# Unsupervised learning

### **Supervised Learning**

- Data: labeled data, feature-response pairs (x, y)
- Goal: to learn a mapping from x to y
- Problem type:
  - Classification
  - Regression

## **Unsupervised Learning**

- Data: *unlabeled* data, features x
- Goal: to uncover hidden structure, patterns, clusters, ...
- Typical tasks
  - Clustering analysis: cluster features or observations into groups with common traits
  - Dimension reduction: transform data from high-dimensional space to a low-dimensional space while preserving as much information as possible
  - **.....**

# Reinforcement Learning

- Data: a sequence of state-action pairs and a cumulative reward
- Goal: to learn a policy (a mapping from state to action) that maximizes the cumulative reward.
- Typical applications:
  - Game-playing (e.g., AlphaGo, Dota2),
  - Robotics control
  - **.....**

### **Quick Summary**

Aspect	Supervised Learning	Unsupervised Learning	Reinforcement Learning
Goal	Learn a mapping from $x$ to $y$	Discover hidden structure/patterns in $\boldsymbol{x}$	Learn a policy that maximizes reward

Aspect	Supervised Learning	Unsupervised Learning	Reinforcement Learning
Data	Labeled data	Unlabeled data	State-action pairs, and delayed rewards
Typical output	Classification or regression model	Clusters, low-dimensional embeddings	Policy

### **Clustering Analysis**

- Popular techniques in analysis of complex data (e.g., genomics data)
- · Aims to detecting homogeneous subgroups among the observations or the features
- Identities of the learned subgroups are unknown, but can often lead to meaningful interpretation after linked with additional information.
- We can cluster observations or features.
  - observations: clustering cancer samples to find similar cancer sub-types
  - features: clustering genes based on similar functions

# Meaningful clusters

Without the groundtruth labels, how do we claim that our clusters results are meaningful?

Link to a clustering playground

### Similarity and dissimilarity measures

Often we have to come up with numeric metrics to measure the similarity or dissimilarity between observations

- Similarity measures
  - Pearson correlation
  - Spearman correlation
  - Kendall's au
- Dissimilarity measures
  - Euclidean distance
  - Manhattan distance

### Similarity measures

When the features are numeric:

• Pearson correlation: This is the "usual" correlation coefficient, and measures the **linear** association between  $X_i$  and  $X_j$ .

- Spearman correlation. This is essentially the Pearson correlation applied to ranked observations.
- Kendall's  $\tau$ . This correlation coefficient uses directly rankings among pairs of observations.

• .....

When the features are not numeric...

### Dissimilarity measure

• Euclidean distance: sum of squared difference between feature values ( $\ell_2$ -norm)

$$d_E(i,j) = \left[\sum_{l=1}^p (X_{i,l} - X_{j,l})^2
ight]^{1/2}$$

• Manhattan distance: sum of absolute difference between feature values ( $\ell_1$ -norm)

$$d_M(i,j) = \sum_{l=1}^p |X_{i,l} - X_{j,l}|$$

• ......

Checkout this example.

## **Common Clustering Methods**

- Hierarchical clustering
  - Sequence of solutions organized in a hierarchical tree structure, called the dendrogram
  - Maintain a hierarchical structure

When the number of clusters decrease, observations in the same cluster stays in the same cluster

- k-Means clustering
  - One of the most popular clustering method
  - Computationally efficient
  - lacktriangledown No hierarchy among clusters When k decreases, observations in the same clusters might be reassigned to different clusters
- And many other methods

### **Dimension Reduction**

- Goal: to transform data from a high-dimensional space to a low-dimensional space, without losing too much information
- Versatile tools for
  - Exploratory data analysis (e.g., tSNE)
  - Data processing for downstream analysis (e.g., principal component regression)
  - Uncover true latent pattern (e.g., intrinsic dimension of neural activities)
- Typical methods:
  - Principal Component Analysis (PCA)
  - t-distributed Stochastic Neighbor Embedding (tSNE)

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