

# NEURONS AND NEURONAL NETWORKS

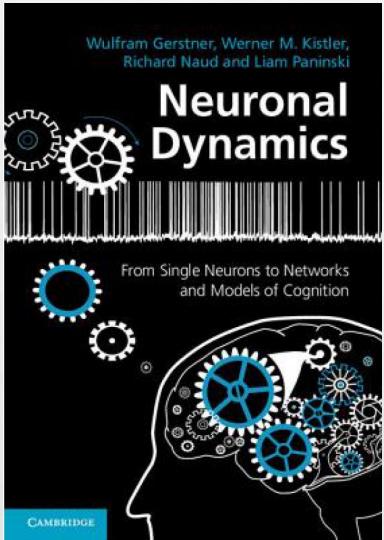
WONKWON LEE

27<sup>TH</sup> NOVEMBER 2017

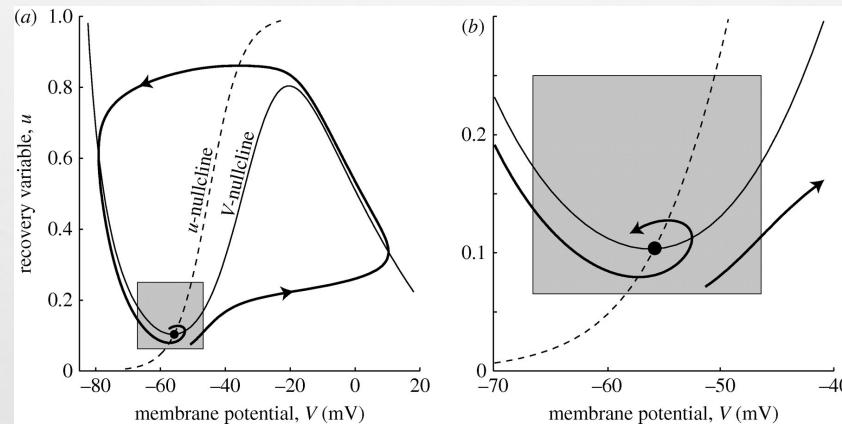
SUPERVISOR: DR. EVA NAVARRO LOPEZ



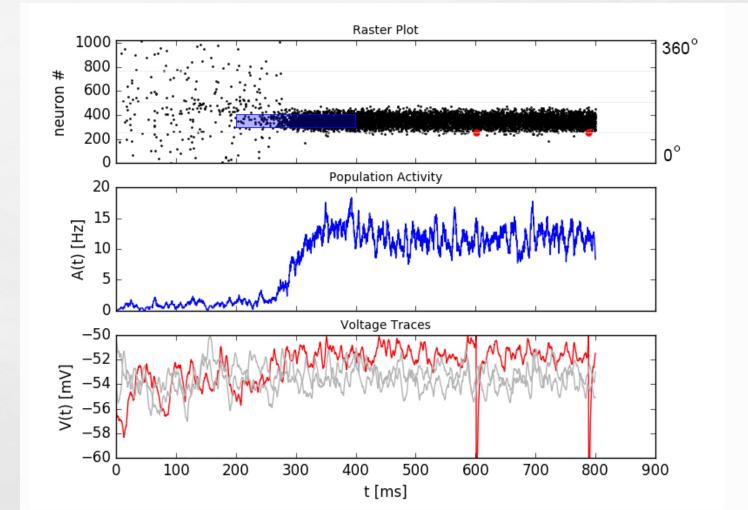
# ABOUT PROJECT



Research



Modelling

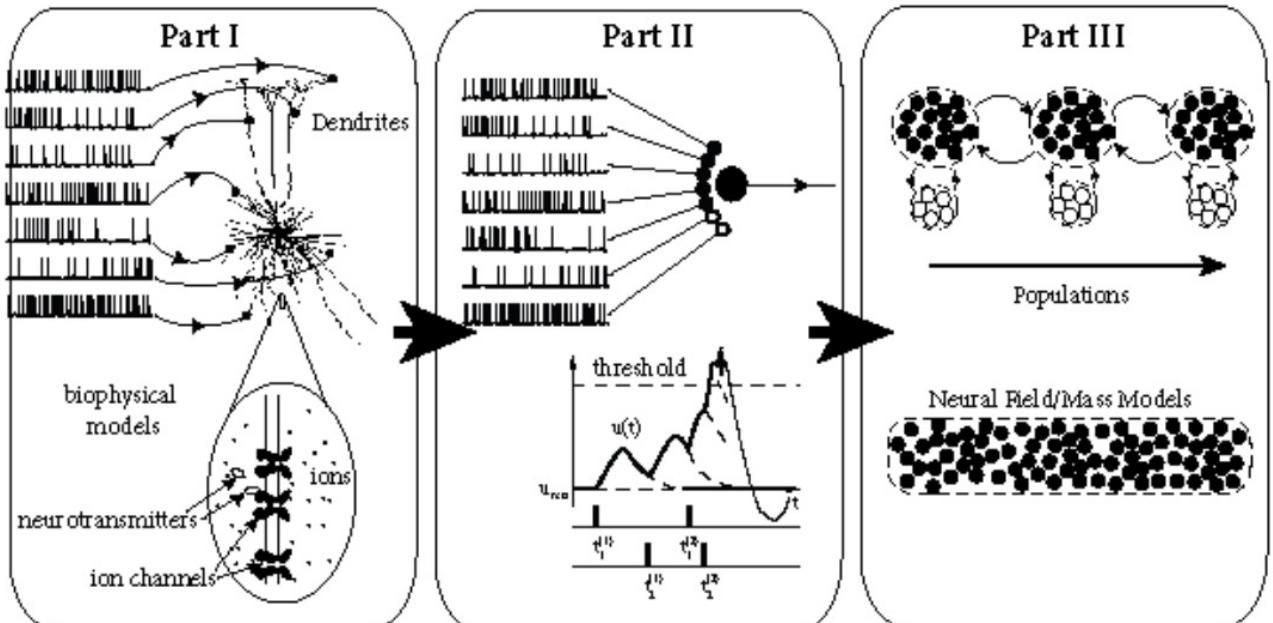


Simulation

# GOALS

- Use Hebbian rule to mathematically model **synaptic plasticity**
- Integrate the models with the neuronal networks
- Analyze how **synaptic plasticity** affects neuronal networks behaviours

# IMPLEMENT



Biophysical  
Neuron

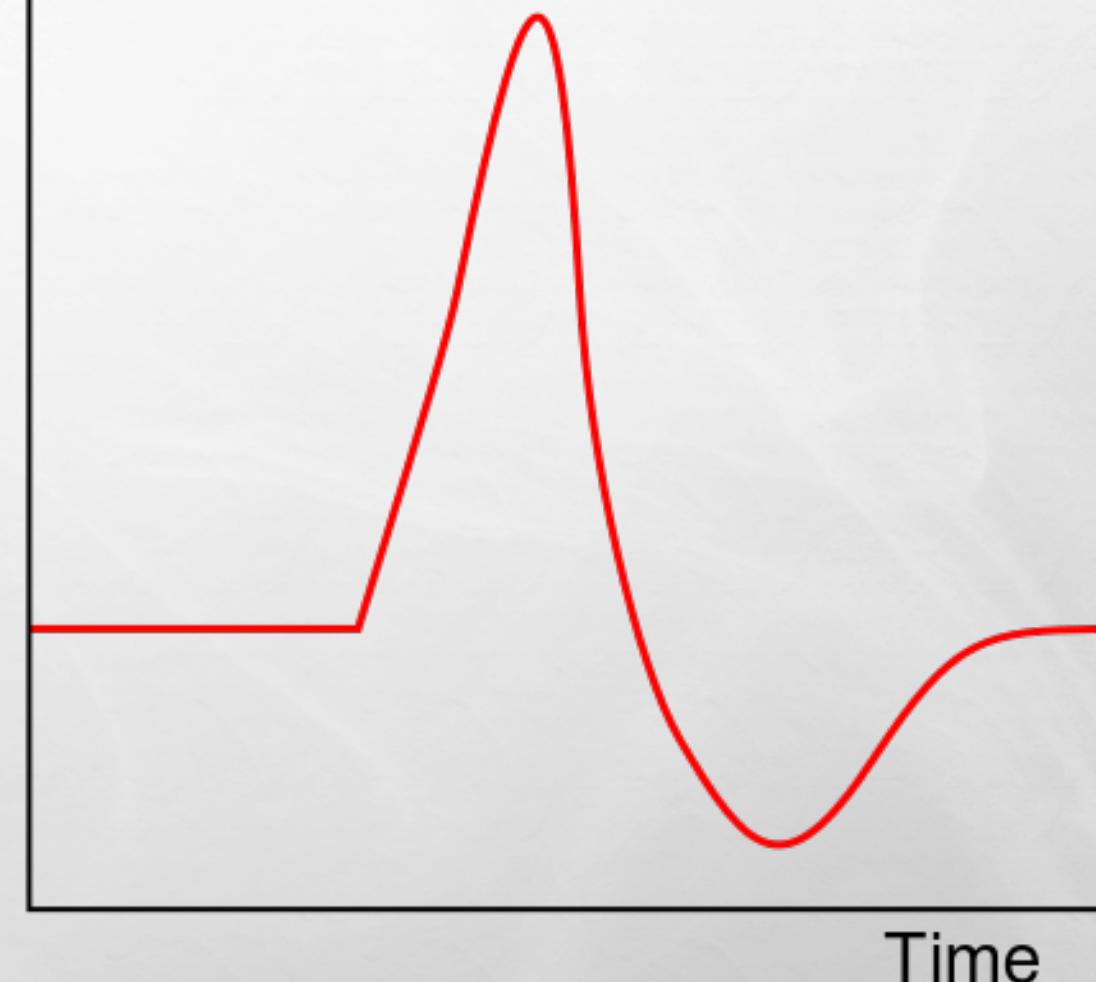
Mathematical  
Model

Neuronal  
Network

# What is a neuron?

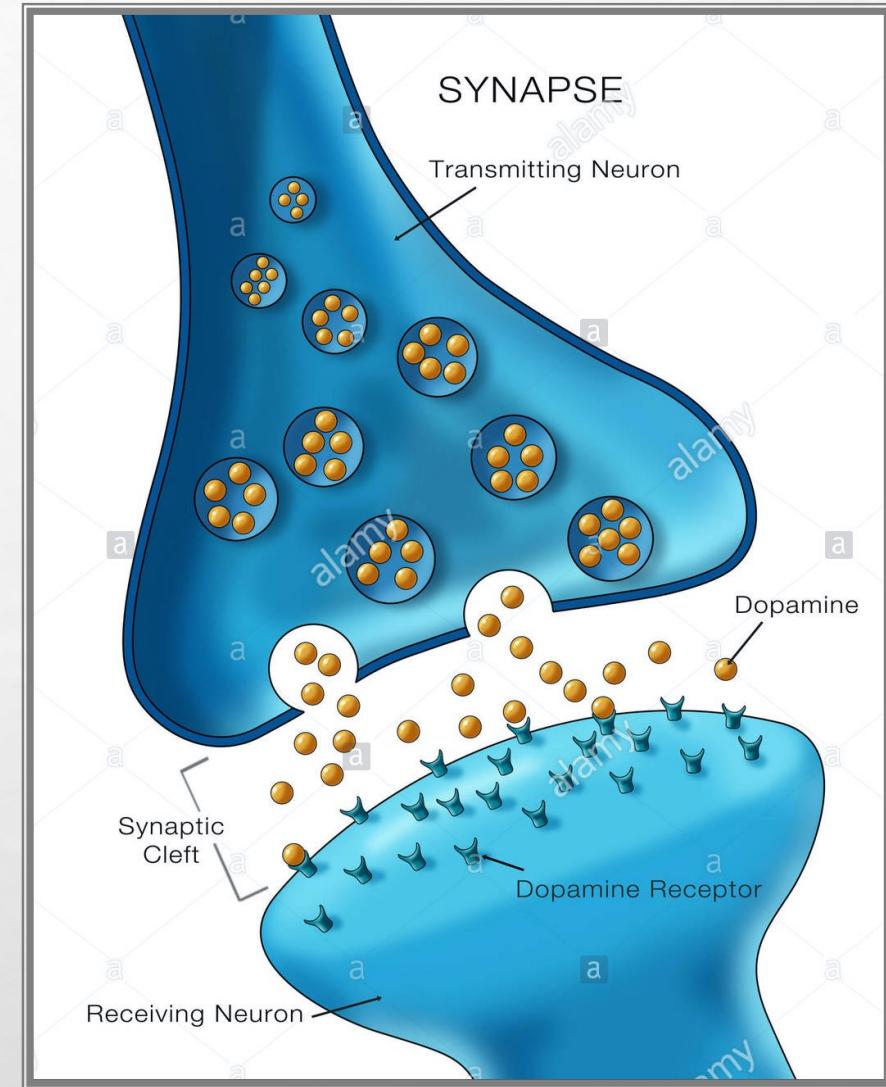
- A neuron is an electrically excitable cell that receives, processes, and transmits information
- Neuron 'spikes' when membrane potential rapidly rises and falls

Membrane potential

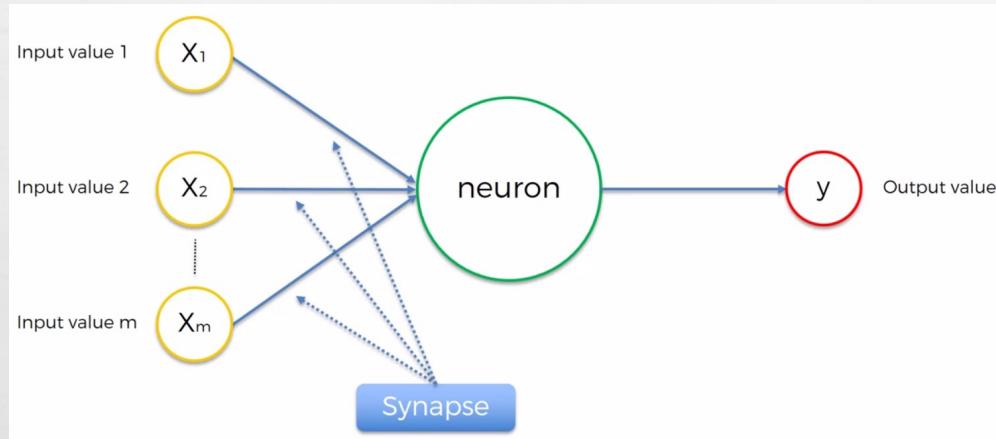


# SYNAPSE?

- The **junction** between two neurons
- Synapse permits a neuron to pass an **electrical signal** to another neuron
- Synapse plays a role in the formation of **memory**



# MODELLING A SINGLE NEURON



$$I(t) = C_m \frac{dV_m(t)}{dt}$$

*Simply a relationship between input membrane current and output membrane voltage*

# LEAKY INTEGRATE-FIRE MODEL

$$I(t) = C_m \frac{dV_m(t)}{dt}$$

Adding “leak” term

$$I(t) - \frac{V_m(t)}{R_m} = C_m \frac{dV_m(t)}{dt}$$

$$\tau_m \frac{du}{dt} = -[u(t) - u_{\text{rest}}] + RI(t)$$

if  $u(t) = \vartheta$  then  $\lim_{\delta \rightarrow 0; \delta > 0} u(t + \delta) = u_r$

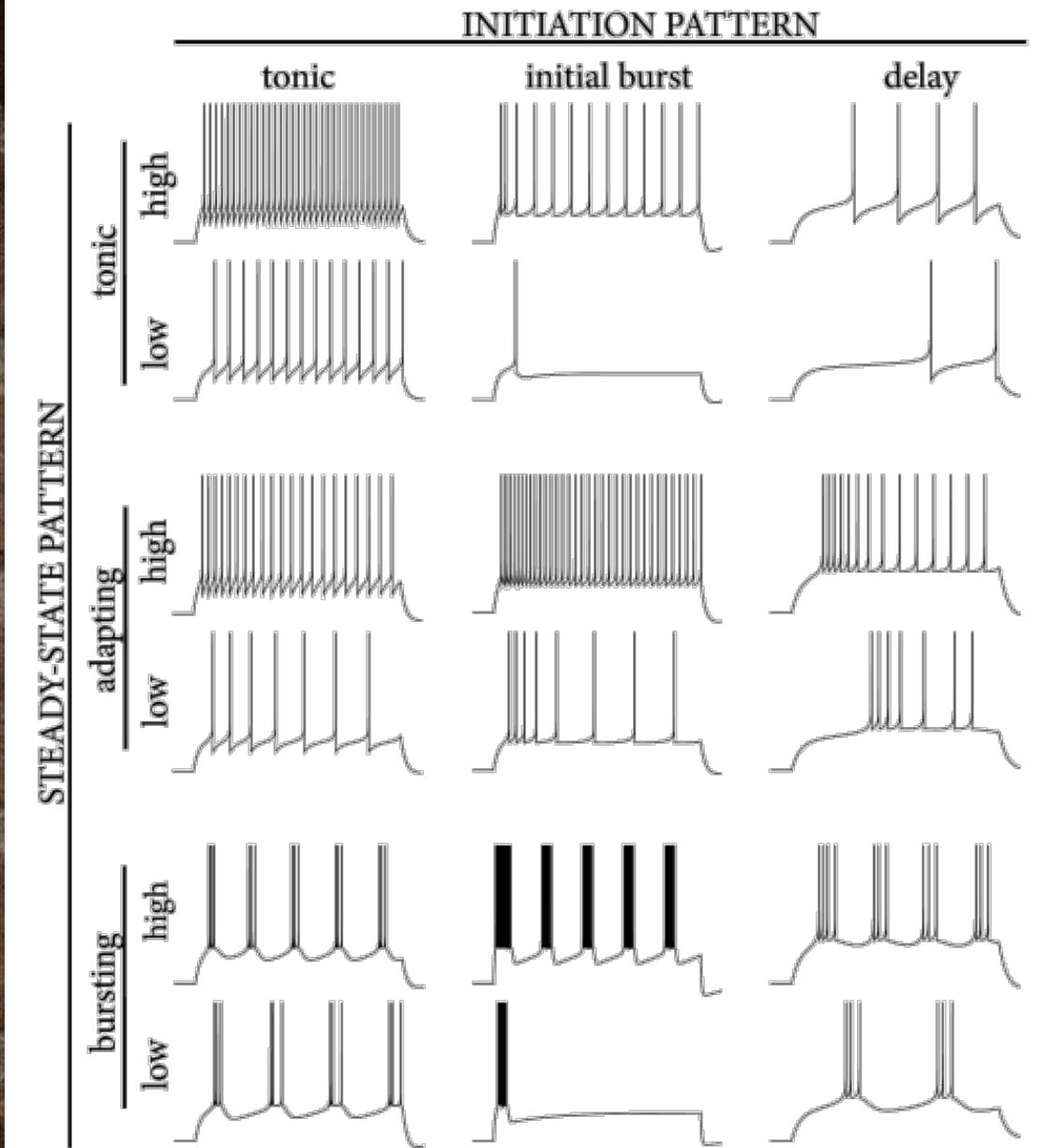
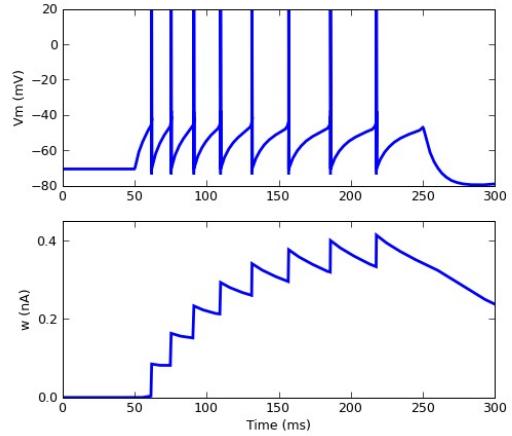
# LIMITATIONS OF LIF MODEL

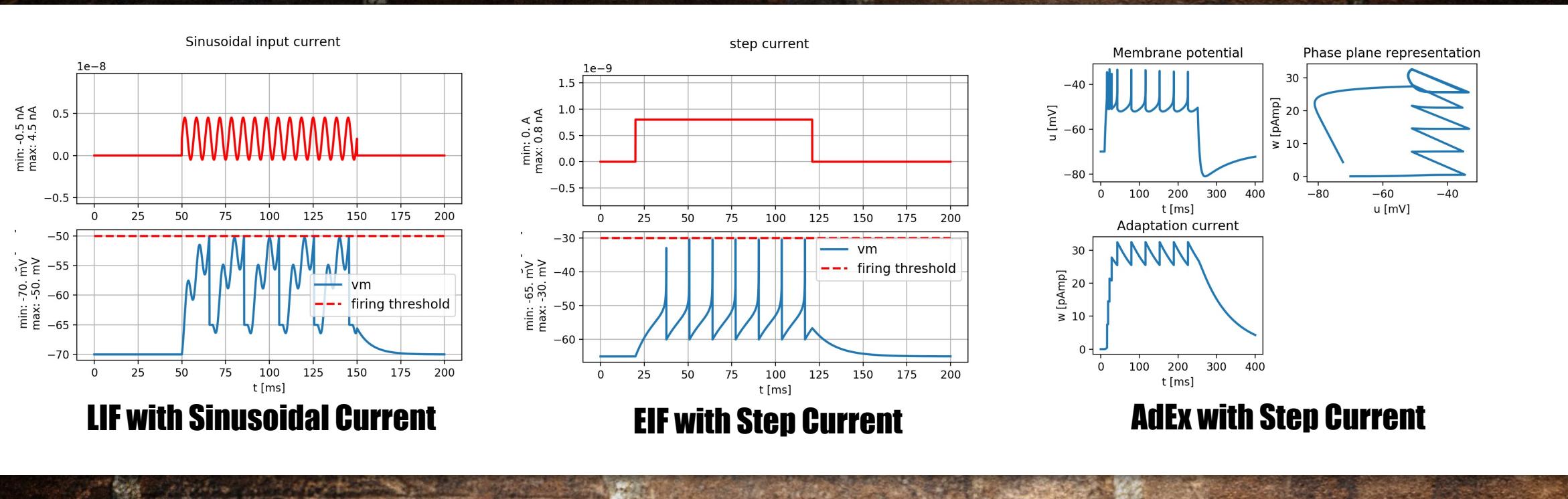
## Quadratic IF vs Exponential IF

- $\tau_m \frac{dv}{dt} = a_0(v - E_m)(v - v_{thresh}) + R_m I$  **linear**
  - **The model is linear**
  - $a_0 > 0, E_m < v_{thresh} < E_{thresh}$
  - **After each spike, the membrane potential is reset; loses memory of previous spikes**
- $$\tau \frac{du}{dt} = -(u - u_{rest}) + \Delta_T \exp\left(\frac{u - \vartheta_{rh}}{\Delta_T}\right) + RI;$$

# ADAPTIVE EXPONENTIAL INTEGRATE-FIRE MODEL

$$\begin{aligned}\tau_m \frac{du}{dt} &= -(u - u_{\text{rest}}) + \Delta_T \exp\left(\frac{u - \vartheta_{rh}}{\Delta_T}\right) - R w + R I(t) \\ \tau_w \frac{dw}{dt} &= a(u - u_{\text{rest}}) - w + b \tau_w \sum_{t^{(f)}} \delta(t - t^{(f)}) .\end{aligned}$$



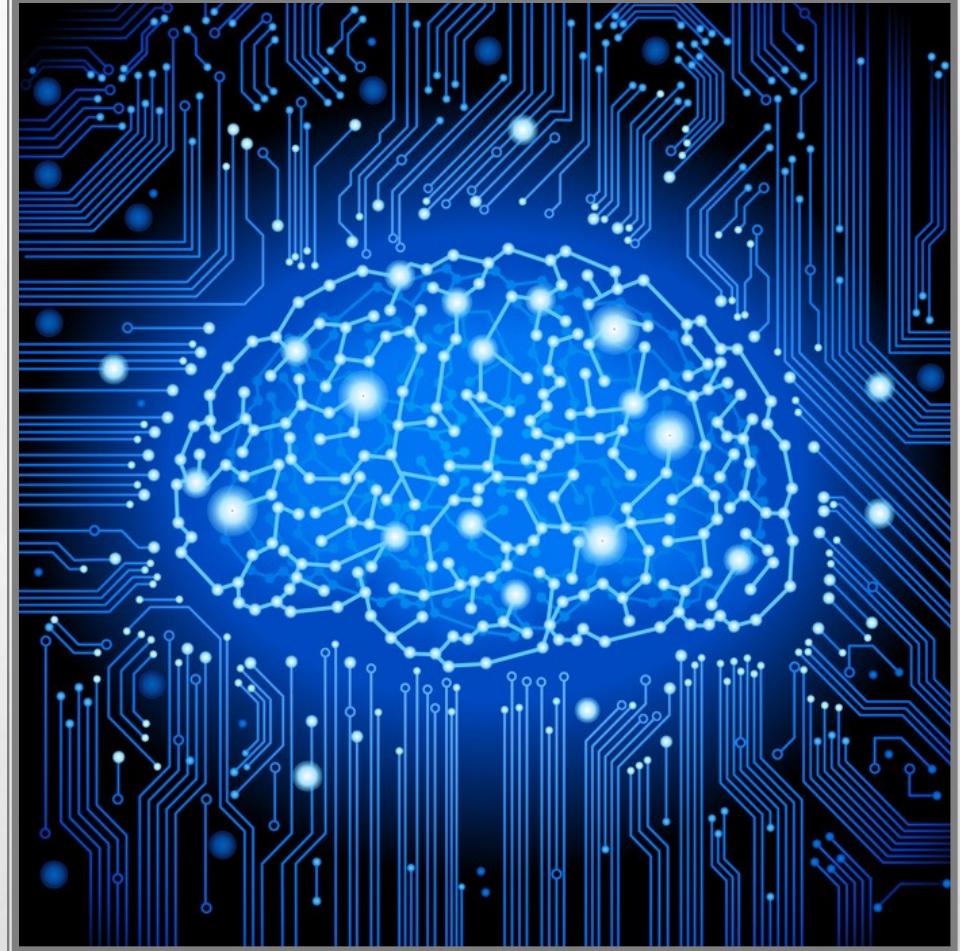


# PRELIMINARY RESULT



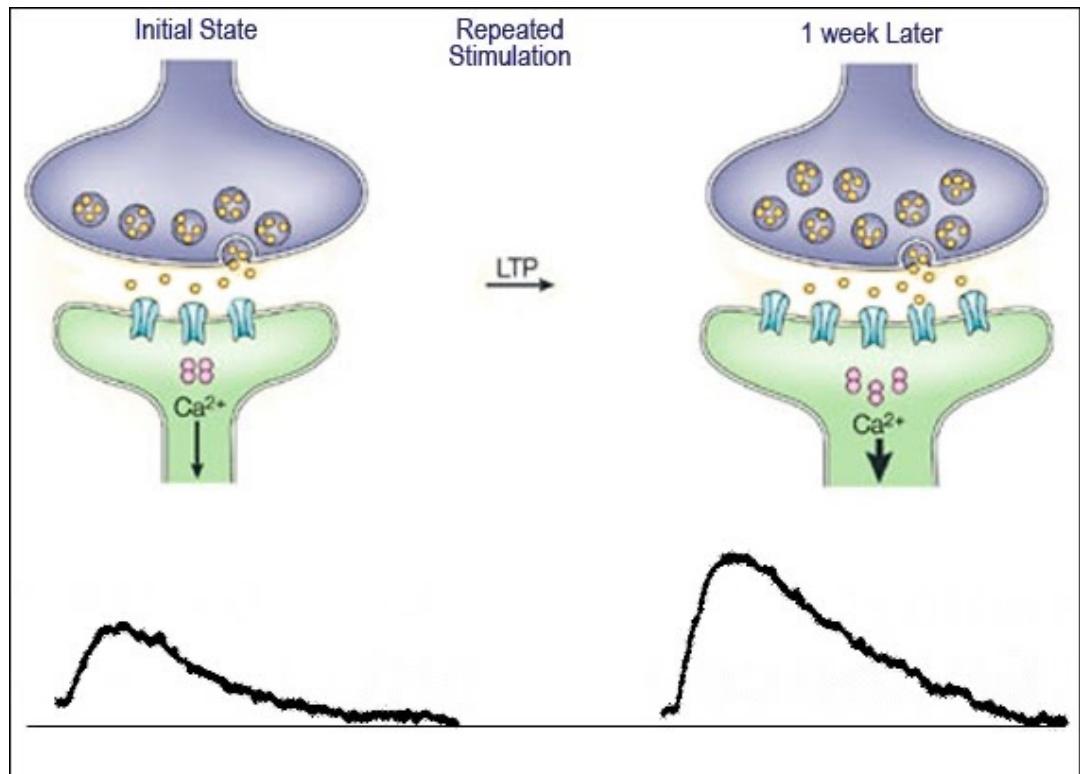
# HOW TO MODEL A NETWORK?

- 1. How many neurons should be created in a network?  
Excitatory & inhibitory with a ratio of 4:1**
  
- 2. How to synchronize neurons?  
Oscillation**
  
- 3. How to make neurons interact?  
Give certain number of connections and weight**



# SYNAPSE PLASTICITY

- Ability of synapses to strengthen or weaken over time, in response to increases or decreases in their activity
- Long-Term Potentiation
- Use Spike-Timing-Dependent-Plasticity Model to measure
- Hebbian Rule



# PROJECT PLAN

- ✓ Develop background knowledge and mathematical understanding
- ✓ Test different simulation tools and decide which one to use for research
- ✓ Implement appropriate single neuron model and investigate the behaviour of the single neuron
- Implement networks of neurons and investigate neuronal behaviours
- Research on synapse plasticity and implement STDP models based on Hebb's rule
- Integrate STDP models to networks and investigate more complicated behaviours
- Analyse how synaptic plasticity can affect neuronal behaviours in short and long period of time

# REFERENCES

- Wulfram Gerstner, W Kistler, R Naud, L Paninski, "Neuronal Dynamics", Cambridge University Press 2014
- Eugene M. Izhikevich, "Dynamical Systems in Neuroscience. The Geometry of Excitability and Bursting", The MIT Press 2010
- D Sterratt, B Graham, A Gillies, D Willshaw, "Principles of Computational Modelling in Neuroscience", Cambridge University Press 2011
- Wulfram Gerstner and Werner M. Kistler, "Spiking Neuron Models", Cambridge University Press 2002
- Caporale N, Dan Y, "Spike timing-dependent plasticity: a Hebbian learning rule". Annual Review of Neuroscience, 2008