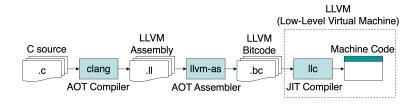
Code Generation

Multiple IRs in the Compiler

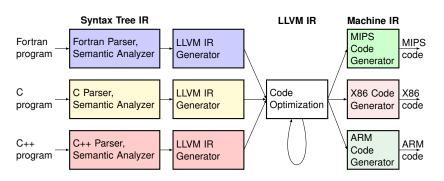
Modern Compiler Framework (Clang/LLVM)

Remember this diagram from our first day?



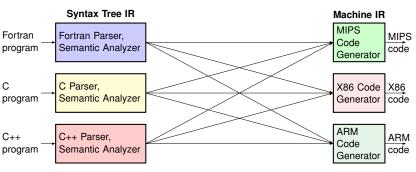
LLVM Bitcode is in LLVM IR (Intermediate Representation)

Modern Compiler Framework (Clang/LLVM)



- Common LLVM IR for all languages and backends means:
 - > Code optimizations need to be written only once
 - Implementation complexity if O(M + N) instead of O(M * N) (where M = number of frontends, N = number of backends)

Why O(M * N) when no common IR?



- Must translate M languages to N machine codes
 - Must also do optimizations during each of these translations

High-Level IRs

- Goal: Express the syntax and semantics of source code
- Examples: Abstract Syntax Tree, Parse Tree
- Differs on: Source code programming language
- Uses:
 - Generated by syntax analysis
 - Used by semantic analysis for binding and type checking
 - Language-specific optimizations (e.g. devirtualization)
 - > Devirtualization: changing polymorphic calls to direct calls
 - Polymorphic method calls are indirect jumps using a vtable (A vtable is a table of function pointers for each class)
 - Sometimes the direct call is inlined into caller method

Low-Level IRs

- Goal: Express code in the ISA of an abstract machine
- Examples: Three address code, Static Single Assignment
- ☐ Differs on: Language and back-end machine agnostic
- Uses:
 - > A common IR that connects front-ends and back-ends
 - Language / machine independent optimizations
 - Common subexpression elimination
 - Constant propagation
 - Loop invariant code motion
 - ...
 - Optimizations done in this common IR unless reason not to

Machine IRs

- Goal: Generate code in the ISA of back-end machine
- Examples: x86 IR, ARM IR, MIPS IR
- ☐ Differs on: Back-end machine ISA
- Uses:
 - > Register allocation / machine code generation
 - > Machine-specific optimizations
 - Strength reduction (replacing op with cheaper op)
 - Vectorization (using CPU vector units if available)
 - ..

Low-Level IRs

Three Address Code

Generic form is X = Y op Z

where X, Y, Z can be variables, constants, or compiler-generated temporaries holding intermediate values

- Characteristics
 - Assembly code for an 'abstract machine'
 - Long expressions are converted to multiple instructions
 - Control flow statements are converted to jumps
 - Machine independent
 - Operations are generic (not tailored to specific machine)
 - Function calls represented as generic call nodes
 - Uses symbolic names rather than register names (Actual locations of symbols are yet to be determined)
- Why this form?
 - > Allows IR to be generated in a machine-agnostic way
 - Optimizations on IR can be done much more easily (Optimizations don't worry about syntactic structure)

Example

An example:

$$x * y + z / w$$
 is translated to

$$t1 = x * y$$
; $t1$, $t2$, $t3$ are temporary variables

$$t2 = z / w$$

$$t3 = t1 + t2$$

- Sequential translation of an AST
- > Internal nodes in AST are translated to temporary variables
- > Can be generated through a depth-first traversal of AST

Common Three-Address Statements (I)

Assignment statement:

$$x = y op z$$

where op is an arithmetic or logical operation (binary operation)

Assignment statement:

$$x = op y$$

where op is an unary operation such as -, not, shift)

Copy statement:

$$x = y$$

Unconditional jump statement:

goto L

where L is label

Common Three-Address Statements (II)

Conditional jump statement: if (x relop y) goto L where relop is a relational operator such as $=, \neq, >, <$ Procedural call statement: param $x_1, ..., param x_n, call F_v, n$ As an example, foo(x1, x2, x3) is translated to param x₁ param x₂ param x₃ call foo. 3 Procedural call return statement: return y where y is the return value (if applicable)

Common Three-Address Statements (III)

Indexed assignment statement:

$$y[i] = x$$

where x is an int and y is an array variable

Address and pointer operation statement:

x = & y; a pointer x is set to the address of y

; y is set to value contained in the location

$$^*y = x$$

; location addressed by y gets value x

Implementation of Three-Address Code

- ☐ There are three possible ways to store the code
 - quadruples
 - > triples
 - indirect triples
- Using quadruples op src1, src2, dest
 - There are four fields at maximum
 - Src1 and src2 are optional
 - Src1, src2, dest are variables (including temporaries)

Examples:

$$x = a + b$$
 => + a, b, x
 $x = -y$ => -y, , x
goto L => goto , , L

Using Triples

- ☐ Tripes have only three fields. How?
 - Destination field of instruction is always a temporary (With the exception of assignments to variables)
 - Replace use of temporary wth pointer to that instruction
 - Instruction no longer needs a destination field!

Example: a = b * (-c) + b * (-c)

	Quadruples				Triple	S	
	ор	src1	src2	dest	ор	src1	src2
(0)	-	С		t1	-	С	
(1)	*	b	t1	t1	*	b	(0)
(2)	-	С		t2	-	С	
(3)	*	b	t2	t2	*	b	(2)
(4)	+	t1	t2	t1	+	(1)	(3)
(5)	=	t1		а	=	а	(4)

More About Triples

☐ Triples for array statements

$$x[i] = y$$

is translated to

- (0) [] x i
- (1) = (0) y
- > That is, one statement is translated to two triples

Using Indirect Triples

- Problem with triples
 - Cannot move code around because instruction numbers will change

	Quadruples				Triple	3	
	op src1 src2 dest		ор	src1	src2		
(0)	-	С		t1	-	С	
(1)	*	b	t1	t1	*	b	(0)
(2)	-	С		t2	-	С	
(3)	*	b	t2	t2	*	b	(2)
(4)	+	t1	t2	t1	+	(1)	(3)
(5)	=	t1		а	=	а	(4)

Using Indirect Triples

- Problem with triples
 - Cannot move code around because instruction numbers will change

	Quadruples					Triple	S
	ор	src1	src2	dest	ор	src1	src2
(0)	-	С		t1	-	С	
(1)	*	b	t1	t1	*	b	(0)
(2)	+	t1	t1	t1	+	(1)	(1)
(3)	=	t1		а	=	а	(4)

Using Indirect Triples

- ➤ IR is a listing of pointers to triples instead of triples themselves
- Triples are stored in a separate triple 'database'
- Can modify listing as long as the database does not change
- > Slightly more overhead but allows optimizations

	Indirect Triples					
	(ptr to triple database)					
(0)	(0)					
(1)	(1)					
(2)	(2)					
(3)	(3)					
(4)	(4)					
(5)	(5)					

	Triples					
	op src1 src2					
(0)	-	С				
(1)	*	b	(0)			
(2) (3)	-	С				
(3)	*	b	(2)			
(4)	+	(1)	(3)			
(5)	=	а	(4)			

After Optimization

	Indirect Triples					
	(ptr to triple database)					
(0)	(0)					
(1)	(1)					
(2)	(4)					
(3)	(5)					

	Triple Database					
	op src1 src2					
(0)	-	С				
(1)	*	b	(0)			
(2)	-	С				
(3)	*	b	(2)			
(4)	+	(1)	(1)			
(5)	=	а	(4)			

- After optimization, some entries in database can be reused
 - > i.e. Entries in triple database do not have to be contiguous

After Optimization

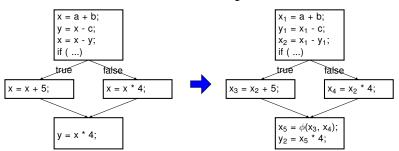
	Indirect Triples					
	(ptr to triple database)					
(0)	(0)					
(1)	(1)					
(2)	(4)					
(3)	(5)					

	Triple Database					
	op src1 src2					
(0)	-	С				
(1)	*	b	(0)			
(2)	(empty)					
(3)	(empty)					
(4)	+	(1)	(1)			
(5)	=	а	(4)			

- After optimization, some entries in database can be reused
 - > i.e. Entries in triple database do not have to be contiguous

Static Single Assignment (SSA)

- Developed by R. Cytron, J. Ferrante, et al. in 1980s
 - Every variable is assigned exactly once i.e. one **DEF**
 - Convert original variable name to name $_{version}$ e.g. $x \rightarrow x_1$, x_2 in different places
 - ightharpoonup Use ϕ -function to combine two DEFs of same original variable on a control flow merge



Benefits of SSA

- SSA can assist compiler optimizations
 - > e.g. remove dead code

$$x = a + b;$$

 $x = c - d;$
 $y = x * b;$
 $x_1 = a + b;$
 $x_2 = c - d;$
 $x_1 = a + b;$
 $x_2 = c - d;$
 $x_1 = a + b;$
 $x_2 = c - d;$
 $x_1 = a + b;$

.... x₁ is defined but never used, it is safe to remove

- Will discuss more in compiler optimization phase
- Intuition: Makes data dependency relationships between instructions more apparent in the IR

Generating IR using Syntax Directed Translation

- What is our parsing scheme?
 - Bottom-up LR/LALR parsing
 - Natural to translate synthesized attributes
 - Hack to translate L-attributed inherited attributes

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- What is our parsing scheme?
 - Bottom-up LR/LALR parsing
 - Natural to translate synthesized attributes
 - Hack to translate L-attributed inherited attributes
- What language structures do we need to translate?
 - Declarations
 - variables, procedures (need to enforce static scoping), ...
 - Assignment statement
 - > Flow of control statement
 - if-then-else, while-do, for-loop, ...
 - Procedure call
 - **>** ..

Attributes to Evaluate in Translation

- Statement S
 - S.code a synthesized attribute that holds IR code of S
- Expression E
 - E.code a synthesized attribute that holds IR code for computing E
 - E.place a synthesized attribute that holds the location where the result of computing E is stored
- Variable declaration:
 - **TV** e.g. int a,b,c;
 - > Type information **T.type T.width**
 - Variable information V.type, V.offset

Attributes to Evaluate in Translation

- Statement **S**
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 - E.place a synthesized attribute that holds the location where the result of computing E is stored
- Variable declaration:
 - **TV** e.g. int a,b,c;
 - > Type information **T.type T.width**
 - Variable information V.type, V.offset
 - What is V.offset?

- When there are multiple variables defined in a procedure,
 - we layout the variable sequentially
 - use variable offset, to get address of x
 - address(x) ← offset
 - offset += sizeof(x.type)

```
void foo() {
   int a;
   int b;
   long long c;
   int d;
}
```

- When there are multiple variables defined in a procedure,
 - we layout the variable sequentially
 - use variable offset, to get address of x
 - address(x) ← offset
 - offset += sizeof(x.type)

```
      void foo() {
      Address

      int a;
      0x0000

      int b;
      0x0004

      long long c;
      0x0008

      int d;
      0x000c

      }
      0x0010
```

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Storage Layout of Variables in a Procedure

- When there are multiple variables defined in a procedure,
 - we layout the variable sequentially
 - use variable offset, to get address of x
 - address(x) ← offset
 - offset += sizeof(x.type)

```
Address
void foo() {
                                                               Offset=16
                         0x0000
   int a:
                                                               Addr(a)\leftarrow0
                                       b
   int b:
                         0x0004
                                                               Addr(b)\leftarrow4
   long long c;
                                       C
                         0x0008
                                                               Addr(c)\leftarrow8
   int d;
                         0x000c
                         0x0010
```

Storage Layout of Variables in a Procedure

- When there are multiple variables defined in a procedure,
 - we layout the variable sequentially
 - use variable offset, to get address of x
 - address(x) ← offset
 - offset += sizeof(x.type)

```
Address
void foo() {
                                                                Offset=20
                          0x0000
   int a:
                                                                Addr(a)\leftarrow0
                                        b
   int b:
                          0x0004
                                                                Addr(b)\leftarrow4
   long long c;
                                        C
                          0x0008
                                                                Addr(c)\leftarrow8
   int d;
                                        C
                          0x000c
                                                                Addr(d)\leftarrow16
                                        d
                          0x0010
```

More About Storage Layout (I)

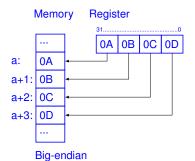
Allocation alignment

- Enforce addr(x) mod sizeof(x.type) == 0
- Most machine architectures are designed such that computation is most efficient at sizeof(x.type) boundaries
 - E.g. Most machines are designed to load integer values at integer word boundaries
 - If not on word boundary, need to load two words and shift & concatenate

More About Storage Layout (II)

Endianness

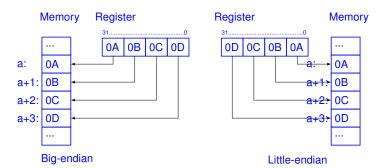
- Big endian stores MSB (most significant byte) in lowest address
- Little endian stores LSB (least significant byte) in lowest address



More About Storage Layout (II)

Endianness

- Big endian stores MSB (most significant byte) in lowest address
- Little endian stores LSB (least significant byte) in lowest address



More About Storage Layout (III)

- Questions still unanswered
 - How are non-local variables laid out?
 - How dynamically allocated variables laid out?

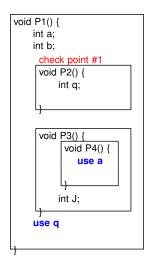
Processing Declarations

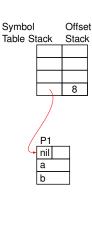
- ☐ Translating the declaration in a single procedure
 - enter(name, type, offset) insert the variable into the symbol table

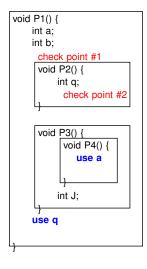
```
\begin{array}{ll} P \rightarrow M \ D \\ M \rightarrow \varepsilon & \{ \ offset=0; \} \ /^* \ reset \ offset \ before \ layout \ ^*/ \\ D \rightarrow D \ ; \ D \\ D \rightarrow T \ id & \{ \ enter(id.name, \ T.type, \ offset); \ offset \ += \ T.width; \} \\ T \rightarrow integer & \{ \ T.type=integer; \ T.width=4; \} \\ T \rightarrow real & \{ \ T.type=real; \ T.width=8; \} \\ T \rightarrow T1[num] & \{ \ T.type=array(num.val, \ T1.type); \\ & \qquad \qquad T.width=num.val \ ^* \ T1.width; \} \\ T \rightarrow \ ^* T1 & \{ \ T.type=ptr(T1.type); \ T.width=4; \} \end{array}
```

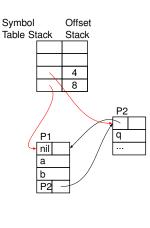
Processing Nested Declarations

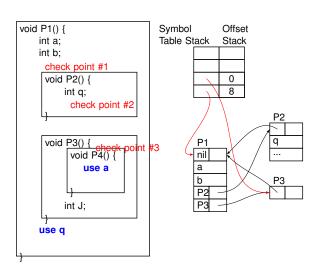
- Need scope information for each level of nesting.
- When encountering a nested procedure declaration...
 - Create a new symbol table when encountering a sub-procedure declaration
 - mktable(ptr); ptr points back to its parent table
 - Store procedure name in parent symbol table, with a pointer pointing to the new table
 - enterproc(parent_table_ptr, proc_id, child_table_ptr)
 - Suspend the processing of parent symbol table
 - Push new table in the active symbol table stack
 - Push the current offset in the offset stack
 - When done, resume the processing of parent symbol table
 - Pop entries in active symbol table stack, offset stack for nested procedure
 - Restore current offset from the offset stack

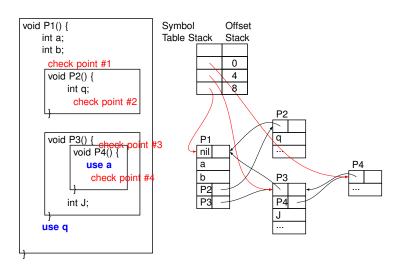


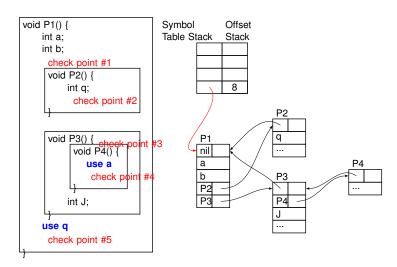












Processing Nested Declarations

Syntax directed translation rules

Processing Statements

- Statements are processed sequentially after processing declarations
 - useful functions:
 lookup (id) search id in symbol table, return nil if none emit() print three address IR
 newtemp() get a new temporary variable

```
\begin{array}{lll} S \rightarrow \text{id} = E & \{ \text{ P=lookup(id); if (P==nil) perror(...); else emit(P '=' E.place);} \} \\ E \rightarrow E1 + E2 \{ \text{ E.place = newtemp(); emit(E.place '=' E1.place '+' E2.place);} \} \\ E \rightarrow E1 * E2 \{ \text{ E.place = newtemp(); emit(E.place '=' E1.place '*' E2.place);} \} \\ E \rightarrow - E1 & \{ \text{ E.place = newtemp(); emit(E.place '=' '-' E1.place);} \} \\ E \rightarrow ( E1 ) & \{ \text{ E.place = E1.place;} \} \\ E \rightarrow \text{id} & \{ \text{ P=lookup(id); E.place=P;} \} \end{array}
```

Processing Array References

- Recall generalized row/column major addressing
- For example:
 - 1-dimension: int x[100]; $x[i_1]$
 - 2-dimension: int x[100][200]; x[i₁][i₂]
 - 3-dimension: int x[100][200][300]; $x[i_1][i_2][i_3]$
- Row major: addressing a k-dimension array item (low; = base = 0)
 - 1-dimension: $A_1 = a_1^*$ width $a_1 = i_1$
 - 2-dimension: $A_2 = a_2^*$ width $a_2 = a_1^* N_2 + i_2$ 3-dimension: $A_3 = a_3^*$ width $a_3 = a_2^* N_3 + i_3$

...

k-dimension: $A_k = a_k^*$ width $a_k = a_{k-1}^* N_k + i_k$

Processing Array References

Processing an array assignment (e.g. A[i] = B[j];)

Processing Boolean Expressions

- Boolean expression: a op b
 - > where op can be <, >, >=, &&, ||, ...
 - 1. Compute just like any other arithmetic expression
 - Good for languages with no short circuiting
 - > Short circuiting:
 - In expression A && B, not evaluating B when A is false
 - In expression A || B, not evaluating B when A is true
 - Without short circuiting, entire expression is evaluated as usual

```
\begin{array}{lll} S \! \to \! \operatorname{id} = E & \equiv & \operatorname{lookup}(\operatorname{id}) = E.\operatorname{place} \\ E \! \to \! (a < b) \text{ or } (c < d \text{ and } e < f) \equiv & t1 = a < b \\ & t2 = c < d \\ & t3 = e < f \\ & t4 = t2 \text{ \&\& } t3 \\ & E.\operatorname{place} = t1 \text{ || } t4 \end{array}
```

Processing Boolean Expressions

- 2. Implement as a series of jumps
 - ➤ For languages with short circuiting (e.g. C/C++), evaluations sometimes have to be 'jumped'
 - Processing a boolean expression:

```
\begin{array}{lll} S \! \to & \text{if E then S1} \\ E \! \to & \text{a < b} & \equiv & \text{E.true} = \text{S1.label}; \\ E.\text{false} = & \text{S.next} \\ & \text{if E goto E.true} \\ & \text{goto E.false} \end{array}
```

S1.label: label created at the address of code S1

S.next: address of code after S
E.true: code to execute on 'true'
E.false: code to execute on 'false'

- > Processing compound boolean expressions:
 - Chain together multiple of above by updating E.true/E.false
 - E→ E1 && E2: E1.true = code for E2, E1.false = S.next
 - \bullet E \rightarrow E1 || E2: E1.false = code for E2, E1.true = S1.label

Processing Boolean Expressions

- 2. Implement as a series of jumps (cont'd)
 - > A short circuited compound boolean expression

```
E \rightarrow (a < b) or (c < d \text{ and } e < f) \equiv if (a < b) goto E.true
                                           goto L1
                                       L1: if (c<d) goto L2
                                           goto E.false
                                       L2: if (e<f) goto E.true
                                           goto E.false
```

- Can apply to other control flow statements $S \rightarrow \text{if E then S1} \mid \text{if E then S1 else S2} \mid \text{while E do S1}$
- Problem: E.true, E.false, S.next are non-L-attributes
 - Depend on code that has not been generated yet S.next: Only available when code after S is generated E.true: Only available when S1 is generated

Syntax Directed Translation

- A non-L-attributed grammar may preclude a one pass syntax directed translation scheme
 - Both top-down and bottom-up SDTS rely on L-attributed grammars
 - How to handle non-L attributes?
 - E.true, E.false, S.next
- Solutions: two methods
 - Two pass approach process the code twice
 - Generate labels in the first pass
 - Replace labels with addresses in the second pass
 - One pass approach
 - Generate holes when address is needed but unknown
 - Fill in holes when addresses is known later on
 - Finish code generation in one pass

Two-Pass Based Syntax Directed Translation Scheme

- Attributes for two pass based approach
 - Expression E
 - Synthesized attributes: E.code
 - —- non-L inherited attributes: **E.true**, **E.false**
 - > Statement S
 - --- Synthesized attributes: S.code
 - --- non-L inherited attributes: S.next
- Evaluation order:

Given rule $S \rightarrow if E$ then S1, the two passes are:

- (1). Generate **E.code** and **S1.code** making a label for E.true
- Replace label E.true with actual address of S1 (Labels E.false and S1.next are inheried from S.next)

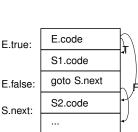
Given rule $S \rightarrow S1 S2$, the two passes are:

- (1). Generate S1.code and S2.code making a label for S1.next
- (2). Replace label **S1.next** with the actual address of S2 (Label **S2.next** is inheried from **S.next**)

Two Pass based Rules

```
S \rightarrow \text{if E then S1} \\ \{ \text{ E.true} = \text{newlabel}; \\ \text{ E.false} = \text{S.next}; \\ \text{S1.next} = \text{S.next}; \\ \text{S.code} = \text{E.code} \mid\mid \text{gen(E.true':')} \mid\mid \text{S1.code}; \} \\ \\ \\ \text{E.talse:} \\ \text{(S.next):} \\ \\ \text{(S.n
```

```
S \rightarrow \text{if E then S1 else S2} \\ \{ & \text{S1.next} = \text{S2.next} = \text{S.next}; \\ & \text{E.true} = \text{newlabel}; \\ & \text{E.false} = \text{newlabel}; \\ & \text{S.code} = \text{E.code} \mid\mid \text{gen(E.true':')} \mid\mid \\ & \text{S1.code} \mid\mid \text{gen('goto ' S.next)} \mid\mid \\ & \text{gen(E.false ':')} \mid\mid \text{S2.code}; \} \\ \end{cases}
```



F.code

S1.code

...

More Two Pass based SDT Rules

```
E \rightarrow id1 \ relop \ id2
                           { E.code=gen('if' id1.place 'relop' id2.place 'goto' E.true) ||
                                       gen('goto' E.false); }
E \rightarrow E1 \text{ or } E2
                           { E1.true = E2.true = E.true;
                              E1.false = newlabel:
                              E2.false = E.false;
                              E.code = E1.code || gen(E1.false ':') || E2.code; }
F \rightarrow F1 and F2
                           { E1.false = E2.false = E.false;
                              E1.true = newlabel:
                              E2.true = E.true:
                              E.code = E1.code || gen(E1.true ':') || E2.code; }
E \rightarrow not E1
                           { E1.true = E.false: E1.false = E.true: E.code = E1.code: }
\mathsf{E} \to \mathsf{true}
                           { E.code = gen('goto' E.true); }
\mathsf{F} \to \mathsf{false}
                           { E.code = gen('goto' E.false); }
```

Problem

- Try this at home. Refer to textbook Chapter 6.6.
- Write SDT rule (two pass) for the following statement

```
S 	o while (a < b) do if (c < d) then S endif endwhile
```

Backpatching

- If grammar contains L-attributes only, then it can be processed in one pass
- However, **we know** there are occasions for non-L attributes
 - Example: E.true, E.false, S.next during code generation
 - Is there a general solution to this problem?

Solution:

- Leave holes for non-L attributes, record their locations in holelists, and fill in the holes when we know the target values
 - holelist: synthesized attribute of 'holes' to be filled in for a particular target value
 - Holes are filled in one shot when target value is known
 - All holes can be replaced at the end of code generation

One-Pass Based Syntax Directed Translation Scheme

- Attributes for two pass based approach
 - Expression E
 - Synthesized attributes: E.code
 E.holes truelist, and E.holes falselist
 - > Statement S
 - Synthesized attributes: S.code and S.holes_nextlist
- Evaluation order:

Given rule $S \rightarrow if E then S1$, below is done in one-pass:

- (1). Gen E.code, making E.holes_truelist, E.holes_falselist
- Gen S1.code, filling in E.holes_truelist and merging S1.holes_nextlist with E.holes_falselist
- (3). Pass on merged list to **S.holes_nextlist**

Given rule $S \rightarrow S1 S2$, below is done in one-pass:

- (1). Gen S1.code making S1.holes_nextlist
- (2). Gen **S2.code** filling in **S1.holes_nextlist** and making **S2.holes_nextlist**
- (3). Pass on S2.holes_nextlist to S.holes_nextlist

Backpatching Rules for Boolean Expressions

- 3 functions for implementing backpatching for IR generation
 - makelist(i) creates a new list with statement index i
 - merge(p1, p2) concatenates list p1 and list p2
 - backpatch(p, i) insert i as target label for each statement in list p

```
\label{eq:energy} \begin{array}{ll} E \rightarrow \text{E1 or M E2} & \{ \text{ backpatch(E1.holes\_falselist, M.quad);} \\ & \text{E.holes\_truelist} = \text{merge(E1.holes\_truelist, E2.holes\_truelist);} \\ & \text{E.holes\_falselist} = \text{E2.holes\_falselist;} \, \} \\ E \rightarrow \text{E1 and M E2} & \{ \text{ backpatch(E1.holes\_truelist, M.quad);} \\ & \text{E.holes\_falselist} = \text{merge(E1.holes\_falselist, E2.holes\_falselist);} \\ & \text{E.holes\_truelist} = \text{E2.holes\_truelist;} \, \} \\ M \rightarrow \varepsilon & \{ \text{M.quad} = \text{nextquad;} \, \} \\ \end{array}
```

More One Pass SDT Rules

```
E \rightarrow not E1
                           { E.holes truelist = E1.holes falselist;
                              E.holes falselist = E1.holes truelist; }
E \rightarrow (E1)
                           { E.holes truelist = E1.holes truelist:
                              E.holes falselist = E1.holes falselist: }
E \rightarrow id1 \text{ relop id2}
                           { E.holes truelist = makelist(nextguad):
                              E.holes falselist = makelist(nextguad+1);
                              emit('if' id1.place 'relop' id2.place 'goto ____');
                              emit('goto'); }
\mathsf{E} \to \mathsf{true}
                           { E.holes truelist = makelist(nextquad);
                              emit('goto '); }
E \rightarrow false
                           { E.holes falselist = makelist(nextquad);
                              emit('goto '); }
```

Backpatching Example

lacksquare E ightarrow (a<b) or M1 (c<d and M2 e<f)

When reducing (a<b) to E1, we have

100: if(a<b) goto ____

 \square When reducing ε to M1, we have

When reducing (c<d) to E2, we have

102: if(c<d) goto ____ 103: goto

 \blacksquare When reducing ε to M2, we have

When reducing (e<f) to E3, we have

104: if(e<f) goto ____

105: goto ____

E1.hole_truelist=(100)

E1.hole_falselist=(101)

M1.quad = 102

E2.hole_truelist=(102)

E2.hole_falselist=(103)

M2.quad = 104

E3.hole_truelist=(104)

E3.hole_falselist=(105)

Backpatching Example (cont.)

```
When reducing (E2 and M2 E3) to E4, we backpatch((102), 104);
       100: if(a<b) goto
                                    E4.hole truelist=(104)
       101: goto
                                   E4.hole falselist=(103,105)
       102: if(c<d) goto 104
       103: goto
       104: if(e<f) goto ____
       105: goto
When reducing (E1 or M1 E4) to E5, we backpatch((101), 102);
       100: if(a<b) goto
                                   E5.hole truelist=(100, 104)
       101: goto 102
                                   E5.hole falselist=(103,105)
       102: if(c<d) goto 104
       103: goto
       104: if(e<f) goto
       105: goto
```

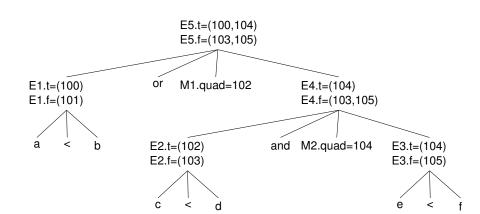
Backpatching Example (cont.)

```
When reducing (E2 and M2 E3) to E4, we backpatch((102), 104);
        100: if(a<b) goto
                                     E4.hole truelist=(104)
        101: goto
                                    E4.hole falselist=(103,105)
        102: if(c<d) goto 104
        103: goto
        104: if(e<f) goto
        105: goto
■ When reducing (E1 or M1 E4) to E5, we backpatch((101), 102);
        100: if(a<b) goto
                                    E5.hole truelist=(100, 104)
        101: goto 102
                                    E5.hole falselist=(103,105)
        102: if(c<d) goto 104
        103: goto
        104: if(e<f) goto
        105: goto ____
  Are we done?
```

Backpatching Example (cont.)

Yes for this expression

```
When reducing (E2 and M2 E3) to E4, we backpatch((102), 104);
          100: if(a<b) goto
                                       E4.hole truelist=(104)
          101: goto
                                      E4.hole falselist=(103,105)
          102: if(c<d) goto 104
          103: goto
          104: if(e<f) goto ____
          105: goto
 When reducing (E1 or M1 E4) to E5, we backpatch((101), 102);
          100: if(a<b) goto
                                      E5.hole truelist=(100, 104)
          101: goto 102
                                      E5.hole falselist=(103,105)
          102: if(c<d) goto 104
          103: goto
          104: if(e<f) goto
          105: goto ____
Are we done?
```



Problem

- Try this at home. Refer to textbook Chapter 6.6, 6.7.
- Write SDT rule (one pass using backpatching) for the following statement

```
\begin{array}{c} S \rightarrow \text{while E1 do} \\ \text{if E2} \\ \text{then S2} \\ \text{endif} \\ \text{endwhile} \end{array}
```

Solution Hint

 \square S \rightarrow while E1 do if E2 then S2 endif endwhile

	Known Attributes	Attributes to Evaluate/Process
Two	E1.code	E1.true, E1.false
Pass	E2.code	E2.true, E2.false
	S2.code	S2.next
	S.next	S.code
One	E1.code, E1.hole_truelist	S.code
Pass	E1.hole_falselist	S.hole_nextlist
	E2.code, E2.hole_truelist	
	E2.hole_falselist	(E1.hole_truelist,E1.hole_falselist)
	S.code, S.hole_nextlist	(E2.hole_truelist,E2.hole_falselist)