# knn

## November 16, 2020

```
[]: from google.colab import drive
   drive.mount('/content/drive/', force_remount=True)
   # enter the foldername in your Drive where you have saved the unzipped
   # 'cs231n' folder containing the '.py', 'classifiers' and 'datasets'
   # folders.
   # e.g. 'cs231n/assignments/assignment1/cs231n/'
   FOLDERNAME = 'cs231n/assignments/assignment11/cs231n/'
   assert FOLDERNAME is not None, "[!] Enter the foldername."
   %cd drive/My\ Drive
   %cp -r $FOLDERNAME ../../
   %cd ../../
   %cd cs231n/datasets/
   !bash get_datasets.sh
   %cd ../../
  Mounted at /content/drive/
  /content/drive/My Drive
  /content
  /content/cs231n/datasets
  --2020-10-15 13:16:04-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
  Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
  Connecting to www.cs.toronto.edu (www.cs.toronto.edu)|128.100.3.30|:80...
  connected.
  HTTP request sent, awaiting response... 200 OK
  Length: 170498071 (163M) [application/x-gzip]
  Saving to: cifar-10-python.tar.gz
  cifar-10-python.tar 100%[===========] 162.60M 15.5MB/s
                                                                       in 12s
  2020-10-15 13:16:16 (13.9 MB/s) - cifar-10-python.tar.gz saved
   [170498071/170498071]
  cifar-10-batches-py/
```

```
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data_batch_3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content
```

# 1 k-Nearest Neighbor (kNN) exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

The kNN classifier consists of two stages:

- During training, the classifier takes the training data and simply remembers it
- During testing, kNN classifies every test image by comparing to all training images and transfering the labels of the k most similar training examples
- The value of k is cross-validated

In this exercise you will implement these steps and understand the basic Image Classification pipeline, cross-validation, and gain proficiency in writing efficient, vectorized code.

```
[]: # Run some setup code for this notebook.
   import random
   import numpy as np
   from cs231n.data_utils import load_CIFAR10
   import matplotlib.pyplot as plt
   from google.colab.patches import cv2_imshow
   # This is a bit of magic to make matplotlib figures appear inline in the
    \rightarrownotebook
   # rather than in a new window.
   %matplotlib inline
   plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
   plt.rcParams['image.interpolation'] = 'nearest'
   plt.rcParams['image.cmap'] = 'gray'
   # Some more magic so that the notebook will reload external python modules;
   # see http://stackoverflow.com/questions/1907993/
    \rightarrow autoreload-of-modules-in-ipython
   %load_ext autoreload
   %autoreload 2
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

```
[]: # Load the raw CIFAR-10 data.
   cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
   # Cleaning up variables to prevent loading data multiple times (which may cause_
    →memory issue)
   try:
      del X_train, y_train
      del X_test, y_test
      print('Clear previously loaded data.')
   except:
      pass
   X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
   # As a sanity check, we print out the size of the training and test data.
   print('Training data shape: ', X_train.shape)
   print('Training labels shape: ', y_train.shape)
   print('Test data shape: ', X_test.shape)
   print('Test labels shape: ', y_test.shape)
   for i in range(10):
     print(y_train[i])
     cv2_imshow(X_train[i])
```

Clear previously loaded data.
Training data shape: (50000, 32, 32, 3)
Training labels shape: (50000,)
Test data shape: (10000, 32, 32, 3)
Test labels shape: (10000,)



9



9











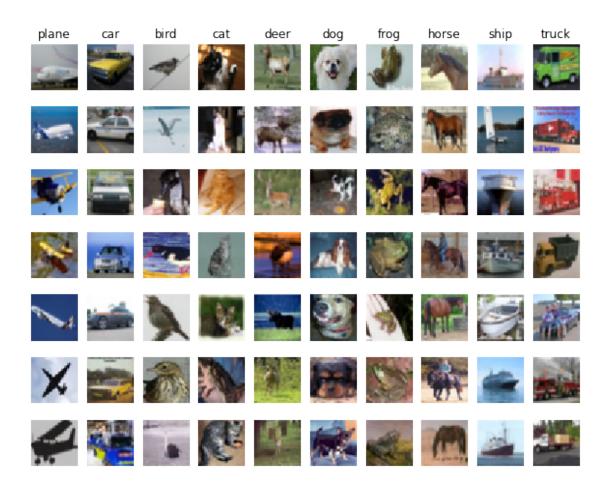






```
[]: # Visualize some examples from the dataset.
   # We show a few examples of training images from each class.
   classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse',

   num_classes = len(classes)
   samples_per_class = 7
   for y, cls in enumerate(classes):
       idxs = np.flatnonzero(y_train == y)
       idxs = np.random.choice(idxs, samples_per_class, replace=False)
       for i, idx in enumerate(idxs):
           plt_idx = i * num_classes + y + 1
           plt.subplot(samples_per_class, num_classes, plt_idx)
           plt.imshow(X_train[idx].astype('uint8'))
           plt.axis('off')
           if i == 0:
               plt.title(cls)
   plt.show()
```



```
[]: # Subsample the data for more efficient code execution in this exercise
   num_training = 5000
   mask = list(range(num_training))
   X_train = X_train[mask]
   y_train = y_train[mask]

   num_test = 500
   mask = list(range(num_test))
   X_test = X_test[mask]
   y_test = y_test[mask]

# Reshape the image data into rows
   X_train = np.reshape(X_train, (X_train.shape[0], -1))
   X_test = np.reshape(X_test, (X_test.shape[0], -1))
   print(X_train.shape, X_test.shape)
```

```
[]: from cs231n.classifiers import KNearestNeighbor

# Create a kNN classifier instance.

# Remember that training a kNN classifier is a noop:

# the Classifier simply remembers the data and does no further processing classifier = KNearestNeighbor()

classifier.train(X_train, y_train)
```

We would now like to classify the test data with the kNN classifier. Recall that we can break down this process into two steps:

- 1. First we must compute the distances between all test examples and all train examples.
- 2. Given these distances, for each test example we find the k nearest examples and have them vote for the label

Lets begin with computing the distance matrix between all training and test examples. For example, if there are Ntr training examples and Nte test examples, this stage should result in a Nte x Ntr matrix where each element (i,j) is the distance between the i-th test and j-th train example.

Note: For the three distance computations that we require you to implement in this notebook, you may not use the np.linalg.norm() function that numpy provides.

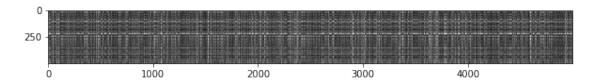
First, open cs231n/classifiers/k\_nearest\_neighbor.py and implement the function compute\_distances\_two\_loops that uses a (very inefficient) double loop over all pairs of (test, train) examples and computes the distance matrix one element at a time.

```
[]: # Open cs231n/classifiers/k_nearest_neighbor.py and implement
# compute_distances_two_loops.

# Test your implementation:
dists = classifier.compute_distances_two_loops(X_test)
print(dists.shape)
```

(500, 5000)

```
[]: # We can visualize the distance matrix: each row is a single test example and # its distances to training examples plt.imshow(dists, interpolation='none') plt.show()
```



### **Inline Question 1**

Notice the structured patterns in the distance matrix, where some rows or columns are visible brighter. (Note that with the default color scheme black indicates low distances while white indicates high distances.)

- What in the data is the cause behind the distinctly bright rows?
- What causes the columns?

Your Answer: fill this in.

```
[]: # Now implement the function predict_labels and run the code below:
# We use k = 1 (which is Nearest Neighbor).
y_test_pred = classifier.predict_labels(dists, k=1)

# Compute and print the fraction of correctly predicted examples
num_correct = np.sum(y_test_pred == y_test)
accuracy = float(num_correct) / num_test
print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))
```

Got 137 / 500 correct => accuracy: 0.274000

You should expect to see approximately 27% accuracy. Now lets try out a larger k, say k = 5:

```
[]: y_test_pred = classifier.predict_labels(dists, k=5)
num_correct = np.sum(y_test_pred == y_test)
accuracy = float(num_correct) / num_test
print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))
```

Got 139 / 500 correct => accuracy: 0.278000

You should expect to see a slightly better performance than with k = 1.

### **Inline Question 2**

We can also use other distance metrics such as L1 distance. For pixel values  $p_{ij}^{(k)}$  at location (i, j) of some image  $I_k$ ,

the mean  $\mu$  across all pixels over all images is

$$\mu = \frac{1}{nhw} \sum_{k=1}^{n} \sum_{i=1}^{h} \sum_{j=1}^{w} p_{ij}^{(k)}$$

And the pixel-wise mean  $\mu_{ij}$  across all images is

$$\mu_{ij} = \frac{1}{n} \sum_{k=1}^{n} p_{ij}^{(k)}.$$

The general standard deviation  $\sigma$  and pixel-wise standard deviation  $\sigma_{ij}$  is defined similarly.

Which of the following preprocessing steps will not change the performance of a Nearest Neighbor classifier that uses L1 distance? Select all that apply. 1. Subtracting the mean  $\mu$  ( $\tilde{p}_{ij}^{(k)} = p_{ij}^{(k)} - \mu$ .) 2. Subtracting the per pixel mean  $\mu_{ij}$  ( $\tilde{p}_{ij}^{(k)} = p_{ij}^{(k)} - \mu_{ij}$ .) 3. Subtracting the mean  $\mu$  and dividing by the standard deviation  $\sigma$ . 4. Subtracting the pixel-wise mean  $\mu_{ij}$  and dividing by the pixel-wise standard deviation  $\sigma_{ij}$ . 5. Rotating the coordinate axes of the data.

Your Answer:

Your Explanation:

```
[]: # Now lets speed up distance matrix computation by using partial vectorization
   # with one loop. Implement the function compute_distances_one_loop and run the
   # code below:
   dists_one = classifier.compute_distances_one_loop(X_test)
   # To ensure that our vectorized implementation is correct, we make sure that it
   # agrees with the naive implementation. There are many ways to decide whether
   # two matrices are similar; one of the simplest is the Frobenius norm. In case
   # you haven't seen it before, the Frobenius norm of two matrices is the square
   # root of the squared sum of differences of all elements; in other words,
    \rightarrowreshape
   # the matrices into vectors and compute the Euclidean distance between them.
   difference = np.linalg.norm(dists - dists_one, ord='fro')
   print('One loop difference was: %f' % (difference, ))
   if difference < 0.001:
       print('Good! The distance matrices are the same')
   else:
       print('Uh-oh! The distance matrices are different')
```

One loop difference was: 0.000000 Good! The distance matrices are the same

```
[]: # Now implement the fully vectorized version inside compute_distances_no_loops
# and run the code
dists_two = classifier.compute_distances_no_loops(X_test)

# check that the distance matrix agrees with the one we computed before:
difference = np.linalg.norm(dists - dists_two, ord='fro')
print('No loop difference was: %f' % (difference, ))
if difference < 0.001:
    print('Good! The distance matrices are the same')
else:
    print('Uh-oh! The distance matrices are different')</pre>
```

No loop difference was: 0.000000 Good! The distance matrices are the same

```
[]: # Let's compare how fast the implementations are

def time_function(f, *args):
    """

    Call a function f with args and return the time (in seconds) that it took
    →to execute.
    """

    import time
    tic = time.time()
    f(*args)
    toc = time.time()
```

Two loop version took 36.342132 seconds One loop version took 31.671019 seconds No loop version took 0.542927 seconds

#### 1.0.1 Cross-validation

We have implemented the k-Nearest Neighbor classifier but we set the value k = 5 arbitrarily. We will now determine the best value of this hyperparameter with cross-validation.

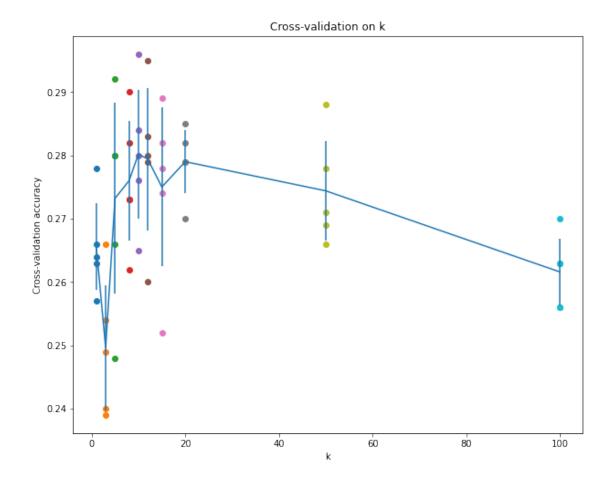
```
[]: num folds = 5
  k_{choices} = [1, 3, 5, 8, 10, 12, 15, 20, 50, 100]
  X train folds = []
  y train folds = []
  # TODO:
   →#
  # Split up the training data into folds. After splitting, X_train_folds and
  # y_train_folds should each be lists of length num_folds, where
   →#
  # y_train_folds[i] is the label vector for the points in X_train_folds[i].
   →#
  # Hint: Look up the numpy array_split function.
                                                                1.1
  # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
  X_train_folds = np.array_split(X_train, num_folds)
  y_train_folds = np.array_split(y_train, num_folds)
```

```
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
# A dictionary holding the accuracies for different values of k that we find
# when running cross-validation. After running cross-validation,
# k_to_accuracies[k] should be a list of length num_folds giving the different
# accuracy values that we found when using that value of k.
k_to_accuracies = {}
# TODO:
→#
\# Perform k-fold cross validation to find the best value of k. For each
# possible value of k, run the k-nearest-neighbor algorithm num_folds times,
⇔#
# where in each case you use all but one of the folds as training data and the
# last fold as a validation set. Store the accuracies for all fold and all
# values of k in the k_to_accuracies dictionary.
                                                                        ш
⇔#
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
for k in k_choices:
 k to accuracies[k] = []
 for j in range(num_folds):
   x_train_fold = np.concatenate([x for num, x in enumerate(X_train_folds) if__
 \rightarrownum!=j])
   y_train_fold = np.concatenate([y for num, y in enumerate(y_train_folds) if__
 \rightarrownum!=j])
   classifier.train(x_train_fold, y_train_fold)
   y fold_pred = classifier.predict(X_train_folds[j],k=k,num_loops =0)
   num_correct = np.sum(y_fold_pred == y_train_folds[j])
   accuracy = float(num_correct) / X_train_folds[j].shape[0]
   k_to_accuracies[k].append(accuracy)
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
print(k_to_accuracies)
# Print out the computed accuracies
for k in sorted(k_to_accuracies):
   for accuracy in k_to_accuracies[k]:
       print('k = %d, accuracy = %f' % (k, accuracy))
```

```
{1: [0.263, 0.257, 0.264, 0.278, 0.266], 3: [0.239, 0.249, 0.24, 0.266, 0.254],
5: [0.248, 0.266, 0.28, 0.292, 0.28], 8: [0.262, 0.282, 0.273, 0.29, 0.273], 10:
[0.265, 0.296, 0.276, 0.284, 0.28], 12: [0.26, 0.295, 0.279, 0.283, 0.28], 15:
[0.252, 0.289, 0.278, 0.282, 0.274], 20: [0.27, 0.279, 0.279, 0.282, 0.285], 50:
[0.271, 0.288, 0.278, 0.269, 0.266], 100: [0.256, 0.27, 0.263, 0.256, 0.263]
k = 1, accuracy = 0.263000
k = 1, accuracy = 0.257000
k = 1, accuracy = 0.264000
k = 1, accuracy = 0.278000
k = 1, accuracy = 0.266000
k = 3, accuracy = 0.239000
k = 3, accuracy = 0.249000
k = 3, accuracy = 0.240000
k = 3, accuracy = 0.266000
k = 3, accuracy = 0.254000
k = 5, accuracy = 0.248000
k = 5, accuracy = 0.266000
k = 5, accuracy = 0.280000
k = 5, accuracy = 0.292000
k = 5, accuracy = 0.280000
k = 8, accuracy = 0.262000
k = 8, accuracy = 0.282000
k = 8, accuracy = 0.273000
k = 8, accuracy = 0.290000
k = 8, accuracy = 0.273000
k = 10, accuracy = 0.265000
k = 10, accuracy = 0.296000
k = 10, accuracy = 0.276000
k = 10, accuracy = 0.284000
k = 10, accuracy = 0.280000
k = 12, accuracy = 0.260000
k = 12, accuracy = 0.295000
k = 12, accuracy = 0.279000
k = 12, accuracy = 0.283000
k = 12, accuracy = 0.280000
k = 15, accuracy = 0.252000
k = 15, accuracy = 0.289000
k = 15, accuracy = 0.278000
k = 15, accuracy = 0.282000
k = 15, accuracy = 0.274000
k = 20, accuracy = 0.270000
k = 20, accuracy = 0.279000
k = 20, accuracy = 0.279000
k = 20, accuracy = 0.282000
k = 20, accuracy = 0.285000
k = 50, accuracy = 0.271000
k = 50, accuracy = 0.288000
```

k = 50, accuracy = 0.278000

```
k = 50, accuracy = 0.269000
  k = 50, accuracy = 0.266000
  k = 100, accuracy = 0.256000
  k = 100, accuracy = 0.270000
  k = 100, accuracy = 0.263000
  k = 100, accuracy = 0.256000
  k = 100, accuracy = 0.263000
[]: # plot the raw observations
   for k in k_choices:
       accuracies = k_to_accuracies[k]
       plt.scatter([k] * len(accuracies), accuracies)
   # plot the trend line with error bars that correspond to standard deviation
   accuracies_mean = np.array([np.mean(v) for k,v in sorted(k_to_accuracies.
    →items())])
   accuracies_std = np.array([np.std(v) for k,v in sorted(k_to_accuracies.
    →items())])
   plt.errorbar(k_choices, accuracies_mean, yerr=accuracies_std)
   plt.title('Cross-validation on k')
   plt.xlabel('k')
   plt.ylabel('Cross-validation accuracy')
   plt.show()
```



```
[]: # Based on the cross-validation results above, choose the best value for k,
    # retrain the classifier using all the training data, and test it on the test
    # data. You should be able to get above 28% accuracy on the test data.
best_k = 10

classifier = KNearestNeighbor()
    classifier.train(X_train, y_train)
    y_test_pred = classifier.predict(X_test, k=best_k)

# Compute and display the accuracy
num_correct = np.sum(y_test_pred == y_test)
accuracy = float(num_correct) / num_test
print('Got %d / %d correct => accuracy: %f' % (num_correct, num_test, accuracy))
```

Got 141 / 500 correct => accuracy: 0.282000

## **Inline Question 3**

Which of the following statements about *k*-Nearest Neighbor (*k*-NN) are true in a classification setting, and for all *k*? Select all that apply. 1. The decision boundary of the k-NN classifier is linear. 2. The training error of a 1-NN will always be lower than that of 5-NN. 3. The test error of a 1-NN

will always be lower than that of a 5-NN. 4. The time needed to classify a test example with the k-NN classifier grows with the size of the training set. 5. None of the above.

```
Your Answer:
Your Explanation:
```

# 2 IMPORTANT

This is the end of this question. Please do the following:

- 1. Click File -> Save to make sure the latest checkpoint of this notebook is saved to your Drive.
- 2. Execute the cell below to download the modified .py files back to your drive.

## svm

## November 16, 2020

```
[2]: from google.colab import drive
   drive.mount('/content/drive', force_remount=True)
   # enter the foldername in your Drive where you have saved the unzipped
    # 'cs231n' folder containing the '.py', 'classifiers' and 'datasets'
    # folders.
    # e.g. 'cs231n/assignments/assignment1/cs231n/'
   FOLDERNAME = 'cs231n/assignments/assignment11/cs231n/'
   assert FOLDERNAME is not None, "[!] Enter the foldername."
   %cd drive/My\ Drive
   %cp -r $FOLDERNAME ../../
   %cd ../../
   %cd cs231n/datasets/
    !bash get_datasets.sh
   %cd ../../
   Mounted at /content/drive
   /content/drive/My Drive
   /content
   /content/cs231n/datasets
   --2020-10-31 14:42:00-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
   Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
   Connecting to www.cs.toronto.edu (www.cs.toronto.edu)|128.100.3.30|:80...
   connected.
   HTTP request sent, awaiting response... 200 OK
   Length: 170498071 (163M) [application/x-gzip]
   Saving to: cifar-10-python.tar.gz
   cifar-10-python.tar 100%[=========>] 162.60M 16.1MB/s
                                                                       in 12s
   2020-10-31 14:42:12 (14.0 MB/s) - cifar-10-python.tar.gz saved
   [170498071/170498071]
   cifar-10-batches-py/
```

```
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data_batch_3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content
```

```
[3]: from google.colab import drive drive.mount('/content/drive')
```

Drive already mounted at /content/drive; to attempt to forcibly remount, call drive.mount("/content/drive", force\_remount=True).

# 1 Multiclass Support Vector Machine exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

In this exercise you will:

- implement a fully-vectorized loss function for the SVM
- implement the fully-vectorized expression for its **analytic gradient**
- check your implementation using numerical gradient
- use a validation set to tune the learning rate and regularization strength
- optimize the loss function with SGD
- visualize the final learned weights

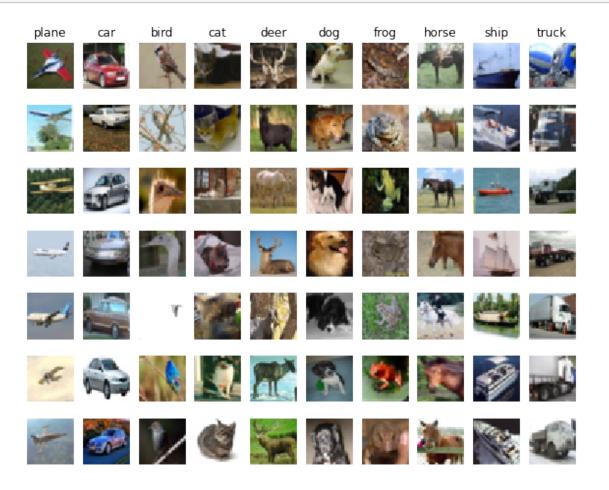
```
[4]: # Run some setup code for this notebook.
import random
import numpy as np
from cs231n.data_utils import load_CIFAR10
import matplotlib.pyplot as plt

# This is a bit of magic to make matplotlib figures appear inline in the
# notebook rather than in a new window.
%matplotlib inline
plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
plt.rcParams['image.interpolation'] = 'nearest'
plt.rcParams['image.cmap'] = 'gray'

# Some more magic so that the notebook will reload external python modules;
# see http://stackoverflow.com/questions/1907993/
→autoreload-of-modules-in-ipython
%load_ext autoreload
```

## 1.1 CIFAR-10 Data Loading and Preprocessing

```
[5]: # Load the raw CIFAR-10 data.
   cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
    # Cleaning up variables to prevent loading data multiple times (which may cause_
    →memory issue)
   try:
      del X_train, y_train
      del X_test, y_test
      print('Clear previously loaded data.')
   except:
      pass
   X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
   # As a sanity check, we print out the size of the training and test data.
   print('Training data shape: ', X_train.shape)
   print('Training labels shape: ', y_train.shape)
   print('Test data shape: ', X_test.shape)
   print('Test labels shape: ', y_test.shape)
   Training data shape: (50000, 32, 32, 3)
   Training labels shape: (50000,)
   Test data shape: (10000, 32, 32, 3)
   Test labels shape: (10000,)
[6]: # Visualize some examples from the dataset.
    # We show a few examples of training images from each class.
   classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', _
    num_classes = len(classes)
   samples_per_class = 7
   for y, cls in enumerate(classes):
        idxs = np.flatnonzero(y_train == y)
       idxs = np.random.choice(idxs, samples_per_class, replace=False)
       for i, idx in enumerate(idxs):
           plt_idx = i * num_classes + y + 1
           plt.subplot(samples_per_class, num_classes, plt_idx)
           plt.imshow(X_train[idx].astype('uint8'))
           plt.axis('off')
           if i == 0:
                plt.title(cls)
```



```
[7]: # Split the data into train, val, and test sets. In addition we will
  # create a small development set as a subset of the training data;
  # we can use this for development so our code runs faster.
  num_training = 49000
  num_validation = 1000
  num_test = 1000
  num_dev = 500

# Our validation set will be num_validation points from the original
  # training set.
  mask = range(num_training, num_training + num_validation)
  X_val = X_train[mask]
  y_val = y_train[mask]

# Our training set will be the first num_train points from the original
  # training set.
  mask = range(num_training)
```

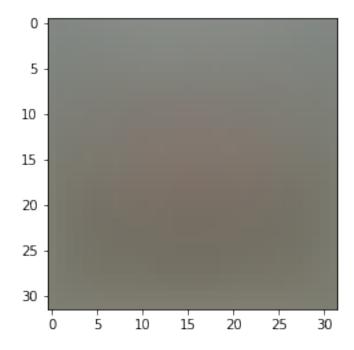
```
X_train = X_train[mask]
   y_train = y_train[mask]
   # We will also make a development set, which is a small subset of
   # the training set.
   mask = np.random.choice(num_training, num_dev, replace=False)
   X_dev = X_train[mask]
   y_dev = y_train[mask]
   # We use the first num_test points of the original test set as our
   # test set.
   mask = range(num_test)
   X_test = X_test[mask]
   y_test = y_test[mask]
   print('Train data shape: ', X_train.shape)
   print('Train labels shape: ', y_train.shape)
   print('Validation data shape: ', X_val.shape)
   print('Validation labels shape: ', y_val.shape)
   print('Test data shape: ', X_test.shape)
   print('Test labels shape: ', y_test.shape)
   print('dev data shape: ', X_dev.shape)
   print('dev labels shape: ', y_dev.shape)
   Train data shape: (49000, 32, 32, 3)
   Train labels shape: (49000,)
   Validation data shape: (1000, 32, 32, 3)
   Validation labels shape: (1000,)
   Test data shape: (1000, 32, 32, 3)
   Test labels shape: (1000,)
   dev data shape: (500, 32, 32, 3)
   dev labels shape: (500,)
[8]: # Preprocessing: reshape the image data into rows
   X_train = np.reshape(X_train, (X_train.shape[0], -1))
   X_val = np.reshape(X_val, (X_val.shape[0], -1))
   X_test = np.reshape(X_test, (X_test.shape[0], -1))
   X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))
   # As a sanity check, print out the shapes of the data
   print('Training data shape: ', X_train.shape)
   print('Validation data shape: ', X_val.shape)
   print('Test data shape: ', X test.shape)
   print('dev data shape: ', X_dev.shape)
```

Training data shape: (49000, 3072) Validation data shape: (1000, 3072)

Test data shape: (1000, 3072) dev data shape: (500, 3072)

```
[9]: # Preprocessing: subtract the mean image
    # first: compute the image mean based on the training data
    mean_image = np.mean(X_train, axis=0)
    print(mean_image[:10]) # print a few of the elements
    plt.figure(figsize=(4,4))
    plt.imshow(mean_image.reshape((32,32,3)).astype('uint8')) # visualize the mean_i
    \rightarrow image
    plt.show()
    # second: subtract the mean image from train and test data
    X_train -= mean_image
    X_val -= mean_image
    X_test -= mean_image
    X_dev -= mean_image
    # third: append the bias dimension of ones (i.e. bias trick) so that our SVM
    # only has to worry about optimizing a single weight matrix W.
    X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
    X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
    X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
    X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])
    print(X_train.shape, X_val.shape, X_test.shape, X_dev.shape)
```

[130.64189796 135.98173469 132.47391837 130.05569388 135.34804082 131.75402041 130.96055102 136.14328571 132.47636735 131.48467347]



(49000, 3073) (1000, 3073) (1000, 3073) (500, 3073)

### 1.2 SVM Classifier

Your code for this section will all be written inside cs231n/classifiers/linear\_svm.py.

As you can see, we have prefilled the function svm\_loss\_naive which uses for loops to evaluate the multiclass SVM loss function.

```
[10]: # Evaluate the naive implementation of the loss we provided for you:
    from cs231n.classifiers.linear_svm import svm_loss_naive
    import time

# generate a random SVM weight matrix of small numbers
W = np.random.randn(3073, 10) * 0.0001

loss, grad = svm_loss_naive(W, X_dev, y_dev, 0.000005)
    print('loss: %f' % (loss, ))
```

loss: 8.659787

The grad returned from the function above is right now all zero. Derive and implement the gradient for the SVM cost function and implement it inline inside the function svm\_loss\_naive. You will find it helpful to interleave your new code inside the existing function.

To check that you have correctly implemented the gradient correctly, you can numerically estimate the gradient of the loss function and compare the numeric estimate to the gradient that you computed. We have provided code that does this for you:

```
[11]: | # Once you've implemented the gradient, recompute it with the code below
     # and gradient check it with the function we provided for you
     # Compute the loss and its gradient at W.
     loss, grad = svm loss naive(W, X dev, y dev, 0.0)
     # Numerically compute the gradient along several randomly chosen dimensions,
      \rightarrow and
     \# compare them with your analytically computed gradient. The numbers should
     # almost exactly along all dimensions.
     from cs231n.gradient_check import grad_check_sparse
     f = lambda w: svm loss naive(w, X dev, y dev, 0.0)[0]
     grad_numerical = grad_check_sparse(f, W, grad)
     # do the gradient check once again with regularization turned on
     # you didn't forget the regularization gradient did you?
     loss, grad = svm_loss_naive(W, X_dev, y_dev, 5e1)
     f = lambda w: svm_loss_naive(w, X_dev, y_dev, 5e1)[0]
     grad_numerical = grad_check_sparse(f, W, grad)
```

```
numerical: 27.881347 analytic: 27.881347, relative error: 4.386332e-12
numerical: -3.442984 analytic: -3.442984, relative error: 9.022026e-11
numerical: -36.483650 analytic: -36.483650, relative error: 3.218546e-12
numerical: 0.860198 analytic: 0.860198, relative error: 1.343047e-10
numerical: 23.281454 analytic: 23.281454, relative error: 6.027333e-12
numerical: 3.938861 analytic: 3.938861, relative error: 8.596875e-11
numerical: 8.955658 analytic: 8.955658, relative error: 5.951003e-11
numerical: 0.811688 analytic: 0.811688, relative error: 3.363333e-10
numerical: -30.686231 analytic: -30.686231, relative error: 9.003166e-12
numerical: 25.263456 analytic: 25.263456, relative error: 2.832219e-13
numerical: -10.861268 analytic: -10.861268, relative error: 2.165120e-11
numerical: 9.152537 analytic: 9.152537, relative error: 7.335679e-12
numerical: 4.405232 analytic: 4.405232, relative error: 2.716483e-11
numerical: 21.657404 analytic: 21.657404, relative error: 4.714144e-12
numerical: 5.224227 analytic: 5.224227, relative error: 4.138674e-12
numerical: -0.932574 analytic: -0.932574, relative error: 4.662305e-11
numerical: 1.875749 analytic: 1.875749, relative error: 1.199456e-10
numerical: -1.179870 analytic: -1.179870, relative error: 1.759459e-10
numerical: -12.578606 analytic: -12.578606, relative error: 2.323077e-12
numerical: -8.810339 analytic: -8.810339, relative error: 2.909927e-11
```

### **Inline Ouestion 1**

It is possible that once in a while a dimension in the gradcheck will not match exactly. What could such a discrepancy be caused by? Is it a reason for concern? What is a simple example in one dimension where a gradient check could fail? How would change the margin affect of the frequency of this happening? Hint: the SVM loss function is not strictly speaking differentiable

Your Answer: fill this in.

Naive loss: 8.659787e+00 computed in 0.145068s Vectorized loss: 8.659787e+00 computed in 0.014101s difference: 0.000000

```
[13]: # Complete the implementation of sum_loss_vectorized, and compute the gradient
     # of the loss function in a vectorized way.
     # The naive implementation and the vectorized implementation should match, but
     # the vectorized version should still be much faster.
     tic = time.time()
     _, grad_naive = svm_loss_naive(W, X_dev, y_dev, 0.000005)
     toc = time.time()
     print('Naive loss and gradient: computed in %fs' % (toc - tic))
     tic = time.time()
     _, grad_vectorized = svm_loss_vectorized(W, X_dev, y_dev, 0.000005)
     toc = time.time()
     print('Vectorized loss and gradient: computed in %fs' % (toc - tic))
     # The loss is a single number, so it is easy to compare the values computed
     # by the two implementations. The gradient on the other hand is a matrix, so
     # we use the Frobenius norm to compare them.
     difference = np.linalg.norm(grad_naive - grad_vectorized, ord='fro')
     print('difference: %f' % difference)
```

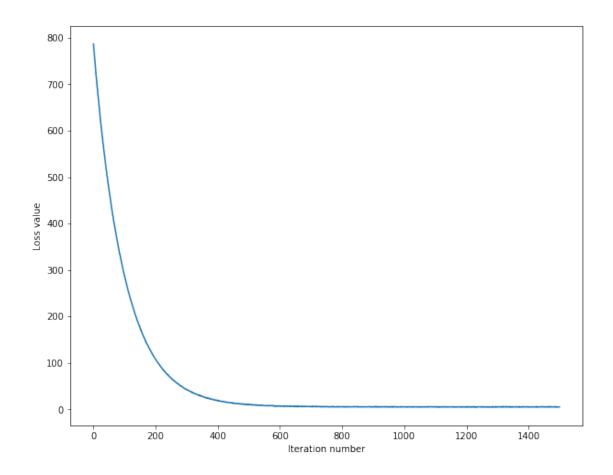
Naive loss and gradient: computed in 0.148298s Vectorized loss and gradient: computed in 0.014367s

#### 1.2.1 Stochastic Gradient Descent

plt.show()

We now have vectorized and efficient expressions for the loss, the gradient and our gradient matches the numerical gradient. We are therefore ready to do SGD to minimize the loss. Your code for this part will be written inside cs231n/classifiers/linear\_classifier.py.

```
[14]: # In the file linear_classifier.py, implement SGD in the function
     # LinearClassifier.train() and then run it with the code below.
     from cs231n.classifiers import LinearSVM
     svm = LinearSVM()
     tic = time.time()
     loss_hist = svm.train(X_train, y_train, learning_rate=1e-7, reg=2.5e4,
                           num_iters=1500, verbose=True)
     toc = time.time()
     print('That took %fs' % (toc - tic))
    iteration 0 / 1500: loss 786.533726
    iteration 100 / 1500: loss 286.593534
    iteration 200 / 1500: loss 107.794532
    iteration 300 / 1500: loss 42.922098
    iteration 400 / 1500: loss 18.738734
    iteration 500 / 1500: loss 10.745089
    iteration 600 / 1500: loss 7.399964
    iteration 700 / 1500: loss 5.539724
    iteration 800 / 1500: loss 5.789220
    iteration 900 / 1500: loss 5.354458
    iteration 1000 / 1500: loss 5.425209
    iteration 1100 / 1500: loss 6.027892
    iteration 1200 / 1500: loss 4.631618
    iteration 1300 / 1500: loss 5.351351
    iteration 1400 / 1500: loss 5.613090
    That took 9.735904s
[15]: # A useful debugging strategy is to plot the loss as a function of
     # iteration number:
     plt.plot(loss_hist)
     plt.xlabel('Iteration number')
     plt.ylabel('Loss value')
```



```
[16]: # Write the LinearSVM.predict function and evaluate the performance on both the
# training and validation set
y_train_pred = svm.predict(X_train)
print('training accuracy: %f' % (np.mean(y_train == y_train_pred), ))
y_val_pred = svm.predict(X_val)
print('validation accuracy: %f' % (np.mean(y_val == y_val_pred), ))
```

training accuracy: 0.370061 validation accuracy: 0.382000

```
[17]: # Use the validation set to tune hyperparameters (regularization strength and # learning rate). You should experiment with different ranges for the learning # rates and regularization strengths; if you are careful you should be able to # get a classification accuracy of about 0.39 on the validation set.

# Note: you may see runtime/overflow warnings during hyper-parameter search. # This may be caused by extreme values, and is not a bug.

# results is dictionary mapping tuples of the form # (learning_rate, regularization_strength) to tuples of the form
```

```
# (training accuracy, validation accuracy). The accuracy is simply the fraction
# of data points that are correctly classified.
results = {}
best_val = -1  # The highest validation accuracy that we have seen so far.
best_svm = None # The LinearSVM object that achieved the highest validation
\rightarrow rate.
# TODO:
→#
# Write code that chooses the best hyperparameters by tuning on the validation
# set. For each combination of hyperparameters, train a linear SVM on the
# training set, compute its accuracy on the training and validation sets, and \Box
# store these numbers in the results dictionary. In addition, store the best
# validation accuracy in best_val and the LinearSVM object that achieves this _
⇔#
# accuracy in best sum.
                                                                      ш
⇔#
# Hint: You should use a small value for num_iters as you develop your
# validation code so that the SVMs don't take much time to train; once you are
# confident that your validation code works, you should rerun the validation
# code with a larger value for num_iters.
⇔#
# Provided as a reference. You may or may not want to change these
\rightarrowhyperparameters
learning_rates = [1.25e-7, 1e-6]
regularization_strengths = [1.4e4, 5e4]
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
for lr in learning_rates:
 for reg in regularization_strengths:
   results[(lr, reg)] = []
   svm = LinearSVM()
```

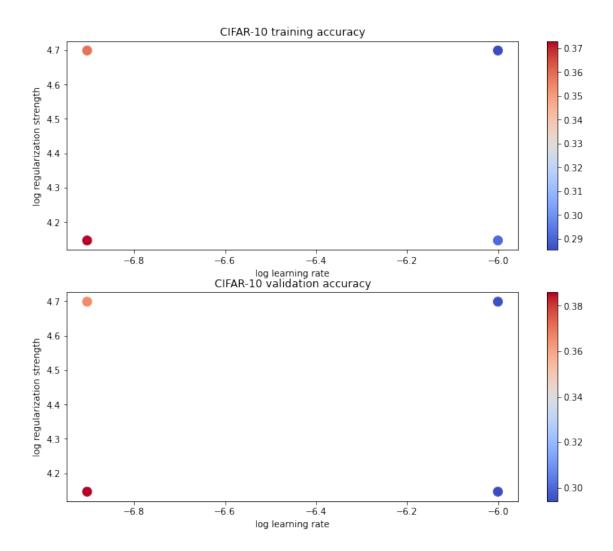
```
loss_hist = svm.train(X_train, y_train, learning rate=lr, reg=reg,_
 →num_iters=1500, verbose=True)
   y_train_pred = svm.predict(X_train)
   acc_train = np.mean(y_train == y_train_pred)
   y_val_pred = svm.predict(X_val)
   acc val = np.mean(y val == y val pred)
   results[(lr, reg)].append(acc train)
   results[(lr, reg)].append(acc val)
   if acc_val > best_val:
     best_val = acc_val
      best_svm = svm
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
# Print out results.
for lr, reg in sorted(results):
   train_accuracy, val_accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
                lr, reg, train_accuracy, val_accuracy))
print('best validation accuracy achieved during cross-validation: %f' %11
 →best_val)
```

```
iteration 0 / 1500: loss 456.818688
iteration 100 / 1500: loss 222.557510
iteration 200 / 1500: loss 111.705424
iteration 300 / 1500: loss 56.952427
iteration 400 / 1500: loss 30.605229
iteration 500 / 1500: loss 17.599649
iteration 600 / 1500: loss 11.339447
iteration 700 / 1500: loss 7.897025
iteration 800 / 1500: loss 6.633609
iteration 900 / 1500: loss 5.903457
iteration 1000 / 1500: loss 5.461978
iteration 1100 / 1500: loss 5.035524
iteration 1200 / 1500: loss 5.135650
iteration 1300 / 1500: loss 4.837058
iteration 1400 / 1500: loss 4.713922
iteration 0 / 1500: loss 1555.285462
iteration 100 / 1500: loss 129.174907
iteration 200 / 1500: loss 15.753453
iteration 300 / 1500: loss 6.449913
iteration 400 / 1500: loss 6.290277
iteration 500 / 1500: loss 5.647991
iteration 600 / 1500: loss 5.617289
iteration 700 / 1500: loss 5.540229
```

```
iteration 800 / 1500: loss 5.826255
    iteration 900 / 1500: loss 6.098454
    iteration 1000 / 1500: loss 5.140625
    iteration 1100 / 1500: loss 5.355898
    iteration 1200 / 1500: loss 5.133326
    iteration 1300 / 1500: loss 6.503322
    iteration 1400 / 1500: loss 5.827592
    iteration 0 / 1500: loss 459.459682
    iteration 100 / 1500: loss 8.722664
    iteration 200 / 1500: loss 6.756962
    iteration 300 / 1500: loss 6.640996
    iteration 400 / 1500: loss 6.559548
    iteration 500 / 1500: loss 6.241611
    iteration 600 / 1500: loss 6.604723
    iteration 700 / 1500: loss 6.222683
    iteration 800 / 1500: loss 6.616584
    iteration 900 / 1500: loss 6.821145
    iteration 1000 / 1500: loss 6.479117
    iteration 1100 / 1500: loss 5.508869
    iteration 1200 / 1500: loss 6.566778
    iteration 1300 / 1500: loss 6.122478
    iteration 1400 / 1500: loss 6.043103
    iteration 0 / 1500: loss 1560.996706
    iteration 100 / 1500: loss 6.001586
    iteration 200 / 1500: loss 7.831540
    iteration 300 / 1500: loss 6.435348
    iteration 400 / 1500: loss 7.786200
    iteration 500 / 1500: loss 7.618199
    iteration 600 / 1500: loss 8.281708
    iteration 700 / 1500: loss 6.791543
    iteration 800 / 1500: loss 6.605087
    iteration 900 / 1500: loss 8.691999
    iteration 1000 / 1500: loss 7.043801
    iteration 1100 / 1500: loss 6.824627
    iteration 1200 / 1500: loss 7.134897
    iteration 1300 / 1500: loss 7.187824
    iteration 1400 / 1500: loss 6.918724
    lr 1.250000e-07 reg 1.400000e+04 train accuracy: 0.373122 val accuracy: 0.386000
    lr 1.250000e-07 reg 5.000000e+04 train accuracy: 0.358959 val accuracy: 0.366000
    lr 1.000000e-06 reg 1.400000e+04 train accuracy: 0.291265 val accuracy: 0.294000
    lr 1.000000e-06 reg 5.000000e+04 train accuracy: 0.285184 val accuracy: 0.295000
    best validation accuracy achieved during cross-validation: 0.386000
[18]: # Visualize the cross-validation results
```

import math
import pdb

```
# pdb.set_trace()
x_scatter = [math.log10(x[0]) for x in results]
y_scatter = [math.log10(x[1]) for x in results]
# plot training accuracy
marker size = 100
colors = [results[x][0] for x in results]
plt.subplot(2, 1, 1)
plt.tight_layout(pad=3)
plt.scatter(x_scatter, y_scatter, marker_size, c=colors, cmap=plt.cm.coolwarm)
plt.colorbar()
plt.xlabel('log learning rate')
plt.ylabel('log regularization strength')
plt.title('CIFAR-10 training accuracy')
# plot validation accuracy
colors = [results[x][1] for x in results] # default size of markers is 20
plt.subplot(2, 1, 2)
plt.scatter(x_scatter, y_scatter, marker_size, c=colors, cmap=plt.cm.coolwarm)
plt.colorbar()
plt.xlabel('log learning rate')
plt.ylabel('log regularization strength')
plt.title('CIFAR-10 validation accuracy')
plt.show()
```



```
[19]: # Evaluate the best sum on test set
y_test_pred = best_svm.predict(X_test)
test_accuracy = np.mean(y_test == y_test_pred)
print('linear SVM on raw pixels final test set accuracy: %f' % test_accuracy)
```

linear SVM on raw pixels final test set accuracy: 0.364000

```
[20]: # Visualize the learned weights for each class.
# Depending on your choice of learning rate and regularization strength, these
→ may
# or may not be nice to look at.
w = best_svm.W[:-1,:] # strip out the bias
w = w.reshape(32, 32, 3, 10)
w_min, w_max = np.min(w), np.max(w)
classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', 
→ 'ship', 'truck']
```

```
for i in range(10):
    plt.subplot(2, 5, i + 1)

# Rescale the weights to be between 0 and 255
    wimg = 255.0 * (w[:, :, :, i].squeeze() - w_min) / (w_max - w_min)
    plt.imshow(wimg.astype('uint8'))
    plt.axis('off')
    plt.title(classes[i])
```





### Inline question 2

Describe what your visualized SVM weights look like, and offer a brief explanation for why they look they way that they do.

Your Answer: fill this in

## 2 IMPORTANT

This is the end of this question. Please do the following:

- 1. Click File -> Save to make sure the latest checkpoint of this notebook is saved to your Drive.
- 2. Execute the cell below to download the modified .py files back to your drive.

# softmax

## November 16, 2020

```
[]: from google.colab import drive
   drive.mount('/content/drive', force_remount=True)
   # enter the foldername in your Drive where you have saved the unzipped
   # 'cs231n' folder containing the '.py', 'classifiers' and 'datasets'
   # folders.
   # e.g. 'cs231n/assignments/assignment1/cs231n/'
   FOLDERNAME = 'cs231n/assignments/assignment11/cs231n/'
   assert FOLDERNAME is not None, "[!] Enter the foldername."
   %cd drive/My\ Drive
   %cp -r $FOLDERNAME ../../
   %cd ../../
   %cd cs231n/datasets/
   !bash get_datasets.sh
   %cd ../../
  Mounted at /content/drive
  /content/drive/My Drive
  /content
  /content/cs231n/datasets
  --2020-10-29 00:28:29-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
  Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
  Connecting to www.cs.toronto.edu (www.cs.toronto.edu)|128.100.3.30|:80...
  connected.
  HTTP request sent, awaiting response... 200 OK
  Length: 170498071 (163M) [application/x-gzip]
  Saving to: cifar-10-python.tar.gz
  cifar-10-python.tar 100%[=========] 162.60M 57.6MB/s
                                                                     in 2.8s
  2020-10-29 00:28:31 (57.6 MB/s) - cifar-10-python.tar.gz saved
   [170498071/170498071]
  cifar-10-batches-py/
```

```
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data_batch_3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content
```

## 1 Softmax exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

This exercise is analogous to the SVM exercise. You will:

- implement a fully-vectorized **loss function** for the Softmax classifier
- implement the fully-vectorized expression for its analytic gradient
- check your implementation with numerical gradient
- use a validation set to tune the learning rate and regularization strength
- optimize the loss function with SGD
- visualize the final learned weights

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

```
[]: def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000, \_ \infty num_dev=500):

"""

Load the CIFAR-10 dataset from disk and perform preprocessing to prepare
```

```
it for the linear classifier. These are the same steps as we used for the
  SVM, but condensed to a single function.
  # Load the raw CIFAR-10 data
  cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
  # Cleaning up variables to prevent loading data multiple times (which may u
→cause memory issue)
  try:
     del X_train, y_train
     del X_test, y_test
     print('Clear previously loaded data.')
  except:
     pass
  X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
  # subsample the data
  mask = list(range(num_training, num_training + num_validation))
  X_val = X_train[mask]
  y val = y train[mask]
  mask = list(range(num_training))
  X_train = X_train[mask]
  y_train = y_train[mask]
  mask = list(range(num_test))
  X_test = X_test[mask]
  y_test = y_test[mask]
  mask = np.random.choice(num_training, num_dev, replace=False)
  X_dev = X_train[mask]
  y_dev = y_train[mask]
  # Preprocessing: reshape the image data into rows
  X_train = np.reshape(X_train, (X_train.shape[0], -1))
  X_val = np.reshape(X_val, (X_val.shape[0], -1))
  X_test = np.reshape(X_test, (X_test.shape[0], -1))
  X_dev = np.reshape(X_dev, (X_dev.shape[0], -1))
  # Normalize the data: subtract the mean image
  mean_image = np.mean(X_train, axis = 0)
  X_train -= mean_image
  X_val -= mean_image
  X_test -= mean_image
  X_dev -= mean_image
  # add bias dimension and transform into columns
  X_train = np.hstack([X_train, np.ones((X_train.shape[0], 1))])
  X_val = np.hstack([X_val, np.ones((X_val.shape[0], 1))])
```

```
X_test = np.hstack([X_test, np.ones((X_test.shape[0], 1))])
X_dev = np.hstack([X_dev, np.ones((X_dev.shape[0], 1))])

return X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev

# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test, X_dev, y_dev = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
print('dev data shape: ', X_dev.shape)
print('dev labels shape: ', y_dev.shape)
```

Train data shape: (49000, 3073)
Train labels shape: (49000,)
Validation data shape: (1000, 3073)
Validation labels shape: (1000,)
Test data shape: (1000, 3073)
Test labels shape: (1000,)
dev data shape: (500, 3073)
dev labels shape: (500,)

#### 1.1 Softmax Classifier

Your code for this section will all be written inside cs231n/classifiers/softmax.py.

```
[]: # First implement the naive softmax loss function with nested loops.
# Open the file cs231n/classifiers/softmax.py and implement the
# softmax_loss_naive function.

from cs231n.classifiers.softmax import softmax_loss_naive
import time

# Generate a random softmax weight matrix and use it to compute the loss.
W = np.random.randn(3073, 10) * 0.0001
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0)

# As a rough sanity check, our loss should be something close to -log(0.1).
print('loss: %f' % loss)
print('sanity check: %f' % (-np.log(0.1)))
```

loss: 2.394795

sanity check: 2.302585

#### **Inline Question 1**

Why do we expect our loss to be close to -log(0.1)? Explain briefly.\*\*

```
Your Answer: Fill this in
```

```
[]: # Complete the implementation of softmax_loss_naive and implement a (naive)
# version of the gradient that uses nested loops.
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 0.0)

# As we did for the SVM, use numeric gradient checking as a debugging tool.
# The numeric gradient should be close to the analytic gradient.
from cs231n.gradient_check import grad_check_sparse
f = lambda w: softmax_loss_naive(w, X_dev, y_dev, 0.0)[0]
grad_numerical = grad_check_sparse(f, W, grad, 10)

# similar to SVM case, do another gradient check with regularization
loss, grad = softmax_loss_naive(W, X_dev, y_dev, 5e1)
f = lambda w: softmax_loss_naive(w, X_dev, y_dev, 5e1)[0]
grad_numerical = grad_check_sparse(f, W, grad, 10)
```

```
numerical: 0.605491 analytic: 0.605491, relative error: 9.614766e-08
numerical: -4.518609 analytic: -4.518609, relative error: 6.510690e-10
numerical: 0.236108 analytic: 0.236108, relative error: 1.706660e-08
numerical: -0.209569 analytic: -0.209569, relative error: 2.367489e-07
numerical: 0.471036 analytic: 0.471036, relative error: 5.384458e-08
numerical: -2.956495 analytic: -2.956495, relative error: 4.285929e-09
numerical: -3.774968 analytic: -3.774968, relative error: 2.093984e-10
numerical: 1.405816 analytic: 1.405816, relative error: 4.933502e-08
numerical: -1.219000 analytic: -1.219000, relative error: 6.069524e-08
numerical: -4.677304 analytic: -4.677304, relative error: 6.600641e-09
numerical: -0.757290 analytic: -0.757290, relative error: 2.750439e-08
numerical: 2.149280 analytic: 2.149280, relative error: 2.925648e-08
numerical: 3.412024 analytic: 3.412024, relative error: 8.672940e-10
numerical: 0.829898 analytic: 0.829898, relative error: 6.648078e-08
numerical: 0.854756 analytic: 0.854756, relative error: 5.413736e-08
numerical: -0.585696 analytic: -0.585696, relative error: 1.397793e-08
numerical: 3.150207 analytic: 3.150207, relative error: 2.534555e-08
numerical: 0.045894 analytic: 0.045894, relative error: 4.290633e-07
numerical: 0.886911 analytic: 0.886911, relative error: 6.036951e-08
numerical: -0.673988 analytic: -0.673988, relative error: 2.747657e-08
```

naive loss: 2.394795e+00 computed in 0.102476s vectorized loss: 2.394795e+00 computed in 0.010961s

Loss difference: 0.000000 Gradient difference: 0.000000

```
[]: # Use the validation set to tune hyperparameters (regularization strength and
   # learning rate). You should experiment with different ranges for the learning
   # rates and regularization strengths; if you are careful you should be able to
   # get a classification accuracy of over 0.35 on the validation set.
  from cs231n.classifiers import Softmax
  results = {}
  best val = -1
  best softmax = None
  # TODO:
   ⇔#
   # Use the validation set to set the learning rate and regularization strength.
   # This should be identical to the validation that you did for the SVM; save
   # the best trained softmax classifer in best_softmax.
   # Provided as a reference. You may or may not want to change these
   \rightarrowhyperparameters
  learning_rates = [1e-7, 5e-7]
  regularization_strengths = [2.5e4, 5e4]
```

```
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
for lr in learning_rates:
 for reg in regularization_strengths:
   results[(lr, reg)] = []
    softmax = Softmax()
   loss_hist = softmax.train(X_train, y_train, learning_rate=lr, reg=reg,_
 →num iters=1500, verbose=True)
   y_train_pred = softmax.predict(X_train)
   acc_train = np.mean(y_train == y_train_pred)
   y_val_pred = softmax.predict(X_val)
   acc_val = np.mean(y_val == y_val_pred)
   results[(lr, reg)].append(acc_train)
   results[(lr, reg)].append(acc_val)
   if acc_val > best_val:
     best_val = acc_val
      best softmax = softmax
# ****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) ****
# Print out results.
for lr, reg in sorted(results):
   train_accuracy, val_accuracy = results[(lr, reg)]
   print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
                lr, reg, train_accuracy, val_accuracy))
print('best validation accuracy achieved during cross-validation: %f' %⊔
 →best val)
```

```
iteration 0 / 1500: loss 778.967814
iteration 100 / 1500: loss 286.086076
iteration 200 / 1500: loss 105.865535
iteration 300 / 1500: loss 40.120965
iteration 400 / 1500: loss 15.966006
iteration 500 / 1500: loss 7.206294
iteration 600 / 1500: loss 3.960088
iteration 700 / 1500: loss 2.785788
iteration 800 / 1500: loss 2.291647
iteration 900 / 1500: loss 2.127284
iteration 1000 / 1500: loss 2.061098
iteration 1100 / 1500: loss 2.145964
iteration 1200 / 1500: loss 2.030166
iteration 1300 / 1500: loss 2.102928
iteration 1400 / 1500: loss 2.034194
iteration 0 / 1500: loss 1524.027386
```

```
iteration 100 / 1500: loss 205.243586
iteration 200 / 1500: loss 29.247044
iteration 300 / 1500: loss 5.776613
iteration 400 / 1500: loss 2.596689
iteration 500 / 1500: loss 2.178669
iteration 600 / 1500: loss 2.186847
iteration 700 / 1500: loss 2.127332
iteration 800 / 1500: loss 2.165645
iteration 900 / 1500: loss 2.148452
iteration 1000 / 1500: loss 2.155111
iteration 1100 / 1500: loss 2.084234
iteration 1200 / 1500: loss 2.132858
iteration 1300 / 1500: loss 2.120289
iteration 1400 / 1500: loss 2.110100
iteration 0 / 1500: loss 778.279117
iteration 100 / 1500: loss 6.874783
iteration 200 / 1500: loss 2.104041
iteration 300 / 1500: loss 2.143942
iteration 400 / 1500: loss 2.086809
iteration 500 / 1500: loss 2.031536
iteration 600 / 1500: loss 2.084568
iteration 700 / 1500: loss 2.068742
iteration 800 / 1500: loss 2.071735
iteration 900 / 1500: loss 2.105688
iteration 1000 / 1500: loss 2.062162
iteration 1100 / 1500: loss 2.130759
iteration 1200 / 1500: loss 2.069172
iteration 1300 / 1500: loss 2.076074
iteration 1400 / 1500: loss 2.083278
iteration 0 / 1500: loss 1543.512413
iteration 100 / 1500: loss 2.175845
iteration 200 / 1500: loss 2.162003
iteration 300 / 1500: loss 2.180083
iteration 400 / 1500: loss 2.144724
iteration 500 / 1500: loss 2.117558
iteration 600 / 1500: loss 2.165986
iteration 700 / 1500: loss 2.171711
iteration 800 / 1500: loss 2.126282
iteration 900 / 1500: loss 2.119241
iteration 1000 / 1500: loss 2.190395
iteration 1100 / 1500: loss 2.150561
iteration 1200 / 1500: loss 2.126373
iteration 1300 / 1500: loss 2.166430
iteration 1400 / 1500: loss 2.168511
lr 1.000000e-07 reg 2.500000e+04 train accuracy: 0.324388 val accuracy: 0.334000
lr 1.000000e-07 reg 5.000000e+04 train accuracy: 0.305122 val accuracy: 0.325000
1r 5.000000e-07 reg 2.500000e+04 train accuracy: 0.329592 val accuracy: 0.340000
lr 5.000000e-07 reg 5.000000e+04 train accuracy: 0.301490 val accuracy: 0.320000
```

best validation accuracy achieved during cross-validation: 0.340000

```
[]: # evaluate on test set
    # Evaluate the best softmax on test set
    y_test_pred = best_softmax.predict(X_test)
    test_accuracy = np.mean(y_test == y_test_pred)
    print('softmax on raw pixels final test set accuracy: %f' % (test_accuracy, ))
```

softmax on raw pixels final test set accuracy: 0.346000

## **Inline Question 2** - True or False

Suppose the overall training loss is defined as the sum of the per-datapoint loss over all training examples. It is possible to add a new datapoint to a training set that would leave the SVM loss unchanged, but this is not the case with the Softmax classifier loss.

### Your Answer:

Your Explanation:





## 2 IMPORTANT

This is the end of this question. Please do the following:

- 1. Click File -> Save to make sure the latest checkpoint of this notebook is saved to your Drive
- 2. Execute the cell below to download the modified .py files back to your drive.

# two\_layer\_net

### November 16, 2020

```
[]: from google.colab import drive
   drive.mount('/content/drive', force_remount=True)
   # enter the foldername in your Drive where you have saved the unzipped
   # 'cs231n' folder containing the '.py', 'classifiers' and 'datasets'
   # folders.
   # e.g. 'cs231n/assignments/assignment1/cs231n/'
   FOLDERNAME = 'cs231n/assignments/assignment11/cs231n/'
   assert FOLDERNAME is not None, "[!] Enter the foldername."
   %cd drive/My\ Drive
   %cp -r $FOLDERNAME ../../
   %cd ../../
   %cd cs231n/datasets/
   !bash get_datasets.sh
   %cd ../../
  Mounted at /content/drive
  /content/drive/My Drive
  /content
  /content/cs231n/datasets
  --2020-10-30 23:19:45-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
  Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
  Connecting to www.cs.toronto.edu (www.cs.toronto.edu)|128.100.3.30|:80...
  connected.
  HTTP request sent, awaiting response... 200 OK
  Length: 170498071 (163M) [application/x-gzip]
  Saving to: cifar-10-python.tar.gz
  cifar-10-python.tar 100%[============] 162.60M 48.0MB/s
                                                                      in 3.7s
  2020-10-30 23:19:49 (43.9 MB/s) - cifar-10-python.tar.gz saved
   [170498071/170498071]
  cifar-10-batches-py/
```

```
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data_batch_3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content
```

# 1 Implementing a Neural Network

In this exercise we will develop a neural network with fully-connected layers to perform classification, and test it out on the CIFAR-10 dataset.

```
[]: # A bit of setup
   import numpy as np
   import matplotlib.pyplot as plt
   from cs231n.classifiers.neural_net import TwoLayerNet
   %matplotlib inline
   plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
   plt.rcParams['image.interpolation'] = 'nearest'
   plt.rcParams['image.cmap'] = 'gray'
   # for auto-reloading external modules
   # see http://stackoverflow.com/questions/1907993/
    \rightarrow autoreload-of-modules-in-ipython
   %load ext autoreload
   %autoreload 2
   def rel_error(x, y):
        """ returns relative error """
       return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

We will use the class TwoLayerNet in the file cs231n/classifiers/neural\_net.py to represent instances of our network. The network parameters are stored in the instance variable self.params where keys are string parameter names and values are numpy arrays. Below, we initialize toy data and a toy model that we will use to develop your implementation.

```
[]: # Create a small net and some toy data to check your implementations.
# Note that we set the random seed for repeatable experiments.

input_size = 4
```

```
hidden_size = 10
num_classes = 3
num_inputs = 5

def init_toy_model():
    np.random.seed(0)
    return TwoLayerNet(input_size, hidden_size, num_classes, std=1e-1)

def init_toy_data():
    np.random.seed(1)
    X = 10 * np.random.randn(num_inputs, input_size)
    y = np.array([0, 1, 2, 2, 1])
    return X, y

net = init_toy_model()
X, y = init_toy_data()
```

# 2 Forward pass: compute scores

Open the file cs231n/classifiers/neural\_net.py and look at the method TwoLayerNet.loss. This function is very similar to the loss functions you have written for the SVM and Softmax exercises: It takes the data and weights and computes the class scores, the loss, and the gradients on the parameters.

Implement the first part of the forward pass which uses the weights and biases to compute the scores for all inputs.

```
[]: scores = net.loss(X)
   print('Your scores:')
   print(scores)
   print()
   print('correct scores:')
   correct_scores = np.asarray([
     [-0.81233741, -1.27654624, -0.70335995],
     [-0.17129677, -1.18803311, -0.47310444],
     [-0.51590475, -1.01354314, -0.8504215],
     [-0.15419291, -0.48629638, -0.52901952],
     [-0.00618733, -0.12435261, -0.15226949]])
   print(correct scores)
   print()
   # The difference should be very small. We get < 1e-7
   print('Difference between your scores and correct scores:')
   print(np.sum(np.abs(scores - correct_scores)))
```

```
Your scores:
[[-0.81233741 -1.27654624 -0.70335995]
[-0.17129677 -1.18803311 -0.47310444]
```

```
[-0.51590475 -1.01354314 -0.8504215]
[-0.15419291 -0.48629638 -0.52901952]
[-0.00618733 -0.12435261 -0.15226949]]

correct scores:
[[-0.81233741 -1.27654624 -0.70335995]
[-0.17129677 -1.18803311 -0.47310444]
[-0.51590475 -1.01354314 -0.8504215]
[-0.15419291 -0.48629638 -0.52901952]
[-0.00618733 -0.12435261 -0.15226949]]

Difference between your scores and correct scores:
3.6802720745909845e-08
```

# 3 Forward pass: compute loss

In the same function, implement the second part that computes the data and regularization loss.

```
[]: loss, _ = net.loss(X, y, reg=0.05)
    correct_loss = 1.30378789133

# should be very small, we get < 1e-12
    print('Difference between your loss and correct loss:')
    print(np.sum(np.abs(loss - correct_loss)))</pre>
```

Difference between your loss and correct loss: 1.7985612998927536e-13

# 4 Backward pass

Implement the rest of the function. This will compute the gradient of the loss with respect to the variables W1, b1, W2, and b2. Now that you (hopefully!) have a correctly implemented forward pass, you can debug your backward pass using a numeric gradient check:

```
print('%s max relative error: %e' % (param_name, rel_error(param_grad_num, ⊔ → grads[param_name])))
```

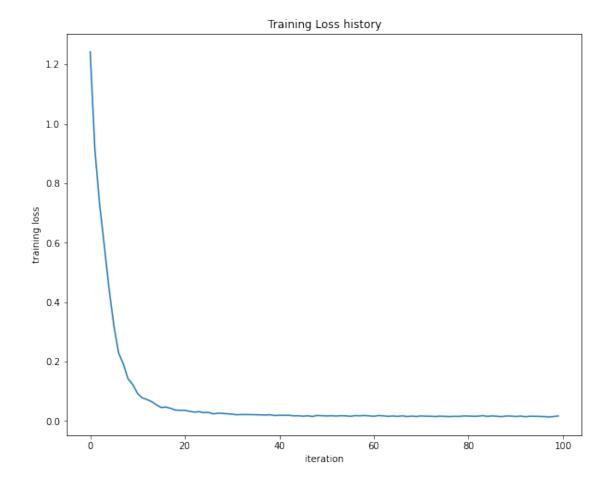
```
W2 max relative error: 3.440708e-09
b2 max relative error: 4.447625e-11
W1 max relative error: 3.561318e-09
b1 max relative error: 2.738421e-09
```

### 5 Train the network

To train the network we will use stochastic gradient descent (SGD), similar to the SVM and Softmax classifiers. Look at the function TwoLayerNet.train and fill in the missing sections to implement the training procedure. This should be very similar to the training procedure you used for the SVM and Softmax classifiers. You will also have to implement TwoLayerNet.predict, as the training process periodically performs prediction to keep track of accuracy over time while the network trains.

Once you have implemented the method, run the code below to train a two-layer network on toy data. You should achieve a training loss less than 0.02.

Final training loss: 0.017149607938732093



## 6 Load the data

Now that you have implemented a two-layer network that passes gradient checks and works on toy data, it's time to load up our favorite CIFAR-10 data so we can use it to train a classifier on a real dataset.

```
try:
       del X_train, y_train
       del X_test, y_test
       print('Clear previously loaded data.')
    except:
       pass
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
    # Subsample the data
    mask = list(range(num_training, num_training + num_validation))
    X_val = X_train[mask]
    y_val = y_train[mask]
    mask = list(range(num_training))
    X_train = X_train[mask]
    y_train = y_train[mask]
    mask = list(range(num_test))
    X_test = X_test[mask]
    y_test = y_test[mask]
    # Normalize the data: subtract the mean image
    mean_image = np.mean(X_train, axis=0)
    X_train -= mean_image
    X val -= mean image
    X_test -= mean_image
    # Reshape data to rows
    X_train = X_train.reshape(num_training, -1)
    X_val = X_val.reshape(num_validation, -1)
    X_test = X_test.reshape(num_test, -1)
    return X_train, y_train, X_val, y_val, X_test, y_test
# Invoke the above function to get our data.
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
print('Train data shape: ', X_train.shape)
print('Train labels shape: ', y_train.shape)
print('Validation data shape: ', X_val.shape)
print('Validation labels shape: ', y_val.shape)
print('Test data shape: ', X_test.shape)
print('Test labels shape: ', y_test.shape)
```

Train data shape: (49000, 3072)
Train labels shape: (49000,)
Validation data shape: (1000, 3072)
Validation labels shape: (1000,)

```
Test data shape: (1000, 3072)
Test labels shape: (1000,)
```

### 7 Train a network

To train our network we will use SGD. In addition, we will adjust the learning rate with an exponential learning rate schedule as optimization proceeds; after each epoch, we will reduce the learning rate by multiplying it by a decay rate.

```
iteration 0 / 1000: loss 2.302954
iteration 100 / 1000: loss 2.302550
iteration 200 / 1000: loss 2.297648
iteration 300 / 1000: loss 2.259602
iteration 400 / 1000: loss 2.204170
iteration 500 / 1000: loss 2.118565
iteration 600 / 1000: loss 2.051535
iteration 700 / 1000: loss 1.988466
iteration 800 / 1000: loss 2.006591
iteration 900 / 1000: loss 1.951473
Validation accuracy: 0.287
```

# 8 Debug the training

With the default parameters we provided above, you should get a validation accuracy of about 0.29 on the validation set. This isn't very good.

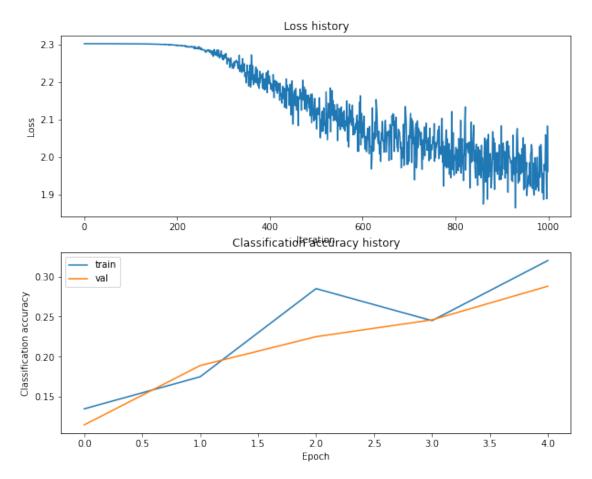
One strategy for getting insight into what's wrong is to plot the loss function and the accuracies on the training and validation sets during optimization.

Another strategy is to visualize the weights that were learned in the first layer of the network. In most neural networks trained on visual data, the first layer weights typically show some visible structure when visualized.

```
[]: # Plot the loss function and train / validation accuracies plt.subplot(2, 1, 1)
```

```
plt.plot(stats['loss_history'])
plt.title('Loss history')
plt.xlabel('Iteration')
plt.ylabel('Loss')

plt.subplot(2, 1, 2)
plt.plot(stats['train_acc_history'], label='train')
plt.plot(stats['val_acc_history'], label='val')
plt.title('Classification accuracy history')
plt.xlabel('Epoch')
plt.ylabel('Classification accuracy')
plt.legend()
plt.show()
```

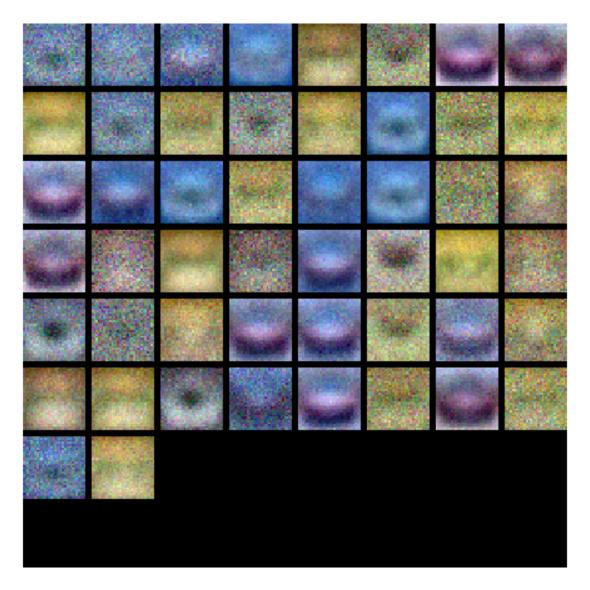


```
[]: from cs231n.vis_utils import visualize_grid

# Visualize the weights of the network

def show_net_weights(net):
```

```
W1 = net.params['W1']
W1 = W1.reshape(32, 32, 3, -1).transpose(3, 0, 1, 2)
plt.imshow(visualize_grid(W1, padding=3).astype('uint8'))
plt.gca().axis('off')
plt.show()
show_net_weights(net)
```



# 9 Tune your hyperparameters

What's wrong?. Looking at the visualizations above, we see that the loss is decreasing more or less linearly, which seems to suggest that the learning rate may be too low. Moreover, there is

no gap between the training and validation accuracy, suggesting that the model we used has low capacity, and that we should increase its size. On the other hand, with a very large model we would expect to see more overfitting, which would manifest itself as a very large gap between the training and validation accuracy.

**Tuning**. Tuning the hyperparameters and developing intuition for how they affect the final performance is a large part of using Neural Networks, so we want you to get a lot of practice. Below, you should experiment with different values of the various hyperparameters, including hidden layer size, learning rate, numer of training epochs, and regularization strength. You might also consider tuning the learning rate decay, but you should be able to get good performance using the default value.

**Approximate results**. You should be aim to achieve a classification accuracy of greater than 48% on the validation set. Our best network gets over 52% on the validation set.

**Experiment**: You goal in this exercise is to get as good of a result on CIFAR-10 as you can (52% could serve as a reference), with a fully-connected Neural Network. Feel free implement your own techniques (e.g. PCA to reduce dimensionality, or adding dropout, or adding features to the solver, etc.).

## Explain your hyperparameter tuning process below.

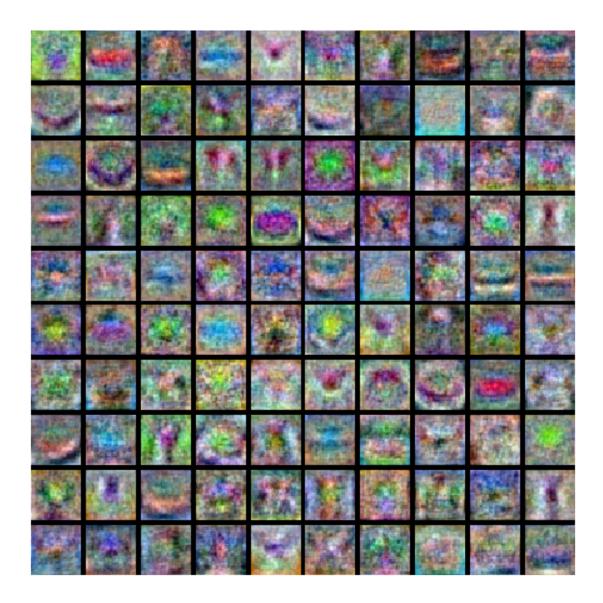
*Your Answer* :

```
[]: best_net = None # store the best model into this
   # TODO: Tune hyperparameters using the validation set. Store your best trained \Box
   # model in best_net.
                                                                     ш
   →#
   #
   # To help debug your network, it may help to use visualizations similar to the \Box
   # ones we used above; these visualizations will have significant qualitative
   →#
   # differences from the ones we saw above for the poorly tuned network.
   #
   # Tweaking hyperparameters by hand can be fun, but you might find it useful to \Box
   →#
   # write code to sweep through possible combinations of hyperparameters
   # automatically like we did on the previous exercises.
   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE) *****
   #results = {} # hidden layer size, learning rate, batch size, reg
   best_val_acc = 0
```

```
best_stats = []
np.random.seed(0)
for i in range(20):
    learning_rates = 10**np.random.uniform(-2,-3)
    #learning_rates = np.random.uniform(0.001,0.003)
    regs = 10**np.random.uniform(-6, -4)
    hidden_sizes = np.random.randint(80,100)
    net = TwoLayerNet(input size, hidden sizes, num classes)
    #Train the network
    stats = net.train(X_train, y_train, X_val, y_val,
            num_iters=1000, batch_size=200,
            learning\_rate = learning\_rates, \ learning\_rate\_decay = 0.95,
            req=reqs, verbose=True)
    val\_acc = (net.predict(X\_val) == y\_val).mean()
    train_acc = (net.predict(X_train) == y_train).mean()
    if val_acc > best_val_acc:
        best_val_acc = val_acc
        best_net = net
    print('lr %e reg %e hidden %d train_accuracy %f val_accuracy⊔
 →%f'%(learning_rates, regs, hidden_sizes, train_acc, val_acc))
print('best validation accuracy : %f' %best_val_acc)
best_val = -1  # The highest validation accuracy that we have seen so far.
log = {}
hidden_size = [80,100]
batch_size = [500]
learning_rate = [2.1e-3]
reg = [0.1, 0.35, 0.5]
for hs in hidden_size:
    for lr in learning_rate:
        for rg in reg:
          for bs in batch_size:
            net = TwoLayerNet(input_size, hs, num_classes)
            stats = net.train(X_train, y_train, X_val, y_val,
                              num_iters=1000, batch_size=bs, learning_rate=lr,
```

```
learning_rate_decay=0.95, reg=rg, verbose=False)
               y_train_pred = net.predict(X_train)
               acc_train = np.mean(y_train == y_train_pred)
               y_val_pred = net.predict(X_val)
               acc_val = np.mean(y_val == y_val_pred)
               if acc_val > best_val:
                 best_val = acc_val
                 best_net = net
               print('lr : %e rg : %e hs : %d bs : %d ,,,,, train_acc %f val_acc_u
    -%f'
               %(lr, rg, hs, bs, acc_train, acc_val))
   print('best val acc : %f' %best_val)
   # *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
  lr : 2.100000e-03 rg : 1.000000e-01 hs : 80 bs : 500 ,,,, train_acc 0.536327
  val_acc 0.507000
  lr : 2.100000e-03 rg : 3.500000e-01 hs : 80 bs : 500 ,,,, train_acc 0.534816
  val acc 0.503000
  lr: 2.100000e-03 rg: 5.000000e-01 hs: 80 bs: 500 ,,,, train_acc 0.525469
  val acc 0.501000
  lr : 2.100000e-03 rg : 1.000000e-01 hs : 100 bs : 500 ,,,, train_acc 0.551980
  val acc 0.516000
  lr : 2.100000e-03 rg : 3.500000e-01 hs : 100 bs : 500 ,,,, train_acc 0.539510
  val_acc 0.494000
  lr: 2.100000e-03 rg: 5.000000e-01 hs: 100 bs: 500,,,,, train_acc 0.528061
  val_acc 0.510000
  best val acc : 0.516000
[]: # Print your validation accuracy: this should be above 48%
   val acc = (best net.predict(X val) == y val).mean()
   print('Validation accuracy: ', val_acc)
  Validation accuracy: 0.516
[]: # Visualize the weights of the best network
```

show\_net\_weights(best\_net)



# 10 Run on the test set

When you are done experimenting, you should evaluate your final trained network on the test set; you should get above 48%.

```
[]: # Print your test accuracy: this should be above 48%
test_acc = (best_net.predict(X_test) == y_test).mean()
print('Test accuracy: ', test_acc)
```

Test accuracy: 0.532

# **Inline Question**

Now that you have trained a Neural Network classifier, you may find that your testing accuracy is much lower than the training accuracy. In what ways can we decrease this gap? Select all that apply.

- 1. Train on a larger dataset.
- 2. Add more hidden units.
- 3. Increase the regularization strength.
- 4. None of the above.

```
Your Answer:
Your Explanation:
```

## 11 IMPORTANT

This is the end of this question. Please do the following:

- 1. Click File -> Save to make sure the latest checkpoint of this notebook is saved to your Drive.
- 2. Execute the cell below to download the modified .py files back to your drive.

## features

## November 16, 2020

```
[1]: from google.colab import drive
   drive.mount('/content/drive', force_remount=True)
   # enter the foldername in your Drive where you have saved the unzipped
    # 'cs231n' folder containing the '.py', 'classifiers' and 'datasets'
    # folders.
    # e.g. 'cs231n/assignments/assignment1/cs231n/'
   FOLDERNAME = 'cs231n/assignments/assignment11/cs231n/'
   assert FOLDERNAME is not None, "[!] Enter the foldername."
   %cd drive/My\ Drive
   %cp -r $FOLDERNAME ../../
   %cd ../../
   %cd cs231n/datasets/
    !bash get_datasets.sh
   %cd ../../
   Mounted at /content/drive
   /content/drive/My Drive
   /content
   /content/cs231n/datasets
   --2020-10-31 21:05:45-- http://www.cs.toronto.edu/~kriz/cifar-10-python.tar.gz
   Resolving www.cs.toronto.edu (www.cs.toronto.edu)... 128.100.3.30
   Connecting to www.cs.toronto.edu (www.cs.toronto.edu)|128.100.3.30|:80...
   connected.
   HTTP request sent, awaiting response... 200 OK
   Length: 170498071 (163M) [application/x-gzip]
   Saving to: cifar-10-python.tar.gz
   cifar-10-python.tar 100%[=========>] 162.60M 16.6MB/s
                                                                       in 11s
   2020-10-31 21:05:57 (14.6 MB/s) - cifar-10-python.tar.gz saved
   [170498071/170498071]
   cifar-10-batches-py/
```

```
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data_batch_3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content
```

## 1 Image features exercise

Complete and hand in this completed worksheet (including its outputs and any supporting code outside of the worksheet) with your assignment submission. For more details see the assignments page on the course website.

We have seen that we can achieve reasonable performance on an image classification task by training a linear classifier on the pixels of the input image. In this exercise we will show that we can improve our classification performance by training linear classifiers not on raw pixels but on features that are computed from the raw pixels.

All of your work for this exercise will be done in this notebook.

#### 1.1 Load data

Similar to previous exercises, we will load CIFAR-10 data from disk.

```
[3]: from cs231n.features import color_histogram_hsv, hog_feature

def get_CIFAR10_data(num_training=49000, num_validation=1000, num_test=1000):
    # Load the raw CIFAR-10 data
    cifar10_dir = 'cs231n/datasets/cifar-10-batches-py'
```

```
# Cleaning up variables to prevent loading data multiple times (which may)
 →cause memory issue)
    try:
       del X_train, y_train
       del X_test, y_test
       print('Clear previously loaded data.')
    except:
       pass
    X_train, y_train, X_test, y_test = load_CIFAR10(cifar10_dir)
    # Subsample the data
    mask = list(range(num_training, num_training + num_validation))
    X_val = X_train[mask]
    y_val = y_train[mask]
    mask = list(range(num_training))
    X_train = X_train[mask]
    y_train = y_train[mask]
    mask = list(range(num test))
    X_test = X_test[mask]
    y_test = y_test[mask]
    return X_train, y_train, X_val, y_val, X_test, y_test
X_train, y_train, X_val, y_val, X_test, y_test = get_CIFAR10_data()
```

#### 1.2 Extract Features

For each image we will compute a Histogram of Oriented Gradients (HOG) as well as a color histogram using the hue channel in HSV color space. We form our final feature vector for each image by concatenating the HOG and color histogram feature vectors.

Roughly speaking, HOG should capture the texture of the image while ignoring color information, and the color histogram represents the color of the input image while ignoring texture. As a result, we expect that using both together ought to work better than using either alone. Verifying this assumption would be a good thing to try for your own interest.

The hog\_feature and color\_histogram\_hsv functions both operate on a single image and return a feature vector for that image. The extract\_features function takes a set of images and a list of feature functions and evaluates each feature function on each image, storing the results in a matrix where each column is the concatenation of all feature vectors for a single image.

```
X_test_feats = extract_features(X_test, feature_fns)
# Preprocessing: Subtract the mean feature
mean_feat = np.mean(X_train_feats, axis=0, keepdims=True)
X_train_feats -= mean_feat
X_val_feats -= mean_feat
X_test_feats -= mean_feat
# Preprocessing: Divide by standard deviation. This ensures that each feature
# has roughly the same scale.
std_feat = np.std(X_train_feats, axis=0, keepdims=True)
X_train_feats /= std_feat
X_val_feats /= std_feat
X_test_feats /= std_feat
# Preprocessing: Add a bias dimension
X train_feats = np.hstack([X_train_feats, np.ones((X_train_feats.shape[0], 1))])
X_val_feats = np.hstack([X_val_feats, np.ones((X_val_feats.shape[0], 1))])
X_test_feats = np.hstack([X_test_feats, np.ones((X_test_feats.shape[0], 1))])
```

```
Done extracting features for 1000 / 49000 images
Done extracting features for 2000 / 49000 images
Done extracting features for 3000 / 49000 images
Done extracting features for 4000 / 49000 images
Done extracting features for 5000 / 49000 images
Done extracting features for 6000 / 49000 images
Done extracting features for 7000 / 49000 images
Done extracting features for 8000 / 49000 images
Done extracting features for 9000 / 49000 images
Done extracting features for 10000 / 49000 images
Done extracting features for 11000 / 49000 images
Done extracting features for 12000 / 49000 images
Done extracting features for 13000 / 49000 images
Done extracting features for 14000 / 49000 images
Done extracting features for 15000 / 49000 images
Done extracting features for 16000 / 49000 images
Done extracting features for 17000 / 49000 images
Done extracting features for 18000 / 49000 images
Done extracting features for 19000 / 49000 images
Done extracting features for 20000 / 49000 images
Done extracting features for 21000 / 49000 images
Done extracting features for 22000 / 49000 images
Done extracting features for 23000 / 49000 images
Done extracting features for 24000 / 49000 images
Done extracting features for 25000 / 49000 images
Done extracting features for 26000 / 49000 images
Done extracting features for 27000 / 49000 images
```

```
Done extracting features for 28000 / 49000 images
Done extracting features for 29000 / 49000 images
Done extracting features for 30000 / 49000 images
Done extracting features for 31000 / 49000 images
Done extracting features for 32000 / 49000 images
Done extracting features for 33000 / 49000 images
Done extracting features for 34000 / 49000 images
Done extracting features for 35000 / 49000 images
Done extracting features for 36000 / 49000 images
Done extracting features for 37000 / 49000 images
Done extracting features for 38000 / 49000 images
Done extracting features for 39000 / 49000 images
Done extracting features for 40000 / 49000 images
Done extracting features for 41000 / 49000 images
Done extracting features for 42000 / 49000 images
Done extracting features for 43000 / 49000 images
Done extracting features for 44000 / 49000 images
Done extracting features for 45000 / 49000 images
Done extracting features for 46000 / 49000 images
Done extracting features for 47000 / 49000 images
Done extracting features for 48000 / 49000 images
Done extracting features for 49000 / 49000 images
```

#### 1.3 Train SVM on features

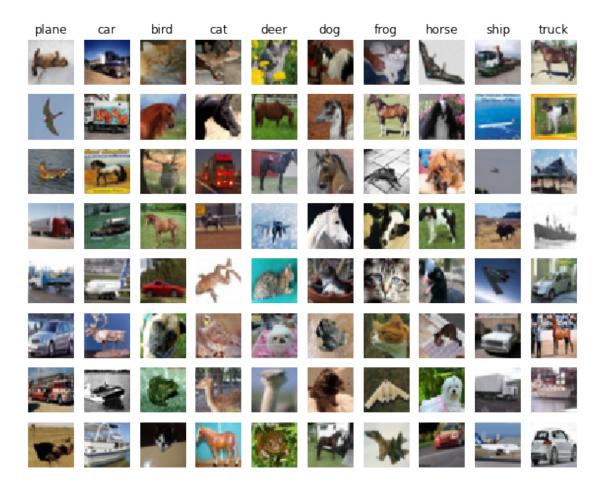
Using the multiclass SVM code developed earlier in the assignment, train SVMs on top of the features extracted above; this should achieve better results than training SVMs directly on top of raw pixels.

```
# the best trained classifer in best sum. You might also want to play
 ⇔#
# with different numbers of bins in the color histogram. If you are careful
# you should be able to get accuracy of near 0.44 on the validation set.
 ⇔#
# *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
for lr in learning rates:
  for reg in regularization_strengths:
    results[(lr, reg)] = []
    svm = LinearSVM()
    loss_hist = svm.train(X_train_feats, y_train, learning_rate=lr, reg=reg,_
 →num iters=1500)
    y_train_pred = svm.predict(X_train_feats)
    acc_train = np.mean(y_train == y_train_pred)
    y_val_pred = svm.predict(X_val_feats)
    acc val = np.mean(y val == y val pred)
    results[(lr, reg)].append(acc_train)
    results[(lr, reg)].append(acc val)
    if acc_val > best_val:
      best_val = acc_val
      best_svm = svm
# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)****
# Print out results.
for lr, reg in sorted(results):
    train_accuracy, val_accuracy = results[(lr, reg)]
    print('lr %e reg %e train accuracy: %f val accuracy: %f' % (
                lr, reg, train_accuracy, val_accuracy))
print('best validation accuracy achieved during cross-validation: %f' %11
 →best_val)
lr 1.000000e-05 reg 1.000000e-01 train accuracy: 0.411306 val accuracy: 0.413000
lr 1.000000e-05 reg 2.500000e-01 train accuracy: 0.405837 val accuracy: 0.407000
lr 1.000000e-05 reg 5.000000e-01 train accuracy: 0.410306 val accuracy: 0.409000
lr 1.000000e-04 reg 1.000000e-01 train accuracy: 0.449653 val accuracy: 0.440000
lr 1.000000e-04 reg 2.500000e-01 train accuracy: 0.451388 val accuracy: 0.445000
lr 1.000000e-04 reg 5.000000e-01 train accuracy: 0.451122 val accuracy: 0.441000
lr 5.000000e-04 reg 1.000000e-01 train accuracy: 0.488857 val accuracy: 0.481000
lr 5.000000e-04 reg 2.500000e-01 train accuracy: 0.488204 val accuracy: 0.481000
lr 5.000000e-04 reg 5.000000e-01 train accuracy: 0.485061 val accuracy: 0.477000
```

```
lr 1.000000e-03 reg 1.000000e-01 train accuracy: 0.499551 val accuracy: 0.479000
lr 1.000000e-03 reg 2.500000e-01 train accuracy: 0.496163 val accuracy: 0.484000
lr 1.000000e-03 reg 5.000000e-01 train accuracy: 0.491898 val accuracy: 0.474000
lr 1.000000e-02 reg 1.000000e-01 train accuracy: 0.503449 val accuracy: 0.489000
lr 1.000000e-02 reg 2.500000e-01 train accuracy: 0.498755 val accuracy: 0.481000
lr 1.000000e-02 reg 5.000000e-01 train accuracy: 0.488163 val accuracy: 0.478000
best validation accuracy achieved during cross-validation: 0.489000
```

#### 0.469

```
[7]: # An important way to gain intuition about how an algorithm works is to
    # visualize the mistakes that it makes. In this visualization, we show examples
    # of images that are misclassified by our current system. The first column
    # shows images that our system labeled as "plane" but whose true label is
    # something other than "plane".
   examples_per_class = 8
   classes = ['plane', 'car', 'bird', 'cat', 'deer', 'dog', 'frog', 'horse', __
    for cls, cls name in enumerate(classes):
        idxs = np.where((y_test != cls) & (y_test_pred == cls))[0]
       idxs = np.random.choice(idxs, examples_per_class, replace=False)
       for i, idx in enumerate(idxs):
           plt.subplot(examples_per_class, len(classes), i * len(classes) + cls + L
     \hookrightarrow 1)
           plt.imshow(X test[idx].astype('uint8'))
           plt.axis('off')
           if i == 0:
                plt.title(cls_name)
   plt.show()
```



#### 1.3.1 Inline question 1:

Describe the misclassification results that you see. Do they make sense? *Your Answer*:

### 1.4 Neural Network on image features

Earlier in this assignment we saw that training a two-layer neural network on raw pixels achieved better classification performance than linear classifiers on raw pixels. In this notebook we have seen that linear classifiers on image features outperform linear classifiers on raw pixels.

For completeness, we should also try training a neural network on image features. This approach should outperform all previous approaches: you should easily be able to achieve over 55% classification accuracy on the test set; our best model achieves about 60% classification accuracy.

```
[8]: # Preprocessing: Remove the bias dimension
    # Make sure to run this cell only ONCE
    print(X_train_feats.shape)
    X_train_feats = X_train_feats[:, :-1]
    X_val_feats = X_val_feats[:, :-1]
```

```
X_test_feats = X_test_feats[:, :-1]
   print(X_train_feats.shape)
   (49000, 155)
   (49000, 154)
[9]: from cs231n.classifiers.neural_net import TwoLayerNet
   input_dim = X_train_feats.shape[1]
   hidden_dim = 500
   num_classes = 10
   net = TwoLayerNet(input_dim, hidden_dim, num_classes)
   best_net = None
   # TODO: Train a two-layer neural network on image features. You may want to
    →#
   # cross-validate various parameters as in previous sections. Store your best
   # model in the best net variable.
    ⇔#
   # *****START OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****
   best_val = -1  # The highest validation accuracy that we have seen so far.
   log = {}
   learning_rate = [3e-1, 4e-1, 5e-1]
   reg = [5e-4, 7.5e-4, 1e-3]
   for lr in learning_rate:
     for rg in reg:
      net = TwoLayerNet(input_dim, hidden_dim, num_classes)
      stats = net.train(X_train_feats, y_train, X_val_feats, y_val,
                      num_iters=1000, batch_size=200, learning_rate=lr,
                       learning_rate_decay=0.95, reg=rg, verbose=False)
      y_train_pred = net.predict(X_train_feats)
      acc_train = np.mean(y_train == y_train_pred)
      y_val_pred = net.predict(X_val_feats)
      acc_val = np.mean(y_val == y_val_pred)
      if acc_val > best_val:
```

```
best_val = acc_val
best_net = net

print('lr : %e rg : %e ,,,, train_acc %f val_acc %f'
    %(lr, rg, acc_train, acc_val))
print('best val acc : %f' %best_val)

# *****END OF YOUR CODE (DO NOT DELETE/MODIFY THIS LINE)*****
```

```
lr : 3.000000e-01 rg : 5.000000e-04 ,,,, train_acc 0.589122 val_acc 0.559000
lr : 3.000000e-01 rg : 7.500000e-04 ,,,, train_acc 0.587020 val_acc 0.552000
lr : 3.000000e-01 rg : 1.000000e-03 ,,,, train_acc 0.581469 val_acc 0.556000
lr : 4.000000e-01 rg : 5.000000e-04 ,,,, train_acc 0.608408 val_acc 0.566000
lr : 4.000000e-01 rg : 7.500000e-04 ,,,, train_acc 0.608714 val_acc 0.580000
lr : 4.000000e-01 rg : 1.000000e-03 ,,,, train_acc 0.602918 val_acc 0.572000
lr : 5.000000e-01 rg : 5.000000e-04 ,,,, train_acc 0.631184 val_acc 0.589000
lr : 5.000000e-01 rg : 7.500000e-04 ,,,, train_acc 0.610490 val_acc 0.565000
lr : 5.000000e-01 rg : 1.000000e-03 ,,,, train_acc 0.610980 val_acc 0.560000
best val acc : 0.589000
```

```
[10]: # Run your best neural net classifier on the test set. You should be able
# to get more than 55% accuracy.

test_acc = (best_net.predict(X_test_feats) == y_test).mean()
print(test_acc)
```

0.576

#### 2 IMPORTANT

This is the end of this question. Please do the following:

- Click File -> Save to make sure the latest checkpoint of this notebook is saved to your Drive.
- 2. Execute the cell below to download the modified .py files back to your drive.

f.write(''.join(open(files).readlines()))