

1. (a) $45_{10} = 00101101_2$
 $128 \ 64 \ 32 \ 16 \ 8 \ 4 \ 2 \ 1$

$$\begin{array}{r|l} 2 & 45 \\ \hline 2 & 22 \text{ r } 1 \\ 2 & 11 \text{ r } 0 \\ 2 & 5 \text{ r } 1 \\ 2 & 2 \text{ r } 1 \\ 2 & 1 \text{ r } 0 \\ 2 & 0 \text{ r } 1 \end{array}$$

$\therefore 45_{10} = 00101101_2$

(b) 108_{10}

$$\begin{array}{r|l} 2 & 108 \\ \hline 2 & 54 \text{ r } 0 \\ 2 & 27 \text{ r } 0 \\ 2 & 13 \text{ r } 1 \Rightarrow 01101100 \\ 2 & 6 \text{ r } 1 \\ 2 & 3 \text{ r } 0 \\ 2 & 1 \text{ r } 1 \\ 1 & 1 \text{ r } 1 \\ & 0 \end{array}$$

$\therefore 108_{10} = 01101100_2$

2. (a) 00101101_2

$= 2 \ 13_{10}$

$= 2 \ D_{16}$

(b) 01101100_2

$= 6 \ 12_{10}$

$= 6 \ C_{16}$

Dec
0
1
2
3
4
5
6
7
8
9
10
11
12
13
14
15

Hex
0
1
2
3
4
5
6
7
8
9
A
B
C
D
E
F

$$\begin{array}{r|l} 2 & 11 \\ \hline 2 & 5 \text{ r } 1 \\ 2 & 2 \text{ r } 1 \\ 2 & 1 \text{ r } 0 \\ & 1 \text{ r } 1 \end{array}$$

$11_{(10)} \Rightarrow 00001011$ Convert to true binary.
 $= 11110100$ Invert the bits.
 $= 11110101_{(2)}$ Add 1.

(b) $-37_{(10)}$

$-37_{(10)} \Rightarrow 00100101_{(2)}$ Convert to true binary.
 $= 11011010_{(2)}$ Invert the bits.
 $= 11011011_{(2)}$ Add 1.

3. (a) 00110110_2
 $32 \ 16 \ 8 \ 4 \ 2 \ 1$
 $= 32+16+4+2$
 $= 54_{10}$

(b) 01010101_2
 $64 \ 32 \ 16 \ 8 \ 4 \ 2 \ 1$
 $= 64+16+4+1$
 $= 85_{10}$

4. (a) $A \ 1 \ 2 \ B_{(16)}$
 $\frac{16^3}{16^3} \frac{16^2}{16^2} \frac{16^1}{16^1} \frac{16^0}{16^0}$
 $= 10 \times 16^3 + 1 \times 16^2 + 2 \times 16^1 + 11 \times 16^0$
 $= 40960 + 256 + 32 + 11$
 $= 41259_{(10)}$

(b) $1 \ C \ 0 \ D_{(16)}$
 $\frac{16^3}{16^3} \frac{16^2}{16^2} \frac{16^1}{16^1} \frac{16^0}{16^0}$
 $= 1 \times 16^3 + 12 \times 16^2 + 0 \times 16^1 + 13 \times 16^0$
 $= 4096 + 3072 + 0 + 13$
 $= 7181_{(10)}$

5. (a) $-11_{(10)}$

$11_{(10)} \Rightarrow 00001011$ Convert to true binary.
 $= 11110100$ Invert the bits.
 $= 11110101_{(2)}$ Add 1.

$$6. a) 101101_{(2C)} \Rightarrow 11101101_{(2C)}$$

Perform sign extension
to 8-bit.

$$11101101_{(2C)}$$

$$= 00010010. \text{ Flip the bits.}$$

$$= 00010011. \text{ Add 1.}$$

$$= 2^3 + 0 + 0 + 2^1 + 2^0 = 16 + 2 + 1 = 19_{10}$$

$$\Rightarrow -19_{10}. \text{ Prepend negative sign.}$$

Verify: -19_{10} to 2C.

$$19_{10} \Rightarrow 00010011$$

$$= 11101100. \text{ Flip the sign.}$$

$$= 11101101. \text{ Add 1. } \checkmark$$

$$b) 1101101_{(2C)} \Rightarrow 11101101_{(2C)}$$

Extend sign.

$$11101101_{(2C)}$$

$$= 00010010. \text{ Flip the bits.}$$

$$= 00010011. \text{ Add 1.}$$

$$= 1 \times 2^4 + 0 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$$

$$= 16 + 0 + 0 + 2 + 1 = 19.$$

$$\Rightarrow -19_{10}. \text{ Prepend negative sign.}$$

★ Leading 1's of a 2's complement binary number are redundant; multiple MSBs are often used to represent the sign after sign extension.

$$7. (a) 11.625_{10}$$

$$= 1011.2^1 2^0 2^{-1} 2^{-2} 2^{-3} 2^{-4}$$

(Simplified)

$$= 1.0111010$$

Fraction

$$= 1.0111010 \times 2^3$$

$$E' = 127 + 3 = 130 = 10000100_2$$

$$\text{Sign} = 0.$$

$$\text{Fraction} = 011101000000000000000000$$

$$\begin{array}{r} 2 \overline{) 11} \\ 2 \overline{) 5} \text{ r } 1 \uparrow \\ 2 \overline{) 2} \text{ r } 1 \uparrow \\ 2 \overline{) 1} \text{ r } 0 \uparrow \\ 1 \text{ r } 1 \end{array}$$

read up.

$$\begin{array}{l} 0.625 \times 2 = 1.25 \\ 0.25 \times 2 = 0.5 \\ 0.5 \times 2 = 1.0 \\ 0.0 \times 2 = 0.0 \end{array}$$

$$130_{10} \text{ to binary: } 2 \overline{) 130}$$

$$\begin{array}{r} 2 \overline{) 130} \\ 2 \overline{) 65} \text{ r } 0 \\ 2 \overline{) 32} \text{ r } 1 \\ 2 \overline{) 16} \text{ r } 0 \\ 2 \overline{) 8} \text{ r } 0 \\ 2 \overline{) 4} \text{ r } 0 \\ 2 \overline{) 2} \text{ r } 0 \\ 2 \overline{) 1} \text{ r } 0 \end{array}$$

$$= 10000100_2$$

$$0 \quad 10000100 \quad 011101000000000000000000$$

Sign Exponent Fraction. (IEEE-754).

Divide into nibbles to convert to hex:

$$01000001001110100000000000000000$$

$$= 4 \quad 1 \quad 3 \quad A \quad 0 \quad 0 \quad 0 \quad 0$$

$$= 0X413A0000_{(16)}.$$

$$7. (b) -0.15625_{10}$$

$$= 0000000000001000$$

$$1.01000 \times 10^{-3}$$

$$\text{Sign} = 1$$

$$E' = 127 - 3 = 124$$

$$= 01111100$$

$$\text{Frac} = 01000000$$

$$0.15625 \times 2 = 0.3125$$

$$0.3125 \times 2 = 0.625$$

$$0.625 \times 2 = 1.25$$

$$0.25 \times 2 = 0.5$$

$$0.5 \times 2 = 1.0$$

$$0.0 \times 2 = 0.0$$

$$124_{10} = 2 \mid 124$$

$$2 \mid 62 \text{ r}0$$

$$2 \mid 31 \text{ r}0$$

$$2 \mid 15 \text{ r}1$$

$$2 \mid 7 \text{ r}1$$

$$2 \mid 3 \text{ r}1$$

$$2 \mid 1 \text{ r}1$$

$$2 \mid 0 \text{ r}1$$

$$1 \text{ r}0$$

$$= 01111100_{(2)}$$

1	01111100	01000000000000000000
Sign	E'	Fraction IEEE-754

$$= 1011110000000000000000000000$$

$$= B E 2 0 0 0 0 0$$

$$= 0XBE200000_{(16)}$$

$$8(a) 0XC1DEC00_{(16)}$$

$$= 0X121B14120000_{(16)}$$

$$= 0X11000001101110110000000000_{(2)}$$

1	10000011	10111011000000000000
Sign	E'	Fraction

$$\text{Sign} = -1$$

$$10000011_{(2)} \Rightarrow 131_{10} = E'$$

$$E = E' - 127 = 131 - 127 = 4$$

$$\Rightarrow -1.10111011000 \times 2^4$$

$$= -11011.11011_{(2)}$$

$$16.84215252 \times 2^{-5}$$

$$\text{Decimal} = -(1 \times 2^4) + (1 \times 2^3) + (0 \times 2^2) + (1 \times 2^1) + (1 \times 2^0)$$

$$= -(16 + 8 + 0 + 2 + 1) = -27$$

$$\text{Fraction} : (1 \times 2^{-1}) + (1 \times 2^{-2}) + (0 \times 2^{-3}) + (1 \times 2^{-4}) + (1 \times 2^{-5})$$

$$= 0.84375$$

$$\therefore \Rightarrow -27.84375_{(10)}$$

$$(b) \text{ 0X } \underline{\underline{3EA8}} \text{ 0000 } (16)$$

$\underline{\underline{31408}}$

$$= \underbrace{0011 \ 1110}_{\text{Sig} \quad E'} \underbrace{1010 \ 1000 \ 0000 \ 0000 \ 0000 \ 0000}_{\text{Fraction}} (4)$$

$$E' = \begin{array}{cccc} 0 & 1 & 1 & 1 \\ \hline & 64 & 32 & 16 \end{array} \begin{array}{cccc} 1 & 1 & 0 & 1 \\ \hline & 8 & 4 & 2 \end{array} \begin{array}{c} (2) \\ 1 \end{array} = (1 \times 64) + (1 \times 32) + (1 \times 16) + (1 \times 8) + (1 \times 4) + (0 \times 2) + (1 \times 1)$$

$$= 64 + 32 + 16 + 8 + 4 + 0 + 1$$

$$= 125$$

$$E' = E + 127$$

$$E = E' - 127$$

$$= 125 - 127$$

$$= -2$$

$$1.0101 \times 2^{-2} = 0.010101$$

$\begin{array}{ccc} \frac{1}{2^2} & \frac{1}{2^4} & \frac{1}{2^6} \end{array}$

$$= (1 \times 2^{-2}) + (1 \times 2^{-4}) + (1 \times 2^{-6})$$

$$= \underline{\underline{0.328125 (10)}}$$