

Homework 5 Q2

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Read in data

```
crime <- read.table("uscrime.txt", header =T)
head(crime)
```

```
##      M So   Ed Po1 Po2   LF M.F Pop   NW   U1 U2 Wealth Ineq
## 1 15.1  1  9.1  5.8  5.6 0.510 95.0  33 30.1 0.108 4.1   3940 26.1
## 2 14.3  0 11.3 10.3  9.5 0.583 101.2  13 10.2 0.096 3.6   5570 19.4
## 3 14.2  1  8.9  4.5  4.4 0.533  96.9  18 21.9 0.094 3.3   3180 25.0
## 4 13.6  0 12.1 14.9 14.1 0.577  99.4 157  8.0 0.102 3.9   6730 16.7
## 5 14.1  0 12.1 10.9 10.1 0.591  98.5  18  3.0 0.091 2.0   5780 17.4
## 6 12.1  0 11.0 11.8 11.5 0.547  96.4  25  4.4 0.084 2.9   6890 12.6
##      Prob      Time Crime
## 1 0.084602 26.2011    791
## 2 0.029599 25.2999   1635
## 3 0.083401 24.3006    578
## 4 0.015801 29.9012   1969
## 5 0.041399 21.2998   1234
## 6 0.034201 20.9995    682
```

Set up model w/ all predictors

```
model <- lm(Crime ~., crime)
summary(model)
```

```
##
## Call:
## lm(formula = Crime ~ ., data = crime)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -395.74  -98.09   -6.69   112.99   512.67
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -5.984e+03  1.628e+03  -3.675  0.000893 ***
## M              8.783e+01  4.171e+01   2.106  0.043443 *
## So            -3.803e+00  1.488e+02  -0.026  0.979765
## Ed             1.883e+02  6.209e+01   3.033  0.004861 **
## Po1            1.928e+02  1.061e+02   1.817  0.078892 .
## Po2           -1.094e+02  1.175e+02  -0.931  0.358830
## LF            -6.638e+02  1.470e+03  -0.452  0.654654
## M.F            1.741e+01  2.035e+01   0.855  0.398995
## Pop           -7.330e-01  1.290e+00  -0.568  0.573845
## NW              4.204e+00  6.481e+00   0.649  0.521279
```

```
## U1          -5.827e+03  4.210e+03  -1.384 0.176238
## U2          1.678e+02  8.234e+01   2.038 0.050161 .
## Wealth      9.617e-02  1.037e-01   0.928 0.360754
## Ineq        7.067e+01  2.272e+01   3.111 0.003983 **
## Prob       -4.855e+03  2.272e+03  -2.137 0.040627 *
## Time       -3.479e+00  7.165e+00  -0.486 0.630708
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 209.1 on 31 degrees of freedom
## Multiple R-squared:  0.8031, Adjusted R-squared:  0.7078
## F-statistic: 8.429 on 15 and 31 DF,  p-value: 3.539e-07
```

Predict with model

```
newdata <- data.frame('M' = 14.0,
                      'So' = 0,
                      'Ed' = 10.0,
                      'Po1' = 12.0,
                      'Po2' = 15.5,
                      'LF' = 0.640,
                      'M.F' = 94.0,
                      'Pop' = 150,
                      'NW' = 1.1,
                      'U1' = 0.120,
                      'U2' = 3.6,
                      'Wealth' = 3200,
                      'Ineq' = 20.1,
                      'Prob' = 0.04,
                      'Time' = 39.0)
pred1 <- predict(model, newdata)
```

Set up model w/ select predictors using stepAIC function in R

```
library(MASS)
model2 <- stepAIC(model)

## Start:  AIC=514.65
## Crime ~ M + So + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 +
##      U2 + Wealth + Ineq + Prob + Time
##
##           Df Sum of Sq    RSS    AIC
## - So        1      29 1354974 512.65
## - LF        1     8917 1363862 512.96
## - Time      1    10304 1365250 513.00
## - Pop       1    14122 1369068 513.14
## - NW        1    18395 1373341 513.28
## - M.F       1    31967 1386913 513.74
## - Wealth    1    37613 1392558 513.94
## - Po2       1    37919 1392865 513.95
## <none>             1354946 514.65
```

```

## - U1      1      83722 1438668 515.47
## - Po1     1      144306 1499252 517.41
## - U2      1      181536 1536482 518.56
## - M       1      193770 1548716 518.93
## - Prob    1      199538 1554484 519.11
## - Ed      1      402117 1757063 524.86
## - Ineq    1      423031 1777977 525.42
##
## Step: AIC=512.65
## Crime ~ M + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 + U2 +
##      Wealth + Ineq + Prob + Time
##
##      Df Sum of Sq      RSS      AIC
## - Time      1      10341 1365315 511.01
## - LF         1      10878 1365852 511.03
## - Pop        1      14127 1369101 511.14
## - NW         1      21626 1376600 511.39
## - M.F        1      32449 1387423 511.76
## - Po2        1      37954 1392929 511.95
## - Wealth     1      39223 1394197 511.99
## <none>              1354974 512.65
## - U1         1      96420 1451395 513.88
## - Po1        1      144302 1499277 515.41
## - U2         1      189859 1544834 516.81
## - M          1      195084 1550059 516.97
## - Prob       1      204463 1559437 517.26
## - Ed         1      403140 1758114 522.89
## - Ineq       1      488834 1843808 525.13
##
## Step: AIC=511.01
## Crime ~ M + Ed + Po1 + Po2 + LF + M.F + Pop + NW + U1 + U2 +
##      Wealth + Ineq + Prob
##
##      Df Sum of Sq      RSS      AIC
## - LF         1      10533 1375848 509.37
## - NW         1      15482 1380797 509.54
## - Pop        1      21846 1387161 509.75
## - Po2        1      28932 1394247 509.99
## - Wealth     1      36070 1401385 510.23
## - M.F        1      41784 1407099 510.42
## <none>              1365315 511.01
## - U1         1      91420 1456735 512.05
## - Po1        1      134137 1499452 513.41
## - U2         1      184143 1549458 514.95
## - M          1      186110 1551425 515.01
## - Prob       1      237493 1602808 516.54
## - Ed         1      409448 1774763 521.33
## - Ineq       1      502909 1868224 523.75
##
## Step: AIC=509.37
## Crime ~ M + Ed + Po1 + Po2 + M.F + Pop + NW + U1 + U2 + Wealth +
##      Ineq + Prob
##
##      Df Sum of Sq      RSS      AIC

```

```

## - NW      1      11675 1387523 507.77
## - Po2     1      21418 1397266 508.09
## - Pop     1      27803 1403651 508.31
## - M.F     1      31252 1407100 508.42
## - Wealth  1      35035 1410883 508.55
## <none>                1375848 509.37
## - U1      1      80954 1456802 510.06
## - Po1     1     123896 1499744 511.42
## - U2      1     190746 1566594 513.47
## - M       1     217716 1593564 514.27
## - Prob    1     226971 1602819 514.54
## - Ed      1     413254 1789103 519.71
## - Ineq    1     500944 1876792 521.96
##
## Step:  AIC=507.77
## Crime ~ M + Ed + Po1 + Po2 + M.F + Pop + U1 + U2 + Wealth + Ineq +
##      Prob
##
##      Df Sum of Sq      RSS      AIC
## - Po2    1      16706 1404229 506.33
## - Pop    1      25793 1413315 506.63
## - M.F    1      26785 1414308 506.66
## - Wealth 1      31551 1419073 506.82
## <none>                1387523 507.77
## - U1     1      83881 1471404 508.52
## - Po1    1     118348 1505871 509.61
## - U2     1     201453 1588976 512.14
## - Prob   1     216760 1604282 512.59
## - M      1     309214 1696737 515.22
## - Ed     1     402754 1790276 517.74
## - Ineq   1     589736 1977259 522.41
##
## Step:  AIC=506.33
## Crime ~ M + Ed + Po1 + M.F + Pop + U1 + U2 + Wealth + Ineq +
##      Prob
##
##      Df Sum of Sq      RSS      AIC
## - Pop    1      22345 1426575 505.07
## - Wealth 1      32142 1436371 505.39
## - M.F    1      36808 1441037 505.54
## <none>                1404229 506.33
## - U1     1      86373 1490602 507.13
## - U2     1     205814 1610043 510.76
## - Prob   1     218607 1622836 511.13
## - M      1     307001 1711230 513.62
## - Ed     1     389502 1793731 515.83
## - Ineq   1     608627 2012856 521.25
## - Po1    1    1050202 2454432 530.57
##
## Step:  AIC=505.07
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Wealth + Ineq + Prob
##
##      Df Sum of Sq      RSS      AIC
## - Wealth 1      26493 1453068 503.93

```

```

## <none>          1426575 505.07
## - M.F      1      84491 1511065 505.77
## - U1      1      99463 1526037 506.24
## - Prob    1      198571 1625145 509.20
## - U2      1      208880 1635455 509.49
## - M      1      320926 1747501 512.61
## - Ed      1      386773 1813348 514.35
## - Ineq    1      594779 2021354 519.45
## - Po1     1     1127277 2553852 530.44
##
## Step:  AIC=503.93
## Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Ineq + Prob
##
##           Df Sum of Sq      RSS      AIC
## <none>          1453068 503.93
## - M.F    1      103159 1556227 505.16
## - U1     1      127044 1580112 505.87
## - Prob   1      247978 1701046 509.34
## - U2     1      255443 1708511 509.55
## - M      1      296790 1749858 510.67
## - Ed     1      445788 1898855 514.51
## - Ineq   1      738244 2191312 521.24
## - Po1    1     1672038 3125105 537.93
summary(model2)

##
## Call:
## lm(formula = Crime ~ M + Ed + Po1 + M.F + U1 + U2 + Ineq + Prob,
##     data = crime)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -444.70 -111.07   3.03  122.15  483.30
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -6426.10     1194.61  -5.379 4.04e-06 ***
## M              93.32       33.50   2.786 0.00828 **
## Ed            180.12       52.75   3.414 0.00153 **
## Po1           102.65       15.52   6.613 8.26e-08 ***
## M.F           22.34       13.60   1.642 0.10874
## U1          -6086.63     3339.27  -1.823 0.07622 .
## U2           187.35       72.48   2.585 0.01371 *
## Ineq          61.33       13.96   4.394 8.63e-05 ***
## Prob        -3796.03     1490.65  -2.547 0.01505 *
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 195.5 on 38 degrees of freedom
## Multiple R-squared:  0.7888, Adjusted R-squared:  0.7444
## F-statistic: 17.74 on 8 and 38 DF,  p-value: 1.159e-10

```

Predict with model2

```
pred2 <- predict(model2, newdata)
```

Compare adjusted r-squared values

```
data.frame('model1' = summary(model)$adj.r.squared, 'model2' = summary(model2)$adj.r.squared)

##      model1      model2
## 1 0.7078062 0.7443692
```

In comparing the predictions, we find the result from model2 more reasonable as it is within the range of Crime values in the data set.

```
data.frame('model1' = pred1, 'model2' = pred2)

##      model1      model2
## 1 155.4349 1038.413

range(crime$Crime)

## [1] 342 1993
```