

Semantic Analysis

The role of semantic analysis is to assign meaning

❏ "It smells fishy."

❏ Lexical analysis

- Tokenizes "It", "smells", "fishy", "."
- Determines noun, verb, adjective, punctuation token types

❏ Syntax analysis

- Parses the grammatical structure of the sentence

❏ Semantic analysis

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- Parses the grammatical structure of the sentence

❑ Semantic analysis

- Assigns meaning to the words "It", "smells", "fishy"
- Flags error if the sentence does not make sense

Semantic Analysis = Binding + Type Checking

- ❑ "I don't wanna eat that sushi."
 - "It smells fishy."
 - "It": the sushi
 - "smells": feels to my nose
 - "fishy": that the sushi has gone bad
- ❑ "The professor says that the exam is going to be easy."
 - "It smells fishy."
 - "It": the situation
 - "smells": feels to my sixth sense
 - "fishy": that it is highly suspicious

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"It smells fishy."
 - "It": the situation
 - "smells": feels to my sixth sense
 - "fishy": that it is highly suspicious
- ❑ Semantic analysis consists of two tasks
 - **Binding**: associating a pronoun to an object
 - **Type checking**: inferring meaning based on type of object

Semantic analysis cannot be done during parsing

❑ Context Free Grammars (CFGs) cannot recognize bindings

- Every use of a name needs to be bound to the declaration.
- Name can refer to a variable, function, class, ...
- Names are called **symbols** in semantic analysis

❑ To do bindings, a CFG must recognize this language:

$$\{\alpha c \alpha \mid \alpha \in (a|b)^*\}$$

The 1st α represents the declaration,

The 2nd α represents a use.

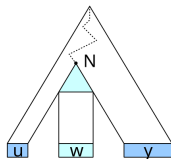
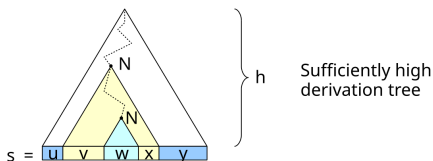
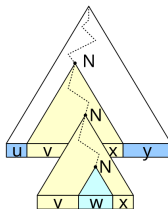
❑ Above language is a Context Sensitive Language

Why is $\{\alpha c \alpha \mid \alpha \in (a|b)^*\}$ not a CFG?

- ❑ We will base our proof on the **pumping lemma** for CFGs.
- ❑ **Pumping lemma:** a theorem about strings in a grammar
 - "lemma": a mathematical term for a theorem
 - "pumping": for a sufficiently long enough string, a substring exists within that string that can be "pumped" (repeated 0 or more times and still be in the language).
- ❑ For example, for the Regular Language $0(0|1)^*0$:
 - A string longer than 2 will look like 000, 010, 0100, ...
 - Let's take "010". Here, substring "1" can be pumped.
 - ("00", "010", "0110", "01110" are all in the language)
- ❑ Pumping Lemma applies to CFGs as well.

Pumping Lemma for CFGs

- For a sufficiently long string s derived from a CFG, s can be written as $s = uvwxy$ (u, v, w, x, y are substrings)
- Where v and x can be pumped and $|vx| \geq 1$.

Generating $uv^kwx^k y$ Generating $uv^kwx^k y$

$\{\alpha c \alpha \mid \alpha \in (a|b)^*\}$ is not a CFG

□ Let's say $s = uvwxy$ is a sufficiently long string in language $\{\alpha c \alpha \mid \alpha \in (a|b)^*\}$,

where v, x can be pumped and $|vx| \geq 1$.

1. The substring $vw x$ must bisect $\alpha c \alpha$.
 - If $vw x$ is contained in 1st α (or mostly contained), if we pump v and x 0 times, 1st α gets shorter than 2nd α .
 - string is no longer in $\{\alpha c \alpha \mid \alpha \in (a|b)^*\}$. Contradiction.
 - The same applies to when $vw x$ is contained in 2nd α .
2. Even when $vw x$ bisects $\alpha c \alpha$, pumping fails.
 - Let string s' be the result of pumping v and x 0 times.
 - Let's say $s' = \alpha_1 c \alpha_2$, where α_1 and α_2 are shortened versions of the 1st and 2nd α s.
 - While $|\alpha_1| = |\alpha_2|$, there exist α_1 and α_2 such that $\alpha_1 \neq \alpha_2$.
 - E.g. $s = abcab$, and $vw x = bca$ where $v = b$ and $x = a$. Then, α_1 becomes "a" and α_2 becomes "b". Contradiction.

Semantic analysis does binding and type checking

□ Semantic analysis performs binding

- Since CFGs cannot recognize bindings, as we just proved
- Done by traversing parse tree produced by syntax analysis
- Definitions are stored in data structure called **symbol table**
- Uses are bound to entries in the symbol table

□ Semantic analysis performs type checking

- Infer what " $a + b$ " means:
 - If a and b are ints, integer add and return int
 - If a and b are floats, FP add and return float
 - If a and b are strings, concatenate and return string
- Infer what " $a.foo()$ " means:
 - If object a is an instance of class A , call $A.foo()$
 - If object a is an instance of class B , call $B.foo()$
- Infer what " $a[i][j]$ " means:
 - Offset from a calculated based on type and dimensions

Semantic analysis also performs semantic checks

- ☐ All symbol uses have a corresponding declaration;
- ☐ All operations are type legal;
- ☐ Inheritance relationships are correct;
- ☐ A class is defined only once;
- ☐ A method in a class is defined only once;
- ☐ ...

Symbol Binding

What is symbol binding?

“Matching symbol **declarations** with **uses**”

 If there are multiple declarations, which one is matched?

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“Matching symbol **declarations** with **uses**”

❑ If there are multiple declarations, which one is matched?

```
void foo()
{
    char x;
    ...
    {
        int x;
        ...
    }
    x = x + 1;
}
```

What is symbol binding?

“Matching symbol **declarations** with **uses**”

❑ If there are multiple declarations, which one is matched?

```
void foo()
{
    char x;
    ...
    {
        int x; ?
    }
    x = x + 1;
}
```

Scope

- ❑ **Binding**: the association of a use of a symbol to the declaration of that symbol
 - Which variable (or function) an identifier is referring to
- ❑ **Scope**: section of program where a declaration is valid
 - Uses in the scope of declaration are bound to it
- ❑ Some implications of scopes
 - A symbol may have different bindings in different scopes
 - Scopes for the same symbol never overlap
 - there is always exactly one binding per symbol use
- ❑ Two types: static scope and dynamic scope

Static Scope


- ❑ Static scope depends on the program text, not run-time behavior (also known as lexical scoping)
 - C/C++, Java, Objective-C
- ❑ Rule: Refer to the closest enclosing declaration

```
void foo()  
{  
    char x;  
  
    ...  
    {  
        int x;  
  
        ...  
    }  
    x = x + 1;  
}
```

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        ...  
    }  
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}
```



Dynamic Scope

- Dynamic scoping depends on bindings formed during the execution of the program
 - LISP, Scheme, Perl
- Rule: Refer to the closest binding in the current execution

```
void foo()  
{  
  (1) char x;  
  (2) if (...) {  
    (3)   int x;  
    (4)   ...  
  }  
  (5) x = x + 1;  
}
```

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void foo()  
{  
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  (2) if (...) {  
    (3)   int x;  
    (4)   ...  
  }  
  (5) x = x + 1;  
}
```

- Which x's declaration is the closest?
 - Execution (a): ...**(1)**...(2)...(5)
 - Execution (b): ...(1)...(2)...**(3)**...(4)...(5)

Static vs. Dynamic Scoping

- ❑ Most languages that started with dynamic scoping (LISP, Scheme, Perl) added static scoping afterwards
- ❑ Why?
 - It is easier for human beings to understand
 - Bindings are visible in code without tracing execution
 - It is easier for compilers to understand
 - Compiler can determine bindings at compile time
 - Compiler can translate identifier to a single memory location
 - Results in generation of efficient code
 - With dynamic scoping...
 - There may be multiple possible bindings for a variable
 - Impossible to determine bindings at compile time
 - All bindings have to be done at execution time (Typically with the help of a hash table)

Symbol Table

Symbol Table

- ❑ **Symbol Table:** A compiler data structure that tracks information about all identifiers (symbols) in a program
 - Maps symbol uses to declarations given a scope
 - Needs to provide bindings according to the current scope

- ❑ Usually discarded after generating the binary code
 - All symbols are mapped to memory locations already
 - For debugging, symbols may be included in binary
 - To map memory locations back to symbols for debuggers
 - For GCC or Clang, add “-g” flag to include symbol tables

Maintaining Symbol Table

Basic idea:

```
int x; ... void foo() { int x; ... x=x+1; } ... x=x+1 ...
```

- In *foo*, add *x* to table, overriding any previous declarations
- After *foo*, remove *x* and restore old declaration if any

Operations

`enter_scope()` start a new nested scope

`exit_scope()` exit current scope

`find_symbol(x)` find declaration of *x*

`add_symbol(x)` add declaration of *x* to symbol table

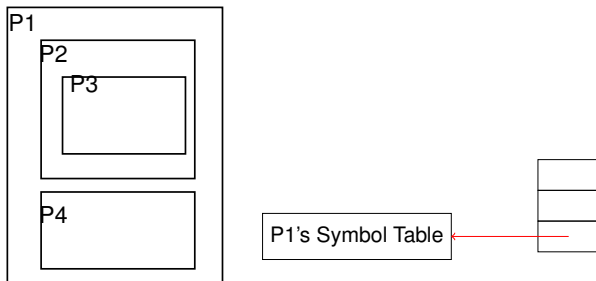
Adding Scope Information to the Symbol Table

- ❏ To handle multiple scopes in a program,
 - (Conceptually) need an individual table for each scope
 - Symbols added to the table may not be deleted just because you exited a scope

```
class X { ... void f1() {...} ... }  
class Y { ... void f2() {...} ... }  
X v;  
call v.f1();
```

- Without deleting symbols, how are scoping rules enforced?
 - ☞ Keep a list of all scopes in the entire program
 - ☞ Keep a stack of active scopes at a given point

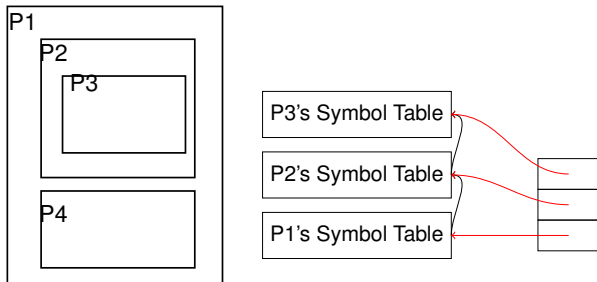
Symbol Table with Multiple Scopes



For nested scopes,

- Search from top of the active symbol table stack
- Remove pointer to symbol table when exiting its scope

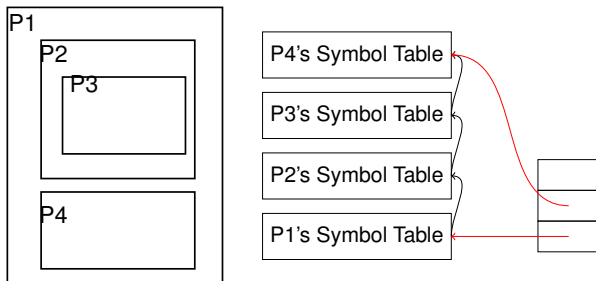
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What Information is Stored in the Symbol Table

Entry in Symbol Table:

string	kind	attributes
--------	------	------------

- String — the name of identifier
- Kind — variable, parameter, function, class, ...

Attributes vary with the kind of symbol

- variable → type, address in memory
- function → return type, parameter types, address

Vary with the language

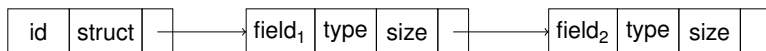
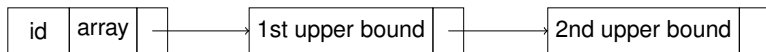
- Fortran's array → type, dimension, dimension size
`real A(5) /* dimension required for static allocation */`
- C's array → type, dimension, optional dimension size
`char A[5]; /* statically sized array */`
`char A[]="hello"; /* dynamically sized to fit content */`

Symbol Table Attribute List

□ Type information might be arbitrarily complicated

➤ In C: struct {
 int a[10];
 char b;
 float c;
 }

□ Store all relevant attributes in an attribute list

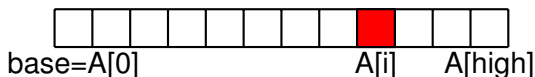


Example application of Type to an operator: Array index operator


Addressing Array Elements

```
int A[0..high];
```

```
A[i] ++;
```



- width — width of element type
- base — address of the first
- high — upper bound of subscript

 Addressing an array element:

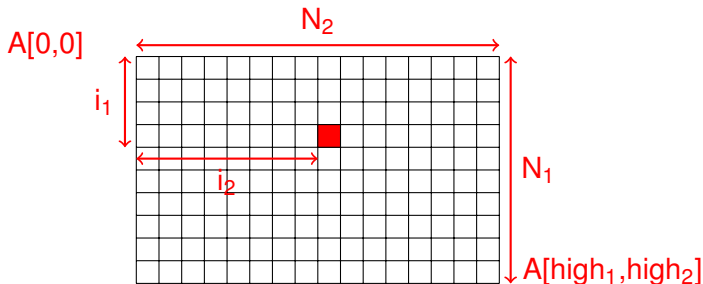
$$\text{address}(A[i]) = \text{base} + i * \text{width}$$
$$\text{offset}(A[i]) = i * \text{width}$$

Multi-dimensional Arrays

- Layout n-dimension items in 1-dimension memory

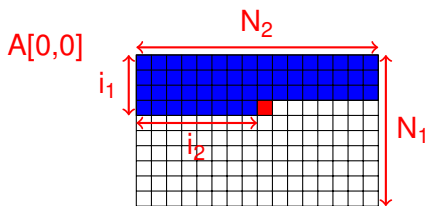
```
int A[N1][N2]; /* int A[0..high1][0..high2]; */
```

```
A[i1][i2] ++;
```



Row Major

Row major — store row by row

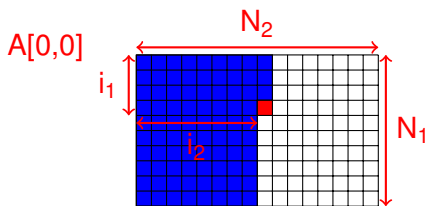


□ Offset includes all the “blue” items before $A[i_1, i_2]$

$$\begin{aligned}
 \text{offset}(A[i_1, i_2]) &= (i_1 * N_2 + i_2) * \text{width} \\
 &= i_1 * N_2 * \text{width} + i_2 * \text{width} \\
 &= \text{offset}(A[i_1]) * N_2 + i_2 * \text{width}
 \end{aligned}$$

Column Major

Column major — store column by column



□ Offset includes all the “blue” items before $A[i_1, i_2]$

$$\begin{aligned} \text{offset}(A[i_1, i_2]) &= (i_2 * N_1 + i_1) * \text{width} \\ &= i_2 * N_1 * \text{width} + i_1 * \text{width} \\ &= i_2 * N_1 * \text{width} + \text{offset}(A[i_1]) \end{aligned}$$

Generalized Row/Column Major

Let $A_k = \text{offset}(A[i_1, i_2, \dots, i_k])$. Then,


Row major

1-dimension: $A_1 = i_1 * \text{width}$

2-dimension: $A_2 = (i_1 * N_2 + i_2) * \text{width} = A_1 * N_2 + i_2 * \text{width}$

3-dimension: $A_3 = (i_1 * N_2 * N_3 + i_2 * N_3 + i_3) * \text{width} = A_2 * N_3 + i_3 * \text{width}$

k-dimension: $A_k = A_{k-1} * N_k + i_k * \text{width}$

 **Type** needs to provide $N_2 \dots N_k$ and width for offset


Column major

1-dimension: $A_1 = i_1 * \text{width}$

2-dimension: $A_2 = (i_2 * N_1 + i_1) * \text{width} = i_2 * N_1 * \text{width} + A_1$

3-dimension: $A_3 = ((i_3 * N_2 + i_2) * N_1 + i_1) * \text{width} = i_3 * N_2 * N_1 * \text{width} + A_2$

k-dimension: $A_k = i_k * N_{k-1} * N_{k-2} * \dots * N_1 * \text{width} + A_{k-1}$

 **Type** needs to provide $N_1 \dots N_{k-1}$ and width for offset

C's implementation

❏ C uses row major

```
int fun1(int p[ ][100])  
{  
  ...  
  int a[100][100];  
  a[i1][i2] = p[i1][i2] + 1;  
}
```

Why is p[][100] allowed?

Why is a[][100] not allowed?

C's implementation

❏ C uses row major

```
int fun1(int p[][100])  
{  
  ...  
  int a[100][100];  
  a[i1][i2] = p[i1][i2] + 1;  
}
```

Why is `p[][100]` allowed?

- The info is enough to compute `p[i1][i2]`'s address
- $A_2 = (i_1 * N_2 + i_2) * \text{width}$ (N_1 is not required)

Why is `a[][100]` not allowed?

- The info is not enough to allocate space for the array

Type Checking

What, Why and When

❑ What is a type?

Type = a set of values + a set of operations on these values

❑ What is type checking?

Verifying and enforcing type consistency

- Only legal values are assigned to a type
- Only legal operations are performed on a type

❑ Why is compile-time type checking desirable?

- Runtime errors may go unnoticed while testing
- Dynamic type checking when static checking infeasible
 - E.g. Java array bounds checks
 - E.g. Type checks to verify C++/Java downcasting

Static vs. Dynamic Typing

❑ Statically typed: C/C++, Java 👉 Our discussion

- Types are explicitly declared or can be inferred from code
- E.g. `int x; /* type of x is int */`
- Efficient code since runtime type checks are not needed

❑ Dynamically typed: Python, JavaScript, PHP

- Type is a runtime property decided only during execution
- E.g. `var x; /* type of x is undecided */`
- Type of x changes depending on the type of value it holds
- More memory since every variable now needs a "type tag"
- Inefficient code due to runtime checks on type tags

Rules of Inference

□ What are *rules of inference*?

- Inference rules have the form
if **Precondition** is true, then **Conclusion** is true
- Below concise notation used to express above statement

Precondition
Conclusion

- In the context of type checking:
if expressions E1, E2 have certain types (Precondition),
expression E3 is legal and has a certain type (Conclusion)

□ Type checking via inference

- Start from variable types and constant types
- Repeatedly apply rules until entire program is inferred legal

Notation for Inference Rules

- By tradition inference rules are written as

$$\frac{\text{Precondition}_1, \dots, \text{Precondition}_n}{\text{Conclusion}}$$

- The precondition/conclusion has the form “**e:T**”

- Meaning

- If **Precondition**₁ and ... and **Precondition**_n are true, then **Conclusion** is true.
- “**e:T**” indicates “**e is of type T**”
- Example: rule-of-inference for add operation

$$\frac{e_1: \text{int} \quad e_2: \text{int}}{e_1 + e_2: \text{int}}$$

Rule: If e_1, e_2 are ints then $e_1 + e_2$ is legal and is an int

Two Simple Rules

[Constant]

$$\frac{\text{**i is an integer**}}{\text{**i: int**}}$$

[Add operation]

$$\frac{\begin{array}{l} \text{**e}_1\text{: int} \\ \text{**e}_2\text{: int} \end{array}}{\text{**e}_1\text{+e}_2\text{:int}}}******$$

□ Example: given “10 is an integer” and “20 is an integer”, is the expression “10+20” legal? Then, what is the type?

$$\frac{\frac{\text{**10 is an integer**}}{\text{**10: int**}} \quad \frac{\text{**20 is an integer**}}{\text{**20: int**}}}{\text{**10+20:int**}}$$

□ This type of reasoning can be applied to the entire program

More Rules

[New]

$$\frac{}{\text{new T: T}}$$

[Not]

$$\frac{e: \text{Boolean}}{\text{not } e: \text{Boolean}}$$

 However,

[Var?]

$$\frac{x \text{ is an identifier}}{x: ?}$$

- the expression itself insufficient to determine type
- **solution:** provide context for this expression

Type Environment

- ❏ A *type environment* gives type info for free variables
 - A variable is *free* if not declared inside the expression
 - It is a function mapping **Symbols** to **Types**
 - Set of declarations active at the current scope
 - Conceptual representation of a symbol table

Type Environment Notation

Let \mathcal{O} be a function from **Symbols** to **Types**,
the sentence $\mathcal{O} \ e:T$

is read as “under the assumption of environment \mathcal{O} ,
expression e has type T ”

$$\frac{i \text{ is an intger}}{\mathcal{O} \ i: \text{int}}$$

$$\frac{\begin{array}{l} \mathcal{O} \ e1: \text{int} \\ \mathcal{O} \ e2: \text{int} \end{array}}{\mathcal{O} \ e1+e2: \text{int}}$$

$$\frac{\mathcal{O}(x) == T}{\mathcal{O} \ x: T}$$

- “if i is an integer, expression i is an int in any environment”
- “if $e1$ and $e2$ are ints in \mathcal{O} , expression $e1+e2$ is int in \mathcal{O} ”
- “if variable x is mapped to int in \mathcal{O} , expression x is int in \mathcal{O} ”

Declaration Rule

[Declaration w/o initialization]

$$\frac{O[T_0/x] \ e_1 : T_1}{O \text{ let } x : T_0 \text{ in } e_1 : T_1}$$

$O[T_0/x]$: environment O modified so that it return T_0 on argument x and behaves as O on all other arguments:

$$O[T_0/x](x) = T_0$$

$$O[T_0/x](y) = O(y) \text{ when } x \neq y$$

- Translation: "If expression e_1 is type T_1 when x is mapped to type T_0 in the current environment, expression e_1 is type T_1 when x is declared to be T_0 in the current environment"

Declaration Rule with Initialization

[Declaration with initialization (initial try)]

$$\frac{\begin{array}{c} \mathbf{O} \ e_0 : T_0 \\ \mathbf{O}[T_0/x] \ e_1 : T_1 \end{array}}{\mathbf{O} \ \text{let } x : T_0 \leftarrow e_0 \text{ in } e_1 : T_1}$$

❏ The rule is too strict (i.e. correct but not complete)

Example

class C inherits P ...

let x:P \leftarrow new C in ...

👉 the above rule does not allow this code

Subtyping

□ Subtyping is a relation \leq on classes

- $X \leq X$
- if X inherits from Y , then $X \leq Y$
- if $X \leq Y$ and $Y \leq Z$, then $X \leq Z$

□ An improvement of our previous rule

[Declaration with initialization]

$$\frac{\begin{array}{c} O\ e_0: T \\ T \leq T_0 \\ O[T_0/x]\ e_1: T_1 \end{array}}{O\ \text{let } x: T_0 \leftarrow e_0\ \text{in } e_1: T_1}$$

- Both versions of declaration rules are correct
- The improved version checks more programs

Assignment

❏ A correct but too strict rule

[Assignment]

$O(id) = T_0$

$O e_1: T_1$

$T_1 \leq T_0$

$O id \leftarrow e_1: T_0$

- The rule does not allow the below code
- ```
class C inherits P { only_in_C() { ... } }
x ← y ← new C
x.only_in_C()
```

# Assignment

□ An improved rule

[Assignment]

$O(id) = T_0$

$O\ e_1: T_1$

$T_1 \leq T_0$

---

$O\ id \leftarrow e_1: T_1$

- The rule now does allow the below code
- ```
class C inherits P { only_in_C() { ... } }
x ← y ← new C
x.only_in_C()
```

If-then-else

Consider

if e_0 then e_1 else e_2

- The result can be either e_1 or e_2
 - The type is either e_1 's type or e_2 's type
- The best that we can do (statically) is the super type larger than e_1 's type and e_2 's type

Least upper bound (LUB)

- $Z = \text{lub}(X, Y)$ — Z is defined as the least upper bound of X and Y iff
- $X \leq Z \wedge Y \leq Z$; Z is an upper bound
 - $X \leq W \wedge Y \leq W \implies Z \leq W$; Z is least among all upper bounds

If-then-else, case

[If-then-else]

$$\frac{\begin{array}{l} \text{O } e_0: \text{Bool} \\ \text{O } e_1: T_1 \\ \text{O } e_2: T_2 \end{array}}{\text{O if } e_0 \text{ then } e_1 \text{ else } e_2 \text{ fi: } \text{lub}(T_1, T_2)}$$

□ The rule allows the below code

let x:float, y:int, z:float in

x \leftarrow if (...) then y else z

/* Assuming $\text{lub}(\text{int}, \text{float}) = \text{float}$ */

Error Recovery

❏ Just like other errors, we should recover from type errors

➤ Too many errors?

let y: int \leftarrow x+2 in y+3

- if x is undefined — reporting an error “x type undefined”
- x+2 is undefined — reporting an error “x+2 type undefined”
- ...

❏ Introduce **no-type** for ill-typed expressions

- It is compatible with all types
- Report the place where **no-type** is generated
 - Reduce the number of error messages

Wrong Declaration Rule (case 1)

□ Consider a hypothetical let rule

[Wrong Declaration with initialization (case 1)]

$$\frac{\begin{array}{c} \mathbf{O} \ e_0: T \\ T \leq T_0 \\ \mathbf{O} \ e_1: T_1 \end{array}}{\mathbf{O} \ \text{let } x: T_0 \leftarrow e_0 \text{ in } e_1: T_1}$$

- How is it different from the the correct rule?
- The following good program does not pass check
`let x: int ← 0 in x+1`

Wrong Declaration Rule (case 2)

❑ Consider a hypothetical let rule

[Wrong Declaration with initialization (case 2)]

$$\frac{\begin{array}{c} \mathbf{O} \ e_0: T \\ T_0 \leq T \\ \mathbf{O}[T_0/x] \ e_1: T_1 \end{array}}{\mathbf{O} \ \text{let } x: T_0 \leftarrow e_0 \ \text{in } e_1: T_1}$$

- How is it different from the the correct rule?
- The following bad program passes the check


```
class B inherits A { only_in_B() { ... } }
let x: B ← new A in x.only_in_B()
```

Discussion

- ❑ Type rules have to be carefully constructed, or
 - The type system becomes unsound
(bad programs are accepted as well typed)
 - The type system becomes unusable
(good programs are rejected as badly typed)

Discussion

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 - Good program: a program where all operations on all values are type consistent **at runtime**

Discussion

- ❑ Type rules have to be carefully constructed, or
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 - The type system becomes unusable
(good programs are rejected as badly typed)
- ❑ What is a “good” program anyway?
 - Good program: a program where all operations on all values are type consistent **at runtime**
- ❑ All runtime behavior not expressed in a static type system
 - At below is a good program rejected by the type system
`obj ← if (x > y) then new Child else new Parent`
`if (x > y) then obj.only_in_Child()`
 - LUB type makes a choice of soundness over usability

Designing a Good Type Checking System

- ❑ A good type system achieves two opposing goals:
 - Prevents **false negative** type errors, that is, runtime errors that are missed by type checking
 - Minimizes **false positive** type errors, that is, type errors that do not cause runtime errors
- ❑ A good type system should allow the following code:

```
class Parent {  
    Parent clone() { return new this.getClass(); }  
}  
class Child inherits Parent { ... }  
void main() {  
    // Error! Assignment of parent to child reference.  
    Child c ← (new Child).clone();  
}  
}
```

What Went Wrong?

- ❑ What is `(new Child).clone()`'s type?
 - Dynamic type — Child
 - Static type — Parent
 - Type system is not able to express runtime types precisely
 - This makes inheriting `clone()` not very useful
 - `clone()` needs redefinition to return correct type anyway
- ❑ A "SELF_TYPE" would be useful in these situations.

SELF_TYPE expresses runtime types precisely

❏ What is SELF_TYPE?

- `clone()` returns “self” instead of “Parent” type
- Self can be Parent or any subclass of Parent

❏ SELF_TYPE is a static type

- Type reflects precise runtime behavior for each class
- Type violations can still be detected at compile time

❏ In practice

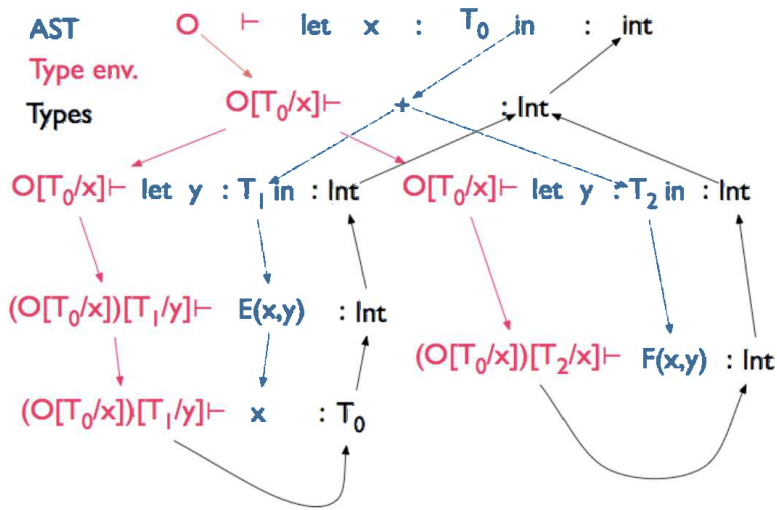
- Python, Rust, Scala: language support for self types
- C++: can emulate using C++ templates
- Java: can emulate to a lesser degree using Java generics

Can Static Type Checking ever be Perfect?

- ❑ Many examples where "good" programs are disallowed
 - Reason for elaborate type systems like generics
 - Why programmers must sometimes typecast anyway

- ❑ Solution? Can't have your cake and eat it too.
 - Dynamic typing: values have types, variables do not
 - + Allows all runtime behaviors that are type consistent
 - Type errors occur at runtime rather than compile time
 - 👉 Best used for fast prototyping (scripting languages)
 - Static typing: variables have declared (or inferred) types
 - + Type errors can be caught at compile time
 - Effort needed to express "good" programs using type system
 - 👉 Best used when reliability is important

Implementing Type Checking on AST



Syntax Directed Definitions (SDDs)

SDD: Definitions of attributes and rules

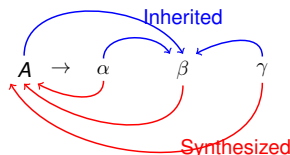
- ❑ Syntax Directed Definitions (SDD):
 1. Set of **attributes** attached to each grammar symbol
 2. Set of **semantic rules** attached to each production
 - Semantic rules define values of attributes

- ❑ Attribute Grammar:
 - An SDD where rules depend only on other attributes (i.e. An SDD that does not rely on any side-effects)
 - Think of it as a "grammar" for semantic analysis

- ❑ Example: let's say we want to define type checking
 - SDD can have semantic rules to access a symbol table
 - Attribute grammar must transmit type info through attributes

Syntax Directed Definition (SDD)

 Semantic rule:



SDD has rule of the form for each CFG production

$$b = f(c_1, c_2, \dots, c_n)$$

either

1. If b is a synthesized attribute of A ,
 c_i ($1 \leq i \leq n$) are attributes of grammar symbols of its Right Hand Side (RHS); or
2. If b is an inherited attribute of one of the symbols of RHS,
 c_i 's are attribute of A and/or other symbols on the RHS

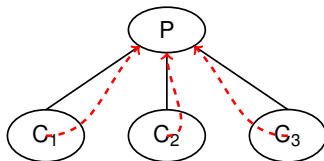
Two Types of Attributes

- ❑ **Synthesized attributes:** attributes are computed from attributes of children nodes

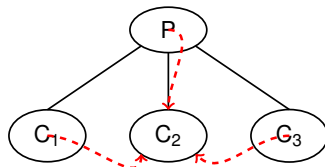
➤ $P.\text{synthesized_attr} = f(C_1.\text{attr}, C_2.\text{attr}, C_3.\text{attr})$

- ❑ **Inherited attributes:** attributes are computed from attributes of sibling and parent nodes

➤ $C_3.\text{inherited_attr} = f(P_1.\text{attr}, C_1.\text{attr}, C_3.\text{attr})$



Synthesized attribute



Inherited attribute

Synthesized Attribute Example

Example

- Each non-terminal symbol is associated with **val** attribute
- The **val** attribute is computed solely from children attributes

[Grammar Rules]

$L \rightarrow E$

$E \rightarrow E_1 + T$

$E \rightarrow T$

$T \rightarrow T_1 * F$

$T \rightarrow F$

$F \rightarrow (E)$

$F \rightarrow \text{digit}$

[Semantic Rules]

$\text{print}(E.\text{val})$

$E.\text{val} = E_1.\text{val} + T.\text{val}$

$E.\text{val} = T.\text{val}$

$T.\text{val} = T_1.\text{val} * F.\text{val}$

$T.\text{val} = F.\text{val}$

$F.\text{val} = E.\text{val}$

$F.\text{val} = \text{digit}.\text{lexval}$

Inherited Attribute Example

Example:

- T.type: synthesized attribute
- L.in: inherited attribute
- id.type: inherited attribute

[Grammar Rules]

$D \rightarrow T L$

$T \rightarrow \text{int}$

$T \rightarrow \text{real}$

$L \rightarrow L_1, \text{id}$

$L \rightarrow \text{id}$

[Semantic Rules]

$L.in = T.type$

$T.type = \text{integer}$

$T.type = \text{real}$

$L_1.in = L.in, \text{id.type} = L.in$

$\text{id.type} = L.in$

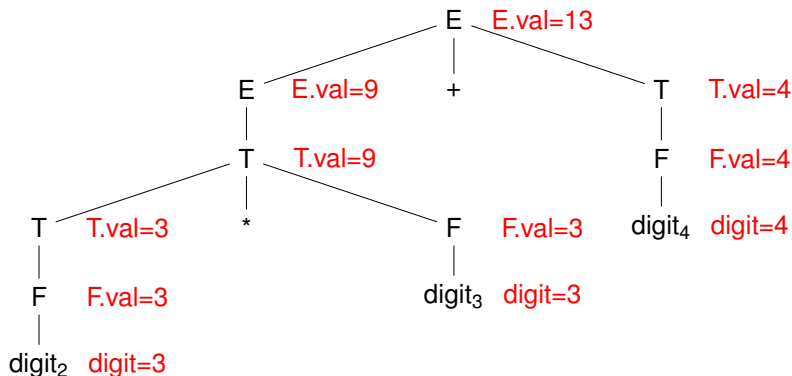
Why is L.in an inherited attribute?

- L.in is computed from a sibling T.type
- $L_1.in$ is computed from a parent L.in

Attribute Parse Tree

■ SDDs produce an attribute parse tree

➤ **Attribute parse tree:** Parse tree decorated with attributes



SDD Implementation

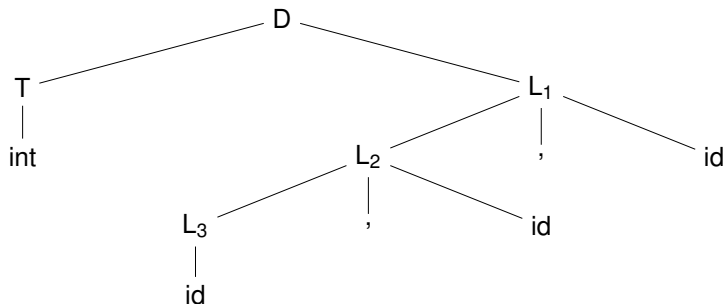
SDD Implementation using Parse Trees

- ❑ Assumes a previous parse stage
 - Input: a parse tree with no attribute annotations
 - Output: an attribute parse tree

- ❑ Goal: compute attribute values from leaf token values
 - Traverse in some order, apply semantic rules at each node
 - Traversal order must consider attribute dependencies

Dependency Graph

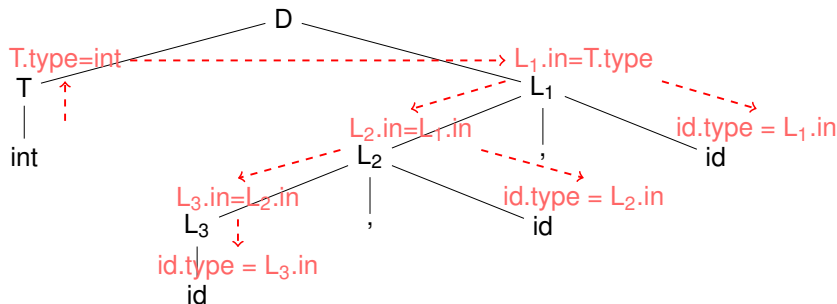
- Directed graph where edges are attribute dependencies
 - "To" attribute is computed base on "from" attribute
 - Must be **acyclic** such that there exists "a" traversal order



Dependency Graph

☐ Directed graph where edges are attribute dependencies

- "To" attribute is computed base on "from" attribute
- Must be **acyclic** such that there exists "a" traversal order



SDD Implementation using SDT

❑ Syntax Directed Translation (SDT)

- Applying semantic rules as part of syntax analysis (parsing)
- Does NOT assume a pre-existing parse tree
- Done through **semantic actions** embedded in grammar

❑ Semantic action:

- Code between curly braces embedded into RHS
- Executed “at that point” in the RHS
 - Top-down: Right after previous symbol has been consumed
 - Bottom-up: After previous symbol has been pushed to stack (when the 'dot' reaches the semantic action)
- Example of building a parse tree:
 - Program : Program IDNum ; Classes
 { \$\$=makeTree(ProgramOp, \$2, \$4); }
- \$2 and \$4 are indices into the parse stack
 - RHS is currently at top of stack waiting to be reduced
 - \$2 is attribute value for IDNum and \$4 is Classes

Syntax Directed Translation Scheme (SDTS)

□ Syntax Directed Translation Scheme (SDTS)

- A "scheme" or plan to perform SDT
- A grammar specification embedded with semantic actions
- Depends on choice of top-down or bottom-up parser

□ Example:

$E \rightarrow T \ R$

$R \rightarrow + \ T \ R$

$R \rightarrow - \ T \ R$

$R \rightarrow \epsilon$

$T \rightarrow (\ E \)$

$T \rightarrow \text{num}$

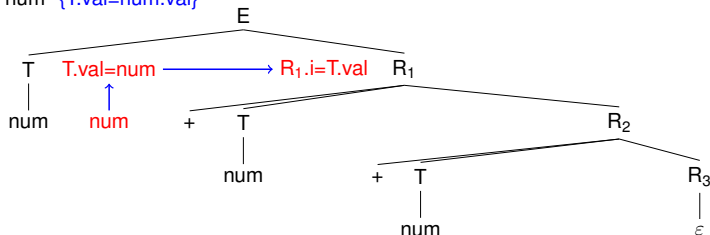
□ Both inherited and synthesized attributes are used

- T — synthesized attribute T.val
- R — inherited attribute R.i
synthesized attribute R.s
- E — synthesized attribute E.val

Syntax Directed Translation Scheme (SDTS)

Evaluating attributes using SDTS

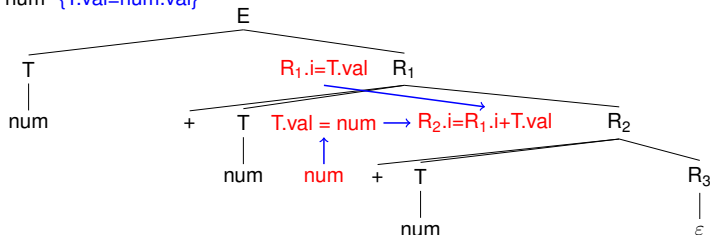
$E \rightarrow T \quad \{R.i=T.val\} \quad R \quad \{E.val=R.s\}$
 $R \rightarrow + \quad T \quad \{R_1.i=R.i+T.val\} \quad R_1 \quad \{R.s=R_1.s\}$
 $R \rightarrow - \quad T \quad \{R_1.i=R.i-T.val\} \quad R_1 \quad \{R.s=R_1.s\}$
 $R \rightarrow \varepsilon \quad \{R.s=R.i\}$
 $T \rightarrow (\quad E \quad \{T.val=E.val\}$
 $T \rightarrow \text{num} \quad \{T.val=\text{num.val}\}$



Syntax Directed Translation Scheme (SDTS)

Evaluating attributes using SDTS

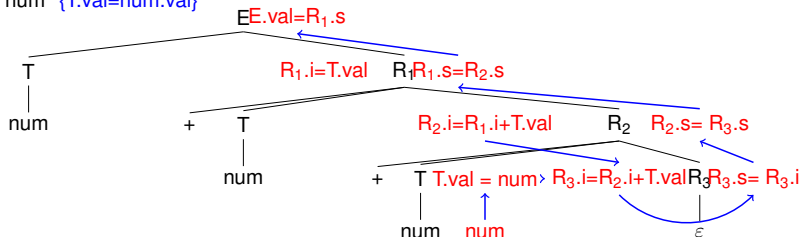
$E \rightarrow T \quad \{R.i=T.val\} \quad R \quad \{E.val=R.s\}$
 $R \rightarrow + \quad T \quad \{R_1.i=R.i+T.val\} \quad R_1 \quad \{R.s=R_1.s\}$
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 $R \rightarrow \varepsilon \quad \{R.s=R.i\}$
 $T \rightarrow (\quad E \quad \{T.val=E.val\}$
 $T \rightarrow \text{num} \quad \{T.val=\text{num.val}\}$



Syntax Directed Translation Scheme (SDTS)

Evaluating attributes using SDTS

$E \rightarrow T \quad \{R.i = T.val\} \quad R \quad \{E.val = R.s\}$
 $R \rightarrow + \quad T \quad \{R_1.i = R.i + T.val\} \quad R_1 \quad \{R.s = R_1.s\}$
 $R \rightarrow - \quad T \quad \{R_1.i = R.i - T.val\} \quad R_1 \quad \{R.s = R_1.s\}$
 $R \rightarrow \epsilon \quad \{R.s = R.i\}$
 $T \rightarrow (\quad E \quad \{T.val = E.val\}$
 $T \rightarrow num \quad \{T.val = num.val\}$



What are the dependencies allowed in SDTS?

- ❑ Parse trees: dependencies only required to be acyclic
- ❑ What is required of dependencies for SDTS?
 - Different parsing schemes see nodes in different orders
 - Top-down parsing — LL(k) parsing
 - Bottom-up parsing — LR(k) parsing
 - What if dependency node has not been seen yet?
- ❑ For certain classes of SDDs, using SDTS is feasible
 - If dependencies of SDD are amenable to parse order
 - This class of SDDs are called L-Attributed Grammars

Left-Attributed Grammar

□ An SDD is L-attributed if each of its attributes is either:

➤ a synthesized attribute of A in $A \rightarrow X_1 \dots X_n$,

or

➤ an inherited attribute of X_j in $A \rightarrow X_1 \dots X_n$ that

- depends on attributes of siblings to its left i.e. $X_1 \dots X_{j-1}$
- and/or depends on parent A

Left-Attributed Grammar

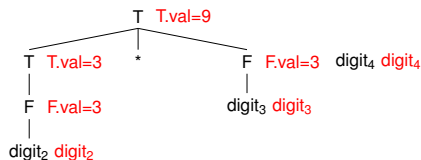
- ❑ An L-Attributed grammar
 - may have synthesized attributes
 - may have inherited attributes but only from left sibling attributes or inherited attributes of the parent
- ❑ Evaluation order
 - Left-to-right depth-first traversal of the parse tree
 - Order for both top-down and bottom-up parsers
 - Evaluate inherited attributes while going down the tree
 - Evaluate synthesized attributes while going up the tree
- ❑ Can be evaluated using SDTS w/o parse tree

Syntax Directed Translation Scheme (SDTS)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

it is natural and easy to evaluate synthesized attributes



parsing stack:

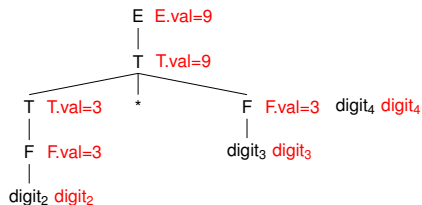
S ₇	T	T.val=9
S ₇	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

□ it is natural and easy to evaluate synthesized attributes



parsing stack:

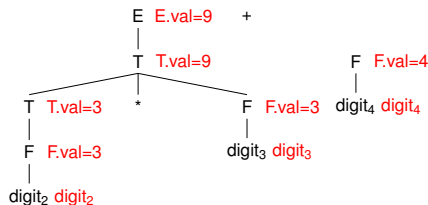
S ₇	E	E.val=9
S ₇	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

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parsing stack:

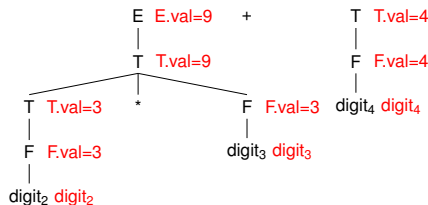
S?	F	F.val=4
S?	+	-
S?	E	E.val=9
S?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

it is natural and easy to evaluate synthesized attributes



parsing stack:

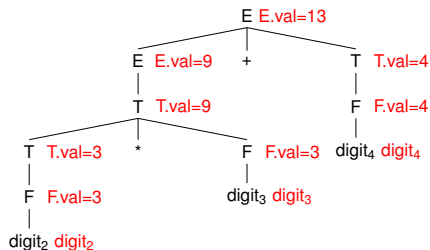
S?	T	T.val=4
S?	+	-
S?	E	E.val=9
S?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

it is natural and easy to evaluate synthesized attributes



parsing stack:

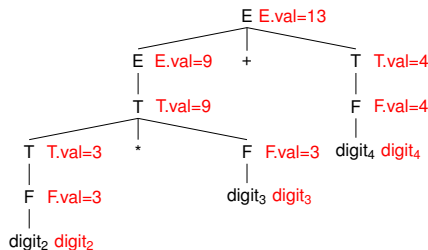
S ₇	E	E.val=13
S ₇	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

- it is natural and easy to evaluate synthesized attributes



parsing stack:

S ₇	E	E.val=13
S ₇	\$	-

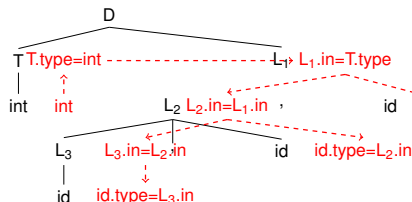
(state) (symbol) (attribute)

- Grammars with only synthesized attributes are called **S-Attributed Grammars**

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

□ it is **not natural** to evaluate inherited attributes



parsing stack:

S?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

□ it is **not natural** to evaluate inherited attributes

```

int          ,          id
          ,          id
id
  
```

parsing stack:

S?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

 it is **not natural** to evaluate inherited attributes

T T.type=int

|
int

↑
int

,

id

,

id

id

parsing stack:

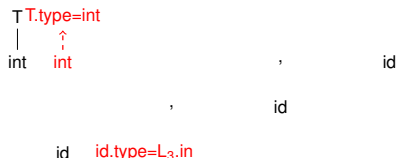
S?	T	T.type=int
S?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

it is **not natural** to evaluate inherited attributes



parsing stack:

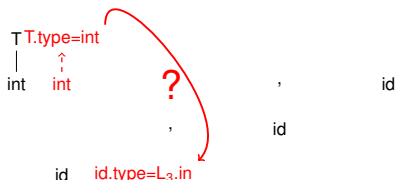
S?	id	id.type=L ₃ .in
S?	T	T.type=int
S?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

it is **not natural** to evaluate inherited attributes



parsing stack:

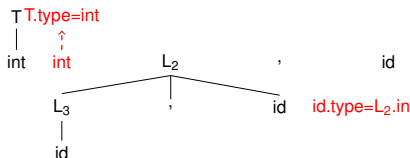
S _?	id	id.type=L ₃ .in
S _?	T	T.type=int
S _?	\$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

it is **not natural** to evaluate inherited attributes



parsing stack:

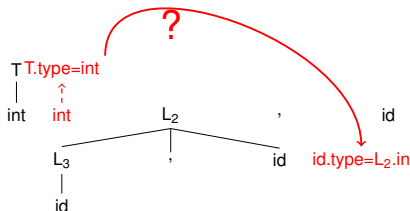
$S_?$	id	$id.type=L_2.in$
$S_?$,	
$S_?$	L_3	$L_3.in=L_2.in$
$S_?$	T	$T.type=int$
$S_?$	$\$$	-

(state) (symbol) (attribute)

Translation Scheme for Bottom-Up Parsing

When using LR parsing (bottom-up parsing),

□ it is **not natural** to evaluate inherited attributes




parsing stack:

S _?	id	id.type=L₂.in
S _?	,	
S _?	L ₃	L ₃ .in=L ₂ .in
S _?	T	T.type=int
S _?	\$	-


(state) (symbol) (attribute)

Evaluating Inherited Attributes using LR

 **Claim:** Given an L-Attributed grammar, inherited attributes needed for the computation are already on the stack

 Recall: What is an L-Attributed grammar?

- May have synthesized attributes
- May have inherited attributes but only from:
 - **Left** sibling attributes
 - Parent attribute

 Finding inherited attributes on the stack

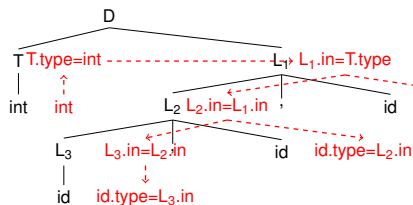
- Left siblings: previously reduced, so already on the stack
- Parent: not yet reduced, but left siblings of the parent used to compute the parent attribute are on the stack

$$D \rightarrow T \quad L$$

$$T \rightarrow \text{int} \quad \{T.\text{type}=\text{int}\}$$

$$T \rightarrow \text{real} \quad \{T.\text{type}=\text{real}\}$$

$$L \rightarrow L \ , \ \text{id} \quad \{\text{id}.\text{type}=\text{stack}[\text{top}-3].\text{type}\}$$

$$L \rightarrow \text{id} \quad \{\text{id}.\text{type}=\text{stack}[\text{top}-1].\text{type}\}$$


parsing stack:

$S_?$	$\$$	-

(state) (symbol) (attribute)

$$D \rightarrow T \quad L$$

$T \rightarrow \text{int} \quad \{T.\text{type}=\text{int}\}$

$$T \rightarrow \text{real} \quad \{T.\text{type}=\text{real}\}$$
$$L \rightarrow L, \quad \text{id} \quad \{\text{id.type} = \text{stack}[\text{top}-3].\text{type}\}$$
$$L \rightarrow \text{id} \quad \{\text{id.type} = \text{stack}[\text{top}-1].\text{type}\}$$

int

,

id

9

id

id

parsing stack:

S?	\$	-

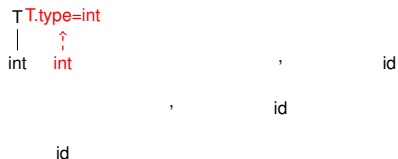
(state) (symbol) (attribute)

$$D \rightarrow T \ L$$

$$T \rightarrow \text{int} \ \{T.\text{type}=\text{int}\}$$

$$T \rightarrow \text{real} \ \{T.\text{type}=\text{real}\}$$

$$L \rightarrow L \ , \ \text{id} \ \{\text{id.type}=\text{stack}[\text{top}-3].\text{type}\}$$

$$L \rightarrow \text{id} \ \{\text{id.type}=\text{stack}[\text{top}-1].\text{type}\}$$


parsing stack:

S _?	T	T.type=int
S _?	\$	-

(state) (symbol) (attribute)

$$D \rightarrow T \mid L$$

$$T \rightarrow \text{int} \quad \{T.\text{type}=\text{int}\}$$

$$T \rightarrow \text{real} \quad \{T.\text{type}=\text{real}\}$$

$$L \rightarrow L, \text{id} \quad \{\text{id.type}=\text{stack}[\text{top}-3].\text{type}\}$$

$$L \rightarrow \text{id} \quad \{\text{id.type}=\text{stack}[\text{top}-1].\text{type}\}$$

T $T.\text{type}=\text{int}$
 \mid \uparrow
 int int , id
 , id
 id id.type=L₃.in

parsing stack:

S _?	id	id.type=stack[top-1]
S _?	T	T.type=int
S _?	\$	-

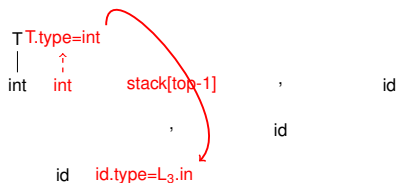
(state) (symbol) (attribute)

$$D \rightarrow T \ L$$

$$T \rightarrow \text{int} \ \{T.\text{type}=\text{int}\}$$

$$T \rightarrow \text{real} \ \{T.\text{type}=\text{real}\}$$

$$L \rightarrow L \ , \ \text{id} \ \{\text{id}.\text{type}=\text{stack}[\text{top}-3].\text{type}\}$$

$$L \rightarrow \text{id} \ \{\text{id}.\text{type}=\text{stack}[\text{top}-1].\text{type}\}$$


parsing stack:

S _?	id	id.type=stack[top-1]
S _?	T	T.type=int
S _?	\$	-

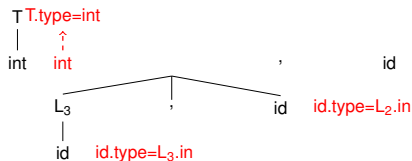
(state) (symbol) (attribute)

$$D \rightarrow T \ L$$

$$T \rightarrow \text{int} \ \{T.\text{type}=\text{int}\}$$

$$T \rightarrow \text{real} \ \{T.\text{type}=\text{real}\}$$

$$L \rightarrow L \ , \ \text{id} \ \{\text{id.type}=\text{stack}[\text{top}-3].\text{type}\}$$

$$L \rightarrow \text{id} \ \{\text{id.type}=\text{stack}[\text{top}-1].\text{type}\}$$


parsing stack:

S _?	id	id.type=stack[top-3]
S _?	,	
S _?	L ₃	L ₃ .in=int
S _?	T	T.type=int
S _?	\$	-

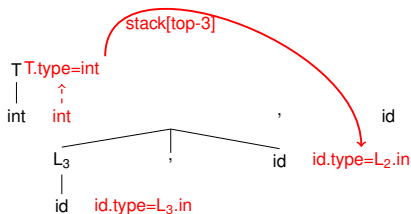
(state) (symbol) (attribute)

$$D \rightarrow T \ L$$

$$T \rightarrow \text{int} \ \{T.\text{type}=\text{int}\}$$

$$T \rightarrow \text{real} \ \{T.\text{type}=\text{real}\}$$

$$L \rightarrow L \ , \ \text{id} \ \{\text{id.type}=\text{stack}[\text{top}-3].\text{type}\}$$

$$L \rightarrow \text{id} \ \{\text{id.type}=\text{stack}[\text{top}-1].\text{type}\}$$


parsing stack:

S ₇	id	id.type=stack[top-3]
S ₇	,	
S ₇	L ₃	L ₃ .in=int
S ₇	T	T.type=int
S ₇	\$	-

(state) (symbol) (attribute)

Marker

- Given the following SDD, where $|\alpha| \neq |\beta|$

$$A \rightarrow X \alpha Y \mid X \beta Y$$

$$Y \rightarrow \gamma \{ \dots = f(X.s) \}$$
- Problem: cannot generate stack location for $X.s$ since X is at different relative stack locations from Y
- Solution: introduce *markers* M_1 and M_2 that are at the same relative stack locations from Y

$$A \rightarrow X \alpha M_1 Y \mid X \beta M_2 Y$$

$$Y \rightarrow \gamma \{ \dots = f(M_{12}.s) \}$$

$$M_1 \rightarrow \varepsilon \{ M_1.s = X.s \}$$

$$M_2 \rightarrow \varepsilon \{ M_2.s = X.s \}$$

(M_{12} = the stack location of M_1 or M_2 , which are identical)
- A marker intuitively marks a stack location that is equidistant from the reduced non-terminal

Example

□ When is a marker necessary and how is it added?

Example 1:

$$\begin{aligned} S &\rightarrow a A \{ C.i = A.s \} C \\ S &\rightarrow b A B \{ C.i = A.s \} C \\ C &\rightarrow c \{ C.s = f(C.i) \} \end{aligned}$$

Solution:

$$\begin{aligned} S &\rightarrow a A \{ C.i = A.s \} C \\ S &\rightarrow b A B \{ M.i=A.s \} M \{ C.i = M.s \} C \\ C &\rightarrow c \{ C.s = f(C.i) \} \\ M &\rightarrow \varepsilon \{ M.s = M.i \} \end{aligned}$$

That is:

$$\begin{aligned} S &\rightarrow a A C \\ S &\rightarrow b A B M C \\ C &\rightarrow c \{ C.s = f(\text{stack}[\text{top}-1]) \} \\ M &\rightarrow \varepsilon \{ M.s = \text{stack}[\text{top}-2] \} \end{aligned}$$

When and how to add a marker

1. Identify the stack offset(s) to find the desired attribute
2. If stack offsets are different, add a marker
3. Add marker where it would result in uniform stack offsets

Example:

$S \rightarrow a \ A \ B \ C \ E \ D$

$S \rightarrow b \ A \ F \ B \ C \ F \ D$

$C \rightarrow c \ \{ /* \ C.s = f(A.s) \ */ \}$

$D \rightarrow d \ \{ /* \ D.s = f(B.s) \ */ \}$

Answer

$S \rightarrow a A B C E D$

$S \rightarrow b A D M B C F D$

$C \rightarrow c \text{ /* C.s = f(stack[top-2]) */}$

$D \rightarrow d \text{ /* D.s = f(stack[top-3]) */}$

$M \rightarrow \varepsilon \text{ /* M.s = f(stack[top-2]) */}$

 Regarding C.s, from stack[top-2], and stack[top-3]

.... add a Marker

 Regarding D.s, always from stack[top-2]

... no need to add

 How about Top-Down Parsing?

Translation Scheme for Top-Down Parsing

❑ Recursive Descent Parsers: Straightforward

➤ Synthesized Attribute

- Say function for non-terminal returns synthesized attribute
- Compute attribute from children function call return values

➤ Inherited Attribute

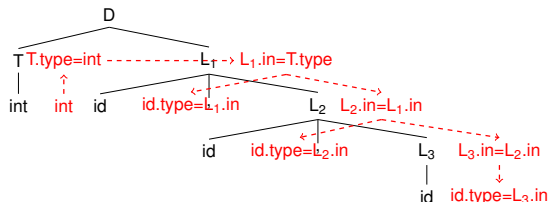
- Pass as argument to function call for inheriting non-terminal
- Left sibling attributes: left sibling calls already complete
- Parent attributes: passed in as arguments to parent function

❑ How about table-driven LL parsers?

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

it is natural to evaluate inherited attributes



parsing stack:

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

□ it is natural to evaluate inherited attributes

D

parsing stack:

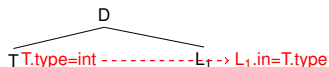
D	

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

□ it is natural to evaluate inherited attributes



parsing stack:

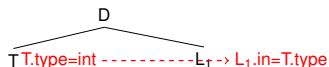
T	T.type=int
L ₁	L ₁ .in=()

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

- it is natural to evaluate inherited attributes



parsing stack:

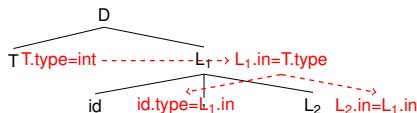
L ₁	L ₁ .in=int

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

- it is natural to evaluate inherited attributes



parsing stack:

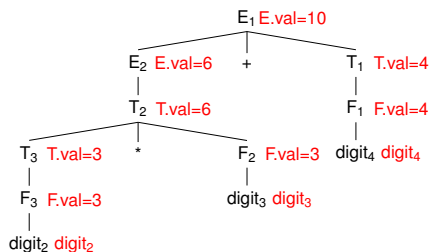
id	id.type=L ₁ .in
,	
L ₂	L ₂ .in=intL ₁ .in

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

it is **not natural** to evaluate synthesized attributes



parsing stack:

(symbol)	(attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

 it is **not natural** to evaluate synthesized attributes

E_1

parsing stack:

E_1	

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

□ it is **not natural** to evaluate synthesized attributes

E_1 $E.val=?$

parsing stack:

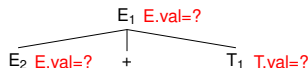
E_1	$E_1.val=?$

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

□ it is **not natural** to evaluate synthesized attributes



parsing stack:

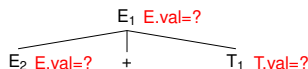
E ₂	E ₂ .val=?
+	
T ₁	T ₁ .val=?

(symbol) (attribute)

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

❑ it is **not natural** to evaluate synthesized attributes



parsing stack:

E ₂	E ₂ .val=?
+	
T ₁	T ₁ .val=?

(symbol) (attribute)

❑ Solution

- Always push a 'dummy' stack item below a non-terminal to hold intermediate values for attribute calculation
- Update dummy item whenever a child node is popped with intermediate value
- When all children nodes have been popped, compute synthesized attribute from stored values

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

❑ it is **not natural** to evaluate synthesized attributes

E_1

parsing stack:

E_1	
$E_1.val$???

(symbol) (attribute)

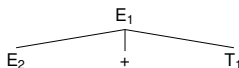
❑ Solution

- Always push a 'dummy' stack item below a non-terminal to hold intermediate values for attribute calculation
- Update dummy item whenever a child node is popped with intermediate value
- When all children nodes have been popped, compute synthesized attribute from stored values

Translation Scheme for LL Parsing

When using LL parsing (top-down parsing),

it is **not natural** to evaluate synthesized attributes



parsing stack:

E_2	
$E_2.val$???
+	
T_1	
$T_1.val$???
$E_1.val$	$E_2.val + T_1.val$

(symbol) (attribute)

Solution

- Always push a 'dummy' stack item below a non-terminal to hold intermediate values for attribute calculation
- Update dummy item whenever a child node is popped with intermediate value
- When all children nodes have been popped, compute synthesized attribute from stored values