## A Proofs of Propositions

**Proof of Proposition 1**. Before jumping into the details of the proposition, we first prove the posterior updating result (3.3). The definition indicates

$$f^{\theta}(x|s) \propto \left[\frac{f(x|s)}{f(x)}\right]^{\theta} = \left(\frac{\alpha}{\alpha+\beta}\right)^{\frac{\theta}{2}}$$
 (A.1)

$$\times \exp\left(-\frac{\theta}{2}\left\{(\alpha+\beta)\left(x-\frac{\alpha z+\beta s}{\alpha+\beta}\right)^2-\alpha(x-z)^2\right\}\right) \tag{A.2}$$

where  $f(\cdot)$  denotes the density function. Since

$$(A.3) = \exp\left\{-\frac{\alpha + \beta(1+\theta)}{2} \left(x - \frac{\alpha z + \beta(1+\theta)s}{\alpha + \beta(1+\theta)}\right)^2\right\},\tag{A.3}$$

we obtain the posterior distribution (3.3).

Substituting  $\hat{s} = \hat{x} + \frac{1}{\sqrt{\beta}}\Phi^{-1}(\hat{x})$  (3.2) into (3.4), we have

$$1 - \Phi\left(\sqrt{\alpha + \beta(1+\theta)} \cdot \frac{\sqrt{\beta}(1+\theta)\Phi^{-1}(\widehat{x}) + \alpha(z-\widehat{x})}{\alpha + \beta(1+\theta)}\right) = c$$

$$\iff \Phi^{-1}(1-c) = \frac{\sqrt{\beta}(1+\theta)\Phi^{-1}(\widehat{x}) + \alpha(z-\widehat{x})}{\sqrt{\alpha + \beta(1+\theta)}}$$

$$\iff \sqrt{1 + \frac{\alpha}{\beta(1+\theta)}} \cdot \frac{\Phi^{-1}(1-c)}{\sqrt{1+\theta}} + \frac{\alpha(\widehat{x}-z)}{\sqrt{\beta}(1+\theta)} = \Phi^{-1}(\widehat{x})$$
(A.4)

Since  $\min_{x \in (0,1)} \frac{d}{dx} \Phi^{-1}(x) = \min_{x \in (0,1)} \frac{1}{\phi(\Phi^{-1}(x))} = \sqrt{2\pi}$ , the equilibrium is in monotone strategies and is unique if and only if

$$\frac{\alpha}{\sqrt{\beta}(1+\theta)} \le \sqrt{2\pi}$$

$$\iff \alpha \le (1+\theta)\sqrt{2\pi\beta}$$

$$\iff \theta \ge \frac{\alpha}{\sqrt{2\pi\beta}} - 1.$$

It only remains to show that the unique monotone equilibrium is the only equilibrium that survives iterated deletion of strictly dominated strategies. Let h(s) denote the threshold that an agent finds it optimal to follow when all other agents use a threshold s. Note that there is a 1-to-1 mapping between the thresholds  $\hat{x}$  that solve (3.2) and the fixed points of h. The monotone equilibria are defined by the fixed points of h. Construct two sequences  $\{\underline{s}_j\}_{j=0}^{\infty}$  and  $\{\overline{s}_j\}_{j=0}^{\infty}$  by  $\underline{s}_0 = -\infty, \underline{s}_j = h(\underline{s}_{j-1})$  and  $\overline{s}_0 = \infty, \overline{s}_j = h(\overline{s}_{j-1})$ . Each sequence is increasing or decreasing with upper or lower bound. Thus, they both converge to some  $\underline{s}$  and  $\overline{x}$ . By continuity of h, these points must be a fixed point of h, which is  $\hat{s}$ . Since the

only strategies that survives after j rounds of iterated deletion of dominated strategies are functions k such that k(s) = 1 for all  $s \leq \underline{s}_j$  and k(s) = 0 for all  $s > \overline{s}_j$ , the only strategy that survives in the limit is the unique monotone equilibrium.

**Proof of Proposition 2.** As  $\beta \to \infty$  with  $\alpha < \infty$ , (LHS) of (A.4) with  $\theta = 0$  becomes  $\Phi^{-1}(1-c)$  and (RHS) of (A.4) with  $\theta = 0$  remains the same. Thus, we obtain  $x_{\infty} = 1-c$  since  $\Phi^{-1}$  is monotone. Similarly, (LHS) of (A.4) becomes  $\Phi^{-1}(1-c)/\sqrt{1+\theta}$  and (RHS) of (A.4) remains the same. Thus, we obtain  $x_{\infty} = \Phi\left(\frac{\Phi^{-1}(1-c)}{\sqrt{1+\theta}}\right)$ .

**Proof of Corollary 1.** Since  $\Phi(\cdot)$  is an monotone increasing function and  $\Phi^{-1}(\cdot)$  undergoes a sign change at  $c = \frac{1}{2}$ , the order of the two equilibrium thresholds flips at  $c = \frac{1}{2}$ .

## **B** Simulation Results

To investigate how effective the comparative statics analysis is for finite values of  $\beta$ , I perform numerical analysis on how the equilibrium threshold changes as I vary the value of c. Since the equilibrium thresholds do not have analytical solutions, I implement simulation exercises with  $\alpha = 0.3$  and  $\beta = 0.5$  so that they satisfy the uniqueness condition of Proposition 1 and 2. For the other parameters, let z = 0 for computational convenience and  $\theta = 0.5$  following the estimation results using survey expectation data in Bordalo et al. (2020).

As expected by Proposition 2 and Corollary 1, equilibrium thresholds differ for Bayesian global games and diagnostic global games. As I change the value of c from 0 to 1, this difference in thresholds becomes narrower, at some point around  $c \in [0.5, 0.6]$  their order is reversed, and the gap becomes larger thereafter. Here, I present 3 cases where c = 0.1, 0.6, 0.9 which illustrate this property well in Figure 2, 3, and 4, where equilibrium thresholds are the intersections of the inverse of the normal distribution and red lines. In addition, I also implement sensitivity analysis with respect to  $\alpha$  and  $\beta$  when c = 0.1, 0.6, 0.9.

Figure 1: Equilibrium thresholds when c=0.1

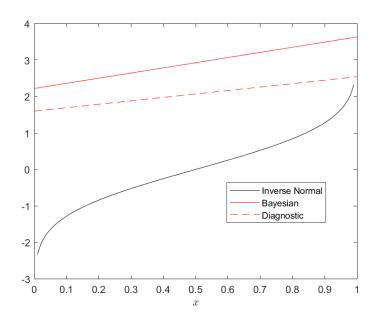


Figure 2: Equilibrium thresholds when c=0.6

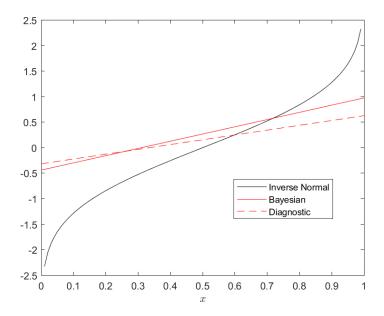


Figure 3: Equilibrium thresholds when c=0.9

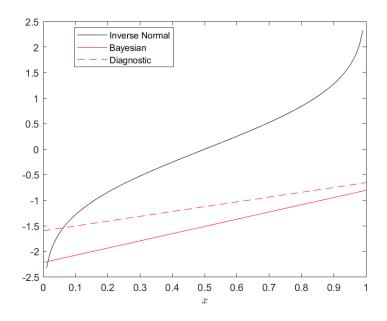


Figure 4: Sensitivity analysis when c = 0.1

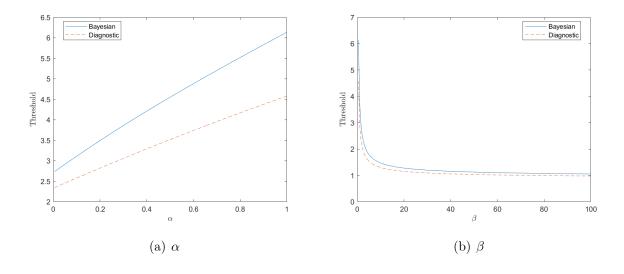


Figure 5: Sensitivity analysis when c=0.6

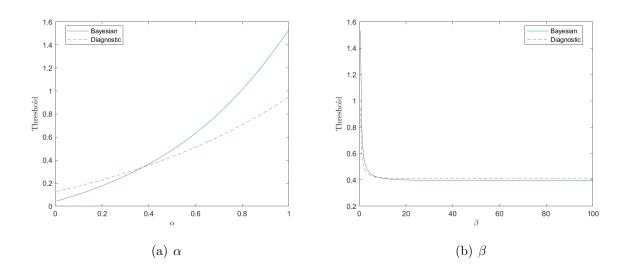
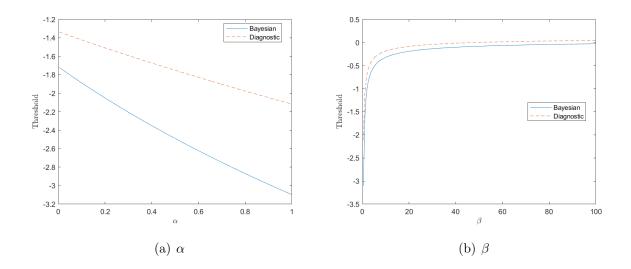


Figure 6: Sensitivity analysis when c = 0.9



## References

[1] Bordalo, P., Gennaioli, N., Ma, Y., and Shleifer, A. (2020). Overreaction in macroe-conomic expectations. *American Economic Review*, 110(9), 2748-82.