

Naïve Bayes

EXAMPLE $P(C) = 0.01$

TEST: 90% it is positive if you have C.

90% it is negative if you don't have C.

SENSITIVITY
SPECIFICITY

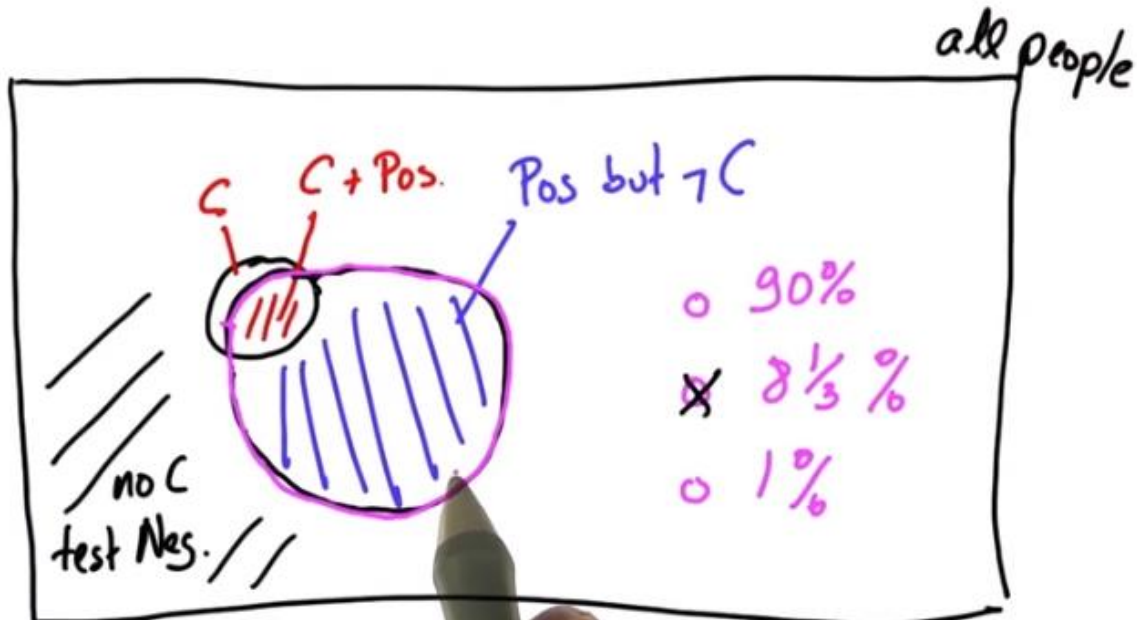
QUESTION: TEST = POSITIVE

PROBABILITY OF HAVING CANCER?

What do you think is now the probability of having that specific type of cancer?

0:51 / 2:37

CC YouTube



0:19 / 0:41

CC YouTube

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Reminder of the question: the prior probability of cancer is 1%, and a sensitivity and specificity are 90%, what's the probability that someone with a positive cancer test actually has the disease?

BAYES RULE



So let's make this specific.

Prior:

$$P(C) = 0.01 = 1\% \quad P(\neg C) = 0.99$$

$$P(Pos|C) = 0.9 = 90\% \quad P(Pos|\neg C) = 0.1$$

$$P(Neg|\neg C) = 0.9$$

Joint:

$$P(C, Pos) = P(C) \cdot P(Pos|C) = 0.009$$

$$P(\neg C, Pos) = P(\neg C) \cdot P(Pos|\neg C) = 0.099$$

Normalizer:

$$P(Pos) = P(C, Pos) + P(\neg C, Pos) = 0.108$$

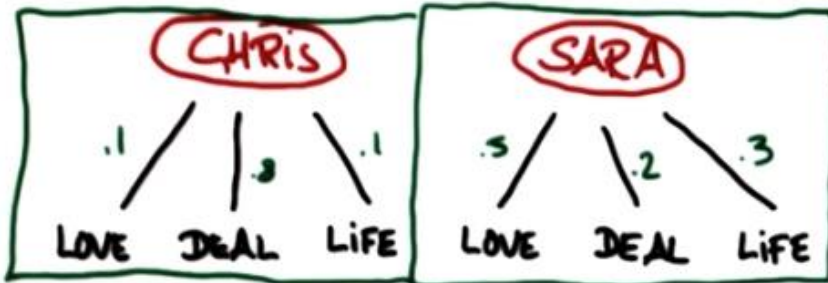
Posterior:

$$P(C|Pos) = 0.0833$$

$$P(\neg C|Pos) = 0.9167$$

$$\left. \begin{array}{l} P(C|Pos) = 0.0833 \\ P(\neg C|Pos) = 0.9167 \end{array} \right\} = \boxed{1}$$

TEXT LEARNING — NAIVE BAYES



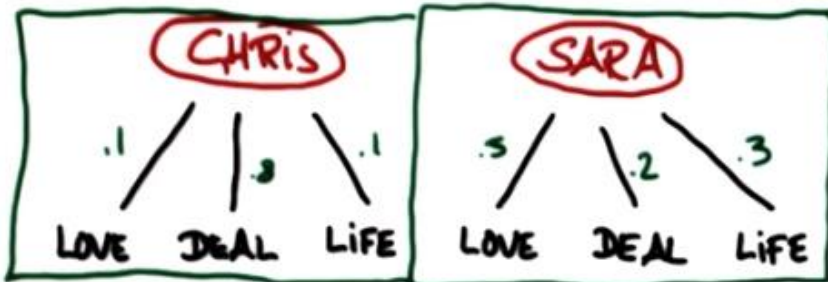
$$P(\text{CHRIS}) = 0.5$$

$$P(\text{SARA}) = 0.5$$

LIFE DEAL

- CHRIS $.1 \cdot .3 \cdot .5 = 0.04$
- SARA $.3 \cdot .2 \cdot .5 = 0.03$

TEXT LEARNING — NAIVE BAYES



$$P(\text{CHRIS}) = 0.5$$

$$P(\text{SARA}) = 0.5$$

$$P(\text{CHRIS} \mid \text{"LIFE DEAL"}) = \frac{.57}{.43}$$

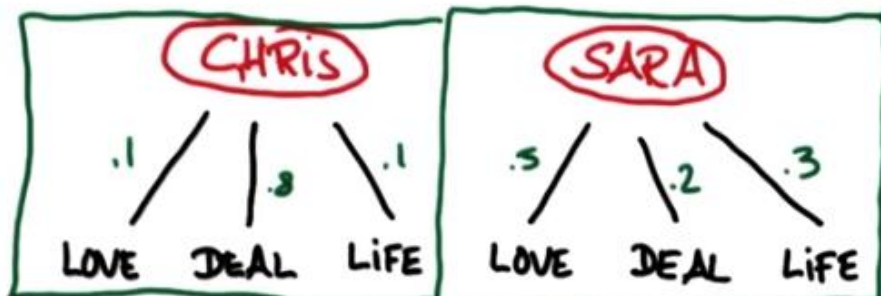
$$P(\text{SARA} \mid \text{"LIFE DEAL"}) = \frac{.43}{.57}$$

0.04
0.03

$$\frac{0.04}{0.04 + 0.03}$$

$\frac{4}{7}$

TEXT LEARNING — NAIVE BAYES



$$P(\text{CHRIS}) = 0.5$$

$$P(\text{SARA}) = 0.5$$

$$P(\text{CHRIS} | \text{"LOVE DEAL"}) = .444$$

$$P(\text{SARA} | \text{"LOVE DEAL"}) = .555$$

$$.1 : .8 : .5 = 0.04$$

$$.5 : .2 : .5 = \frac{0.05}{0.09}$$

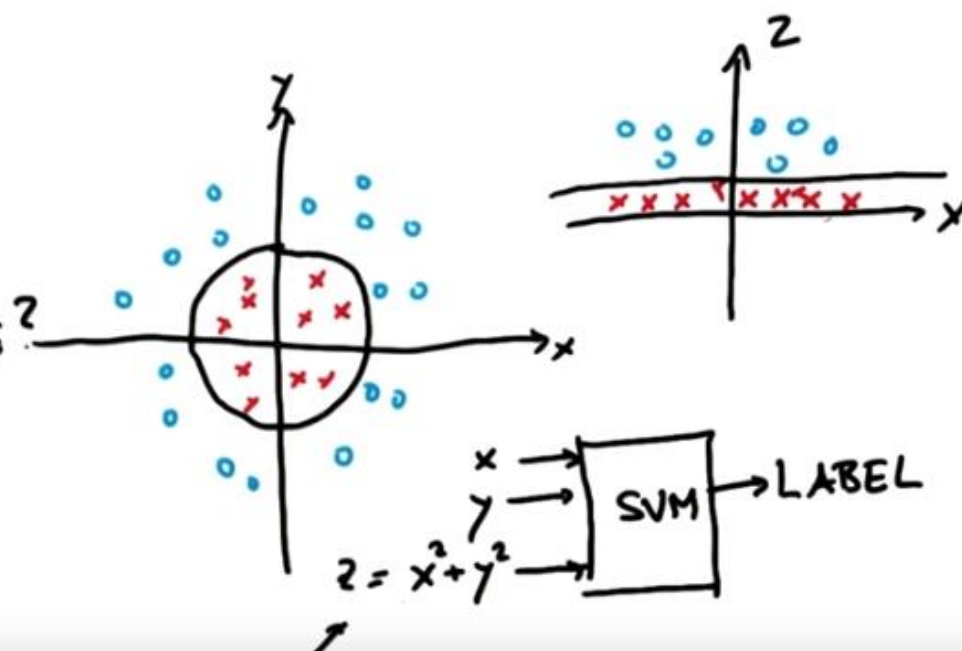
SVM

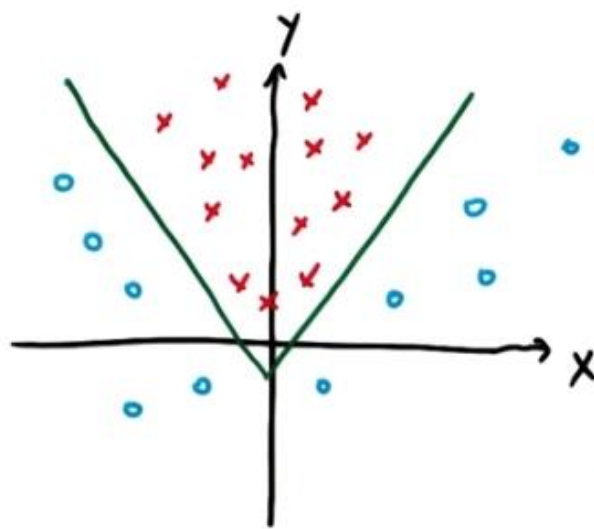
SVM

IS THIS
LINEARLY
SEPERABLE?

✗ YES

○ NO





ADD FEATURE

o $x^2 + y^2$

o $|x|$

o $|y|$

Parameters in Machine Learning

For an SVM?

→ kernel

→ C

→ gamma

kernel

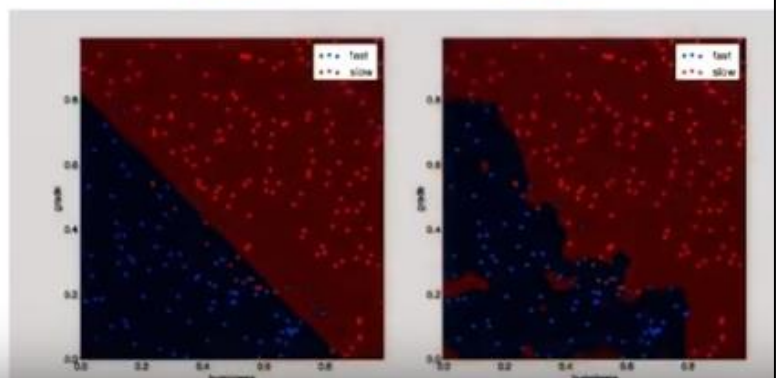
linear

rbf

gamma

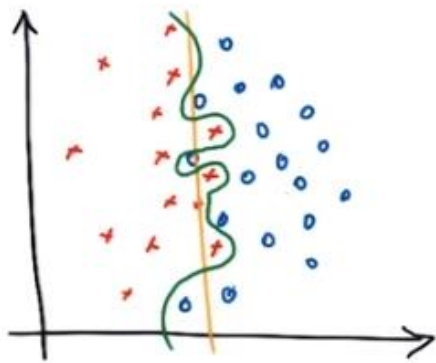
1000.

1000.



SVM C Parameter

C — controls tradeoff between smooth decision boundary and classifying training points correctly



Quiz

does a large C mean you expect a smooth boundary, or that you will get more training points correct?

☐ smooth boundary

☒ more training points correct

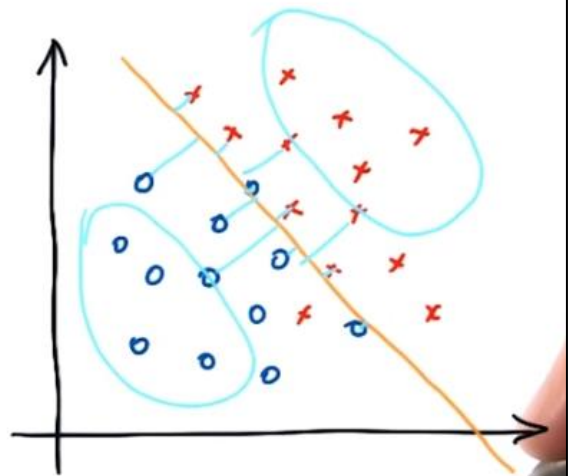
use rbf kernel!

SVM γ (gamma) parameter

γ — defines how far the influence of a single training example reaches

low values — far

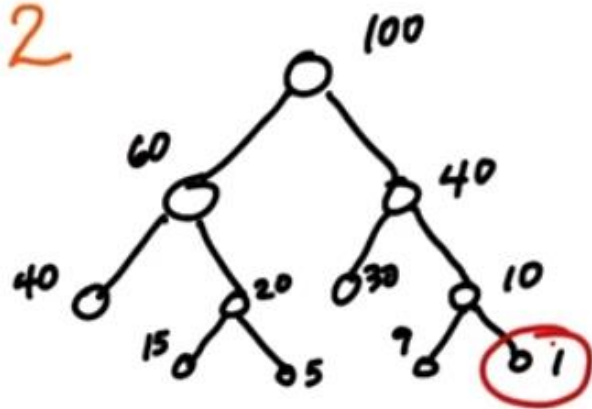
high values — close



Decision Tree

$\text{min_samples_split} = 2$

quiz: which node can I not split further?

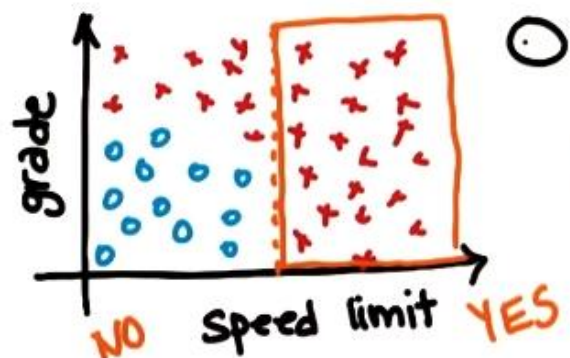
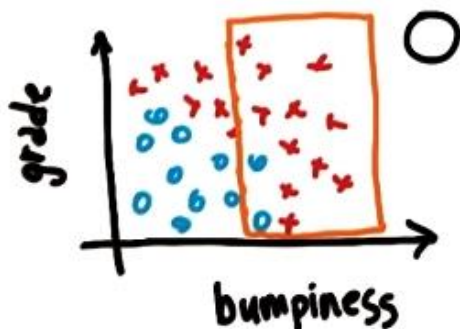


Entropy

← controls how a DT decides where to split the data

definition: measure of **impurity** in a bunch of examples

example | SPEED LIMIT



Entropy

← controls how a DT decides where to split the data

definition: measure of **impurity** in a bunch of examples

$$\text{entropy} = \sum_i -p_i \log_2(p_i)$$

sum over
all classes

fraction of examples in
class i

Entropy

← controls how a DT decides where to split the data

definition: measure of **impurity** in a bunch of examples

all examples are **same class**

→ entropy = 0

examples are **evenly split** between classes

→ entropy = 1.0

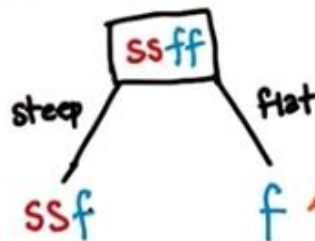
intuition

Information Gain

$$\text{information gain} = \text{entropy (parent)} - \left[\text{weighted average} \right] \text{entropy (children)}$$

grade	bumpiness	speed limit	speed
steep	bumpy	yes	slow
steep	smooth	yes	slow
flat	bumpy	no	fast
steep	smooth	no	fast

entropy of parent = 1.0



$$P_{\text{slow}} = 2/3$$

$$P_{\text{fast}} = 1/3$$

entropy of this node? 0

Information Gain

$$\text{information gain} = \text{entropy (parent)} - \left[\text{weighted average} \right] \text{entropy (children)}$$

grade	bumpiness	speed limit	speed
steep	bumpy	yes	slow
steep	smooth	yes	slow
flat	bumpy	no	fast
steep	smooth	no	fast

entropy (flat) = 0

$$P_{\text{slow}} = 2/3 \quad P_{\text{fast}} = 1/3$$

entropy of parent = 1.0

$$\text{entropy} = \sum_i -P_i \log_2 P_i$$

$$\text{entropy} = \left[-\frac{2}{3} \log_2 \left(\frac{2}{3} \right) - \frac{1}{3} \log_2 \left(\frac{1}{3} \right) \right]$$

$$= 0.9184$$

Algorithms (Pick One)

k nearest neighbors — classic, simple, easy to understand

adaboost

random forest

} "ensemble methods"
meta classifiers built from (usually)
decision trees