some miscellaneous aspects, such as the level of aggregation and the unconstrained forecasting. Section 7 gives an overview of the considered case study (Plaza Hotel). Section 8 presents the simulations results, and finally Section 9 is the conclusion of the work.

## 2 Related Work

There has been few work on the topic of hotel room arrivals forecasting. Most of the work derives from approaches developed for the airline reservations forecasting problem. The airline problem has many similarities with the hotel room problem, such as dealing with reservations, cancelations, etc. But, there are still nontrivial differences that have to be taken into account. For example the length of stay is a variable existing in the hotel room problem, but not in the airline problem. A good review of the forecasting approaches can be found in Lee (1990) for the airline problem and Weatherford and Kimes (2003) for the hotel room problem. Basically, the approaches can be grouped into two categories: historical booking models and advanced booking models. Historical booking models consider only the arrivals or the occupancy time series, and apply time series models (such as exponential smoothing, ARIMA, etc) on these. No use is made of the reservations data. Examples of applications of the historical booking models include Sa (1987) and Lee (1990), both of which applied ARIMA models.

The advanced booking approach, on the other hand, makes use of the reservations data, and utilizes the concept of "pick-up". This means that given $K$ reservations for a future day $T$, we expect to "pick-up" $N$ more reservations from now until $T$. The forecast will then be $K + N$. There are two versions of the pick-up model (see also Weatherford and Kimes (2003)). In the additive version we add to the current number of reservations the average number of reservations typically picked up between the current date and the arrival date (of course taking seasonality into account). The multiplicative pick-up model is similar except that we add a percentage of the current number of reservations, rather than an amount independent of that number. Examples of applications of the advanced booking models include L'Heureux (1986), and also the extensions introduced by Sa (1987), Wickham (1995), Skwarek (1996), Weatherford (1997), and Bitran and Gilbert (1998), who extended the approach by adding a linear regression component. There has been work combining the advanced booking approach and the historical booking approach using concepts of forecast combination (see Ben-Akiva (1987)). The problem, however, with the advanced booking approaches is that they are designed to forecast only the arrivals, but not the occupancy. Forecasting occupancy is an essential task for developing a revenue management system.

There has also been analytical attempts to model net bookings in the presence of reservations arrivals and cancelations. The so-called stochastic model has been developed by Lee (1990) for the airline problem. In that approach the reservations process is modeled as a "birth-death process", see

Bailey (1964). This is a branch of the area of stochastic processes that analyzes the dynamics of births and deaths in a population. In our case each reservation is considered as a "birth", and each cancelation is considered as a "death" of an existing reservation. It is not clear, however, how to extend this approach to the hotel room case, where there is a third dimension to the problem represented by the length of stay.

Most of the above references are developed mainly for the airline problem. There is little work applied to the hotel room problem. Weatherford and Kimes (2003) compared between a number of historical booking models and advanced booking models for daily hotel room arrivals forecasting. They found that the additive pick-up and the linear regression-based advanced booking approach gave the best results. Zakhary et al. (2008) focused on the advanced booking approaches, and compared between different variations. Yuksel (2007) applied several versions of exponential smoothing, as well as ARIMA and some Delphi methods, to forecasting monthly hotel arrivals. Ben Ghalia and Wang (2000) developed a forecasting system using aspects of fuzzy modeling that can accommodate judgmental facts. Pfeifer and Bodily (1990) considered a space-time ARMA approach for the hotel room arrivals problem. Andrew et al. (1990) applied the Box-Jenkins approach and exponential smoothing to forecasting monthly hotel occupancy rates. Also, Chow et al. (1998) used ARIMA for the hotel occupancy forecasting problem. Schwartz and Hiemstra (1997) applied a novel idea for daily occupancy forecasting. They compare the shapes of the booking curves for the previous days to that of the current day. Then, they base the forecast on the most similar booking curve. Rajopadhye et al. (2001)'s model is probably the only model that has some aspect of simulation like our approach. Their approach, however, is different and is of a smaller scale than our approach. Their main approach is a time series forecasting model using Holt-Winter's exponential smoothing, but they also use a simulation approach to obtain short term forecasts as well.

# 3 Problem Description and Definitions

Hotel arrivals are mainly driven by two processes of opposing effects: *reservations* and *cancelations*. A potential hotel guest makes a reservation, typically a few days or a few weeks before the intended arrival day (if space is available). Typically the rate of reservations arrivals picks up significantly as arrival day gets closer. A *denied* reservation request is a request which is rejected by the hotel due to lack of room availability for all or part of the intended stay period. Reservations can get canceled any time before arrival.

The cancelation rate also increases, the closer we get to the arrival day, but it is also influenced by the hotel's cancelation policy (which could include some penalties). The *total bookings* at any time $\tau$ before arrival day $t$ is the total reservations net of cancelations made for the particular arrival day (thus it equals total reservations minus total cancelations made up to this time $\tau$). The *booking curve* is the graph of total bookings as a function of time until arrival (i.e. $t - \tau$). The *arrivals* represent the net number of guests that check-in at a particular day $t$. *Occupancy* is the number of occupied rooms at a particular day $t$. It could as well be measured as a percentage of the hotel room capacity. These latter two time series are in this study the target variables to be forecasted.

*Walk-in* customers are customers that check-in without reservations. For example they just show up at the hotel requesting a room for the current day. Also, some potential guests, who have reserved a room, do not show up on arrival day (potentially forfeiting their or part of their first night's payment). These are called *no-shows*.

Every room is reserved for a number of nights. This is called the *length of stay* or LOS. After the guest arrives, he could possibly check-out before the expected check-out date, leading to an *understay*. He could also check-out after the expected check-out date, leading to an *overstay*.

There has been recent interest in the hotel industry in applying revenue management systems (in short RM systems). A large improvement in hotel revenue and/or profit could potentially be achieved when applying well-designed RM systems. Most RM systems work by segmenting the customers into categories, and dynamically allocating a number of rooms and specifying the price for each category according to the expected demand, in a way that maximizes hotel revenue (Vinod (2004)).

Another aspect of revenue management is the implementation of an overbooking strategy. This means that the hotel will allow bookings to exceed the available hotel capacity, in anticipation that several reservations will be canceled. This strategy is expected to increase the level of hotel occupancy, and hence also the revenue. However, there is the flip side that if more guests with valid reservations arrive than available rooms the hotel would lose some good will and possibly incur some extra costs related to rebooking the extra guests in neighboring hotels ("walking the guests").

The need for accurate arrivals and occupancy forecasting arises due to the following aspects:

- The optimal number of rooms in each room category in an RM system is mainly influenced by future room demand.

- The price of each category should also be fixed according to the future demand. This arises from the well-known supply/demand relationship. For this and for the previous item, these quantities are determined in the framework of some formulated optimization problem.

- The optimal overbooking strategy can be determined as well. In fact, the proposed model allows for obtaining forecasts in the presence of any specific overbooking strategy.

We note that even though our approach gives the flexibility to incorporate an overbooking strategy, at this point we will not consider it in our experimental simulations and we will focus only on the forecasting aspect.

# 4 Estimation of the System's Components

As mentioned, there are two major phases in our approach. In the first phase we estimate all the parameters of the reservations process. In the second phase we simulate the reservations process forward in time to obtain the forecasts (using the estimates obtained in the first phase). In this section we describe in detail the parameter estimation phase.

## 4.1 Seasonality

Seasonality is a major factor that considerably affects the level of room demand. Most hotels have busy periods, where demand pushes up to full occupancy, and low periods with plenty of vacant rooms. By mastering the periods of high and low demand, pricing and room allocation can achieve more efficient revenue optimization.

In the hotel business the days are usually categorized into: high season or low season. Some hotels, however, have more seasonal levels. For example, Plaza Hotel, our case study, has a third seasonal level that they label "very low season". For concreteness sake, we will follow the case of Plaza Hotel in this description. Of course, the model can be easily customized to accommodate the seasons' convention of any other hotel. Thus, we classified seasonality into three categories:

- High season.

- Low season.

- Very low season.

The classification of the different days of the year into these three seasonal regimes is obtained by consulting with the hotel managers. A good strategy when forecasting a time series is to deseasonalize the time series (see Franses (1998)), in order to have the forecasting model focus on the medium term or long term variations or trends. Towards this end, the seasonal average curve has to be estimated. We have chosen a multiplicative seasonality model. The seasonal average is estimated as follows:

$$s_{\text{avg}}(t) = \frac{1}{N_H} \sum_{t' \in S_H} \frac{s(t')}{\text{Avg}(s(\tau))} \quad \text{for } t \in \ S_H \tag{1}$$

$$s_{\text{avg}}(t) = \frac{1}{N_L} \sum_{t' \in S_L} \frac{s(t')}{\text{Avg}(s(\tau))} \quad \text{for } t \in \ S_L \tag{2}$$

$$s_{\text{avg}}(t) = \frac{1}{N_{VL}} \sum_{t' \in S_{VL}} \frac{s(t')}{\text{Avg}(s(\tau))} \quad \text{for } t \in \ S_{VL} \tag{3}$$

where $S_H$, $S_L$ and $S_{VL}$ are the sets of respectively the high season days, the low season days, and the very low season days. As mentioned, these are determined by the hotel managers. The size of these sets is respectively $N_H$, $N_L$ and $N_{VL}$. The term $s(t)$ that is averaged here is the total reservations that arrived for arrival day $t$, taking out the cancelations that occurred. A precise definition of this variable, as well as the rationale for excluding the cancelations will be given next subsection. Concerning $\text{Avg}(s(\tau))$, it represents the average of $s(t)$ over the year in which it exists. One can see that Equations (1), (2), and (3) lead to a tri-level piecewise constant function.

Subsequent to computing the seasonal averages, we deseasonalize the series, as follows:

$$s_{\text{des1}}(t) = \frac{s(t)}{s_{\text{avg}}(t)} \tag{4}$$

where the subscript "des1" means a deseasonalized series, and the number 1 attached to it signifies that it is still an intermediate step as one more step will be considered in the next paragraphs.

This analysis so far considers only the seasonality regimes in the different periods of the year. There is another source of seasonality, namely day of the week seasonality (or in short weekly seasonality). While hotels that cater to business guests will have high weekday guest traffic, the converse is true for resort hotels. Their busy periods will be during the weekend. As such, the day of week arrival numbers will follow a distinct pattern. When estimating the weekly seasonality, we consider the deseasonalized time series, obtained in the previous seasonality analysis step, that is $s_{\text{des1}}(t)$. We then apply the following weekly deseasonalization algorithm:

1. For every time series point (of the series $s_{\text{des1}}(t)$) compute the average value for the week containing it. Denote this by $AvgWk$.

2. Compute the relative or normalized time series value:

$$s'_i(t) = \frac{s_{i,\text{des1}}(t)}{AvgWk} \quad (5)$$

   where $s_{i,\text{des1}}(t)$ is the time series value at time $t$ (i.e. $s_{\text{des1}}(t)$) that happens to be of day of the week $i$, and $s'_i(t)$ is the normalized time series value assuming it is of day of the week $i$. This normalization step is designed to take away the effects of any trend or level shift that would affect the relative values for the different days of the week.

3. The seasonal average $s_i^W$ (where $i$ designates the day of the week) is given by

$$s_i^W = \text{Median}_t(s'_i(t)) \quad (6)$$

A distinctive feature of this deseasonalization algorithm is the use of the median instead of the average. Weekly seasonality involves in most cases sharp pulses. If using the average, the peak of the seasonal average becomes blunter and shorter, leading to detrimental results. The median, on the other hand, leads to preserving the typical shape of the peaks observed during the week. One can also have a distinct weekly average for each of the three seasonal regimes (the high season, the low season and very low season). In our implementation we used this latter approach.

The deseasonalization is then obtained as:

$$s_{\text{des}}(t) = \frac{s_{i,\text{des1}}(t)}{s_i^W} \quad (7)$$

where $s_{\text{des}}(t)$ represents the final deseasonalized series. The forecasting model will be applied on this time series. Of course, after the forecasting step all these normalizing factors will be multiplied back to restore the seasonal effects of the forecasted portion of the time series.

As mentioned, we obtain the classification of the days of the year to the different seasonal regimes from the hotel managers. It is generally possible to estimate the high, medium and low seasonal periods exclusively from the data using some statistical technique. However, we believe that the information provided by hotel managers should take precedence. They are more knowledgeable about future events, such as a convention or a sports event. We therefore believe that the best approach is to obtain the seasonal average using a combination of information provided by the managers (to obtain the major high and low season periods and relevant future city events) and statistical approaches (to obtain the precise seasonal level within each season and to obtain the weekly seasonal average).

## 4.2 Reservations

Reservations represent the amount of bookings that arrive with time for a particular arrival day. It is a central variable in our whole simulations approach. But, at the same time it is also the most challenging component to model. The reason is its dependence on two time indexes: the reservation day (i.e. the day the room is booked) and the arrival day (the intended day for the guest to check in). A possible way to model reservations arrivals is to use a Poisson process. Because of the discrete nature of the way the data are recorded (i.e. by days) this approach can lead to difficulties and rounding inaccuracies. So we opted for a different approach whereby we model the reservations arrivals as Bernoulli trials.

Let $B(i,t)$ be the expected number of reservations for arrival day $t$ that are booked exactly $i$ days before arrival. (In that sense $B(0,t)$ represents the expected number of walk-in guests.) We call $B(i,t)$ the *reservation curve.* Because of the random nature of the reservations process, more or less reservations than $B(i,t)$ will actually occur, as from among the guests that would potentially come some reservations would materialize and some not. As such, we assume that reservations obey a binomial distribution with probability $p$. Thus,

$$B(i,t) = Np \tag{8}$$

where $N$ is the size of "potential" population from which possible reservations can come for the particular reservation and arrival dates, and $p$ is the probability that the reservation will materialize. The previous equation is for the purpose of preserving the fact that the mean of this binomial experiment should equal $B(i,t)$ (since by definition $B(i,t)$ is the expected number of reservations).

The main issue here is to estimate $B(i,t)$. Once available, then one can simply generate future reservations data by generating Bernoulli trials. The problem, however, is that for each arrival time $t$ we have only one realization of the reservation curve $B(-,t)$, and it will of course be grossly inaccuarate to base the estimate on that single realization. However, beyond up and down shifts with the seasonality variations, the shape of the booking curve does not change much. We have verified that by visually screening the data. However, we found that this uniformity is up to a certain limit. That is, the actual shape would change somewhat between the extreme seasonal conditions.

To separate the effect of “shape” from “level” (of the reservation curve), we assume:

$$B(i,t) = s(t)B'(i) \tag{9}$$

where $B'(i)$ is the *normalized reservation curve* (it sums to 1, i.e. $\sum_{i=0}^{\infty} B'(i) = 1$), and it represents the absolute shape of the booking curve, ignoring the effect of its magnitude. The variable $s(t)$ represents the level or magnitude of the booking curve. It more or less represents how the seasonal effects adjust the level of the booking curve by shifting it up or down in a multiplicative manner.

Based on the above realization that the shape varies somewhat between different seasonality regimes, we assume that there are three distinct shapes of the normalized booking curve $B'(i)$: one pertaining to the high season, $B'_H(i)$, one pertaining to the low season $B'_L(i)$, and another representing the very low season $B'_{VL}(i)$. To estimate these quantities, we average over the days occurring in the respective seasonal regimes:

$$\hat{B}'_H(i) = \frac{1}{N_H} \sum_{t \in S_H} \frac{R(i,t)}{\sum_{j=1}^{\infty} R(j,t)} \tag{10}$$

where $S_H$ is the set of high season days, as defined in Subsection 4.1 (let its size be $N_H$), and $R(i,t)$ denotes the actual number of reservations for arrival day $t$ that are booked $i$ days before arrival. In contrast to $B(i,t)$, which is the *expectation* and is an *unknown* quantity, $R(i,t)$ is the actual number of reservations and it is an observed quantity. Note that we likewise normalized $R(i,t)$ in the above summation (in Eq. 10) so that we focus on the shape rather than level. We have similar equations for the other two regimes:

$$\hat{B}'_L(i) = \frac{1}{N_L} \sum_{t \in S_L} \frac{R(i,t)}{\sum_{j=1}^{\infty} R(j,t)} \tag{11}$$

$$\hat{B}'_{VL}(i) = \frac{1}{N_{VL}} \sum_{t \in S_{VL}} \frac{R(i,t)}{\sum_{j=1}^{\infty} R(j,t)} \tag{12}$$

where $S_L$ and $S_{VL}$ are the sets of respectively low season days, and very low season days. The sizes of these sets are respectively $N_L$ and $N_{VL}$.

Concerning the level multiplier $s(t)$, it is estimated as follows:

$$\hat{s}(t) = \sum_{i=0}^{\infty} R(i,t) \tag{13}$$

The reason for the previous equation is that by summing both sides of Eq. (9) over the index $i$, we get

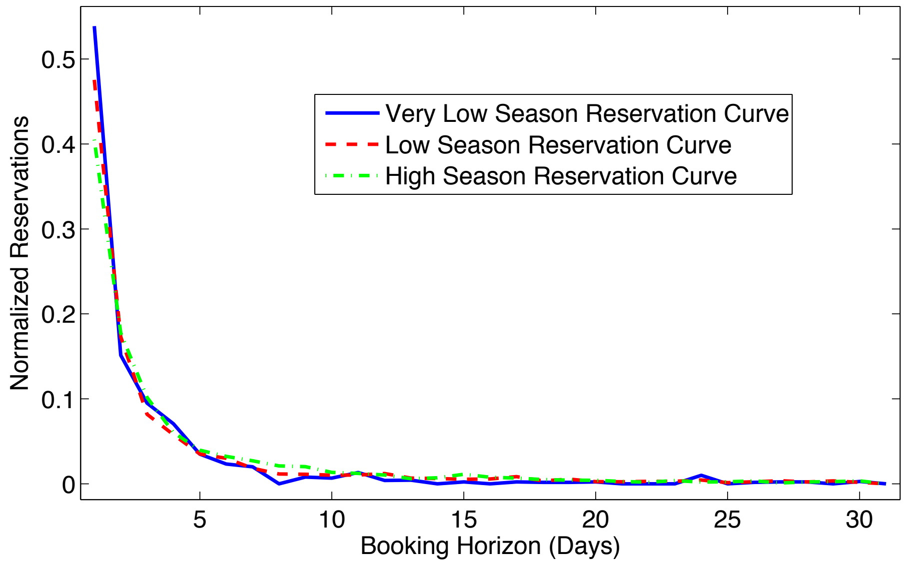


Figure 1: Plaza Hotel's normalized reservation curve $B'(i)$ as a Function of the Booking Horizon (Time before Arrival) for the Three Seasonal Regimes

$$\sum_{i=0}^{\infty} B(i,t) = s(t) \tag{14}$$

(because $\sum_i B'(i) = 1$). Since $R(i,t)$ is a realization from a distribution whose mean is $B(i,t)$, then Eq. (13) can be considered an estimate of $s(t)$. Note that it is fair to assume that the reservations process has little serial correlation (with $i$), thus making the estimate in Eq. (13) reasonably accurate. Of course in all the previous summations the upper limit will practically be some bound $I$ (rather than $\infty$) beyond which no reservations usually come. Figure 1 shows the normalized reservation curve $B'(i)$ as a function of the booking horizon (time before arrival) for the three seasonal regimes, as estimated from the in-sample period for our Plaza Hotel case study. We can see that in the low season and especially in the very low season regimes more reservations come immediately before arrival day, which is an expected observation.

The estimated $\hat{s}(t)$, which represents the sum of all reservations for arrival day $t$ (see Eq. 13), represents a measure of room demand. This is the variable for which we apply the deseasonalization step, as detailed in the last subsection. After the deseasonalization step, we apply a forecasting method to project this variable forward in time. The reason for using this variable instead of the net arrivals is that it purely handles reservations only. On the other hand, the net arrivals variable takes away the cancelations, and it will therefore be hard to disentangle the two processes (i.e. the reservations and cancelations processes) by observing only the arrivals forecast.

As mentioned, for the purpose of simulating the reservations process, we consider a binomial distribution, with Eq. (8) guaranteeing equality of the mean of the distribution to the expected reservations number. There are however, two variables involved, $N$ and $p$, and this could therefore allow us to fit an additional quantity (other than the mean) for more faithful representation. We took the additional quantity to be the variance. Hence we set the two quantities $N$ and $p$ so that the following two equations are satisfied:

$$\hat{B}(i,t) = Np \tag{15}$$

$$\frac{1}{TI}\sum_{t=1}^{T}\sum_{i=1}^{I}\left(\hat{B}(i,t) - R(i,t)\right)^2 = Np(1-p) \tag{16}$$

where $\hat{B}(i,t) \equiv \hat{s}(t)\hat{B}'(i)$ is the estimate obtained using the procedure described above (Eqs. 10-13). Note that for each $i$ and $t$ we have distinct $N$ and $p$. The second equation specifies that the variance of the binomial process equals the empirical variance observed from the data. Notice that this empirical variance is computed using all arrival times $t$ and all number of days $i$ before arrival (or else, if we assume a variable variance, data will not be sufficient).

## 4.3 Cancelations

Reservations can be canceled any day before arrival day. The rates of cancelations vary according to the time until arrival. Typically, they increase as we get close to arrival day. However, if there are some penalties for cancelations that occur beyond a certain day, cancelations will decrease dramatically. We assume that the cancelation rate (say $c(i)$) is a function of the number of days $i$ until arrival day. It is defined as the mean fraction of net bookings that get canceled. For example, consider that we are focusing on arrival day $t$, and that we are at $i^{th}$ days before that arrival day. Assume that at the close of the previous day there are $H(i+1,t)$ bookings (or reservations at hand) for that arrival day $t$. If $c(i) = 5\%$, then the expected number of reservations to be canceled at the current day (day $i$ before arrival) is $0.05H(i+1,t)$. Also, as a result, $c(0)$ represents the mean fraction of no-shows.

Of course $c(i)$ gives only the mean value. The actual number that ends up being canceled is a random variable. We model that random variable

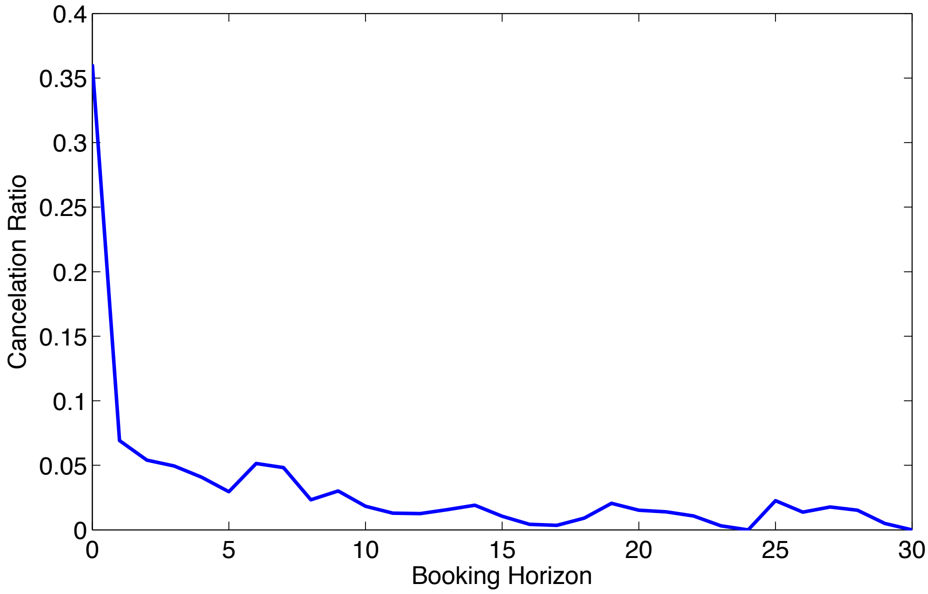


Figure 2: Cancellation Ratio as a Function of the Booking Horizon (Time before Arrival) for Plaza Hotel

as binomial. Specifically, we assume $H(i+1,t)$ Bernoulli trials, each one with probability $p \equiv c(i)$ of being canceled. The cancelation mean curve $c(i)$ is estimated from the reservations data of the in-sample period. Note that we have assumed a similar cancelation mean curve $c(i)$ for all seasonal regimes. The reason is that the estimate of $c(i)$ turned out to be a little noisy. Disaggregating it among the three main seasonal regimes will aggravate the estimation error. Figure 2 shows the cancelation mean curve $c(i)$ for the case study of Plaza Hotel, as estimated from the in-sample period. Once $c(i)$ is estimated, it is used when we simulate the reservations and cancelations processes forward in time using the aforementioned binomial generation process.

## 4.4 Length of Stay

The length of stay (call it $T_L$, or LOS in short) for hotel guests varies according to the type of the hotel's clientele. Business travelers tend to stay for one or two nights, while vacationers could stay up to a week. The LOS plays a major role in our simulation system. In fact the length of stay can actually impact the hotel occupancy of the near future, as well as lead to

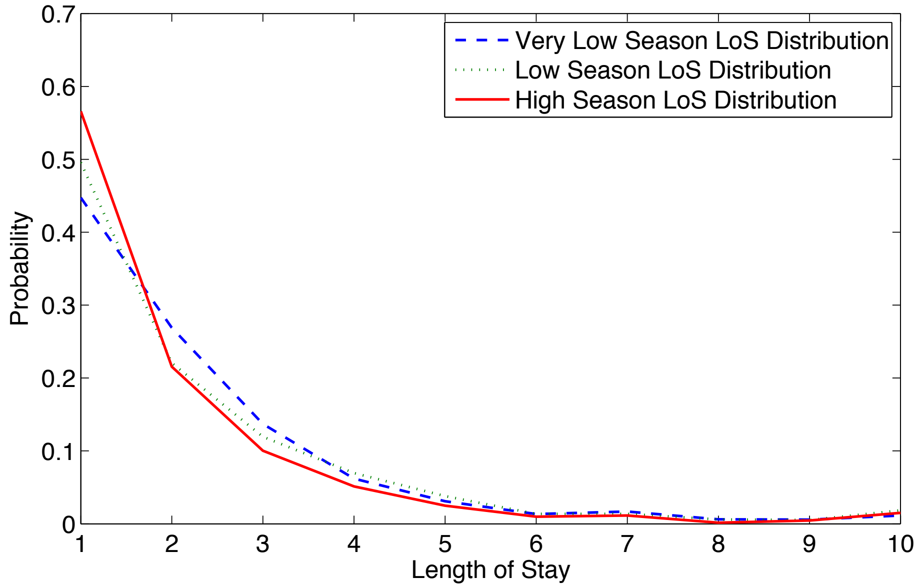


Figure 3: Length of Stay Distributions for the Different Seasonal Regimes for Plaza Hotel

denials of booking attempts (even for future days). When tracking an arriving reservation until it materializes and the guest arrives, the LOS has to be specified. Towards this end, we consider a distribution of the LOS, and estimate it from the in-sample portion of the data. Then, in the simulations phase we generate an actual stay scenario for every reservation using this distribution. It is conceivable that $T_L$ would be influenced by some factors. In our work with hotel data we observed that typically the time from booking to arrival does not impact the LOS. That leaves one potential influence factor: the seasonal cycle. To test this possible dependence, we have estimated $p(T_L|S_H)$, $p(T_L|S_M)$, $p(T_L|S_L)$, that is the distribution of the LOS in each of the three seasonal regimes. Figure 3 shows these curves for the Plaza Hotel case study. One can see that these distributions differ somewhat. We therefore decided to use in our model these season-specific LOS distributions.

One could also in principle model understays and overstays. One way is to estimate a distribution of the number of days the guest stays more (or less) than he reserved. We did not model this aspect in our simulation as it is a bit involved, and its impact on accuracy will probably be limited.

## 4.5 Group Reservations

A large amount of tourism travel nowadays is through pre-arranged tour packages. This means that the tourist has a planned itinerary, with stays in specific hotels for specific dates. This way the tour operator can achieve block reservations in the hotels and hence obtain a lower cost that can be passed on to the traveler. Kimes (1999) performed an insightful analysis and developed a forecasting model for group reservations in hotels. Group reservations have their specific dynamics, which we consider in this simulator. For example, we allow whole block cancelations. We define a block or a group as a group of reservations that are reserved at the same day, for the same arrival and departure date, and by the same travel operator. In our system we model the group size $g$ by some distribution $p(g)$. This distribution is estimated from the historical data by checking the sizes of all the reservation blocks. Actually we lump all group and non-group data into one set and estimate the distribution from this set. In such a case $g = 1$ represents an individual (or non-group) reservation, and $p(1)$ represents the probability or fraction of non-group reservations.

Once estimated, in the simulation stage the group reservations are generated as follows. We generate a reservation according to the estimated reservation curve (as described in 4.2). This reservation could be a group (of some specific size) or a non-group reservation. Then, we generate a number $g$ using the distribution $p(g)$. This generated $g$ will then represent the group size. It could equal 1 (actually with a high probability), which simply means it was just an individual (or non-group) reservation.

## 4.6 Trend Estimation

As mentioned, the variable $s_{des}(t)$ represents some measure of deseasonalized room demand (with excluding the cancelations effect). It is also possible to use the $s_{des}(t)$ time series to gauge trends in overall room demand. For this reason we apply a forecasting model for predicting this variable in the considered forecast horizon. Our ultimate goal is to simulate the room reservations process in some forecast horizon. The variables used should therefore reflect future values, rather than present values. It is anticipated that the general room demand will exhibit some medium-term trend, reflecting changing hotel conditions, and external effects that affect tourism demand and business conditions in the area. As such, this forecasting step should estimate this trend. The other variables in the model are mainly distributions and mean values (such as reservation curve, cancelation curve, LOS, etc). They are not anticipated to change in the medium term (beyond changes due to the seasonality effect discussed before). These quantities reflect customer behavior issues that typically change only in the long term. We have verified this claim, by estimating these distributions and averages in two contiguous six months periods for our case study. We found that the estimates are close.

We use Holt's exponential smoothing model for forecasting the room demand variable $s_{des}(t)$. The Holt's exponential smoothing model is based on estimating smoothed versions of the level and the trend of the time series Hyndman et al. (2008). Then, the level plus the trend is extrapolated forward to obtain the forecast. The governing equations for updating the trend and the level are given by Gardner (2006):

$$
\begin{aligned}
l_t &= \alpha s_t + (1-\alpha)(l_{t-1} + b_{t-1}) && (17) \\
b_t &= \gamma(s_t - l_{t-1}) + (1-\gamma) b_{t-1} && (18)
\end{aligned}
$$

where $s_t \equiv s_{des}(t)$ is the variable to be forecasted (room demand variable), $l_t$ is the estimated level and $b_t$ is the estimated trend of the time series. The forecast is given by a linear extrapolation in time:

$$
\hat{s}_{t+m} = l_t + m b_t \tag{19}
$$

There are five parameters that have to be set, before applying the forecasting step. These are $\alpha$ and $\gamma$, the smoothing constants for respectively the level variable and the trend variable, $l_0$ and $b_0$, the starting values for respectively the level and trend, and $\sigma$, the standard deviation of the error term. We used the approach by Andrawis and Atiya (2009) that is based on the maximum likelihood concept.

Once the forecast of $s_{des}(t)$ is obtained for the required horizon, the seasonal effects will be restored back, to obtain $\hat{s}(t)$. Then, the detailed reservation curves for the future can be constructed (as they are the product of the normalized booking curves $B'(i)$ and the forecasted $\hat{s}(t)$ variable, see Eq. (9)).

# 5 The Overall Monte Carlo Simulation System

Once we have estimated the parameters such as the seasonal average, the reservation curve, etc, as detailed in the last section, we can now apply the forecast step. In this step we simulate forward the processes of reservations arrivals, cancelations etc, exactly as they happen in the model that we have developed. We use all the parameter values obtained in the estimation step. Because of the randomness aspect of the reservations process one realization of this simulation is naturally not sufficient. We need to generate many paths in a Monte Carlo fashion, and then take the mean of these paths at any future instant of time $t$ as the forecast. This applies to whatever quantity we would like to forecast, such as reservations arrivals or occupancy.

When at a particular day a forecast is needed for some horizon, we make use of the information that we have about the reservations already at hand. This will be the starting point upon which reservations will keep building. For example, we are at time $t$ and we would like to forecast arrivals at time $t+5$. Assume that the hotel has already 20 reservations for that future date. Then any new reservations that will be simulated forward will add to these 20 reservations. Conversely, any future cancelations simulated will be subtracted out from these 20 reservations. This effect could significantly influence the forecasted variables, with this effect slowly decaying as the lead time increases. Below is the forecasting algorithm's details:

*Algorithm Demand Forecasting:*

1. Let $t$ be the current time and $t+1 : t+T$ be the horizon to be forecasted. From the hotel records we know that we have $R(i, t')$ reservations for arrival day $t' = t+1, \ldots, t+T, \quad i \geq t' - t$.

2. We know the variable $s(t')$ for all previous times $t' \leq t$ (it is defined by Eq. (13)). Forecast $s(t')$ for the considered horizon, as discussed in Subsection 4.6. Let the forecasts be $\hat{s}(t')$, $t' = t+1, \ldots, t+T$.

3. For $\tau = t+1$ to $t+T$ perform the following:

   (a) *Cancelations:* Generate cancelations from a binomial distribution, as follows. For every arrival day $t'$, $t' = \tau, \ldots, t+T$ the bookings (or reservations at hand) are $H(t' - \tau + 1, t')$. The average fraction of cancelations is $c(t' - \tau)$ where the $c$ function has been already estimated from the historical data in the parameter estimation phase. We generate a Bernoulli trial for each reservation with probability $p = c(t' - \tau)$ that a cancelation will actually occur for that reservation. Remove the canceled reservations and correspondingly update the new booking matrix $H(t' - \tau + 1, t')$.

   (b) *Reservations:* Generate new reservations for every arrival time $t'$, $t' = \tau, \ldots, t+T$. The reservation curve for some time $t'$ will be one of the normalized reservations templates: $B'_H(i)$, $B'_L(i)$ or $B'_{VL}(i)$ (depending on which seasonal regime $t'$ falls in) multiplied by the forecasted level $\hat{s}(t')$. Generate the reservations using a binomial distribution with number of trials $N$ and probability $p$ determined according to (15) (16).

(c) *Group Reservations:* For every generated reservation determine the group size by generating a number (per reservation) according to the group size distribution. Note that if this number turns out to equal 1 then this means it is an individual reservation (which is usually the higher probability case).

(d) *Length of Stay:* For every reservation generate an LOS according to the estimated season-specific LOS distribution.

(e) For every reservation generated in Steps b)-d) determine if it will be accepted or denied. A reservation is accepted if during the intended duration of stay there is room availability, else it is denied. If the hotel has an overbooking policy, then a reservation is accepted if it is within the bounds of this overbooking policy, else it is denied. Note that Steps b)-d) for generating a reservation, with all its features including the decision of whether to accept or deny the reservation, have to be performed in a sequential manner, one reservation at a time.

4. Repeat Step 3) for $K$ times to get $K$ Monte Carlo paths for future reservations. Obtain the mean (or median) for these paths for each of the arrivals variable and the occupancy variable (mean or median over the $K$ paths for each time step). These are the forecasts.

# 6 Miscellaneous Aspects

## 6.1 Level of Aggregation

Many revenue management systems prefer to have the demand forecast segmented by category (Vinod (2004)). As detailed before, a pricing policy on the basis of various guest categories is at the heart of a successful RM system. Categories, such as by rate, guest type, room type, length of stay, are usually considered in most hotels. One procedure (disaggregate forecasting) is to consider each category's guest flow separately, and develop a separate forecasting model for each category. The alternative procedure (aggregate forecasting) is to develop an aggregate model and then disaggregate by breaking down the aggregate forecast into its disaggregate constituents in some reasonable way (Weatherford and Kimes (2003)). In our simulation based model, the latter could be performed as follows. We estimate a common set of parameters for all categories using all the available historical data set. When forecasting, each category has its own set of reservations at hand. Starting from these reservations, we perform a simulation forward in time to obtain the forecasts for each category (the forecasts will generally be different for each category due to the different starting reservation numbers).

Each of the disaggregate and the aggregate approaches have their own strong and weak points. For example, the advantage of the disaggregate approach is the specificity of the estimated set of parameters to the considered category. The disadvantage, however, is that by considering each category separately, the data could get considerably diluted to the extent that the parameter estimates would be of suspect accuracy. Of course, a middle ground could be taken, by combining some categories into a few major ones that are known to possess different parameter sets. Then, we disaggregate further in the forecast step. For example we could categorize as business guests versus leisure, and/or high rate versus low rate. These dichotomies would probably have different reservation curves, and different cancelation and LOS profiles.

## 6.2 Unconstrained Demand Forecasting

The reservations data that is typically recorded in the hotel's books do not entirely gauge the whole amount of room demand. Some would be guests have attempted to reserve, but were turned down because of lack of availability or because of the booking limit imposed on the relevant category: these are called *denied reservations*. Unconstrained demand is the total demand including these denied reservations. In other words, it is the total amount of reservations that would have come, had the hotel accepted every arriving reservation attempt. (An analogous definition applies for arrivals as well.) For the purpose of revenue management, unconstrained demand is the more relevant quantity to consider. The problem is that denial data are usually not recorded in the hotels, or if recorded, they are considered to be unreliable. Even if there were attempts to record denials, it will be very hard to determine if an inquiry about room availability would have eventually led to an actual reservation, had the answer been positive instead of negative. For these reasons, the problem of forecasting of unconstrained demand is a very challenging issue. The dominant approach in the literature has been to assume certain distributions for the variables and use the concept of censoring (see Lee (1990) and Weatherford and Kimes (2003)). Another approach is to use the concept of detruncation. Skwarek (1996) used pick-up detruncation while Wickham (1995) used booking curve detruncation. These approaches are based on estimating the number or fraction of reservations that were denied.

We extended the proposed Monte Carlo approach to the unconstrained forecasting case. The approach follows more a detrucation-type methodology, as the other censoring approach will become analytically too involved. The steps of the proposed method are as follows:

*Algorithm Unconstrained Forecasting:*

1. Estimate the parameters, distributions, etc, exactly as detailed in Section 4 using the constrained historical data. Let the parameter set be $S$.

2. Simulate Monte Carlo paths as detailed in Section 5 (Algorithm Demand Forecasting), Steps 1-3) based on using the constrained parameter set $S$, on the historical (or in-sample) period (*not* on the forecasting period). We implement Steps 1-3 exactly, except that we assume unlimited hotel capacity. This means no simulated reservations will be denied.

3. Re-estimate the parameters as detailed in Section 4 using the reservations data generated in the previous step (Step 2 of this algorithm). Note that unlike how it is done in Step 1 in this algorithm or in Section 4 we have here many Monte Carlo paths (in other words reservation paths). We make use of all these reservations scenarios in the parameter estimation step. This can only enhance the accuracy (relative to an estimate using only one reservations scenario).

# 7 The Plaza Hotel Case Study

We applied the proposed forecasting model to the problem of forecasting the arrivals and the occupancy of Plaza Hotel, Alexandria, Egypt, as a detailed case study. Plaza Hotel is a mid-sized four star sea-side hotel, located on the Mediterranean Sea. It has 134 rooms partitioned into 11 single rooms (studio type), 91 double rooms, 32 suites (12 junior suites and 20 deluxe suites). Its clientele is a mix of business, leisure, and foreign tourist guests. The type of business guests covers conferences, government, sporting clubs, corporations, etc.

Modern revenue management approaches (the type discussed earlier) have recently started to attract some interest from hotels in Egypt. A good fraction of five star hotels in Egypt apply some form of revenue management (Shehata (2005)). On the other hand, the majority (if any) of four star hotels and lower do not apply any form of revenue management. Plaza Hotel plans to implement a revenue management system. As a first step, an

Table 1: The In-Sample and the Three Months Ahead Forecast Periods for the Three Forecasted Snapshots

| Snapshot No. | In-Sample Period | Forecast Period |
|---|---|---|
| 1 | 1-Oct-2006 - 30-Sep-2007 | 1-Oct-2007 - 31-Dec-2007 |
| 2 | 1-Oct-2006 - 31-Oct-2007 | 1-Nov-2007 - 31-Jan-2008 |
| 3 | 1-Oct-2006 - 30-Nov-2007 | 1-Dec-2007 - 29-Feb-2008 |

arrivals and occupancy forecasting model needs to be developed. In collaboration with the hotel, we apply our proposed forecasting model to the hotel's data.

# 8 Simulation Results

## 8.1 The Hotel Data

We have applied the proposed Monte Carlo simulation forecasting model on the data of Plaza Hotel. We have obtained a full set of data covering the period from 1-Oct-2006 until 1-Mar-2008. The breadth of the data is extensive, and they include all aspects of the reservations, with all its details, such as room type, customer category, rate category, etc.

We have considered a three months ahead forecast, using an expanding window approach for the estimation or in-sample set. In that set up we forecast three months ahead at three snapshots during the last five months of the data. Table 1 shows the in-sample periods and the forecast periods for the three snapshots. We considered both daily forecasting (that is forecasting every day in the three-months forecast horizon), as well as weekly forecasting (forecasting only week-by-week in the three-months forecast horizon). In practice, the hotel will probably be interested in daily forecasting for the short period ahead, followed by weekly forecasting for the farther period ahead. We have considered forecasting aggregate room demand (arrivals as well as occupancy), rather than disaggregate by room type or other category. For Plaza Hotel, the partition of rooms by type is not very rigid, as rooms get frequently converted from one type to another according to need.

## 8.2 Seasonal Analysis

As mentioned in 4.1 we have used a tri-level seasonal regime classification, with the levels being: high season, low season, and very low season. The

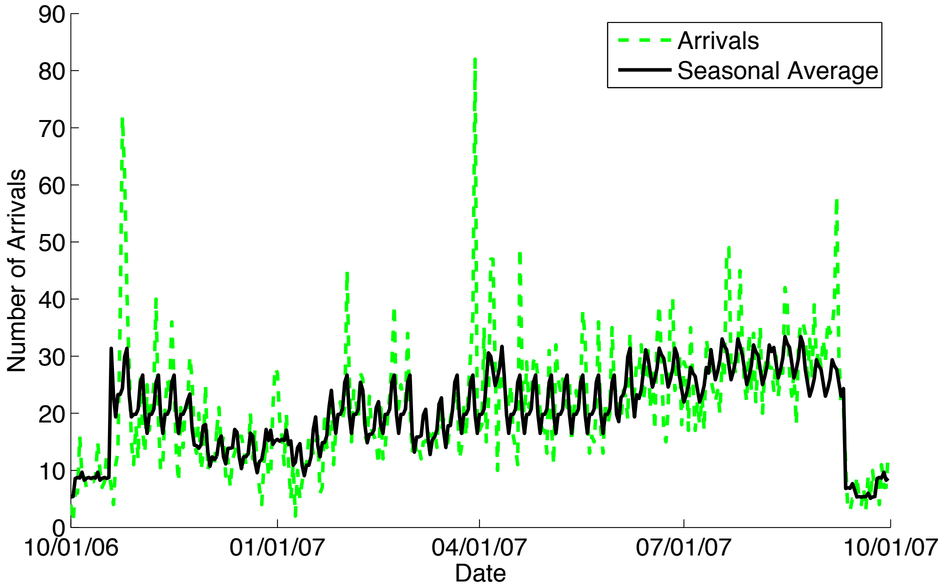


Figure 4: The Arrivals Time Series for the In-Sample Period, Together with the Seasonal Average

reason for the third "very low season" is that the period of the month of Ramadan is exceptionally low in demand. The month of Ramadan is the holy month in the islamic calendar that precedes one of the major islamic feasts, the "Eid El-Fetr". The appendix lists the dates of the different seasonal regimes, as identified by the Plaza Hotel managers.

Plaza Hotel also possesses a distinct day of the week pattern of arrivals. Alexandria is about 230 km away from Cairo, the capital and most populous city in Egypt. It therefore attracts visitors over the weekend (the weekend holiday in Egypt is Friday and Saturday).

Figure 4 shows the arrivals time series for the in-sample period, together with the estimated seasonal average. As mentioned in Subsection 4.1, the best seasonality analysis approach is an interactive approach, whereby we make use of the information provided by the hotel managers, and pose it in a statistical framework. For example in our case we find that the seasonal average obtained in the first step of the seasonal decomposition (see Subsection 4.1, Equations (1), (2), and (3)) is a tri-level function, with a different level for each of the three seasonal regimes. Upon talking to the Plaza Hotel managers, they indicated that not all high season peaks possess similar guest traffic. So, we also implemented a modification whereby each high season period has its own level (i.e. its own $s_{avg}(t)$, whereby the summation in Eq. (1) is restricted to the subperiod of the high season in which time $t$ falls). We also implemented another modification, on a concern pointed out by the Plaza Hotel managers. The low season is also too large to simply have a one-level seasonal average. So we have partitioned that period into subperiods that are obtained by detecting clusters of relatively high or relatively low periods using some moving average mechanism (as the hotel managers could not identify the subperiods and we had to rely on the data).

## 8.3 The Compared Models

To obtain a comparative idea about the relative performance of the proposed forecasting model, we have applied to the same data five competing forecasting models. As mentioned in Section 2, there are two major categories of forecasting models. The first one, the historical booking models, consider only the arrivals or the occupancy time series, and apply time series forecasting models on these. The second one, the advanced booking or the pick-up approaches, model the amount of reservations to be "picked up" until arrival day.

We have considered one model from the first category, and four models from the second category. The five compared models are as follows:

1. A historical booking model using Holt's exponential smoothing using the maximum likelihood approach by Andrawis and Atiya (2009) for estimating the parameters (see Subsection 4.6 for an overview over Holt's exponential smoothing). We used a deseasonalization strategy similar to the one we used in our proposed model (as described in Subsection 4.1).

2. Additive classical pick-up using simple moving average.

3. Additive advanced pick-up using simple moving average.

4. Additive classical pick-up using exponential smoothing.

5. Multiplicative classical pick-up using exponential smoothing.

Note that additive/multiplicative corresponds to the way the reservations are picked up. Also, by classical we mean that we use only completed booking curves, and by advanced we mean that we use not-yet-completed booking curves. Simple/exponential smoothing corresponds to the way we compute the average reservations to be picked up. Note that Zakhary et al. (2008)

conducted a comparison between the different variations of the pick-up approach and found models 2), 3) and 5) have been among the top three models. The disadvantage of the pick-up approach is that it applies only to arrivals forecasting, but *not* to occupancy forecasting.

We used as error measure the symmetric mean absolute percentage error, defined (whether for the arrivals or occupancy time series) as

$$SMAPE = \frac{1}{M} \sum_{j=1}^{3} \sum_{m} \frac{|\hat{y}_m^{(j)} - y_m^{(j)}|}{(|\hat{y}_m^{(j)}| + |y_m^{(j)}|)/2} * 100 \tag{20}$$

where $y_m^{(j)}$ and $\hat{y}_m^{(j)}$ are respectively the actual time series value and the forecast for forecast period $j$ (as mentioned there are three 3-months-ahead forecast periods, listed in the last column of Table 1). Also, $M$ is the total number of points that are forecasted (the sum of the points in the three forecast periods).

## 8.4 Results

Table 2 shows the SMAPE error measure for the proposed Monte Carlo model and the five competing models for the case of daily forecasting. Similarly, Table 3 shows the SMAPE error measure for the proposed model and the competing models for the case of weekly forecasting. Also, Figure 5 shows the forecast of the proposed Monte Carlo model versus actual for the first three-months ahead forecast period. Also shown are the one standard deviation confidence bands. Figure 6 shows the forecast and the actual (with the confidence bands) for the occupancy for the first three-months ahead forecast period (also for the proposed Monte Carlo model).

One can deduce the following observations. The proposed Monte Carlo model beats all the competing models for both the arrivals forecasting and the occupancy forecasting problems, and for the daily forecasting, as well as the weekly forecasting problems. For the arrivals forecasting, the outperformance is considerable, when compared with the Holt's exponential smoothing model and with two of the pick-up models. The two most competitive pick-up models, the additive classical pick-up using simple moving average and the additive advanced pick-up using simple moving average, are still about 4% behind the proposed model in SMAPE for the daily arrivals forecasting, and 1-1.5% behind for the weekly arrivals forecasting. The drawback, however, for the pick-up models is its inapplicability to the occupancy forecasting problem. As seen in the table, the proposed model is the undisputed winner for the occupancy forecasting case. As mentioned before, other than forecasting accuracy the advantage of the proposed model is its versatility.

Table 2: The Overall Forecast Error for the Out-of-Sample Periods for the Proposed Monte Carlo Model and the Five Competing Models for the Case of Daily Forecasting

| **Model** | **Arrivals SMAPE** | **Occup SMAPE** |
|---|---|---|
| Proposed Monte Carlo | 43.9 | 37.7 |
| Pickup (Add, Class, Simple) | 48.3 | - |
| Pickup (Add, Adv, Simple) | 47.9 | - |
| Pickup (Add, Class, Exp) | 54.8 | - |
| Pickup (Mul, Class, Exp) | 97.9 | - |
| Exp Smoothing | 63.8 | 61.1 |

Table 3: The Overall Forecast Error for the Out-of-Sample Periods for the Proposed Monte Carlo Model and the Five Competing Models for the Case of Weekly Forecasting

| **Model** | **Arrivals SMAPE** | **Occup SMAPE** |
|---|---|---|
| Proposed Monte Carlo | 21.5 | 23.4 |
| Pickup (Add, Class, Simple) | 23.1 | - |
| Pickup (Add, Adv, Simple) | 22.5 | - |
| Pickup (Add, Class, Exp) | 35.1 | - |
| Pickup (Mul, Class, Exp) | 100.7 | - |
| Exp Smoothing | 49.2 | 41.2 |

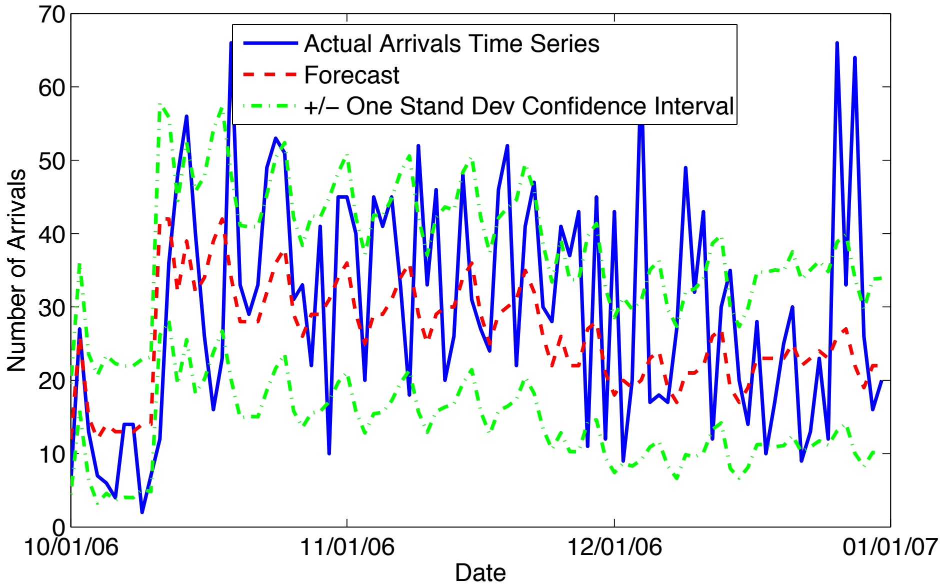


Figure 5: The Forecast Versus the Actual for the Arrivals for the First Three-Months Ahead Forecast Period

It can basically obtain almost any quantity of interest or almost any desired computation, for example: unconstrained demand, a forecast of the number of denials, the impact of a particular overbooking strategy, the probability of reaching hotel capacity, and the density of the forecasted quantities. All these computations are highly desirable for a revenue management professional. For example, Figures 7 and 8 show the distributions of the forecasted arrivals and occupancy (respectively) at the 30 days ahead snapshot. From these figures one can discover interesting facts, for example the right skewness of the distribution, and the very low probability of getting less than 7 or 8 reservations.

# 9 Conclusions

In this paper we have proposed a new model for hotel arrivals and occupancy forecasting using Monte Carlo simulation. The proposed model has two main phases. In the first phase we estimate the parameters related to the reservations process. In the second phase we simulate the reservations process forward in time, making use of the estimated parameters obtained in Phase

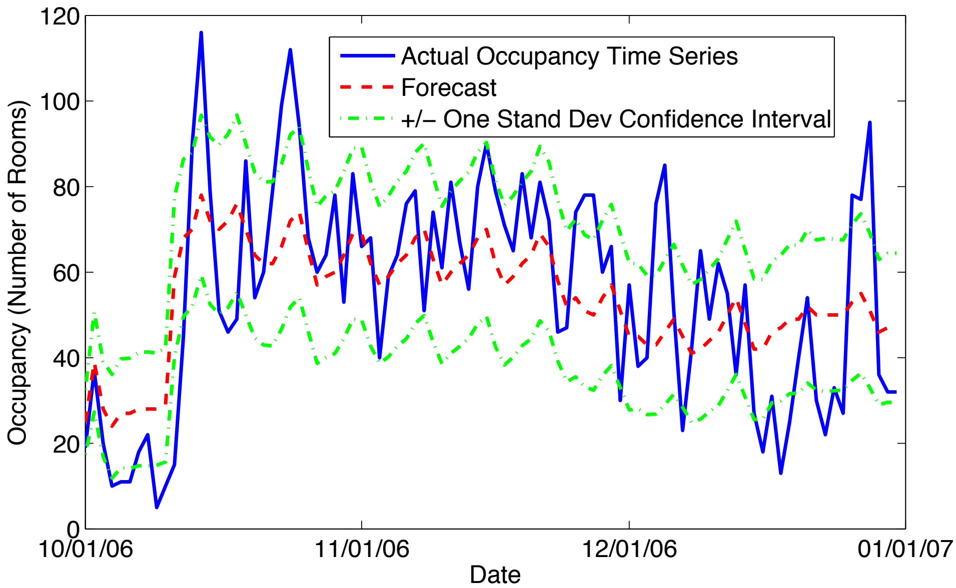


Figure 6: The Forecast Versus the Actual for the Occupancy for the First Three-Months Ahead Forecast Period

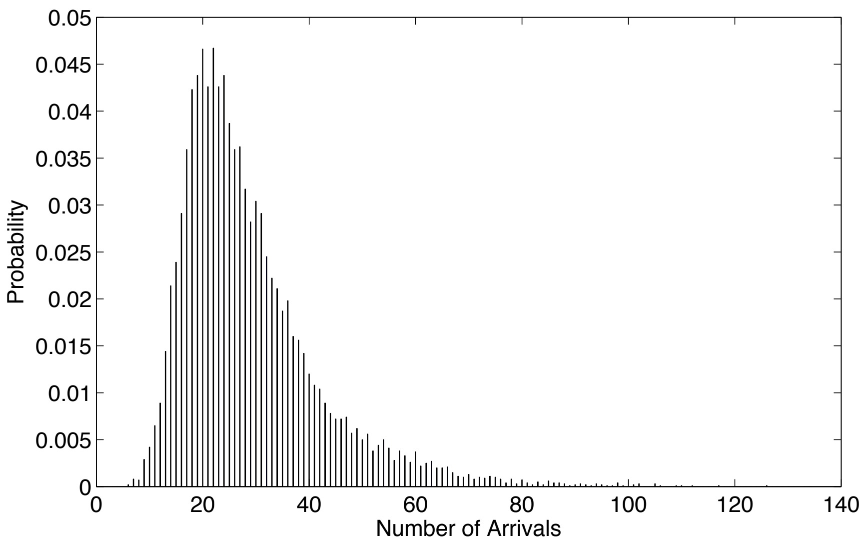


Figure 7: The Forecast Distribution of the Arrivals for Day Thirty Snapshot (Each Bar Corresponds to a Specific Number of Rooms)

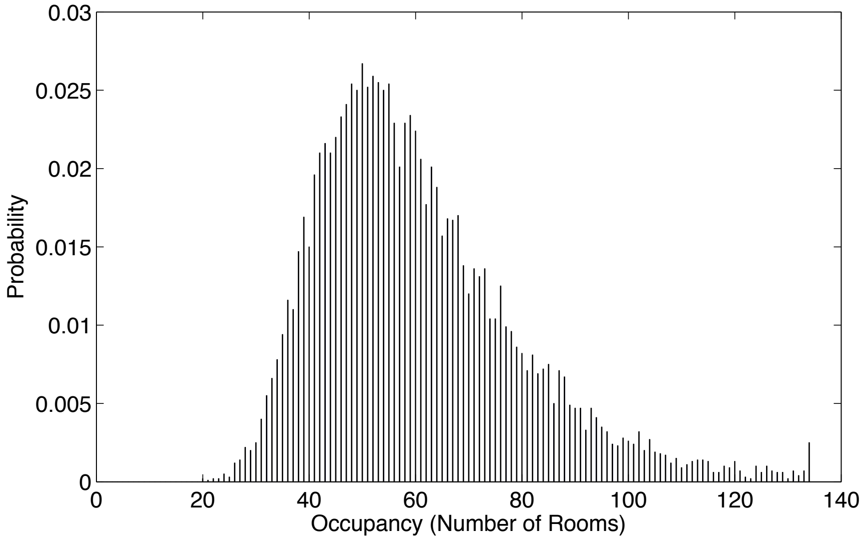


Figure 8: The Forecast Distribution of the Occupancy for Day Thirty Snapshot (Each Bar Corresponds to a Specific Number of Rooms)

1. We considered as a case study the Plaza Hotel of Alexandria, Egypt. The proposed forecasting model achieves good forecasting accuracy and beats other competing forecasting models. It also exhibits other nice features, such as obtaining densities for any variable of interest. In other words, it estimates the whole picture of what will happen in the future for all processes, and in a probabilistic way.

# Appendix

Table 4 shows the different seasonal periods for Plaza Hotel, as determined by the managers. Shown is the very low season period and the high season periods. Any other period is considered low season. We made use of these periods to determine the seasonal average.

# Acknowledgement

We would like to acknowledge the help of Hossam Shehata of Alexandria University. His help has been invaluable in giving us information and insights about the hotel business, and in interfacing with Plaza Hotel managers.

Table 4: The Dates of the Different Seasonal Regimes for Plaza Hotel (the Rest of the Days are Low Season Days)

| **Start Date** | **End Date** | **Occasion** | **Season Type** |
|---|---|---|---|
| 05/01/2006 | 14/01/2006 | Eid Adha | High Season |
| 28/03/2006 | 03/04/2006 | Petroleum Convention | High Season |
| 20/04/2006 | 26/04/2006 | Easter | High Season |
| 15/06/2006 | 15/09/2006 | Summer | High Season |
| 19/09/2006 | 18/10/2006 | Ramadan | Very Low Season |
| 19/10/2006 | 28/10/2006 | Eid Fitr | High Season |
| 28/12/2006 | 07/01/2007 | Eid Adha | High Season |
| 05/04/2007 | 11/04/2007 | Easter | High Season |
| 15/06/2007 | 15/09/2007 | Summer | High Season |
| 11/09/2007 | 10/10/2007 | Ramadan | Very Low Season |
| 11/10/2007 | 20/10/2007 | Eid Fitr | High Season |
| 17/12/2007 | 25/12/2007 | Eid Adha | High Season |
| 24/04/2008 | 03/05/2008 | Easter | High Season |
| 18/05/2008 | 23/05/2008 | Petroleum Convention | High Season |
| 01/06/2008 | 31/08/2008 | Summer | High Season |
| 25/08/2008 | 24/09/2008 | Ramadan | Very Low Season |
| 25/09/2008 | 06/10/2008 | Eid Fitr | High Season |
| 04/12/2008 | 13/12/2008 | Eid Adha | High Season |

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