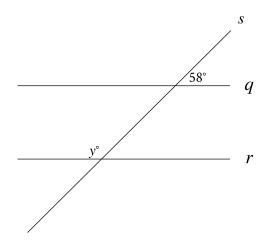
## Question ID 686b5212

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: 686b5212



Note: Figure not drawn to scale.

In the figure, line q is parallel to line r, and both lines are intersected by line s. If y = 2x + 8, what is the value of x?

#### ID: 686b5212 Answer

Correct Answer: 57

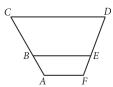
Rationale

The correct answer is 57. Based on the figure, the angle with measure  $y^{\circ}$  and the angle vertical to the angle with measure  $58^{\circ}$  are same side interior angles. Since vertical angles are congruent, the angle vertical to the angle with measure  $58^{\circ}$  also has measure  $58^{\circ}$ . It's given that lines q and r are parallel. Therefore, same side interior angles between lines q and r are supplementary. It follows that y + 58 = 180. If y = 2x + 8, then the value of x can be found by substituting 2x + 8 for y in the equation y + 58 = 180, which yields 2x + 8 + 58 = 180, or 2x + 66 = 180. Subtracting 66 from both sides of this equation yields 2x = 114. Dividing both sides of this equation by 2 yields x = 57. Thus, if y = 2x + 8, the value of x is 57.

# **Question ID 81b664bc**

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: 81b664bc



In the figure above,  $\overline{AF}$ ,  $\overline{BE}$ , and  $\overline{CD}$  are parallel. Points B and E lie on  $\overline{AC}$  and

 $\overline{FD}$ , respectively. If AB = 9, BC = 18.5, and FE = 8.5, what is the length of  $\overline{ED}$ , to the nearest tenth?

A. 16.8

B. 17.5

C. 18.4

D. 19.6

#### ID: 81b664bc Answer

Correct Answer: B

Rationale

Choice B is correct. Since  $\overline{AF}$ ,  $\overline{BE}$ , and  $\overline{CD}$  are parallel, quadrilaterals  $\overline{AFEB}$  and  $\overline{BEDC}$  are similar. Let x represent the

length of  $\overline{ED}$ . With similar figures, the ratios of the lengths of corresponding sides are equal. It follows that  $\frac{9}{18.5} = \frac{8.5}{x}$ . Multiplying both sides of this equation by 18.5 and by x yields 9x = (18.5)(8.5), or 9x = 157.25. Dividing both sides of this equation by 9 yields x = 17.47, which to the nearest tenth is 17.5.

Choices A, C, and D are incorrect and may result from errors made when setting up the proportion.

## Question ID 94364a79

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: 94364a79

Two nearby trees are perpendicular to the ground, which is flat. One of these trees is 10 feet tall and has a shadow that is 5 feet long. At the same time, the shadow of the other tree is 2 feet long. How tall, in feet, is the other tree?

- A. 3
- B. **4**
- C. 8
- D. 27

#### ID: 94364a79 Answer

Correct Answer: B

Rationale

Choice B is correct. Each tree and its shadow can be modeled using a right triangle, where the height of the tree and the length of its shadow are the legs of the triangle. At a given point in time, the right triangles formed by two nearby trees and their respective shadows will be similar. Therefore, if the height of the other tree is x, in feet, the value of x can be calculated by solving the proportional relationship  $\frac{10 \text{ feet tall}}{5 \text{ feet long}} = \frac{x \text{ feet tall}}{2 \text{ feet long}}$ . This equation is equivalent to  $\frac{10}{5} = \frac{x}{2}$ , or  $2 = \frac{x}{2}$ . Multiplying each side of the equation  $2 = \frac{x}{2}$  by 2 yields 4 = x. Therefore, the other tree is 4 feet tall.

Choice A is incorrect and may result from calculating the difference between the lengths of the shadows, rather than the height of the other tree.

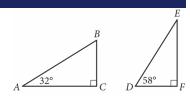
Choice C is incorrect and may result from calculating the difference between the height of the 10-foot-tall tree and the length of the shadow of the other tree, rather than calculating the height of the other tree.

Choice D is incorrect and may result from a conceptual or calculation error.

# Question ID 933fee1a

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: 933fee1a



Triangles ABC and DEF are shown above. Which of the

BC

following is equal to the ratio  $\overline{AB}$ ?

A. DE

DF

DF

EF

D. *DE* 

## ID: 933fee1a Answer

Correct Answer: B

Rationale

Choice B is correct. In right triangle ABC, the measure of angle B must be 58° because the sum of the measure of angle A, which is 32°, and the measure of angle B is 90°. Angle D in the right triangle DEF has measure 58°. Hence, triangles ABC and DEF are similar (by angle-angle similarity). Since  $\overline{BC}$  is the side opposite to the angle with measure 32° and AB is the

hypotenuse in right triangle ABC, the ratio  $\overline{AB}$  is equal to  $\overline{DF}$ .

Alternate approach: The trigonometric ratios can be used to answer this question. In right triangle ABC, the ratio

$$\frac{BC}{AB} = \sin(32^\circ)$$
. The angle E in triangle DEF has measure 32° because  $M(\angle D) + M(\angle E) = 90^\circ$ . In triangle DEF, the ratio

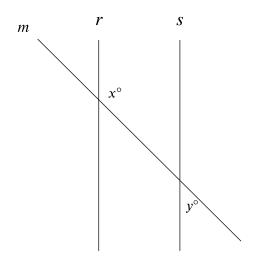
$$\frac{DF}{DE} = \sin(32^{\circ})$$
. Therefore,  $\frac{DF}{DE} = \frac{BC}{AB}$ .

Choice A is incorrect because  $\frac{DE}{DF}$  is the reciprocal of the ratio  $\frac{BC}{AB}$ . Choice C is incorrect because  $\frac{DF}{EF} = \frac{BC}{AC}$ , not  $\frac{BC}{AB}$ . Choice D is incorrect because  $\frac{EF}{DE} = \frac{AC}{AB}$ , not  $\frac{BC}{AB}$ .

## Question ID a4c05a1b

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: a4c05a1b



Note: Figure not drawn to scale.

In the figure shown, lines r and s are parallel, and line m intersects both lines. If y < 65, which of the following must be true?

A. x < 115

B. x > 115

C. x + y < 180

D. x + y > 180

#### ID: a4c05a1b Answer

Correct Answer: B

Rationale

Choice B is correct. In the figure shown, the angle measuring  $y^{\circ}$  is congruent to its vertical angle formed by lines s and m, so the measure of the vertical angle is also  $y^{\circ}$ . The vertical angle forms a same-side interior angle pair with the angle measuring  $x^{\circ}$ . It's given that lines r and s are parallel. Therefore, same-side interior angles in the figure are supplementary, which means the sum of the measure of the vertical angle and the measure of the angle measuring  $x^{\circ}$  is  $180^{\circ}$ , or x + y = 180. Subtracting  $x^{\circ}$  from both sides of this equation yields y = 180 - x. Substituting y = 180 - x for  $y^{\circ}$  in the inequality y < 65 yields  $y^{\circ} = 180 - x$ . Subtracting  $y^{\circ} = 180 - x$ . Subtracting

Choice A is incorrect and may result from conceptual or calculation errors.

Choice C is incorrect. x + y must be equal to, not less than, 180.

Choice D is incorrect. x + y must be equal to, not greater than, 180.

# **Question ID d3fe472f**

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

## ID: d3fe472f

Triangle ABC is similar to triangle XYZ, such that A, B, and C correspond to X, Y, and Z respectively. The length of each side of triangle XYZ is  $\mathbf{2}$  times the length of its corresponding side in triangle ABC. The measure of side AB is  $\mathbf{16}$ . What is the measure of side XY?

- A. 14
- B. **16**
- C. 18
- D. **32**

#### ID: d3fe472f Answer

Correct Answer: D

Rationale

Choice D is correct. It's given that triangle ABC is similar to triangle XYZ, such that A, B, and C correspond to X, Y, and Z, respectively. Therefore, side AB corresponds to side XY. Since the length of each side of triangle XYZ is 2 times the length of its corresponding side in triangle ABC, it follows that the measure of side XY is 2 times the measure of side AB. Thus, since the measure of side AB is 16, then the measure of side XY is 216, or 32.

Choice A is incorrect and may result from conceptual or calculation errors.

Choice B is incorrect. This is the measure of side AB, not side XY.

Choice C is incorrect and may result from conceptual or calculation errors.

# **Question ID fd8745fc**

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

## ID: fd8745fc

In triangle JKL, the measures of  $\angle K$  and  $\angle L$  are each  $48^\circ$ . What is the measure of  $\angle J$ , in degrees? (Disregard the degree symbol when entering your answer.)

#### ID: fd8745fc Answer

Correct Answer: 84

Rationale

The correct answer is 84. The sum of the measures of the interior angles of a triangle is  $180^{\circ}$ . It's given that in triangle JKL, the measures of  $\angle K$  and  $\angle L$  are each  $48^{\circ}$ . Adding the measures, in degrees, of  $\angle K$  and  $\angle L$  gives 48 + 48, or 96. Therefore, the measure of  $\angle J$ , in degrees, is 180 - 96, or 84.

# Question ID c7bed21d

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: c7bed21d

Quadrilateral P'Q'R'S' is similar to quadrilateral PQRS, where P, Q, R, and S correspond to P', Q', R', and S', respectively. The measure of angle P is  $\mathbf{30}^\circ$ , the measure of angle Q is  $\mathbf{50}^\circ$ , and the measure of angle R is  $\mathbf{70}^\circ$ . The length of each side of P'Q'R'S' is  $\mathbf{3}$  times the length of each corresponding side of PQRS. What is the measure of angle P'?

- A. 10°
- B. 30°
- C. 40°
- D. 90°

#### ID: c7bed21d Answer

Correct Answer: B

Rationale

Choice B is correct. It's given that quadrilateral P'Q'R'S' is similar to quadrilateral PQRS, where P, Q, R, and S correspond to P', Q', R', and S', respectively. Since corresponding angles of similar quadrilaterals are congruent, it follows that the measure of angle P is equal to the measure of angle P'. It's given that the measure of angle P is O'. Therefore, the measure of angle O'0 is O'0.

Choice A is incorrect. This is  $\frac{1}{3}$  the measure of angle P'.

Choice C is incorrect and may result from conceptual or calculation errors.

Choice D is incorrect. This is 3 times the measure of angle  $P^{'}$ .

# Question ID 1c3d613c

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

# ID: 1c3d613c B C D E Note: Figures not drawn to scale.

Triangle ABC and triangle DEF are shown. The relationship between the side

lengths of the two triangles is such that  $\frac{AB}{DE} = \frac{BC}{EF} = \frac{AC}{DF} = 3$ . If the measure

of angle *BAC* is 20°, what is the measure, in degrees, of angle *EDF*? (Disregard the degree symbol when gridding your answer.)

#### ID: 1c3d613c Answer

#### Rationale

The correct answer is 20. By the equality given, the three pairs of corresponding sides of the two triangles are in the same proportion. By the side-side (SSS) similarity theorem, triangle ABC is similar to triangle DEF. In similar triangles, the measures of corresponding angles are congruent. Since angle BAC corresponds to angle EDF, these two angles are congruent and their measures are equal. It's given that the measure of angle BAC is 20°, so the measure of angle EDF is also 20°.

## **Question ID 901e3285**

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

#### ID: 901e3285

In triangle ABC, the measure of angle A is  $50^{\circ}$ . If triangle ABC is isosceles, which of the following is NOT a possible measure of angle B?

- A. 50°
- B. 65°
- C. 80°
- D. 100°

#### ID: 901e3285 Answer

Correct Answer: D

Rationale

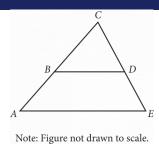
Choice D is correct. The sum of the three interior angles in a triangle is  $180^{\circ}$ . It's given that angle A measures  $50^{\circ}$ . If angle B measured  $100^{\circ}$ , the measure of angle C would be  $180^{\circ} - (50^{\circ} + 100^{\circ}) = 30^{\circ}$ . Thus, the measures of the angles in the triangle would be  $50^{\circ}$ ,  $100^{\circ}$ , and  $30^{\circ}$ . However, an isosceles triangle has two angles of equal measure. Therefore, angle B can't measure  $100^{\circ}$ .

Choice A is incorrect. If angle B has measure  $50^{\circ}$ , then angle C would measure  $180^{\circ} - (50^{\circ} + 50^{\circ}) = 80^{\circ}$ , and  $50^{\circ}$ , and  $50^{\circ}$ , and  $80^{\circ}$  could be the angle measures of an isosceles triangle. Choice B is incorrect. If angle B has measure  $65^{\circ}$ , then angle C would measure  $180^{\circ} - (65^{\circ} + 50^{\circ}) = 65^{\circ}$ , and  $50^{\circ}$ ,  $65^{\circ}$ , and  $65^{\circ}$  could be the angle measures of an isosceles triangle. Choice C is incorrect. If angle B has measure  $80^{\circ}$ , then angle C would measure  $180^{\circ} - (80^{\circ} + 50^{\circ}) = 50^{\circ}$ , and  $50^{\circ}$ ,  $80^{\circ}$ , and  $50^{\circ}$  could be the angle measures of an isosceles triangle.

## Question ID 6dd463ca

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

## ID: 6dd463ca



In the figure above, segments AE and BD are parallel. If angle BDC measures 58° and angle ACE measures 62°, what is the measure of angle CAE?

A. 58°

B. 60°

C. 62°

D. 120°

#### ID: 6dd463ca Answer

Correct Answer: B

#### Rationale

Choice B is correct. It's given that angle ACE measures  $62^{\circ}$ . Since segments AE and BD are parallel, angles BDC and CEA are congruent. Therefore, angle CEA measures  $58^{\circ}$ . The sum of the measures of angles ACE, CEA, and CAE is  $180^{\circ}$  since the sum of the interior angles of triangle ACE is equal to  $180^{\circ}$ . Let the measure of angle CAE be  $X^{\circ}$ . Therefore, 62+58+x=180, which simplifies to x=60. Thus, the measure of angle CAE is  $60^{\circ}$ .

Choice A is incorrect. This is the measure of angle AEC, not that of angle CAE. Choice C is incorrect. This is the measure of angle ACE, not that of CAE. Choice D is incorrect. This is the sum of the measures of angles ACE and CEA.

# Question ID 4ff7b652

Assessment	Test	Domain	Skill	Difficulty
SAT	Math	Geometry and Trigonometry	Lines, angles, and triangles	

## ID: 4ff7b652

Right triangles LMN and PQR are similar, where L and M correspond to P and Q, respectively. Angle M has a measure of  $S3^{\circ}$ . What is the measure of angle Q?

- A. 37°
- B. **53**°
- C.  $127^{\circ}$
- D.  $143\degree$

#### ID: 4ff7b652 Answer

Correct Answer: B

Rationale

Choice B is correct. It's given that triangle LMN is similar to triangle PQR. Corresponding angles of similar triangles are congruent. Since angle M and angle Q correspond to each other, they must be congruent. Therefore, if the measure of angle M is  $53^{\circ}$ , then the measure of angle Q is also  $53^{\circ}$ .

Choice A is incorrect and may result from concluding that angle M and angle Q are complementary rather than congruent.

Choice C is incorrect and may result from concluding that angle M and angle Q are supplementary rather than congruent.

Choice D is incorrect and may result from conceptual or calculation errors.