

**Problem 1.** Base Python, Method of Least Squares

Let **base python** refer to the python distribution from [www.python.org](http://www.python.org). Please use only base python to complete the following tasks and submit a functioning python script, SLR.py.

[1] Generate a training set containing 50 observations according to

$$Y_i = 10 + 0.5x_i + \epsilon_i \text{ or } \mathbf{y} = 10 + 0.5\mathbf{x} + \boldsymbol{\epsilon}$$

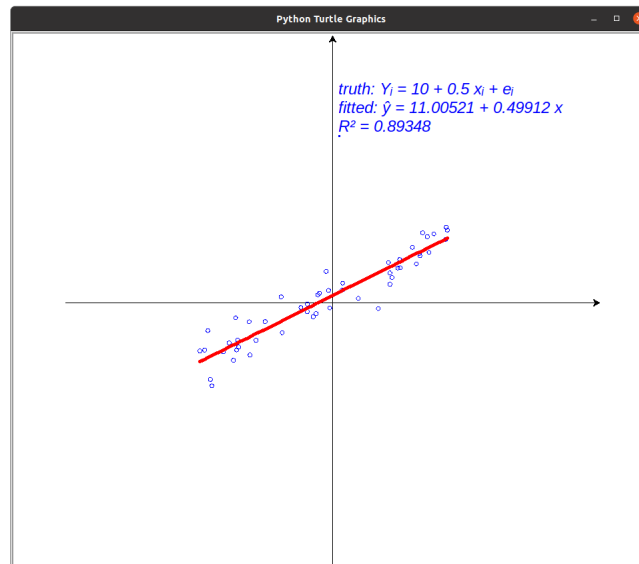
where  $x_i \in (-200, 200)$  and  $E(\epsilon_i) = 0, Var(\epsilon_i) = 400$  and  $\epsilon_i$  are independent random variables.

[2] Adopt the model  $E(Y_i) = \beta_0 + \beta_1 x_i$  and apply the *method of least squares* to the training set to estimate the model parameters and produce the fitted values:

$$\hat{y}_i = \hat{\beta}_0 + \hat{\beta}_1 x_i$$

[3] Calculate the coefficient of determination  $R^2$  of the fitted model.

[4] Use turtle graphics to present a scatter plot of the training set, the fitted regression line, and the related annotation, similar to the one below.



You may find the following resources useful.

random — Generate pseudo-random numbers

<https://docs.python.org/release/3.10.2/library/random.html>

random.uniform(a, b)

random.gauss(mu, sigma)

turtle — Turtle graphics

<https://docs.python.org/release/3.10.2/library/turtle.html>

turtle.write()

ClassFolder/U1-BasePy/Lib-standard-turtle.py

data structures

ClassFolder/U1-BasePy/BasePython-DataStructures.html

program control

ClassFolder/U1-BasePy/BasePython-ControlFlow.html

unicode character table

<https://unicode-table.com/en/>