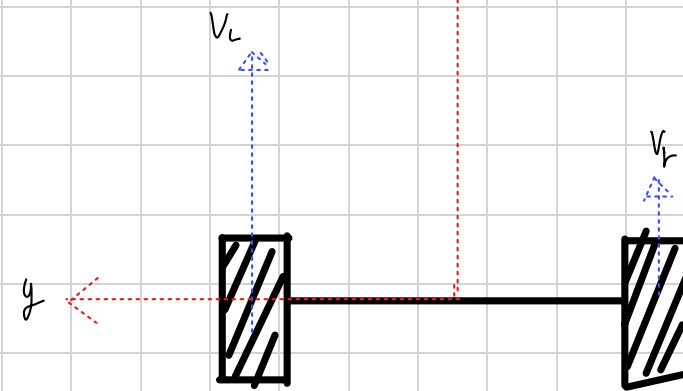


$${}^G P_R = \begin{bmatrix} x_p \\ y_p \\ \theta \end{bmatrix}$$

$${}^G \dot{P}_R = f(l, r, \theta, \dot{\phi}_r, \dot{\phi}_l)$$

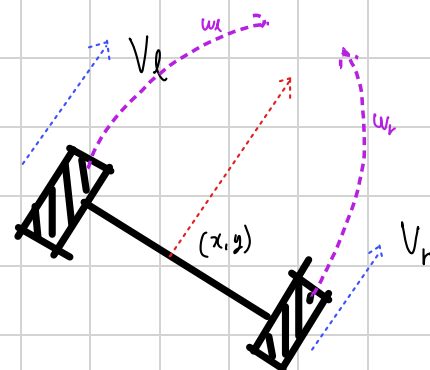
1) \dot{x}, \dot{y}



$$\dot{x} = \frac{1}{2}(V_r + V_l)$$

$$\dot{y} = 0$$

2) $\dot{\theta}$



$$\dot{\theta} = \omega_r + \omega_l$$

$$= \frac{V_r}{2l} - \frac{V_l}{2l}$$

3) Jacobian matrix

$$\begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} \frac{1}{2}V_r + \frac{1}{2}V_l \\ 0 \\ \frac{1}{2l}V_r - \frac{1}{2l}V_l \end{bmatrix} = \begin{bmatrix} \frac{1}{2}r\dot{\phi}_r + \frac{1}{2}r\dot{\phi}_l \\ 0 \\ \frac{1}{2l}r\dot{\phi}_r - \frac{1}{2l}r\dot{\phi}_l \end{bmatrix} = \frac{r}{2l} \begin{bmatrix} l & l \\ 0 & 0 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \dot{\phi}_r \\ \dot{\phi}_l \end{bmatrix}$$

4) Jacobian matrix

$${}^G \dot{P}_R = R^T(\theta) \begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \begin{bmatrix} \cos\theta & \sin\theta & 0 \\ -\sin\theta & \cos\theta & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \dot{x} \\ \dot{y} \\ \dot{\theta} \end{bmatrix} = \frac{r}{2l} \begin{bmatrix} c & s & 0 \\ -s & c & 0 \\ 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} l & l \\ 0 & 0 \\ 1 & -1 \end{bmatrix} \begin{bmatrix} \dot{\phi}_r \\ \dot{\phi}_l \end{bmatrix}$$