

# Ancient Admixture in Human History

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**ABSTRACT** Population mixture is an important process in biology. We present a suite of methods for learning about population mixtures, implemented in a software package called ADMIXTOOLS, that support formal tests for whether mixture occurred and make it possible to infer proportions and dates of mixture. We also describe the development of a new single nucleotide polymorphism (SNP) array consisting of 629,433 sites with clearly documented ascertainment that was specifically designed for population genetic analyses and that we genotyped in 934 individuals from 53 diverse populations. To illustrate the methods, we give a number of examples that provide new insights about the history of human admixture. The most striking finding is a clear signal of admixture into northern Europe, with one ancestral population related to present-day Basques and Sardinians and the other related to present-day populations of northeast Asia and the Americas. This likely reflects a history of admixture between Neolithic migrants and the indigenous Mesolithic population of Europe, consistent with recent analyses of ancient bones from Sweden and the sequencing of the genome of the Tyrolean "Iceman."

**A**DMIXTURE between populations is a fundamental process that shapes genetic variation and disease risk. For example, African Americans and Latinos derive their genomes from mixtures of individuals who trace their ancestry to divergent populations. Study of the ancestral origin of the admixed individuals provides an opportunity to infer the history of the ancestral groups, some of whom may no longer be extant. The two main classes of methods in this field are local ancestry-based methods and global ancestry-based methods. Local ancestry-based methods such as LAMP (Sankararaman *et al.* 2008), HAPMIX (Price *et al.* 2009), and PCADMIX (Brisbin 2010) deconvolve ancestry at each locus in the genome and provide individual-level information about ancestry. While these methods provide valuable insights into the recent history of populations, they have reduced power to detect older events. The most commonly used methods for studying global ancestry are principal component analysis (PCA) (Patterson *et al.* 2006) and model-based clustering methods such as STRUCTURE (Pritchard *et al.* 2000) and

ADMIXTURE (Alexander *et al.* 2009). While these are powerful tools for detecting population substructure, they do not provide any formal tests for admixture (the patterns in data detected using these methods can be generated by multiple population histories). For instance, Novembre *et al.* (2008) showed that isolation-by-distance can generate PCA gradients that are similar to those that arise from long-distance historical migrations, making PCA results difficult to interpret from a historical perspective. STRUCTURE/ADMIXTURE results are also difficult to interpret historically, because these methods work either without explicitly fitting a historical model or by fitting a model that assumes that all the populations have radiated from a single ancestral group, which is unrealistic.

An alternative approach is to make explicit inferences about history by fitting phylogenetic tree-based models to genetic data. A limitation of this approach, however, is that many of these methods do not allow for the possibility of migrations between groups, whereas most human populations derive ancestry from multiple ancestral groups. Indeed there is only a handful of examples of human groups in which there is no evidence of genetic admixture today. In this article, we describe a suite of methods that formally test for a history of population mixture and allow researchers to build models of population relationships (including admixture) that fit genetic data. These methods are inspired by the ideas by Cavalli-Sforza and Edwards (1967), who fit phylogenetic

Copyright © 2012 by the Genetics Society of America  
doi: 10.1534/genetics.112.145037

Manuscript received March 24, 2012; accepted for publication August 28, 2012

Supporting information is available online at <http://www.genetics.org/lookup/suppl/doi:10.1534/genetics.112.145037/-/DC1>.

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trees of population relationships to the  $F_{st}$  values measuring allele frequency differentiation between pairs of populations. Later studies by Thompson (1975); Lathrop (1982); Waddell and Penny (1996); and Beerli and Felsenstein (2001) are more similar in spirit to our methods, in that they describe frameworks for fitting population mixture events (not just simple phylogenetic trees) to the allele frequencies observed in multiple populations, although the technical details are quite different from our work. In what follows we describe five methods: the *three-population test*, *D-statistics*,  *$F_4$ -ratio estimation*, *admixture graph fitting*, and *rolloff*. These have been introduced in some form in earlier articles (Reich *et al.* 2009; Green *et al.* 2010; Durand *et al.* 2011; Moorjani *et al.* 2011) but not coherently together and with the key material placed in supplementary sections, making it difficult for readers to understand the methods and their scope. We also release a software package, ADMIXTOOLS, that implements these five methods for users interested in applying them to studies of population history.

The first four techniques are based on studying patterns of allele frequency correlations across populations. The three-population test is a formal test of admixture and can provide clear evidence of admixture, even if the gene flow events occurred hundreds of generations ago. The *four-population test* implemented here as *D-statistics* is also a formal test for admixture, which not only can provide evidence for admixture but also can provide some information about the directionality of the gene flow.  *$F_4$ -ratio estimation* allows inference of the mixing proportions of an admixture event, even without access to accurate surrogates for the ancestral populations. However, this method demands more assumptions about the historical phylogeny. Admixture graph fitting allows one to build a model of population relationships for an arbitrarily large number of populations simultaneously and to assess whether it fits the allele frequency correlation patterns among populations. Admixture graph fitting has some similarities to the *TreeMix* method of Pickrell and Pritchard (2012) but differs in that *TreeMix* allows users to automatically explore the space of possible models and to find the one that best fits the data (our method does not), while our method provides a rigorous test for whether a proposed model fits the data (*TreeMix* does not).

It is important to point out that all four of the methods described in the previous paragraph measure allele frequency correlations among populations using the *f*-statistics and *D-statistics* that we define precisely in what follows. The expected values of these statistics are functions not just of the demographic history relating the populations, but also of the way that the analyzed polymorphisms were discovered (the so-called ascertainment process). In principle, explicit inferences about the demographic history of populations can be made using the magnitudes of allele frequency correlation statistics, an idea that is exploited to great advantage by Durand *et al.* (2011); however, for this approach to work, it is essential to analyze sites with rigorously documented ascertainment, as are available, for example, from whole-genome sequencing data. Here our approach is fundamentally

different in that we are focusing on tests for a history of admixture that assess whether particular statistics are consistent with 0. The expectation of zero in the absence of admixture is robust to all but the most extreme ascertainment processes, and thus these methods provide valid tests for admixture even using data from SNP arrays with complex ascertainment. We show this robustness both by simulation and with application to real data. In some simple scenarios, we also demonstrate this robustness theoretically. Furthermore, we show that ratios of *f*-statistics can provide precise estimates of admixture proportions that are robust to both details of the ascertainment and to population size changes over the course of history, even if the *f*-statistics in the numerator and denominator themselves have magnitudes that are affected by ascertainment.

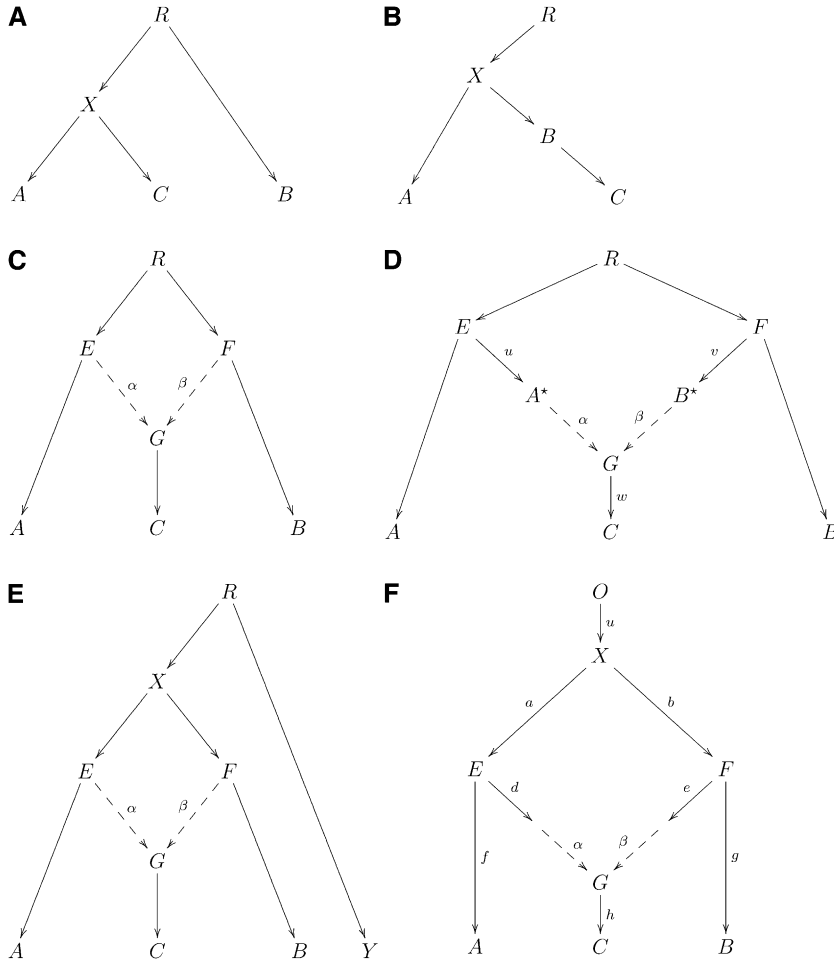
The fifth method that we introduce in this study, *rolloff*, is an approach for estimating the date of admixture which models the decay of admixture linkage disequilibrium in the target population. *Rolloff* uses different statistics from those used by haplotype-based methods such as *STRUCTURE* (Pritchard *et al.* 2000) and *HAPMIX* (Price *et al.* 2009). The most relevant comparison is to the method of Pool and Nielsen (2009), who like us are specifically interested in learning about history, and who estimate population mixture dates by studying the distribution of ancestry tracts inherited from the two ancestral populations. A limitation of the Pool and Nielsen (2009) approach, however, is that it assumes that local ancestry inference is perfect, whereas in fact most local ancestry methods are unable to accurately infer the short ancestry tracts that are typical for older dates of mixture. Precisely for these reasons, the *HAPMIX* article cautions against using *HAPMIX* for date estimation (Price *et al.* 2009). In contrast, *rolloff* does not require accurate reconstruction of the breakpoints across the chromosomes or data from good surrogates for the ancestors, making it possible to interrogate older dates. Simulations that we report in what follows show that *rolloff* can produce unbiased and quite accurate estimates for dates up to 500 generations in the past.

## Materials and Methods

Throughout this article, unless otherwise stated, we consider biallelic markers only, and we ignore the possibility of recurrent or back mutations. Our notation in this article is that we write  $f_2$  (and later  $f_3, f_4$ ) for *statistics*: empirical quantities that we can compute from data, and  $F_2$  (and later  $F_3, F_4$ ) for corresponding *theoretical* quantities that depend on an assumed phylogeny (and the ascertainment). We define “drift” as the frequency change of an allele along a graph edge (hence drift between two populations *A* and *B* is a function of the difference in the allele frequency of polymorphisms in *A* and *B*).

### The three-population test and introduction of *f*-statistics

We begin with a description of the three-population test. First we give some theory. Consider the tree of Figure 1A.



**Figure 1** *f*-statistics: (A) A simple phylogenetic tree, (B) the additivity of branch lengths; the genetic drift between (A, B) computed using our *f*-statistic-based methods is the same as the sum of the genetic drifts between (A, B) and (B, C), regardless of the population in which SNPs are ascertained, (C) phylogenetic tree with simple admixture, (D) a more general form of Figure 1C, (E) example of an outgroup case, and (F) example of admixture with an outgroup.

We see that the path from C to A and the path from C to B just share the edge from C to X. Let  $a'$ ,  $b'$ ,  $c'$  be allele frequencies in the populations A, B, C, respectively, at a single polymorphism. Define

$$F_3(C; A, B) = E[(c' - a')(c' - b')].$$

We, similarly, in an obvious notation define

$$F_2(A, B) = E[(a' - b')^2]$$

$$F_4(A, B; C, D) = E[(a' - b')(c' - d')].$$

Choice of the allele does not affect any of  $F_2$ ,  $F_3$ ,  $F_4$  as choosing the alternate allele simply flips the sign of both terms in the product. We refer to  $F_2(A, B)$  as the *branch length* between populations A and B. We use these branch lengths in admixture graph fitting for graph edges.

Our *F*-values should be viewed as population parameters, but we note that they depend both on the demography and choice of SNPs. In Appendix A we give formulae that use sample frequencies and that yield unbiased estimates of the corresponding *F* parameters. The unbiased estimates of *F* computed using these formulae at each marker are then averaged over many markers to form our *f*-statistics.

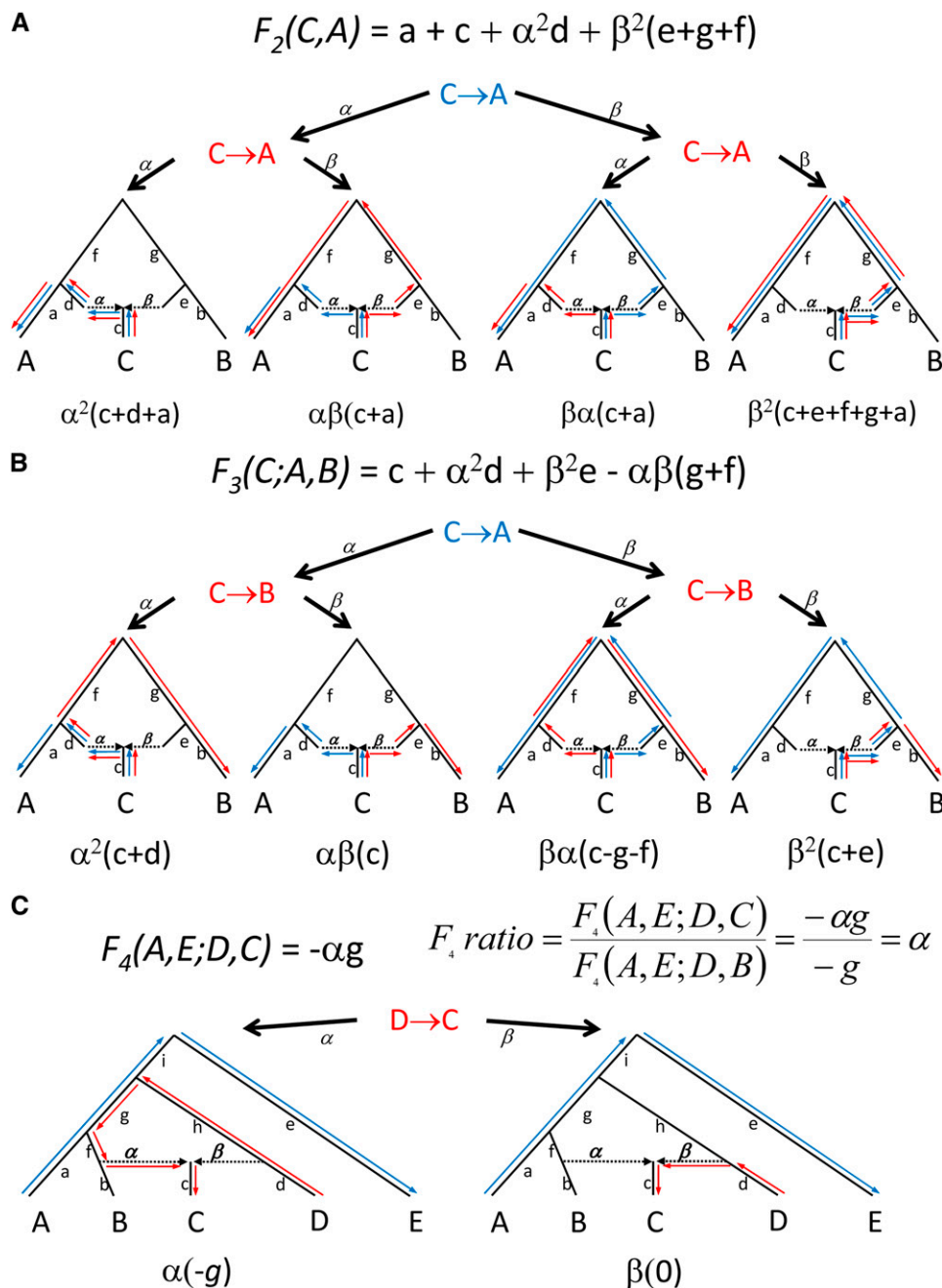
The results that follow hold rigorously if we identify the polymorphisms we are studying in an outgroup (that is, we select SNPs based on patterns of genetic variation in populations that all have the same genetic relationship to populations A, B, C). Since only markers with variation in A, B, C are relevant to the analysis, then by ascertaining in an outgroup we ensure that our markers are polymorphic in the root population of A, B, C. Later on, we discuss how other strategies for ascertaining polymorphisms would be expected to affect our results. In general, our tests for admixture and estimates of admixture proportion are strikingly robust to the ascertainment processes that are typical for human SNP array data, as we verify both by simulations and by empirical analysis.

Suppose the allele frequency of a SNP is  $r$  at the root. In the tree of Figure 1A, let  $a'$ ,  $b'$ ,  $c'$ ,  $x'$ ,  $r'$  be allele frequencies in A, B, C, X, R. Condition on  $r'$ . Then

$$E[(c' - a')(c' - b')] = E[(c' - x' + x' - a')(c' - x' + x' - b')] = E[(c' - x')^2] \geq 0$$

since  $E[a' | x'] = x'$ , and  $E[x' - b'] = E[r' - b' - (r' - x')] = 0$ . If the phylogeny has C as an outgroup (switching B, C in Figure 1A), then a similar argument shows that

$$E[(c' - a')(c' - b')] = E[(r' - c')^2] + E[(r' - x')^2] \geq 0.$$



**Figure 2** Visual computation of expected values of  $F_2$ ,  $F_3$ , and  $F_4$  statistics. See Appendix 2 for a discussion of this figure.

There is an intuitive way to think about the expected values of  $f$ -statistics, which relies on tracing the overlap of genetic drift paths between the first and second terms in the quadratic expression, as illustrated in Figure 2 and discussed further in Appendix B. For example,  $E[(c' - a')(c' - b')]$  can be negative only if population  $C$  has ancestry from populations related to both  $A$  and  $B$ . Only in this case are there paths between  $C$  and  $A$  and  $C$  and  $B$  that also take opposite drift directions through the tree (Figure 1C and Figure 2), which contributes to a negative expectation for the statistics. The observation of a significantly negative value of  $f_3(C; A, B)$  is thus evidence of complex phylogeny in  $C$ . We prove this formally in Appendix C (Theorem 1). In Appendix D, we

also relax our assumptions about the ascertainment process, showing that  $F_3$  is guaranteed to be positive if  $C$  is unadmixed under quite general conditions, for example, polymorphic in the root  $R$  and in addition ascertained as polymorphic in any of  $A, B, C$ . It is important to recognize, however, that a history of admixture does not always result in a negative  $f_3(C; A, B)$ -statistic. If population  $C$  has experienced a high degree of population-specific drift (perhaps due to founder events after admixture), it can mask the signal so that  $f_3(C; A, B)$  might not be negative.

An important feature of this test is that it definitively shows that the history of mixture occurred in population  $C$ ; a complex history for  $A$  or  $B$  cannot produce negative  $F_3(C;$

$A, B$ ). To explain why this is so, we recapitulate material from Reich *et al.* (2009). If population  $A$  is admixed then if we pick an allele of  $A$ , it must have originated in one of the admixing populations. Pick alleles  $\alpha, \beta$  from populations  $A$  and  $B$  and  $\gamma_1, \gamma_2$  independently from  $C$ , coding 1 for a reference allele, 0 for a variant, etc. Thus,  $F_3(C; A, B) = E[(\gamma_1 - \alpha)(\gamma_2 - \beta)]$ . Suppose population  $A$  is admixed;  $B$  and  $C$  are not admixed. The allele  $\alpha$  sampled from population  $A$  can take more than one path through the ancestral populations.  $F_3(C; A, B)$  can then be computed as a weighted average over the possible phylogenies, in all of which the quantity has a positive expectation because  $A$  and  $B$  are now unadmixed (Appendix B and Figure 2). In conclusion, the diagram makes it visually evident that if  $F_3(C; A, B) < 0$  then population  $C$  itself must have a complex history.

### Additivity of $F_2$ along a tree branch

In this article we consider generalizations of phylogenetic trees where graph edges indicate that one population is a descendant of another. Consider the phylogenetic tree in Figure 1B, and a marker polymorphic at the root. Drift on a given edge is a random variable with mean 0. For if  $A \rightarrow B$  is a graph edge, with corresponding allele frequencies  $a', b'$ ,

$$E[b'|a'] = a'.$$

This is the *martingale* property of allele frequency diffusion. Drifts on two distinct edges of a tree are orthogonal, where orthogonality of random variables  $X, Y$  simply means that  $E[XY] = 0$ . In our context this means that the drifts on distinct edges have mean 0 and are uncorrelated.

A valuable feature of our  $F$ -statistics definition is that branch lengths on the tree (as defined by  $F_2$ ) are additive. We illustrate this with an example from human history (Figure 1B). (We note that all examples in this article refer to human history, although the methods should apply equally well to other species.) In this example,  $A$  and  $C$  are present-day populations that split from an ancestral population  $X$ .  $B$  is an ancestral population to  $C$ . For instance,  $A$  might be modern Yoruba,  $C$  a European population, and  $B$  an ancient population, perhaps a sample from archeological material of a population that existed thousands of years ago. We assume here that we ascertain in an outgroup (implying polymorphism at the root) and again assume neutrality and that we can ignore recurrent or backmutations. Then we mean by additivity that

$$F_2(A, C) = F_2(A, B) + F_2(B, C)$$

for

$$\begin{aligned} E[(a' - c')^2] &= E[(a' - b' + b' - c')^2] \\ &= E[(a' - b')^2] + E[(b' - c')^2] + 2E[(a' - b')(b' - c')], \end{aligned}$$

but the last term is 0 since the change in allele frequencies (drifts)  $X \rightarrow A, X \rightarrow B, B \rightarrow C$  are all uncorrelated.

We remark that our  $F_2$ -distance resembles the familiar  $F_{st}$ , but is not the same. In particular, parts of a graph that are far from the root (in genetic drift distance) have  $F_2$  reduced. Some insight into this effect is given by considering the simple graph

$$R \xrightarrow{\tau_1} A \xrightarrow{\tau_2} B,$$

where  $\tau_1, \tau_2$  are drift times on the standard diffusion time-scale (two random alleles of  $B$  have probability  $e^{-\tau_2}$  that they have not coalesced in the ancestral population  $A$ ).

If  $r', a', b'$  are allele frequencies in  $R, A, B$ , respectively, then  $F_2(A, B) = E[(a' - b')^2]$ . Write  $E_r, E_a$  for expectations conditional on population allele frequencies  $r', a'$ . Then  $E_a[(a' - b')^2] = a'(1 - a')(1 - e^{-\tau_2})$  (Nei 1987, Chap. 13). Moreover  $E_r[a'(1 - a')] = r'(1 - r')e^{-\tau_1}$ . Hence

$$F_2(A, B) = E[r'(1 - r')e^{-\tau_1}(1 - e^{-\tau_2})].$$

Informally the drift from  $R \rightarrow A$  shrinks  $F_2(A, B)$  by a factor  $e^{-\tau_1}$ . Thus expected drift is *additive*,

$$F_2(R, B) = F_2(R, A) + F_2(A, B),$$

but the drift does depend on ascertainment. For a given edge, the more distant the root, the smaller the drift. A loose analogy is projecting a curved surface, such as part of the globe, into a plane. Locally all is well, but any projection will cause distortion in the large. Additivity in  $F_2$  distances is all we require in what follows. We note that there is no assumption here that population sizes are constant along a branch edge, and so we are *not* assuming linearity of branch lengths in time.

### Expected values of our $f$ -statistics

We can calculate expected values for our  $f$ -statistics, at least for simple demographic histories that involve population splits and admixture events. We assume that genetic drift events on distinct edges are uncorrelated, which as mentioned before will be true if we ascertain in an outgroup, and our alleles are neutral.

We give an illustration for  $f_3$ -statistics. Consider the demography shown in Figure 1C. Populations  $E, F$  split from a root population  $R$ .  $G$  then was formed by admixture in proportions  $\alpha: \beta$  ( $\beta = 1 - \alpha$ ). Modern populations  $A, B, C$  are then formed by drift from  $E, F, G$ . We want to calculate the expected value of  $f_3(C; A, B)$ . Assume that our ascertainment is such that drifts on distinct edges are orthogonal, which will hold true if we ascertained the markers in an outgroup.

We recapitulate some material from (Reich *et al.* 2009, Supplementary S2, Sect. 2.2). As before let  $a', b', c'$  be population allele frequencies in  $A, B, C$ , and let  $g'$  be the allele frequency in  $G$  and so on:

$$F_3(C; A, B) = E[(c' - a')(c' - b')].$$

We see by orthogonality of drifts that

$$F_3(C; A, B) = E[(g' - a')(g' - b')] + E[(g' - c')^2],$$

which we write as

$$F_3(C; A, B) = F_3(G; A, B) + F_2(C, G). \quad (1)$$

Now, label alleles at a marker 0, 1. Then picking chromosomes from our populations independently we can write

$$F_3(G; A, B) = E[(g_1 - a_1)(g_2 - b_1)],$$

where  $a_1, b_1$  are alleles chosen randomly in populations  $A, B$  and  $g_1, g_2$  are alleles chosen randomly and independently in population  $G$ . Similarly, we define  $e_1, e_2, f_1$ , and  $f_2$ . However,  $g_1$  originated from  $E$  with probability  $\alpha$  and so on. Thus

$$\begin{aligned} F_3(G; A, B) &= E[(g_1 - a_1)(g_2 - b_1)] \\ &= \alpha^2 E[(e_1 - a_1)(e_2 - b_1)] \\ &\quad + \beta^2 E[(f_1 - a_1)(f_2 - b_1)] \\ &\quad + \alpha\beta E[(e_1 - a_1)(f_1 - b_1)] \\ &\quad + \alpha\beta E[(f_1 - a_1)(e_1 - b_1)], \end{aligned}$$

where  $a_1, a_2$  are independently picked from  $E$  and  $b_1, b_2$  from  $F$ . The first three terms vanish. Further

$$E[(f_1 - a_1)(e_1 - b_1)] = -E[(e_1 - f_1)^2].$$

This shows that under our assumptions of orthogonal drift on distinct edges,

$$F_3(C; A, B) = F_2(C, G) - \alpha\beta F_2(E, F). \quad (2)$$

It might appear that Figure 1C is too restricted, as it assumes that the admixing populations  $E, F$  are ancestral to  $A, B$  and that we should consider the more general graph shown in Figure 1D. But it turns out that using our  $f$ -statistics alone (and not the more general allelic spectrum) that even if  $\alpha, \beta$  are known, we can obtain information only about

$$\alpha^2 u + \beta^2 v + w.$$

Thus in fitting admixture graphs to  $f$ -statistics, we can, without loss of generality, fit all the genetic drift specific to the admixed population on the lineage directly ancestral to the admixed population (the lineage leading from  $C$  to  $G$  in Figure 1C).

### The outgroup case

Care though is needed in interpretation. Consider Figure 1E. Here a similar calculation to the one just given shows (again assuming orthogonality of drift on each edge) that

$$F_3(C; A, Y) = F_2(C, G) + \beta^2 F_2(F, X) - \alpha\beta F_2(E, X). \quad (3)$$

Note that  $Y$  has little to do with the admixture into  $C$  and we obtain the same  $F_3$  value for any population  $Y$  that splits off from  $A$  more anciently than  $X$ .

We call this case, where we have apparent admixture between  $A$  and  $Y$ , the *outgroup case*, and it needs to be carefully considered when recovering population relationships.

### Estimates of mixing proportions

We want to estimate, or at least bound, the mixing proportions that have resulted in the ancestral population of  $C$ . With further strong assumptions on the phylogeny we can get quite precise estimates even without accurate surrogates for the ancestral populations (see Reich *et al.* 2009 and the  $F_4$ -ratio estimation that we describe below, for examples). Also if we have data from populations that are accurate surrogates for the ancestral admixing population (and we can ignore the drift post admixture), the problem is much easier. For instance, in Patterson *et al.* (2010) we give an estimator that works well even when the sample sizes of the relevant populations are small, and we have multiple admixing populations whose deep phylogenetic relationships we may not understand. Here we show a method that obtains useful bounds, without requiring full knowledge of the phylogeny, although the bounds are not very precise. Note that although our three-population test remains valid even if the populations  $A, B$  are admixed, the mixing proportions we calculate are not meaningful unless the assumed phylogeny is at least roughly correct. Indeed even discussing mixing from an ancestral population of  $A$  hardly makes sense if  $A$  is admixed itself subsequent to the admixing event in  $C$ . This is discussed further when we present data from Human Genome Diversity Panel (HGDP) populations.

In much of the work in this article, we analyze some populations  $A, B, C$  and need an outgroup, which split off from the ancestral population of  $A, B, C$  before the population split of  $A, B$ . For example, in Figure 1E,  $Y$  is such an outgroup. Usually, when studying a group of populations within a species, a plausible outgroup can be proposed. The outgroup assumption can then be checked using the methods of this article, by adding an individual from a more distantly related population, which can be treated as a second outgroup. For instance, with human populations from Eurasia, Yoruba or San Bushmen from sub-Saharan Africa will often be plausible outgroups.<sup>1</sup> Our second outgroup here is simply being used to check a phylogenetic assumption in our primary analysis, and we do *not* require polymorphism at the root for this narrow purpose. Chimpanzee is always a good second outgroup for studies of humans.

Consider the phylogeny of Figure 1F. Here  $\alpha, \beta$  are mixing parameters ( $\alpha + \beta = 1$ ) and we show drift distances along the graph edges. Note that here we use  $a, b, \dots$ , as branch lengths ( $F_2$  distances), not sample or population allele frequencies as we do elsewhere in this article. Thus, for example,  $F_2(O, X) = u$ . Now we can obtain estimates of

<sup>1</sup> There is no completely satisfactory term for the 'Khoisan' peoples of southern Africa; see Barnard (1992, introduction) for a sensitive discussion. We prefer 'Bushmen' following Barnard. However, the standard name for the HGDP Bushmen sample is 'San' in the genetic literature [for example Cann *et al.* (2002)], and we use this specifically to refer to these samples.

$$\begin{aligned}
Z_0 &= u = F_3(O; A, B) \\
Z_1 &= u + \alpha a = F_3(O; A, C) \\
Z_2 &= u + \beta b = F_3(O; B, C) \\
Z_3 &= u + a + f = F_2(O; A) \\
Z_4 &= u + b + g = F_2(O; B) \\
Z_5 &= u + h + \alpha^2(a + d) + \beta^2(b + e) = F_2(O; C).
\end{aligned}$$

We also have estimates of

$$F = h - \alpha\beta(a + b) = F_3(C; A, B).$$

Set  $Y_i = Z_i - Z_0$ ,  $i = 0 \dots 5$ , which eliminates  $u$ . This shows that any population  $O$  which is a true outgroup should (up to statistical noise) give similar estimates for  $Y_i$  (Figure 1F). We have three inequalities:

$$\begin{aligned}
\alpha &\geq Y_1/Y_3 \\
\beta &\geq Y_2/Y_4 \\
\alpha\beta(a + b) &\leq -F.
\end{aligned}$$

Using  $\alpha a = Y_1$ ,  $\beta b = Y_2$  we can rewrite these as

$$\begin{aligned}
Y_1/Y_3 &\leq \alpha \leq 1 - Y_2/Y_4 \\
\alpha(Y_2 - Y_1) &\geq -F - Y_1,
\end{aligned}$$

giving lower and upper bounds on  $\alpha$ , which we write as  $\alpha_L, \alpha_U$  in the tables of results that follow. These bounds can be computed by a program *qpBound* in the ADMIXTOOLS software package that we make available with this article.

Although these bounds will be nearly invariant to choices of the outgroup  $O$ , choices for the source populations  $A, B$  may make a substantial difference. We give an example in a discussion of the relationship of Siberian populations to Europeans. In principle we can give standard errors for the bounds, but these are not easily interpretable, and we think that in most cases systematic errors (for instance, that our phylogeny is not exactly correct) are likely to dominate.

We observe that in some cases the lower bound exceeds the upper, even when the  $Z$ -score for admixture of population  $C$  is highly significant. We interpret this as suggesting that our simple model for the relationships of the three populations is wrong. A negative  $Z$ -score indeed implies that  $C$  has a complex history, but if  $A$  or  $B$  also has a complex history, then a recovered mixing coefficient  $\alpha$  has no real meaning.

### Estimation and normalization

With all our  $f$ -statistics it is critical that we can compute unbiased estimates of the population  $F$ -parameter for a single SNP, with finite sample sizes. Without that, our estimates will be biased, even if we average over many unlinked SNPs. The explicit formulae for  $f_2, f_3, f_4$  that we present in Appendix A (previously given in Reich *et al.* 2009, Supplementary Material) are in fact minimum variance unbiased estimates of the corresponding  $F$ -parameters, at least for a single marker.

The expected (absolute) values of an  $f$ -statistic, such as  $f_3$ , strongly depends on the distribution of the derived allele frequencies of the SNPs examined; for example, if many

SNPs are present that have a low average allele frequency across the populations being examined, then the magnitude of  $f_3$  will be reduced. To see this, suppose that we are computing  $f_3(C; A, B)$ , and as before  $a', b', c'$  are population frequencies of an allele in  $A, B, C$ . If the allele frequencies are small, then it is obvious that the expected value of  $f_3(C; A, B)$  will be small in absolute magnitude as well. Importantly, however, the sign of an  $f$ -statistic is not dependent on the absolute magnitudes of the allele frequencies (all that it depends on is the relative magnitudes across the populations being compared). Thus, a significant deviation of an  $f$ -statistic from 0 can serve as a statistically valid test for admixture, regardless of the ascertainment of the SNPs that are analyzed. However, to reduce the dependence of the value of the  $f_3$ -statistic on allele frequencies for some of our practical computations, in all of the empirical analyses we report below, we normalize using an estimate for each SNP of the heterozygosity of the target population  $C$ . Specifically, for each SNP  $i$ , we compute unbiased estimates  $\hat{T}_i, \hat{B}_i$  of both

$$\begin{aligned}
T_i &= (c' - a')(c' - b') \\
B_i &= 2c'(1 - c').
\end{aligned}$$

Now we normalize our  $f_3$ -statistic computing

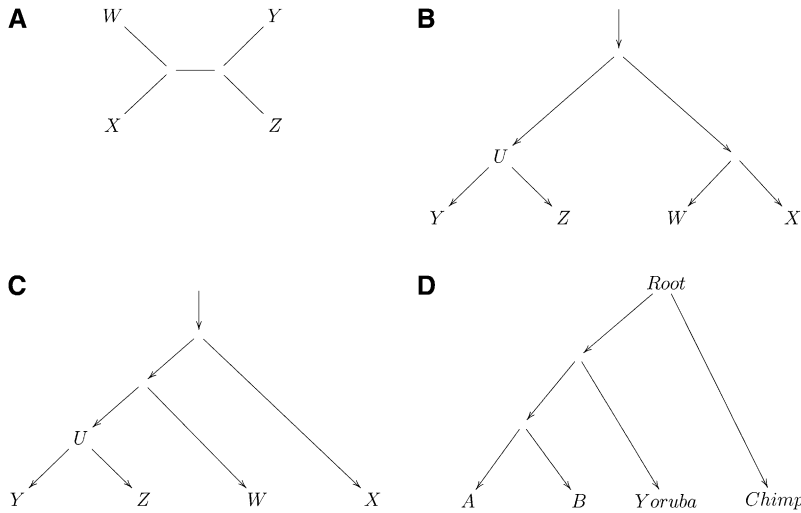
$$f_3^* = \frac{\sum_i \hat{T}_i}{\sum_i \hat{B}_i}.$$

This greatly reduces the numerical dependence of  $f_3$  on the allelic spectrum of the SNPs examined, without making much difference to statistical significance measures such as a  $Z$ -score. We note that we use  $f_3$  and  $f_3^*$  interchangeably in many places in this article. Both of these statistics give qualitatively similar results and thus if the goal is only to test if  $f_3$  has negative expected value then the inference should be unaffected.

### D-statistics

The  $D$ -statistic test was first introduced in Green *et al.* (2010) where it was used to evaluate formally whether modern humans have some Neandertal ancestry. Further theory and applications of  $D$ -statistics can be found in Reich *et al.* (2010) and Durand *et al.* (2011). A very similar statistic  $f_4$  was used to provide evidence of admixture in India (Reich *et al.* 2009), where we called it a four-population test. The  $D$ -statistic was also recently used as a convenient statistic for studying locus-specific introgression of genetic material controlling coloration in *Heliconius* butterflies (Dasmahapatra *et al.* 2012).

Let  $W, X, Y, Z$  be four populations, with a phylogeny that corresponds to the unrooted tree of Figure 3A. For SNP  $i$  suppose variant population allele frequencies are  $w', x', y', z'$ , respectively. Choose an allele at random from each of the four populations. Then we define a “BABA” event to mean that the  $W$  and  $Y$  alleles agree, and the  $X$  and  $Z$  alleles agree, while the  $W$  and  $X$  alleles are distinct. We define an “ABBA” event similarly, now with the  $W$  and  $Z$  alleles in agreement.



**Figure 3** *D*-statistics provide formal tests for whether an unrooted phylogenetic tree applies to the data, assuming that the analyzed SNPs are ascertained as polymorphic in a population that is an outgroup to both populations (Y, Z) that make up one of the clades. (A) A simple unrooted phylogeny, (B) phylogenies in which (Y, Z) and (W, X) are clades that diverge from a common root, (C) phylogenies in which (Y, Z) are a clade and W and X are increasingly distant outgroups, and (D) a phylogeny to test if human Eurasian populations (A, B) form a clade with respect to sub-Saharan Africans (Yoruba).

Let  $Num_i$  and  $Den_i$  be the numerator and denominator of the statistic:

$$Num_i = P(BABA) - P(ABBA) = (w' - x')(y' - z')$$

$$Den_i = P(BABA) + P(ABBA) = (w' + x' - 2w'x')(y' + z' - 2y'z').$$

For SNP data these values can be computed using either population or sample allele frequencies. Durand *et al.* (2011) showed that replacing population allele frequencies ( $w', y'$ , etc.) by the sample allele frequencies yields unbiased estimates of  $Num_i$ ,  $Den_i$ . Thus if  $w, x, y, z$  are sample allele frequencies we define

$$\hat{Num}_i = (w - x)(y - z)$$

$$\hat{Den}_i = (w + x - 2wx)(y + z - 2yz)$$

and, in a similar spirit to our normalized  $f_3$ -statistic  $f_3^*$  we define the *D*-statistic  $D(W, X; Y, Z)$  as

$$D = \frac{\sum_i \hat{Num}_i}{\sum_i \hat{Den}_i},$$

summing both the numerator and denominator over many SNPs and only then taking the ratio. If we ascertain in an outgroup, then if (W, X) and (Y, Z) are clades in the population tree, it is easy to see that  $E[Num_i] = 0$ . We can compute a standard error for *D* using the weighted block jackknife (Busing *et al.* 1999). The number of standard errors that this quantity is from zero forms a Z-score, which is approximately normally distributed and thus yields a formal test for whether (W, X) indeed forms a clade.

More generally, if the relationship of the analyzed populations is as shown in Figure 3B or Figure 3C and we ascertain in an outgroup or in {W, X} then *D* should be zero up to statistical noise. The reason is that if *U* is the ancestral population to Y, Z and  $u', y', z'$  are population allele frequencies in U, Y, Z, then  $E[y' - z' | u'] = E[y' | u'] - E[z' | u'] = 0$ . Here there is no need to assume polymorphism at the root of the tree, as for a SNP to make a nonzero contribution to *D* we must have polymorphism at both {Y, Z} and {W, X}. If the

tree assumption is correct, drift between Y, Z and between W, X are independent so that  $E[Num_i] = 0$ . Thus testing whether *D* is consistent with zero constitutes a test for whether (W, X) and (Y, Z) are clades in the population tree.

As mentioned earlier, *D*-statistics are very similar to the four-population test statistics introduced in Reich *et al.* (2009). The primary difference is in the computation of the denominator of *D*. For statistical estimation, and testing for “treeness,” the *D*-statistics are preferable, as the denominator of *D*, the total number of ABBA and BABA events, is uninformative for whether a tree phylogeny is supported by the data, while *D* has a natural interpretation: the extent of the deviation on a normalized scale from  $-1$  to  $1$ .

As an example, let us assume that two human Eurasian populations A, B are a clade with respect to West Africans (Yoruba). Assume the phylogeny shown in Figure 3D and that we ascertain in an outgroup to A, B. Then

$$E[D(\text{Chimp}, \text{Yoruba}; A, B)] = 0.$$

#### *F*<sub>4</sub>-ratio estimation

*F*<sub>4</sub>-ratio estimation, previously referred to as *f*<sub>4</sub>-ancestry estimation in Reich *et al.* (2009), is a method for estimating ancestry proportions in an admixed population, under the assumption that we have a correct historical model.

Consider the phylogeny of Figure 4. The population X is an admixture of populations B' and C' (possibly with subsequent drift). We have genetic data from populations A, B, X, C, O.

Since  $F_4(A, O; C', C) = 0$  it follows that

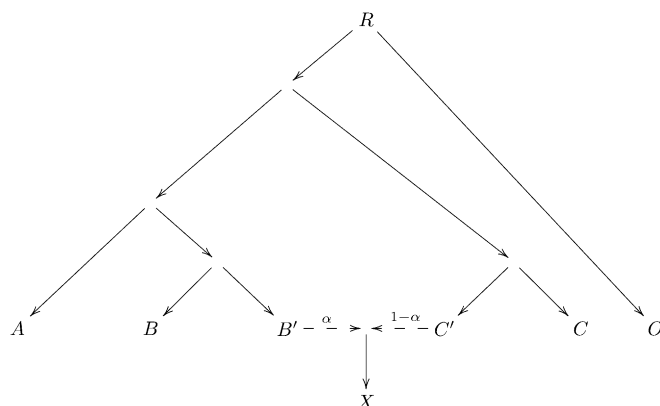
$$F_4(A, O; X, C) = \alpha F_4(A, O; B', C) = \alpha F_4(A, O; B, C). \quad (4)$$

Thus an estimate of  $\alpha$  is obtained as

$$\hat{\alpha} = \frac{f_4(A, O; X, C)}{f_4(A, O; B, C)}, \quad (5)$$

where the estimates in both numerator and denominator are obtained by summing over many SNPs.





**Figure 4** A phylogeny explaining  $f_4$ -ratio estimation.

As we can obtain unbiased  $F_4$ -statistics by sampling a single allele from each population, we can apply this test to sequence data, where we pick a single allele, from a high-quality read, for all relevant populations at each polymorphic site. In practice this must be done with care as both sequencing error that is correlated between samples and systematic misalignment of reads to a reference sequence can distort the statistics.

#### Examples of $F_4$ -ratio estimation

Reich *et al.* (2009) provide evidence that most human South Asian populations can be modeled as a mixture of Ancestral North Indians (ANI) and Ancestral South Indians (ASI) and that if we set, using the labeling above,

##### Label Population

A	Adygei
B	CEU (HapMap European Americans)
X	Indian (many populations)
C	Onge (indigenous Andamanese)
O	Papuan (Dai and HapMap YRI West Africans also work)

we get estimates of the mixing coefficients that are robust, have quite small standard errors, and are in conformity with other estimation methods. See Reich *et al.* (2009, Supplementary S5) for further details.

As another example, in Reich *et al.* (2010) and Green *et al.* (2010) evidence was given that there was gene flow (introgression) from Neandertals into non-Africans. Further, a sister group to Neandertals, “Denisovans” represented by a fossil from Denisova cave, Siberia, shows no evidence of having contributed genes to present-day humans in mainland Eurasia (Reich *et al.* 2010, 2011). The phylogeny is that of Figure 4 if we set:

##### Label Population

A	Denisova
B	Neandertal
X	French (or almost any population from Eurasia)
C	Yoruba
O	Chimpanzee

Here  $B'$  is the population of Neandertals that admixed, which forms a clade with the Neandertals from Vindija that

were sequenced by Green *et al.* (2010). So for this example, we obtain an estimate of  $\alpha$ , the proportion of Neandertal gene flow into French as  $0.022 \pm 0.007$  (see Reich *et al.* 2010, S18, for more detail).

#### Simulations to test the accuracy of $f$ - and $D$ -statistic-based historical inferences

We carried out coalescent simulations of five populations related according to Figure 4, using *ms* (Hudson 2002). Detailed information about the simulations is given in Appendix D.

Table 1 shows that using the three-population test,  $D$ -statistics, and  $F_4$ -ratio estimation, we reliably detect mixture events and obtain accurate estimates of mixture proportions, even for widely varied demographic histories and strategies for discovering polymorphisms.

The simulations also document important features of our methods. As mentioned earlier, the only case where the  $f_3$ -statistic for a population that is truly admixed fails to be negative is when the population has experienced a high degree of population-specific genetic drift after the admixture occurred. Further, the  $D$ -statistics show a substantial deviation from 0 only when an admixture event occurred in the history of the four populations contributing to the statistic. Finally, the estimates of admixture proportions using  $F_4$ -ratio estimation are accurate for all ascertainment strategies and demographies.

#### Effect of ascertainment process on $f$ - and $D$ -statistics

So far, we have assumed that we have sequence data from all populations and ascertainment is not an issue. However, the ascertainment of polymorphisms (for example, enriching the set of analyzed SNPs for ancestry informative markers) can modulate the magnitudes of  $F_3$ ,  $F_4$ , and  $D$ . Empirically, we observe that in commercial SNP arrays developed for genome-wide association studies (like Affymetrix 6.0 and Illumina 610-Quad), ascertainment does indeed affect the observed magnitudes of these statistics, but importantly, does not cause them to be biased away from zero if this is their expected value in the absence of complex ascertainment (e.g., for complete genome sequencing data). This is key to the robustness of our tests for admixture: since our tests are largely based on evaluating whether particular  $f$ - or  $D$ -statistics are consistent with zero, and SNP ascertainment almost never causes a deviation from zero, the ascertainment process does not appear to be contributing to spuriously significant signals of admixture. We have verified this through two lines of analysis. First, we carried out simulations showing that tests of admixture (as well as  $F_4$ -ratio estimation) performed using these methods are robust to very different SNP ascertainment strategies (Table 1). Second, we report analyses of data from a new SNP array with known ascertainment that we designed specifically for studies of population history. Even when we use radically different ascertainment schemes, and even when we use widely used commercial SNP arrays, inferences about history are indistinguishable (Table 9).

**Table 1** Behavior of  $F$ - and  $D$ -statistics for a simulated scenarios of admixture

Scenario	$F_{st}(C, B)$	$F_{st}(O, B)$	$D(A, B; C, O)$	$D(A, X; C, O)$	$f_3(B; A, C)$	$f_3(X; A, C)$	$f_4$ -ratio
Baseline	0.10	0.14	0.00	-0.08	0.002	-0.005	0.47
Vary sample size $n = 2$ from each population	0.10	0.14	0.00	-0.08	0.002	-0.005	0.47
Vary SNP ascertainment							
Use all sites (full sequencing data)	0.10	0.13	0.00	-0.11	0.001	-0.002	0.47
Polymorphic in a single $B$ individual	0.10	0.16	-0.01	-0.06	0.003	-0.006	0.47
Polymorphic in a single $C$ individual	0.10	0.16	0.00	-0.13	0.003	-0.007	0.46
Polymorphic in a single $X$ individual	0.11	0.16	0.00	-0.11	0.003	-0.007	0.49
Polymorphic in two individuals: $B$ and $O$	0.10	0.16	-0.01	-0.08	0.002	-0.005	0.46
Vary demography							
$N_A = 2,000$ (vs. 50,000) pop $A$ bottleneck	0.10	0.14	0.00	-0.08	0.002	-0.005	0.48
$N_B = 2,000$ (vs. 12,000) pop $B$ bottleneck	0.14	0.17	0.00	-0.08	0.011	-0.004	0.48
$N_C = 1,000$ (vs. 25,000) pop $C$ bottleneck	0.16	0.14	0.00	-0.08	0.002	-0.005	0.46
$N_X = 500$ (vs. 10,000) pop $X$ bottleneck	0.10	0.14	0.00	-0.08	0.002	0.004	0.47
$N_{ABB'} = 3,000$ (vs. 7,000) $ABB'$ bottleneck	0.14	0.17	0.00	-0.09	0.002	-0.007	0.47

We carried out simulations for populations related according to Figure 4 using *ms* (Hudson 2002) with the command: `.ms 110 1000000 -t 1 -l 5 22 22 22 22 -n 1 8.0 -n 2 2.5 -n 3 5.0 -n 4 1.2 -n 5 1.0 -es 0.001 5 0.47 -en 0.001001 6 1.0 -ej 0.0060 5 4 -ej 0.007 6 2 -en 0.007001 2 0.33 -ej 0.01 4 3 -en 0.01001 3 0.7 -ej 0.03 3 2 -en 0.030001 2 0.25 -ej 0.06 2 1 -en 0.060001 1 1.0`. We chose parameters to produce pairwise  $F_{ST}$  similar to that for  $A = \text{Adygei}$ ,  $B = \text{French}$ ,  $X = \text{Uygur}$ ,  $C = \text{Han}$  and  $O = \text{Yoruba}$ . The baseline simulations correspond to  $n = 20$  samples from each population; SNPs ascertained as heterozygous in a single individual from the outgroup  $O$ ; and a mixture proportion of  $\alpha = 0.47$ . Times are in generations with the subscript indicating the populations derived from the split:  $t_{\text{admix}} = 40$ ,  $t_{BB'} = 240$ ,  $t_{ABB'} = 400$ ,  $t_{CC'} = 280$ ,  $t_{ABB'} = 400$ ,  $t_{ABB'CC'} = 1,200$ ,  $t_O = 2,400$ . The diploid population sizes are indicated by a subscript corresponding to the population to which they are ancestral in Figure 4 and are:  $N_A = 50,000$ ,  $N_B = 12,000$ ,  $N_{B'} = 10,000$ ,  $N_{BB'} = 12,000$ ,  $N_C = 25,000$ ,  $N_{C'} = 10,000$ ,  $N_{CC'} = 3,300$ ,  $N_O = 80,000$ ,  $N_{ABB'} = 7,000$ ,  $N_{ABB'CC'} = 2,500$ ,  $N_{ABB'CC'O} = 10,000$ . All simulations involved  $10^6$  replicates except for the run involving 2 samples (a single heterozygous individual) from each population, where we increased this to  $10^7$  replicates to accommodate the noisier results.

**Admixture graph fitting:** We next describe *qpGraph*, our tool for building a model of population relationships from  $f$ -statistics. We first remark that given  $n$  populations  $P_1, P_2, \dots, P_n$ , then

1. the  $f$ -statistics ( $f_2, f_3$  and  $f_4$ ) span a linear space  $V_F$  of dimension  $\binom{n}{2}$ ,
2. all  $f$ -statistics can be found as linear sums of statistics  $f_2(P_i; P_j) 1 \leq i < j$ , and
3. fix a population (say  $P_1$ ). Then all  $f$ -statistics can be found as linear sums of statistics  $f_3(P_1; P_i, P_j)$ ,  $f_2(P_1, P_i) 1 < i < j$ .

These statements are true, both for the theoretical  $F$ -values, and for our  $f$ -statistics, at least when we have no missing data, so that for all populations our  $f$ -statistics are computed on the same set of markers.

Requirements 2 and 3, above, describe bases for the vector space  $V_F$ . We usually find the basis of 3 to be the most convenient computationally. More detail can be found in Reich *et al.* (2009, Supplement paragraph 2.3).

Thus choose a basis. From genotype data we can calculate as follows:

1.  $f$ -statistics on the basis. Call the resulting  $\binom{n}{2}$  long vector  $\mathbf{f}$ .
2. An estimated error covariance  $Q$  of  $\mathbf{f}$  using the weighted block jackknife (Busing *et al.* 1999).

Now, given a graph topology, as well as graph parameters (edge values and admixture weights), we can calculate  $\mathbf{g}$ , the expected value of  $\mathbf{f}$ .

A natural score function is

$$S_1(\mathbf{g}) = -\frac{1}{2}(\mathbf{g}-\mathbf{f})'Q^{-1}(\mathbf{g}-\mathbf{f}), \quad (6)$$

an approximate log-likelihood. Note that nonindependence of the SNPs is taken into account by the jackknife. A technical problem is that for  $n$  large our estimate  $Q$  of the error covariance is not stable. In particular, the smallest eigenvalue of  $Q$  may be unreasonably small. This is a common issue in multivariate statistics. Our program *qpGraph* allows a least-squares option with a score function

$$S_2(\mathbf{g}) = -\frac{1}{2} \sum_i \frac{(\mathbf{g}_i - \mathbf{f}_i)^2}{(Q_{ii} + \lambda)}, \quad (7)$$

where  $\lambda$  is a small constant introduced to avoid numerical problems. The score  $S_2$  is not basis independent, but in practice seems robust.

Maximizing  $S_1$  or  $S_2$  is straightforward, at least if  $n$  is moderate, which is the only case in which we recommend using *qpGraph*. We note that given the admixture weights, both score functions  $S_1, S_2$  are quadratic in the edge lengths, and thus can be maximized using linear algebra. This reduces the maximization to the choice of admixture weights. We use the commercial routine *nag\_opt\_simplex* from the Numerical Algorithms Group (<http://www.nag.com/numeric/cl/manual/pdf/e04/e04ccc.pdf>), which has an efficient implementation of least squares. Users of *qpGraph* will need to have access to *nag*, or substitute an equivalent subroutine.

### Interpretation and limitations of qpGraph

1. A major use of *qpGraph* is to show that a hypothesized phylogeny must be incorrect. This generalizes our *D*-statistic test, which is testing a simple tree on four populations.
2. After fitting parameters, study of which *f*-statistics fit poorly can lead to insights as to how the model must be wrong.
3. Overfitting can be a problem, especially if we hypothesize many admixing events, but only have data for a few populations.

### Simulations validate the performance of qpGraph

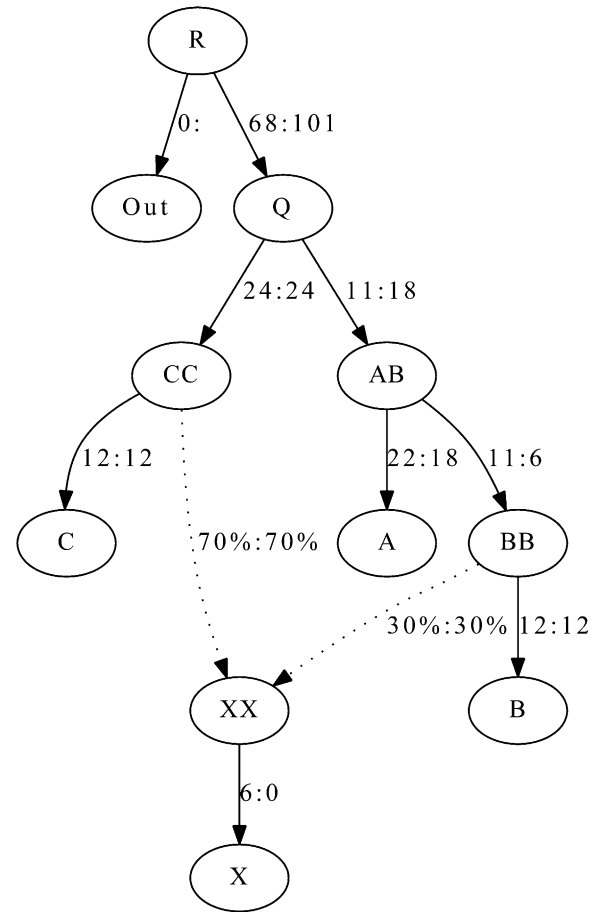
We show in Figure 5 an example in which we simulated a demography with five observed populations *Out*, *A*, *B*, *C*, and *X* and one admixture event. We simulated 50,000 unlinked SNPs, ascertained as heterozygous in a single diploid individual from the outgroup *Out*. Sample sizes were 50 in all populations and the historical population sizes were all taken to be 10,000. We show that we can accurately recover the drift lengths and admixture proportions using *qpGraph*.

**Rolloff:** Our fifth technique, rolloff, studies the decay of admixture linkage disequilibrium with distance to infer the date of admixture. Importantly, we do *not* consider multi-marker haplotypes, but instead study the joint allelic distribution at pairs of markers, where the markers are stratified into bins by genetic distance. This method was first introduced in Moorjani *et al.* (2011) where it was used to infer the date of sub-Saharan African gene flow into southern Europeans, Levantines, and Jews.

Suppose we have an admixed population and for simplicity assume that the population is homogeneous (which usually implies that the admixture is not very recent).

Let us also assume that admixture occurred over a very short time span (pulse admixture model), and since then our admixed (target) population has not experienced further large-scale immigration from the source populations. Call the two admixing (ancestral) populations *A*, *B*. Consider two alleles on a chromosome in an admixed individual at loci that are a distance *d* apart. Then *n* generations after admixture, with probability  $e^{-nd}$  the two alleles belonged, at the admixing time, to a single chromosome.

Suppose we have a weight function *w* at each SNP that is positive when the variant allele has a higher frequency in population *A* than in *B* and negative in the reverse situation. For each SNP *s*, let *w*(*s*) be the weight for SNP *s*. For every pair of SNPs *s*<sub>1</sub>, *s*<sub>2</sub>, we compute an LD-based score *z*(*s*<sub>1</sub>, *s*<sub>2</sub>) which is positive if the two variant alleles are in linkage disequilibrium; that is, they appear on the same chromosome more often than would be expected assuming independence. For diploid unphased data, which is what we have here, we simply let *v*<sub>1</sub>, *v*<sub>2</sub> be the vectors of genotype counts of the variant allele, dropping any samples with missing data. Let *m* be the number of samples in which neither



**Figure 5** Admixture graph fitting: We show an admixture graph fitted by *qpGraph* for simulated data. We simulated 50,000 unlinked SNPs ascertained as heterozygous in a single diploid individual from the outgroup *Out*. Sample sizes were 50 in all populations and the historical population sizes were all taken to be 10,000. The true values of parameters are before the colon and the estimated values afterward. Mixture proportions are given as percentages, and branch lengths are given in units of  $F_{st}$  (before the colon) and  $f_2$  values (after).  $F_2$  and  $F_{st}$  are multiplied by 1000. The fitted admixture weights are exact, up to the resolution shown, while the match of branch lengths to the truth is rather approximate.

*s*<sub>1</sub> or *s*<sub>2</sub> has missing data. Let  $\rho$  be the Pearson correlation between *v*<sub>1</sub>, *v*<sub>2</sub>. We apply a small refinement, insisting that  $m \geq 4$  and clipping  $\rho$  to the interval  $[-0.9, 0.9]$ . Then we use Fisher's *z*-transformation,

$$z = \frac{\sqrt{m-3}}{2} \log\left(\frac{1+\rho}{1-\rho}\right),$$

which is known to improve the tail behavior of *z*. In practice this refinement makes little difference to our results.

Now we form a correlation between our *z*-scores and the weight function. Explicitly, for a bin-width *x*, define the “bin” *S*(*d*), *d* = *x*, 2*x*, 3*x*, ... by the set of SNP pairs (*s*<sub>1</sub>, *s*<sub>2</sub>), where

$$S(d) = \{(s_1, s_2) | d - x < u_2 - u_1 \leq d\},$$

where *u*<sub>*i*</sub> is the genetic position of SNP *s*<sub>*i*</sub>.

Then we define  $A(d)$  to be the correlation coefficient

$$A(d) = \frac{\sum_{s_1, s_2 \in \mathcal{S}(d)} w(s_1)w(s_2)z(s_1, s_2)}{\left[ \sum_{s_1, s_2 \in \mathcal{S}(d)} (w(s_1)w(s_2))^2 \sum_{s_1, s_2 \in \mathcal{S}(d)} (z(s_1, s_2))^2 \right]^{1/2}} \quad (8)$$

Here in both numerator and denominator we sum over pairs of SNPs approximately  $d$  units apart (counting SNP pairs into discrete bins). In this study, we set a bin size of 0.1 cM in all our examples. In practice, different choices of bin sizes only qualitatively affect the results (Moorjani *et al.* 2011).

Having computed  $A(d)$  over a suitable distance range, we fit

$$A(d) \approx A_0 e^{-nd} \quad (9)$$

by least squares and interpret  $n$  as an admixture date in generations. Equation 9 follows because a recombination event on a chromosome since admixture decorrelates the alleles at the two SNPs being considered, and  $e^{-nd}$  is the probability that no such event occurred. (Implicitly, we assume here that the number of recombinations over a genetic interval of  $d$  in  $n$  generations is Poisson distributed with mean  $nd$ . Because of crossover interference, this is not exact, but it is an excellent approximation for the  $d$  and  $n$  relevant here.)

By fitting a single exponential distribution to the output, we have assumed a single pulse model of admixture. However, in the case of continuous migration we can expect the recovered date to lie within the time period spanned by the start and end of the admixture events. We further discuss rolloff date estimates in the context of continuous migration in applications to real data (below). We estimate standard errors using a weighted block jackknife (Busing *et al.* 1999) where we drop one chromosome in each run.

### Choice of weight function

In many applications, we have access to two modern populations  $A, B$ , which we can regard as surrogates for the true admixing populations, and in this context we can simply use the difference of empirical frequencies of the variant allele as our weight. For example, to study the admixture in African Americans, very good surrogates for the ancestral populations are Yoruba and North Europeans. However, a strength of rolloff is that it provides unbiased dates even without access to accurate surrogates for the ancestral populations. That is, rolloff is robust to use of highly divergent populations as surrogates. In cases when the ancestrals are no longer extant or data from the ancestrals are not available, but we have access to multiple admixed populations with differing admixture proportions (as for instance happens in India (Reich *et al.* 2009), we can use the “SNP loadings” generated from principal component analysis (PCA) as appropriate weights. This also gives unbiased dates for the admixture events.

**Table 2 Performance of rolloff**

Reference populations	$F_{st}(1)$	$F_{st}(2)$	Estimated date $\pm$ SE
CEU, YRI	0.000	0.000	107 $\pm$ 4
Basque, Mandenka	0.009	0.009	106 $\pm$ 4
Druze, LWK(HapMap)	0.017	0.008	105 $\pm$ 4
Gujarati(HapMap), Maasai	0.034	0.026	107 $\pm$ 4

We simulated data for 20 admixed individuals with 20%/80% CEU and YRI admixture that occurred 100 generations ago. We ran rolloff using “reference populations” shown above that were increasing divergent from CEU ( $F_{st}(1)$ ) and YRI ( $F_{st}(2)$ ). Estimated dates are shown in generations.

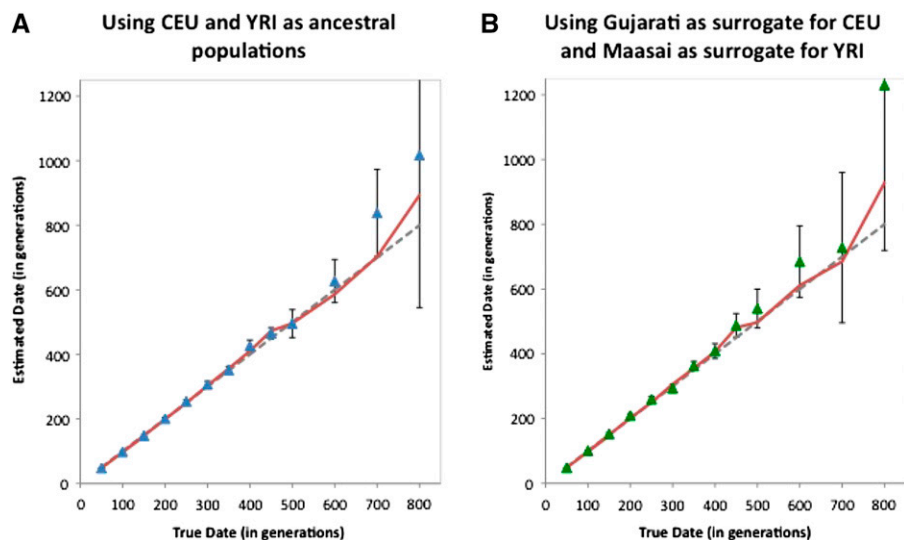
### Simulations to test rolloff

We ran three sets of simulations. The goals of these simulations were

1. to access the accuracy of the estimated dates, in cases for which data from accurate ancestral populations are not available,
2. to investigate the bias seen in Moorjani *et al.* (2011),
3. to test the effect of genetic drift that occurred after admixture.

We describe the results of each of these investigations in turn.

1. First, we report simulation results that test the robustness of inferences of dates of admixture when data from accurate ancestral populations are not available. We simulated data for 20 individuals using phased data from HapMap European Americans (CEU) and HapMap West Africans (YRI), where the mixture date was set to 100 generations before present and the proportion of European ancestry was 20%. We ran rolloff using pairs of reference populations that were increasingly divergent from the true ancestral populations used in the simulation. The results are shown in Table 2 and are better than those of the rather similar simulations in Moorjani *et al.* (2011). Here we use more SNPs (378K instead of 83K) and 20 admixed individuals rather than 10. The improved results likely reflect the fact that we are analyzing larger numbers of admixed individuals and SNPs in these simulations, which improves the accuracy of rolloff inferences by reducing sampling noise in the calculation of the Z-score. In analyzing real data, we have found that the accuracy of rolloff results improves rapidly with sample size; this feature of rolloff contrasts markedly with allele frequency correlation statistics like  $f$ -statistics where the accuracy of estimation increases only marginally as sample sizes increase above five individuals per population.
2. Second, we report simulation results investigating the bias seen in Moorjani *et al.* (2011). Moorjani *et al.* (2011) showed that low sample size and admixture proportion can cause a bias in the estimated dates. In our new simulations, we generated haplotypes for 100 individuals using phased data from HapMap CEU and HapMap YRI, where the mixture date was between 50 and 800 generations ago (Figure 6) and the proportion of European ancestry was 20%. We ran rolloff with two sets of reference populations:



**Figure 6** rolloff simulation results: We simulated data for 100 individuals of 20% European and 80% African ancestry, where the mixture occurred between 50 and 800 generations ago. Phased data from HapMap3 CEU and YRI populations was used for the simulations. We performed rolloff analysis using CEU and YRI (A) and using Gujarati and Maasai (B) as reference populations. We plot the true date of mixture (dotted line) against the estimated date computed by rolloff (points in blue A and green B). Standard errors were calculated using the weighted block jackknife. To test the bias in the estimated dates, we repeated each simulation 10 times. The estimated date based on the 10 simulations is shown in red.

- (1) the true ancestral populations (CEU and YRI) and (2) the divergent populations Gujarati ( $F_{st}(\text{CEU}, \text{Gujarati}) = 0.03$  and Maasai ( $F_{st}(\text{YRI}, \text{Maasai}) = 0.03$ ). We show the results for one run and the mean date from each group of 10 runs in Figures 6, A and B. These results show no important bias, and the date estimates, even in the more difficult case where we used Gujarati and Maasai as assumed ancestrals, are tightly clustered near the “truth” up to 500 generations (around 15,000 years). This shows that the bias is removed with larger sample sizes.
3. The simulations reported above sample haplotypes without replacement, effectively removing the impact of genetic drift after admixture. To study the effect of drift post-dating admixture, we performed simulations using the MaCS coalescent simulator (Chen *et al.* 2009). We simulated data for one chromosome (100 Mb) for three populations (say, A, B, and C). We set the effective population size ( $N_e$ ) for all populations to 12,500, the mutation rate to  $2 \times 10^{-8}$ /bp/generation, and the recombination rate to  $1.0 \times 10^{-8}$ /bp/generation. Consider the phylogeny in Figure 1C. *G* is an admixed population that has 80%/20% ancestry from *E* and *F*, with an admixture time (*t*) set to be 30, 100, or 200 generations before the present. Populations A, B, C are formed by drift from *E*, *F*, *G*, respectively.  $F_{st}(A, B) = 0.16$  (similar to that of  $F_{st}(\text{YRI}, \text{CEU})$ ). We performed rolloff analysis with C as the target ( $n = 30$ ) and A and B as the reference populations. We estimated the standard error using a weighted block jackknife where the block size was set to 10 cM. The estimated dates of admixture were  $28 \pm 4$ ,  $97 \pm 10$ , and  $212 \pm 19$  corresponding the true admixture dates of 30, 100, and 200 generations, respectively. This shows that the estimated dates are not measurably affected by genetic drift post-dating the admixture event.

### A SNP array designed for population genetics

We conclude our presentation of our methods by describing a new experimental resource and publicly available data set

that we have generated for facilitating studies of human population history and that we use in many of the applications that follow.

For studies that aim to fit models of human history to genetic data, it is highly desirable to have an exact record of how polymorphisms were chosen. Unfortunately, conventional SNP arrays developed for medical genetics have a complex ascertainment process that is nearly impossible to reconstruct and model (but see Wollstein *et al.* 2010). While the methods reported in our study are robust in theory and also in simulation to a range of strategies for how polymorphisms were ascertained (Table 1), we nevertheless wished to empirically validate our findings on a data set without such uncertainties.

Here, we report on a novel SNP array that we developed that is now released as the *Affymetrix Human Origins* array. This includes 13 panels of SNPs, each ascertained in a rigorously documented way that is described in File S1, allowing users to choose the one most useful for a particular analysis. The first 12 are based on a strategy used in Keinan *et al.* (2007), discovering SNPs as heterozygotes in a single individual of known ancestry for whom sequence data are available (from Green *et al.* 2010; Reich *et al.* 2010) and then confirming the site as heterozygous with a different assay. After the validation steps described in File S1 (which serves as technical documentation for the new SNP array), we had the following number of SNPs from each panel: San, 163,313; Yoruba, 124,115; French, 111,970; Han, 78,253; Papuan (two panels), 48,531 and 12,117; Cambodian, 16,987; Bougainville, 14,988; Sardinian, 12,922; Mbuti, 12,162; Mongolian, 10,757; Karitiana, 2,634. The 13th ascertainment consisted of 151,435 SNPs where a randomly chosen San allele was derived (different from the reference Chimpanzee allele) and a randomly chosen Denisova allele (Reich *et al.* 2010) was ancestral (same as chimpanzee). The array was designed so that all sites from panels 1–13 had data from chimpanzee as well as from Vindija Neandertals and Denisova, but the values of the Neandertal and Denisova alleles were not used for ascertainment (except for the 13th ascertainment).

Throughout the design process, we avoided sources of bias that could cause inferences to be affected by genetic data from human samples other than the discovery individual. Our identification of candidate SNPs was carried out entirely using sequencing reads mapped to the chimpanzee genome (*PanTro2*), so that we were not biased by the ancestry of the human reference sequence. In addition, we designed assays blinded to prior information on the positions of polymorphisms and did not take advantage of prior work that Affymetrix had done to optimize assays for SNPs already reported in databases. After initial testing of 1,353,671 SNPs on two screening arrays, we filtered to a final set of 542,399 SNPs that passed all quality-control criteria. We also added a set of 84,044 “compatibility SNPs” that were chosen to have a high overlap with SNPs previously included on standard Affymetrix and Illumina arrays, to facilitate coanalysis with data collected on other SNP arrays. The final array contains 629,443 unique and validated SNPs, and its technical details are described in [File S1](#).

We successfully genotyped the array in 934 samples from the HGDP and made the data publicly available on August 12, 2011, at [ftp://ftp.cephb.fr/hgdp\\_supp10/](ftp://ftp.cephb.fr/hgdp_supp10/). The present study analyzes a curated version of this data set in which we have used principal component analysis (Patterson *et al.* 2006) to remove samples that are outliers relative to others from their same populations; 828 samples remained after this procedure. This curated data set is available for download from the Reich laboratory website ([http://genetics.med.harvard.edu/reich/Reich\\_Lab/Datasets.html](http://genetics.med.harvard.edu/reich/Reich_Lab/Datasets.html)).

## Results and Discussion

### Initial application to data: South African Xhosa

The Xhosa are a South African population whose ancestors are mostly Bantu speakers from the Nguni group, although they also have some Bushman ancestors (Patterson *et al.* 2010). We first ran our three-population test with San (HGDP) (Cann *et al.* 2002) and Yoruba (HapMap) (International Hapmap 3 Consortium 2010) as source populations and 20 samples of Xhosa as the target population, a sample set already described in Patterson *et al.* (2010). We obtain an  $f_3$ -statistic of  $-0.009$  with a  $Z$ -score of  $-33.5$ , as computed with the weighted block jackknife (Busing *et al.* 1999).

Note that the admixing Bantu-speaking population is known to have been Nguni and certainly was not Nigerian Yoruba. However, as explained earlier, this is not crucial, if the actual admixing population is related genetically (Bantu speakers have an ancient origin in West Africa). If  $\alpha$  is the admixing proportion of San here, we obtain using our bounding technique with Han Chinese as an outgroup,

$$0.19 \leq \alpha \leq 0.55.$$

Although this interval is wide, it does show that the Bushmen have made a major contribution to Xhosa genomes.

### Xhosa: rolloff

We then applied our rolloff technique, using San and Yoruba as the reference populations, obtaining a very clear exponential admixture LD curve (Figure 7A). We estimate a date of  $25.3 \pm 1.1$  generations, yielding a date of about  $740 \pm 30$  years before present (YBP) assuming 29 years per generation (we also assume this generation time in the analyses that follow) (Fenner 2005).

Archeological and linguistic evidence show that the Nguni are a population that migrated south from the Great Lakes area of East Africa. For the dating of the migration we quote:

From an archaeological perspective, the first appearance of Nguni speakers can be recognized by a break in ceramic style; the Nguni style is quite different from the Early Iron Age sequence in the area. This break is dated to about AD 1200 (Huffman 2010).

More detail on Nguni migrations and archeology can be found in Huffman (2004).

Our date is slightly more recent than the dates obtained from the archeology, but very reasonable, since gene flow from the Bushmen into the Nguni plausibly continued after initial contact.

### Admixture of the Uyghur

The Uyghur are known to be historically admixed, but we wanted to try our methods on them. We analyzed a small sample (nine individuals from HGDP) (Cann *et al.* 2002). Our three-population test using French and Japanese as sources and Uyghur as target gives a  $Z$ -score of  $-76.1$ , a remarkably significant value. Exploring this a little further, we get the results shown in Table 3.

Using Han instead of Japanese is historically more plausible and statistically not significantly different. Our bounding methods suggest that the West Eurasian admixture  $\alpha$  is in the range

$$0.452 \leq \alpha \leq 0.525.$$

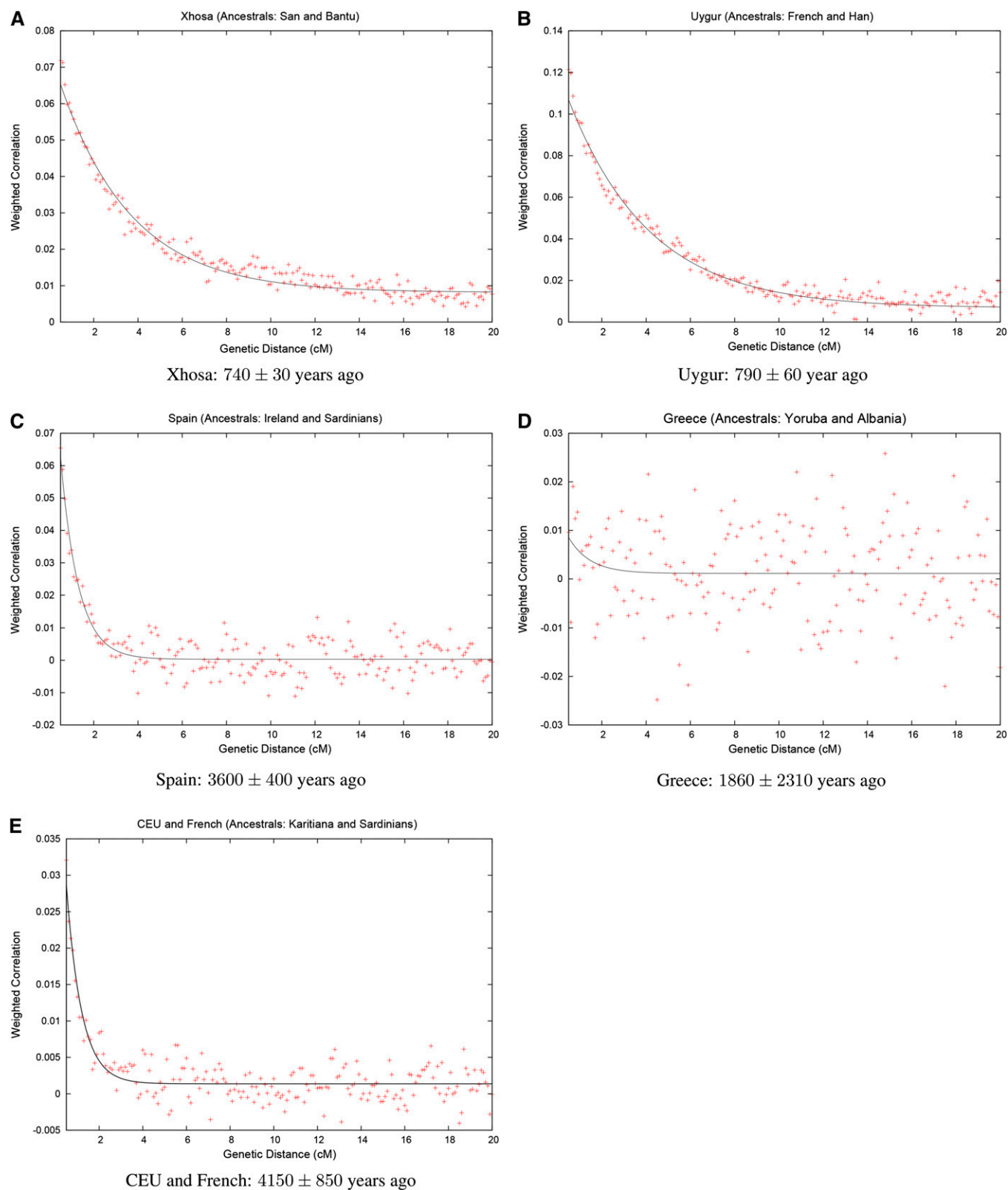
We used French and Han for the source populations here. Russian as a source is significantly weaker than French. We believe that the likely reason is that our Russian samples have more gene flow from East Asia than the French samples, and this weakens the signal. We confirm this by finding that  $D(\text{Yoruba}, \text{Han}; \text{French}, \text{Russian}) = 0.192$ ,  $Z = 26.3$ . The fact that we obtain very similar statistics when we substitute a very different sub-Saharan African population (HGDP San) for Yoruba ( $D = 0.189$ ,  $Z = 23.9$ ) indicates that the gene flow does not involve an African population, and instead the findings reflect gene flow between relatives of the Han and Russians.

### Uyghur: rolloff

Applying rolloff we again get a very clear decay curve (Figure 7B). We estimate a date of  $790 \pm 60$  YBP.

Uyghur genetics has been analyzed in two articles by Xu, Jin, and colleagues (Xu *et al.* 2008; Xu and Jin 2008), using





**Figure 7** rolloff analysis of real data: We applied rolloff to compute admixture LD between all pairs of markers in each admixed population. We plot the correlation as a function of genetic distance for (A) Xhosa, (B) Uygur, (C) Spain, (D) Greece, and (E) CEU and French. The title of each includes information about the reference populations that were used for the analysis. We fit an exponential distribution to the output of rolloff to estimate the date of the mixture (estimated dates  $\pm$ SE shown in years). We do not show inter-SNP intervals of  $<0.5$  cM as we have found that at this distance admixture LD begins to be confounded by background LD.

**Table 3**  $f_3(\text{Uygur}; A, B)$ 

Source populations	$f_3$	Z
French, Japanese	−0.0255	−76.109
French, Han	−0.0254	−77.185
Russian, Japanese	−0.0216	−68.232
Russian, Han	−0.0217	−68.486

several sets of samples, one of which is the same set of HGDP samples we analyze here. Xu and Jin, primarily using ancestry informative markers (AIMs), estimate West Eurasian admixture proportions of ~50%, in agreement with our analysis, but also an admixture date estimate using STRUCTURE 2.0 (Falush *et al.* 2003) of more than 100 generations that is substantially older than ours.

Why are the admixture dates that we obtain so much more recent than those suggested by Xu and Jin? We suspect that STRUCTURE 2.0 systematically overestimates the admixture date, when the reference populations (source populations for the admixture) are not close to the true populations, so that the assumed distribution of haplotypes is in error. It has been suggested (Mackerras 1972) that the West Eurasian component was Tocharian, an ancient Indo-European-speaking population, whose genetics are essentially unknown. Xu and Jin used 60 European American (HapMap CEU) samples to model the European component in the Uygur, and if the admixture is indeed related to the Tocharians it is plausible that they were substantially genetically drifted relative to the CEU, providing a potential explanation for the discrepancy.

Our date of ~800 years before present is not in conformity with Mackerras(1972), who places the admixture in the eighth century of the common era. Our date though is rather precisely in accordance with the rise of the Mongols under Genghis Khan (1206–1368), a turbulent time in the region that the Uygur inhabit. Could there be multiple admixture events and we are primarily dating the most recent?

### Northern European gene flow into Spain

While investigating the genetic history of Spain, we discovered an interesting signal of admixture involving Sardinia and northern Europe. We made a data set by merging genotypes from samples from the population reference sample (POPRES) (Nelson *et al.* 2008), HGDP (Li *et al.* 2008), and HapMap Phase 3 (International Hapmap 3 Consortium 2010). We ran our three-population test on triples of populations using Spain as a target (admixed population). We had 137 Spanish individuals in our sample. With Sardinian fixed as a source, we find a clear signal using almost any population from northern Europe. Table 4 gives the top  $f_3$ -statistics with corresponding Z-scores. The high score for the Russian and Adygei is likely to be partially confounded with the effect discussed in the section on flow from Asia into Europe (below).

A geographical structure is clear, with the largest magnitude  $f_3$ -statistics seen for source populations that are northern European or Slavic. The Z-score is unsurprisingly more significant for populations with a larger sample size. (Note

**Table 4** Three-population test results showing northern European gene flow into Spain

X (data set)	Sample size	$f_3(\text{Sardinian}, X; \text{Spain})$	Z-score
Russian (H)	25	−0.0025	−22.90
Norway	3	−0.0021	−9.49
Ireland	62	−0.0020	−24.31
Poland	22	−0.0019	−18.88
Sweden	11	−0.0018	−13.21
Orcadian (H)	15	−0.0018	−14.59
Scotland	5	−0.0017	−10.01
Russia	6	−0.0016	−9.82
UK	388	−0.0015	−28.21
CEU (HapMap)	113	−0.0015	−21.79
Netherlands	17	−0.0014	−12.45
Germany	75	−0.0013	−19.36
Czech	11	−0.0012	−9.33
Hungary	19	−0.0012	−11.98
Belgium	43	−0.0010	−13.76
Adygei (H)	17	−0.0010	−7.44
Austria	14	−0.0009	−7.89
Bosnia	9	−0.0008	−5.68
Croatia	8	−0.0007	−5.33
Swiss-German	84	−0.0007	−11.67
French (H)	28	−0.0005	−6.33
Swiss-French	760	−0.0005	−11.77
Switzerland	168	−0.0005	−9.60
France	92	−0.0004	−8.07
Romania	14	−0.0004	−3.62
Serbia	3	−0.0004	−1.75
Basque (H)	24	−0.0001	−1.08
Portugal	134	0.0001	2.15
Macedonia	4	0.0003	1.60
Swiss-Italian	13	0.0004	3.11
Albania	3	0.0004	1.75
Greece	7	0.0006	4.27
Tuscan (H)	8	0.0009	5.88
Italian (H)	12	0.0009	7.86
Italy	225	0.0009	16.58
Cyprus	4	0.0014	6.56

Here the CEU are from HapMap3, and the HGDP populations are indicated by (H) in parentheses.

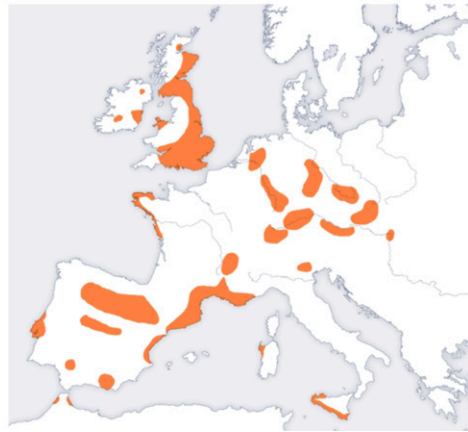
that positive Z-scores are not meaningful here.) We were concerned that the Slavic scores might be confounded by a central Asian component and therefore decided to concentrate our attention on Ireland as a surrogate for the ancestral population as they have a substantial sample size ( $n = 62$ ).

### Spain: rolloff

We applied rolloff to Spain using Ireland and Sardinians as the reference populations. In Figure 7C we show a rolloff curve. The rolloff of signed LD out to about 2 cM is clear and gives an admixture age of  $3600 \pm 400$  YBP (the standard error was computed using a block jackknife with a block size of 5 cM).

We have detected here a signal of gene flow from populations related to present-day northern Europeans into Spain around 2000 B.C. We discuss a likely interpretation. At this time there was a characteristic pottery termed “bell-beakers” believed to correspond to a population spread across Iberia and northern Europe. We hypothesize that we are seeing here a genetic signal of the “Bell-Beaker culture” (Harrison





**Figure 8** Bell-Beaker culture. On the left we show some Beaker culture objects (from Bruchsal City Museum). On the right we show a map of Bell-Beaker attested sites. We are grateful to Thomas Ihle for the Bruchsal Museum photograph. It is licensed under the Creative Commons Attribution-Share Alike 3.0 Unported license, and a GNU Free documentation license. The map is public domain, licensed under a creative commons license, and adapted from a map in Harrison (1980).

1980). Initial cultural flow of the Bell-Beakers appears to have been from South to North, but the full story may be complex. Indeed one hypothesis is that after an initial expansion from Iberia there was a reverse flow back to Iberia (Czebreszuk 2003); this “reflux” model is broadly concordant with our genetic results, and if this is the correct explanation it suggests that this reverse flow may have been accompanied by substantial population movement. (See Figures 8, 9, and 10.)

It is important to point out that we are not detecting gene flow from Germanic peoples (Suevi, Vandals, Visigoths) into Spain even though it is known that they migrated into Iberia around 500 A.D. We believe such migration must have occurred, based on the historical record (and perhaps is biasing our admixture date to be too recent), but any accompanying gene flow must have occurred at a lower level than the much earlier flow we discuss.

### **An example of the outgroup case**

Populations closely related geographically often mix genetically, which leaves a clear signal in PCA plots. An example is that isolation-by-distance effects dominate much of the genetic patterning of Europe (Lao *et al.* 2008; Novembre *et al.* 2008). This can lead to significant  $f_3$ -statistics and is related to the *outgroup case* we have already discussed. Here is an example. We find

$$f_3(\text{Greece; Albania, YRI}) = -0.0047 \quad Z = -5.8.$$

[YRI are HapMap Yoruba Nigerians (International Hapmap 3 Consortium 2010).] Sub-Saharan populations (including HGDP San) all give a  $Z < -4.0$  when paired with Albania, and even  $f_3(\text{Greece; Albania, Papuan}) = -0.0033$  ( $Z = -3.5$ ). There may be a low level of sub-Saharan ancestry in our Greek samples, contributing to our signal, but the consistent pattern of highly significant  $f_3$ -statistics suggests that we are primarily seeing an outgroup case.

We attempted to date Albanian-related gene flow into Greece using rolloff [with HapMap Yoruba and Albanian as the source populations (Figure 7D)]. However, the technique evidently fails here. Formally we get a date of  $62 \pm 77$  generations, which is not significantly different from zero. It is

possible that the admixture is very old ( $>500$  generations) or the gene flow was continuous at a low level, and our basic rolloff model does not work well here.

### **Admixture events detected in Human Genome Diversity Panel populations**

We ran our  $f_3$ -statistic on all possible triples of populations from the HGDP, genotyped on an Illumina 650Y array (Table 5) (Rosenberg 2006; Li *et al.* 2008).

Here we show for each HGDP target population (column 3) the two-source populations with the most negative (most significant)  $f_3$ -statistic. We compute  $Z$  using the block jackknife as we did earlier and just show entries with  $Z < -4$ . We bound  $\alpha$ , the mixing coefficient involving the first source population, as

$$\alpha_L < \alpha \leq \alpha_U,$$

where  $\alpha_L$ ,  $\alpha_U$  are computed with HGDP San as outgroup using the methodology of estimating mixing proportions that we have already discussed.

In four cases indicated by an asterisk in the last column,  $\alpha_L > \alpha_R$ , suggesting that our three-population phylogeny is not feasible. We suspect (and in some cases the table itself proves) that here the admixing (source) populations are themselves admixed.

It is likely that there are other lines in our table where our source populations are admixed, but that this has not been detected by our rather coarse admixing bounds. In such situations our bounds may be misleading.

Many entries are easily interpretable, for instance the admixture of Uyghur (Xu *et al.* 2008; Xu and Jin 2008) (which we have already discussed), Hazara, Mozabite (Corander and Marttinen 2006; Li *et al.* 2008), and Maya (Mao *et al.* 2007) are historically attested. The entry for Bantu-SouthAfrica is likely detecting the same phenomenon that we already discussed in connection with the Xhosa.

However, there is much of additional interest here. Note, for example, the entry for Tu, a people with a complex history and clearly with both East Asian and West Eurasian ancestry. It is important to realize that the finding here by no means

implies that the target population is admixed from the two given source populations. For example, in the second line, we do not believe that Japanese, or modern Italians, have contributed genes to the Hazara. Instead one should interpret this line as meaning that an East Asian population related genetically to a population ancestral to the Japanese has admixed with a West Eurasian population. As another example, the most negative  $f_3$ -statistic for the Maya arises when we use as source populations Mozabite (north African) and Surui (an indigenous population of South America in whom we have detected no post-Colombian gene flow). The Mozabites are themselves admixed, with sub-Saharan and West Eurasian gene flow. We think that the Maya samples have three-way admixture (European, West African, and Native American) and the incorrect two-way admixture model is simply doing the best it can (Table 5).

### Insensitivity to the ascertainment of polymorphisms

In the *Materials and Methods* section we described a novel SNP array with known ascertainment that we developed specifically for population genetics (now available as the Affymetrix Human Origins array). The array contains SNPs ascertained in 13 different ways, 12 of which involved ascer-

taining a heterozygote in a single individual of known ancestry from the HGDP. We genotyped 934 unrelated individuals from the HGDP (Cann *et al.* 2002) and here report the value of  $f_3$ -statistics on either SNPs ascertained as a heterozygote in a single HGDP San individual, or at SNPs ascertained in a single Han Chinese (Table 6). We show Z-statistics for these two ascertainment in the last two columns. The number of SNPs used is reduced relative to the 644,247 analyzed in Li *et al.* (2008); we had 124,440 SNPs for the first ascertainment and 59,251 for the second ascertainment, after removing SNPs at hypermutable CpG dinucleotides. Thus, we expect standard errors on  $f_3$  to be larger and the Z-scores to be smaller, as we observe. The correlation coefficient between the Z-scores for the 2008 data ( $Z_{2008}$ ) and our newly ascertained data are in each case  $\sim 0.99$ . We were concerned that this correlation coefficient might be inflated by the very large Z-statistics for some populations, such as the Hazara and Uygur, but the correlation coefficients remain very large if we divide the table into two halves and analyze separately the most significant and least significant entries.

Ascertainment on a *San* heterozygote or a *Han* heterozygote are very different phylogenetically, and the *San* are

**Table 5** Three-population test in HGDP

Source1	Source2	Target	$f_3$	Z-score	$\alpha_L$	$\alpha_U$	$Z_{San}$	$Z_{Han}$	$\alpha_L > \alpha_R$
Japanese	Italian	Uygur	-0.0259	-74.79	0.484	0.573	-46.08	-42.31	
Japanese	Italian	Hazara	-0.0230	-74.05	0.46	0.615	-45.19	-42.22	
Yoruba	Sardinian	Mozabite	-0.0211	-56.95	0.288	0.304	-40.65	-31.16	
Mozabite	Surui	Maya	-0.0149	-19.67	0.165	0.408	-11.51	-9.40	
Yoruba	San	Bantu-SA	-0.0107	-31.39	0.677	0.839	-24.67	-16.70	
Yoruba	Sardinian	Palestinian	-0.0107	-36.70	0.07	0.157	-25.64	-18.35	
Yoruba	Sardinian	Bedouin	-0.0104	-33.73	0.07	0.185	-23.37	-14.24	
Druze	Yi	Burusho	-0.0090	-27.62	0.558	0.731	-15.94	-13.59	
Sardinian	Karitiana	Russian	-0.0086	-20.68	0.694	0.923	-10.07	-10.98	
Druze	Karitiana	Pathan	-0.0084	-22.25	0.547	0.922	-10.68	-9.37	
Han	Orcadian	Tu	-0.0076	-20.64	0.875	0.926	-12.38	-8.98	
Mbuti	Orcadian	Makrani	-0.0076	-19.56	0.038	0.151	-11.87	-6.61	
Han	Orcadian	Mongola	-0.0075	-19.21	0.879	0.916	-12.63	-8.16	
Han	French	Xibo	-0.0069	-16.92	0.888	0.922	-9.52	-8.19	
Druze	Dai	Sindhi	-0.0067	-21.99	0.467	0.877	-12.25	-8.40	
Sardinian	Karitiana	French	-0.0060	-18.36	0.816	0.964	-9.55	-9.33	
Dai	Italian	Cambodian	-0.0060	-13.16	0.846	0.928	-6.78	-6.43	
Sardinian	Karitiana	Adygei	-0.0057	-13.03	0.635	0.956	-5.60	-5.59	
Biaka	Sardinian	Bantu-Kenya	-0.0054	-13.42	0.405	0.834	-9.65	-7.15	
Sardinian	Karitiana	Tuscan	-0.0052	-11.26	0.803	0.962	-5.12	-4.76	
Sardinian	Pima	Italian	-0.0045	-12.48	0.84	0.97	-7.48	-5.66	
Druze	Karitiana	Balochi	-0.0044	-11.58	0.483	0.96	-6.96	-6.30	
Daur	Dai	Han	-0.0026	-13.20	0.664	0.26	-7.89	-6.31	*
Han	Orcadian	Han-NChina	-0.0025	-7.09	0.958	0.97	-4.16	-2.74	
Han	Yakut	Daur	-0.0025	-9.05	0.6	0.588	-6.91	-5.78	*
Druze	Karitiana	Brahui	-0.0025	-6.43	0.47	0.964	-2.23	-2.41	
Hezhen	Dai	Tujia	-0.0021	-6.97	0.452	0.39	-4.36	-3.94	*
Sardinian	Karitiana	Orcadian	-0.0019	-4.31	0.803	0.952	-2.18	-3.24	
She	Yakut	Oroqen	-0.0017	-5.13	0.422	0.296	-4.99	-2.44	*

This table only lists the most significantly negative  $f_3$ -statistics observed in HGDP samples. For each target population, we loop over all possible pairs of source populations, and report the pair that produces the most negative  $f_3$ -statistic. Here we only print results for target populations for which the most negative  $f_3$ -statistic is significant after correcting for multiple hypothesis testing; that is, the Z-score is more than 4 standard errors below zero. For the line with Bantu-SA as target, we used HGDP Han as an outgroup. In four cases indicated by an asterisk in the last column, the lower bound on the admixture proportion  $\alpha_L$  is greater than the upper bound  $\alpha_R$ , suggesting that our proposed three-population phylogeny is not feasible. We suspect that here the admixing (source) populations are themselves admixed. The 2 Z-score columns are with San and Han het ascertainment respectively.

unlikely to have been used in the construction of the 2008 SNP panel, so the consistency of findings for these distinct ascertainment processes provides empirical evidence, confirming our expectations from theory and findings from simulation (Table 1) that the SNP ascertainment process does not have a substantial effect on inferences of admixture from the  $f_3$ -statistics (Table 6).

### **Evidence for Northeast Asian-related genetic material in Europe**

We single out from Table 5 the score for French arising as an admixture of Karitiana, an indigenous population from Brazil, and Sardinians. The Z-score of  $-18.4$  is unambiguously statistically significant. We do not of course think that there has been substantial gene flow back into Europe from Amazonia.

The only plausible explanation we can see for our signal of admixture into the French is that an ancient northern Eurasian population contributed genetic material to both the ancestral population of the Americas and the ancestral population of northern Europe. This was quite surprising to us, and in the remainder of the article this is the effect we discuss.

We are not dealing here with the *outgroup case*, where the effect is simply caused by Sardinian-related gene flow into the French. If that were the case, then we would expect to see that (French, Sardinian) are approximately a clade with respect to sub-Saharan Africa and Native Americans. There is some modest level of sub-Saharan (probably West African related) gene flow from Africa into Sardinia as is shown by analyses in Moorjani *et al.* (2011), but no evidence for gene flow from the San (Bushmen), which is indeed historically most unlikely. But if we compute  $D(\text{San}, \text{Karitiana}, \text{French}, \text{Sardinian})$  we obtain a value of  $-0.0178$  and a Z-score of  $-18.1$ . Thus we have here gene flow “related” to South America into mainland Europe to a greater extent than into Sardinia.

### **Further confirmation**

We merged two SNP array data sets that included data from Europeans and other relevant populations: POPRES (Nelson *et al.* 2008) and HGDP (Li *et al.* 2008). We considered only populations with a sample size of at least 10.

We considered European populations with Sardinian and Karitiana as sources and computed the statistic  $f_3(X; \text{Karitian}, \text{Sardinian})$ , where  $X$  is various European populations. We also added Druze, as a representative population of the Middle East (Table 7). The effect is pervasive across Europe, with nearly all populations showing a highly significant effect. Orcadians and Cyprus are island populations with known island-specific founder events that could plausibly mask admixture signals produced by the three-population test, so the absence of the signal in these populations does not provide compelling evidence that they are not admixed. Our Cypriot samples are also likely to have some proportion of Levantine ancestry (like the Druze) that does not seem to be affected by whatever historical events are driving our negative  $f_3$ -statistic. We can use any Central American or South American population to demonstrate this effect, in place of the Karitiana.

**Table 6 Correlation of Z-scores with distinct ascertainments**

Selected Z	Correlation $Z_{2008}, Z_{\text{San}}$	Correlation $Z_{2008}, Z_{\text{Han}}$
Most negative Z	0.981	0.995
Least negative Z	0.875	0.944
Overall	0.987	0.991

If we replace the Sardinian population by Basque as a source, the effect is systematically smaller, but still enormously statistically significant for most of the populations of Europe (Table 7). We note that in our three populations from mainland Italy [TSI (Hapmap Tuscans), Tuscan, and Italian] the effect essentially disappears when using Basque as a source, although it is quite clear and significant with Sardinian. This is not explored further here, but suggests that further investigation of the genetic relationships of Basque, Sardinian, and other populations of Europe might be fruitful.

### **Replication using a novel SNP array**

The signal above is overwhelmingly statistically significant but we found the effect quite surprising, especially as on common-sense grounds one would expect substantial recent gene flow from the general Spanish and French populations into the Basque, and from mainland Italy into Sardinia, which would weaken the observed effect. We wanted to exclude the possibility that what we are seeing here is an effect of how SNPs were chosen for the medical genetics array used for genotyping. Could the ascertainment be producing false-positive signals of admixture? If, for example, SNPs were chosen specifically so that the population frequencies were very different in Sardinia and northern Europe, an artifactual signal would be expected to arise. This seemed implausible but we had no way to exclude it.

We therefore returned to analysis of data from the Affymetrix Human Origins SNP array with known ascertainment. We show statistics for  $f_3(\text{French}; \text{Karitiana}, \text{Sardinian})$  for all 13 ascertainment and compare them to the statistics for the genotype data from the Illumina 650Y array developed for medical genetics (Li *et al.* 2008) (Table 8).

All our Z-scores are highly significant with a very wide range of ascertainment, except for the ascertainment consisting of finding a heterozygote in a Karitiana sample, where the number of SNPs involved is small (thus reducing power). We can safely conclude that the effect is real and that the French have a complex history.

There is evidence that the effect here is substantially stronger in northern than in southern Europe. We confirm this using the statistic  $D(\text{San}, \text{Karitiana}; \text{French}, \text{Italian})$ , which has a Z-score of  $-6.4$  on the Illumina 650Y SNP array panel and  $-3.5$  on our population genetics panel ascertained with a San heterozygote. These results show that the Karitiana are significantly more closely related to the French than to the Italians. The Italian samples here are from Bergamo, northern Italy. A likely explanation for these findings is discussed below where we apply rolloff to date this admixture event.

**Table 7**  $f_3(X; \text{Karitiana, Sardinian/Basque})$ 

<i>X</i>	Sardinian		Basque	
	$f_3$	<i>Z</i>	$f_3$	<i>Z</i>
Russian	−0.0084	−15.78	−0.0074	−15.04
Romania	−0.0070	−13.86	−0.0036	−7.05
Hungary	−0.0069	−14.65	−0.0045	−9.44
English	−0.0068	−9.20	−0.0047	−6.54
Croatia	−0.0065	−10.09	−0.0036	−5.32
Turkey	−0.0064	−7.81	−0.0021	−2.51
Russia	−0.0063	−8.56	−0.0044	−6.01
Macedonia	−0.0062	−6.70	−0.0019	−2.06
Scotland	−0.0061	−7.53	−0.0045	−5.52
Yugoslavia	−0.0058	−14.66	−0.0020	−4.68
Portugal	−0.0058	−16.84	−0.0021	−5.93
French	−0.0057	−13.81	−0.0030	−7.14
Austria	−0.0057	−11.32	−0.0029	−5.38
Sweden	−0.0057	−9.44	−0.0042	−7.49
Spain	−0.0056	−16.43	−0.0024	−7.24
France	−0.0056	−15.67	−0.0028	−7.66
Australia	−0.0056	−13.88	−0.0034	−8.89
Switzerland	−0.0055	−15.08	−0.0025	−6.98
Swiss-French	−0.0055	−15.48	−0.0025	−7.37
Czech	−0.0054	−9.39	−0.0034	−6.07
Belgium	−0.0054	−12.55	−0.0029	−6.98
Adygei	−0.0053	−9.27	−0.0020	−3.35
Bosnia	−0.0051	−8.35	−0.0019	−3.07
Swiss-German	−0.0050	−12.75	−0.0022	−5.99
Germany	−0.0049	−12.09	−0.0027	−7.03
UK	−0.0048	−12.40	−0.0031	−8.63
Swiss-Italian	−0.0048	−9.31	−0.0009	−1.76
TSI	−0.0047	−13.46	−0.0001	−0.39
CEU	−0.0047	−11.72	−0.0029	−7.79
Greece	−0.0046	−7.11	0.0002	> 0
Netherlands	−0.0043	−8.09	−0.0023	−4.51
Tuscan	−0.0043	−6.94	0.0001	> 0
Italian	−0.0043	−8.37	0.0002	> 0
Poland	−0.0040	−7.94	−0.0023	−4.69
Ireland	−0.0038	−8.10	−0.0025	−6.28
Cyprus	−0.0024	−2.53	0.0036	> 0
Orcadian	−0.0018	−3.11	−0.0002	−0.32
Druze	0.0040	> 0	0.009763	> 0

As an aside we have repeatedly assumed that back-mutations (or recurrent mutations) are not importantly affecting our results. As evidence that this assumption is reasonable, in Table 9 we compute two of our most important *D*-statistic-based tests for treeness using a variety of increasingly distant outgroups ranging from modern human outgroups to chimpanzee, gorilla, orangutan, and macaque. Results are entirely consistent across this enormous range of genetic divergence. For example, for the crucial statistic  $D(\text{Outgroup, Karitiana; Sardinian, French})$ , which demonstrates the signal of Northeast Asian-related admixture in northern Europeans, we find that *Z*-scores are consistently positive with high significance whichever outgroup is used. As a second example, when we test if the San are consistent with being an outgroup to two Eurasian populations through the statistic  $D(\text{Outgroup, San; Sardinian, Han})$  we detect no significant deviation from zero whichever outgroup is used.

**Table 8** Three-population test with 14 ascertainsments shows the robustness of the signal of Northeast Asian-related admixture in northern Europeans

$f_3(\text{French; Karitiana, Sardinian})$	<i>Z</i>	<i>N</i>	Ascertainment
−0.006	−18.36	586414	Li <i>et al.</i> (2008)
−0.007	−11.49	107525	French
−0.006	−9.06	69626	Han
−0.006	−8.19	40725	Papuan
−0.005	−9.43	92566	San
−0.006	−9.92	82416	Yoruba
−0.006	−5.27	7193	MbutiPygmy
−0.003	−1.91	2396	Karitiana
−0.004	−4.33	12400	Sardinian
−0.006	−5.84	12963	Melanesian
−0.006	−5.91	15171	Cambodian
−0.006	−5.48	9655	Mongola
−0.007	−6.55	10166	Papuan
−0.006	−11.55	83385	Denisova/San

Two different Papuan samples were used for ascertainment. The last column indicates the ascertainment used, while the column headed *N* is the number of SNPs contributing to  $f_3$ , so that SNPs monomorphic in all samples of (Karitiana, Sardinian, French) are not counted.

### Siberian populations

We obtained Illumina SNP array data from Hancock *et al.* (2011) from the Naukan and Chukchi, Siberian peoples who live in extreme northeastern Siberia. After merging with the 2008 Illumina 650Y SNP array data on HGDP samples (Li *et al.* 2008) we obtain the  $f_3$ -statistics in Table 10.

We can assume here that we have a common admixture event to explain. Although the statistics for Chukchi are (slightly) weaker than those in the Native Americans, we obtain better bounds on the mixing coefficient  $\alpha$  of between 5% and 18%. We caution that if the Sardinians are themselves admixed with Asian ancestry although less so than other Europeans (a scenario we think is historically plausible), then we will have underestimated the Asian-related mixture proportion in Europeans.

We wanted to test if (French, Sardinian) form a clade relative to (Karitiana, Chukchi), which would, for example, be the case if the admixing population to northern Europe had a common ancestor with an ancestor of Karitiana and Chukchi. In our data set,

$$D(\text{Karitiana, Chukchi; French, Sardinian}) = 0.0040, Z = 4.9,$$

while this hypothesis predicted  $D = 0$ . Thus, we can rule out this alternative hypothesis.

One possible explanation for these findings is that the ancestral Karitiana were closer genetically to the northern Eurasian population that contributed genes to northern Europeans than are the Chukchi. The original migration into the Americas occurred at least 15,000 YBP, so there is ample time for some population inflow into the Chukchi peninsula since then. However, the Chukchi and Naukan samples show no evidence of recent west Eurasian admixture, and we specifically tested for ethnic Russian admixture, finding nothing.

**Table 9 Z-scores produce consistent inferences whatever outgroup we use**

Outgroup (O)	Yoruba	San	Chimpanzee	Gorilla	Orangutan	Macaque
<i>D</i> (O, Karitiana; Sardinian, French)	10.5	8.9	7.3	7.0	6.9	6.7
<i>D</i> (O, San; Sardinian, Han)	N/A	N/A	−1.1	−0.8	−0.5	−0.5

We carried out a rolloff analysis in which we attempted to learn about the date of the admixture events in the history of northern Europeans. We pooled samples from CEU, a population of largely northern European origin (International Hapmap 3 Consortium 2010) with HGDP French to form our target admixed population, wishing to maximize the sample size. The surrogate ancestral populations for this analysis are Karitiana and Sardinian.

The admixture date we are analyzing here is old, and to improve the performance of rolloff here and in the analysis of northern European gene flow into Spain reported above, we filtered out two regions of the genome that have substantial structural variation that is not accurately modeled by rolloff, which assumes Poisson-distributed recombination events between two alleles (Mills *et al.* 2011). The two regions we filtered out were HLA on chromosome 6 and the *p*-telomeric region on chromosome 8, which we found in practice contributed to anomalous rolloff signals in some of our analyses. Our signals should be robust to removal of small genomic regions.

In Figure 7E we show the rolloff results. The signal is clear enough, although noisy. We estimate an admixture date of  $4150 \pm 850$  YBP. Our standard errors computed using a block jackknife (block size of 5 cM) are uncomfortably large here.

However, this date must be treated with great caution. We obtained a data set from the Illumina iControl database (<http://www.illumina.com/science/icontribdb.ilmn>) of “Caucasians” and after curation have 1232 samples of European ancestry genotyped on an Illumina SNP array panel. We merged the data with the HGDP Illumina 650Y genotype data obtaining a data set with 561,268 SNPs. Applying rolloff to this sample with HGDP Karitiana and Sardinians as sources, we get a much more recent date of  $2200 \pm 762$  YBP. We think that this is not a technical problem with rolloff, but rather, it is an issue of interpretation that is a challenge for all methods for estimating dates of admixture events.

Our admixture signal is stronger in northern Europe as we showed above in the context of discussing the statistic *D* (San, Karitiana; French, Italian). It seems plausible that the initial admixture might have been exclusively in northern Europe, but since this ancient event, there has been extensive gene flow within Europe, as shown, for example, in Lao

*et al.* (2008) and Novembre *et al.* (2008). But if northern and southern Europe have differing amounts of “Asian” admixture, this intra-European flow is confounding to our analysis. The more recent gene flow between northern and southern Europe will contribute to our inferring too recent a date. Admixture into one section of a population, followed by slow mixing within the population, may be quite common in human history and will substantially complicate the dating for any genetic method.

### Interpretation in light of ancient DNA

Ancient DNA studies have documented a clean break between the genetic structure of the Mesolithic hunter-gatherers of Europe and the Neolithic first farmers who followed them. Mitochondrial analyses have shown that the first farmers in central Europe, belonging to the linear pottery culture (LBK), were genetically strongly differentiated from European hunter-gatherers (Bramanti *et al.* 2009), with an affinity to present-day Near Eastern and Anatolian populations (Haak *et al.* 2010). More recently, new insight has come from analysis of ancient nuclear DNA from three hunter-gatherers and one Neolithic farmer who lived roughly contemporaneously at about 5000 YBP in what is now Sweden (Skoglund *et al.* 2012). The farmer's DNA shows a signal of genetic relatedness to Sardinians that is not present in the hunter-gatherers who have much more relatedness to present-day northern Europeans. These findings suggest that the arrival of agriculture in Europe involved massive movements of genes (not just culture) from the Near East to Europe and that people descending from the Near Eastern migrants initially reached as far north as Sweden with little mixing with the hunter-gatherers they encountered. However, the fact that today, northern Europeans have a strong signal of admixture of these two groups, as proven by this study and consistent with the findings of (Skoglund *et al.* 2012), indicates that these two ancestral groups subsequently mixed.

Combining the ancient DNA evidence with our results, we hypothesize that agriculturalists with genetic ancestry close to modern Sardinians immigrated into all parts of Europe along with the spread of agriculture. In Sardinia, the Basque country, and perhaps other parts of southern Europe they largely replaced the indigenous Mesolithic populations, explaining why we observe no signal of admixture in

**Table 10 The signal of admixture in the French is robust to the Northeast Asian-related population that is used as the surrogate for the ancestral admixing population**

Sources; Target	$f_3$	<i>Z</i>	$\alpha_L$	$\alpha_U$	<i>N</i>
Karitiana, Sardinian; French	−0.006	−18.36	0.036	0.184	586406
Naukan, Sardinian; French	−0.005	−16.73	0.051	0.176	393216
Chukchi, Sardinian; French	−0.005	−15.92	0.056	0.174	393466

Sardinians today to the limits of our resolution. In contrast, the migrants did not replace the indigenous populations in northern Europe and instead lived side-by-side with them, admixing over time (perhaps over thousands of years). Such a scenario would explain why northern European populations today are admixed and also have a rolloff admixture date that is substantially more recent than the initial arrival of agriculture in northern Europe.

An alternative history that could produce the signal of Asian-related admixture in northern Europeans is admixture from steppe herders speaking Indo-European languages, who after domesticating the horse would have had a military and technological advantage over agriculturalists (Anthony 2007). However, this hypothesis cannot explain the ancient DNA result that northern Europeans today appear admixed between populations related to Neolithic and Mesolithic Europeans (Skoglund *et al.* 2012), and so even if the steppe hypothesis has some truth, it can explain only part of the data.

We show an admixture graph that corresponds to our hypothesis in Figure 9.

To test the predictions of our hypothesized historical scenario, we downloaded the recently published DNA sequence of the Tyrolean “Iceman” (Keller *et al.* 2012). The Iceman lived (and died) in the Tyrolean Alps close to the border of modern Austria and Italy. From isotopic analysis (Muller *et al.* 2003) he was probably born within 60 miles of the site at which he was found. To analyze the Iceman data, we applied similar filtering steps as those applied in the analysis of the Neandertal genome (Green *et al.* 2010). After filtering on map quality and sequence quality of a base as described in that study, we chose a random read covering each base of the Affymetrix Human Origins array. This produced nearly 590,000 sites for analysis.

Our *D*-statistic analysis suggests that the Iceman and the HGDP Sardinians are consistent with being a clade, providing formal support for the findings of Keller *et al.* (2012) who reported that the Iceman is close genetically to modern Sardinians based on PCA. Concretely, our test for whether they are a clade is

$$D(\text{Yoruba, Karitiana; Iceman, Sardinian}) = -0.0045, Z = -1.3. \quad (10)$$

This *D*-statistic shows no significant deviation from zero, in contrast with the highly significant evidence that the Iceman and French are not a clade:

$$D(\text{Yoruba, Karitiana; Iceman, French}) = 0.0224, Z = 6.3.$$

Our failure to detect a signal of admixture using the *D*-statistic is not due to reduced power on account of having only one sample, since when we recompute the statistic of (10) using each of the 26 French individuals in turn in place of Iceman, the *Z*-scores are all significant, ranging from  $-3.1$  to  $-8.5$ . These results imply that Iceman has less northeast Asian-related ancestry than a typical modern North European, but the data are consistent with Iceman having the same amount of northeast Asian-related ancestry as Sardinians. Further confirmation for this interpretation comes from the very similar magnitude  $f_3$ -statistics that we observe when using either Sardinians or Iceman as a source for the admixture:

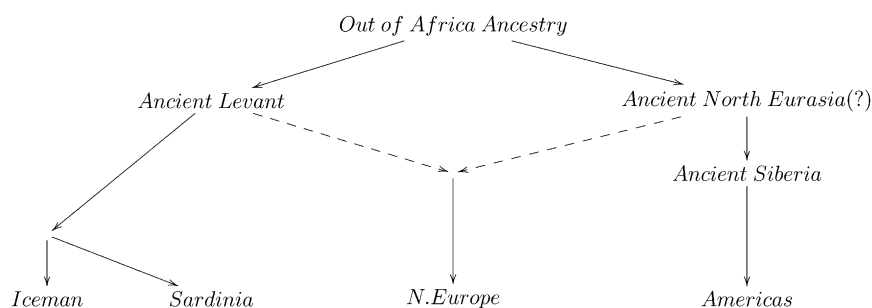
$$f_3(\text{French; Iceman, Karitiana}) = -0.007, Z = -5.8$$

$$f_3(\text{French; Sardinian, Karitiana}) = -0.006, Z = -14.8.$$

The *Z*-score for Iceman is of smaller magnitude than that for the Sardinian samples, because with a single individual we have much more sampling noise. However, the important quantity in this context is the magnitude of the  $f_3$ -statistic. Thus the Iceman harbors less northeast Asian-related genetic material than modern French, and the northeast Asian-related genetic material is not detectably different in Iceman and the HGDP Sardinians, to the limits of our resolution.

A caveat to these analyses is that the relatively poor quality and highly fragmented DNA sequence fragments from Iceman may occasionally align incorrectly to the reference human genome sequence (and in particular, may do so at a rate higher than that of the comparison data from present-day humans), which could in theory bias the *D*-statistics. However, our point here is simply that to the limits of the analyses we have been able to carry out, Iceman and modern Sardinians are consistent with forming a clade, supporting the hypothesis we sketched out above.

Although the Iceman lived near where he was found, it cannot be logically excluded that his genetic ancestry was unusual for the region. For instance, his parents might have been migrants from ancient Sardinia. However, the Iceman does not carry the signal of northeast Asian ancestry that we have detected in northern Europeans, and lived at least 2000 years after the arrival of farming in Europe. If his genome was typical of the region in which he lived, the northeast Asian-related genetic material that is currently widespread in northern



**Figure 9** Northeast Asian-related admixture in northern Europe. A proposed model of population relationships that can explain some features observed in our genetic data.



Italy and southern Austria must be due to admixture events and/or migrations that occurred well after the advent of agriculture in the region, supporting the hypothesis, presented above, that Neolithic farmers of near eastern origin initially largely replaced the indigenous Mesolithic population of southern Europe and that only well afterward did they develop the signal of major admixture that they harbor today.

### **Summary of inferences about European history from our methods**

Our methods for analyzing genetic data have led to several novel inferences about history, showing the power of the approaches. In particular, we have presented evidence suggesting that the genetic history of Europe from around 5000 B.C. includes:

1. the arrival of Neolithic farmers probably from the Middle East,
2. nearly complete replacement of the indigenous Mesolithic southern European populations by Neolithic migrants and admixture between the Neolithic farmers and the indigenous Europeans in the north,
3. substantial population movement into Spain occurring around the same time as the archeologically attested Bell-Beaker phenomenon (Harrison 1980),
4. subsequent mating between peoples of neighboring regions, resulting in isolation-by-distance (Lao *et al.* 2008; Novembre *et al.* 2008). This tended to smooth out population structure that existed 4000 years ago.

Further, the populations of Sardinia and the Basque country today have been substantially less influenced by these events.

### **Software**

We release a software package, ADMIXTOOLS, that implements five methods: the three-population test,  $D$ -statistics,  $F_4$ -ratio estimation, admixture graph fitting, and rolloff. In addition, it computes lower and upper bounds on admixture proportions based on  $f_3$ -statistics. ADMIXTOOLS can be downloaded from the following URL: [http://genetics.med.harvard.edu/reich/Reich\\_Lab/Software.html](http://genetics.med.harvard.edu/reich/Reich_Lab/Software.html).

### **Data sets used**

The following data sets are used:

HapMap Phase 3 (International Hapmap 3 Consortium 2010), HGPDP genotyped on the Illumina 650K array (Li *et al.* 2008), HGPDP genotyped on the Affymetrix Human Origins array, POPRES (Nelson *et al.* 2008), Siberian data (Hancock *et al.* 2011), and Xhosa data (Patterson *et al.* 2010).

### **Acknowledgments**

We are grateful to Mark Achtman, David Anthony, Vanessa Hayes, and Mike McCormick for instructive and helpful conversations, Mark Daly for a useful technical suggestion, and Thomas Huffman for references on the history of the Nguni. Joe Felsenstein made us aware of some references we would otherwise have missed. Wolfgang Haak corrected

some of our misinterpretations of the Bell-Beaker culture and shared some valuable references. We thank Anna Di Rienzo for early access to the data of (Hancock *et al.* 2011) from peoples of Siberia. We thank Graham Coop, Rasmus Nielsen, and several anonymous referees whose reading of the manuscript allowed us to make numerous improvements and clarifications. This work was supported by U.S. National Science Foundation HOMINID grant 1032255, and by National Institutes of Health grant GM100233.

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Communicating editor: R. Nielsen



## Appendix A: Unbiased Estimates of $f$ -Statistics

Fix a marker (SNP) for now. We have populations  $A, B, C, D$  in which the variant allele frequencies are  $a', b', c', d'$ , respectively. Sample counts of the variant and reference alleles are  $n_A, n'_A$ , etc. Set

$$n_A + n'_A = s_A, \text{ etc.},$$

so that  $s_A$  is the total number of alleles observed in population  $A$ . Define  $a = n_A/s_A$ , the sample allele frequency in  $A$ , with  $b, c, d$  defined similarly. Thus  $a', b', c', d'$  are population frequencies and  $a, b, c, d$  are allele frequencies in a finite sample. We first define

$$h_A = a'(1 - a')$$

so that  $2h_A$  is the heterozygosity of population  $A$ . Set

$$\hat{h}_A = \frac{n_A n'_A}{s_A(s_A - 1)}.$$

Then  $\hat{h}_A$  is an unbiased estimator of  $h_A$ . We now can show that

$$\hat{F}_2(A, B) = (a - b)^2 - \hat{h}_A/s_A - \hat{h}_B/s_B$$

$$\hat{F}_3(C; A, B) = (c - a)(c - b) - \hat{h}_C/s_C$$

$$\hat{F}_4(A, B; C, D) = (a - b)(c - d)$$

are unbiased estimates of  $F_2(A, B)$ ,  $F_3(C; A, B)$ , and  $F_4(A, B; C, D)$ , respectively. For completeness we give estimates in the same spirit for  $F_{st}(A, B)$ . We define

$$F_{st}(A, B) = \frac{(a' - b')^2}{a'(1 - b') + b'(1 - a')},$$

which we note differs from the definition of Cavalli-Sforza in his magisterial book Cavalli-Sforza *et al.* (1994), and (at least in the case of unequal sample sizes) the definition in Weir and Cockerham (1984).

Write  $N, D$  for the numerator and denominator of the above expression. Then  $N = F_2(A, B)$ , and we have already given an unbiased estimator. We can write  $D = N + h_A + h_B$  and so an unbiased estimator for  $D$  is

$$\hat{D} = \hat{F}_2(A, B) + \hat{h}_A + \hat{h}_B.$$

This definition and these estimators were used in Reich *et al.* (2009) and are implemented in our widely used program *smartpca* Patterson *et al.* (2006). An article in preparation explores  $F_{st}$  in much greater detail.

## Appendix B: Visual Interpretation of $f$ -Statistics

The expected value of  $f$ -statistics can be computed in a visually interpretable way by writing down all the possible genetic drift paths through the admixture graph relating the populations involved in the  $f$ -statistic. For each of the statistics we compute

$F_2(A, C)$ : Overlap between the genetic drift paths  $A \rightarrow C, A \rightarrow C$

$F_3(C; A, B)$ : Overlap between the genetic drift paths  $C \rightarrow A, C \rightarrow B$

$F_4(A, E; D, C)$ : Overlap between the genetic drift paths  $A \rightarrow E, D \rightarrow C$

If there is no admixture, then the expected value of an  $f$ -statistic can be computed from the overlap of the two drift paths in the single phylogenetic tree relating the populations. If admixture occurred, the drift can take alternative paths, and we need to write down trees corresponding to each of the possible paths and weight their contribution by the probability that the drifts take that path.

There is a loose analogy here to the Feynman diagrams (Kotikov 1991a,b), used by particle physicists to perform computations about the strength of the interaction among fundamental particles such as quarks and photons. The Feynman diagrams correspond exactly to the terms of a mathematical equation (a path integral) and provide a way to compute its

value. Each corresponds to a different path by which particles can interact. By writing down all possible Feynman diagrams relating two particles (all possible ways that they can interact through intermediate particles), computing the contribution to the integral from each Feynman diagram, and combining the results, one can compute the strength of the interaction.

Figure 2 shows how this strategy can be used to obtain expected values for  $f_2$ ,  $f_3$ , and  $f_4$ -statistics. The material below is meant to be read in conjunction with that figure:

$$E[f_2(C, A)] = (c - a)(c - a).$$

The expected value of  $f_2(C, A)$  can be computed by the overlaps of the genetic drifts  $C \rightarrow A$ ,  $C \rightarrow A$  over all four possible paths in the tree with weights  $\alpha^2$ ,  $\alpha\beta$ ,  $\beta\alpha$ , and  $\beta^2$ . The expected values can be counterintuitive. For example, Neandertal gene flow into non-Africans has most probably reduced rather than increased allelic frequency differentiation between Africans and non-Africans. If  $A$  is Yoruba,  $C$  is French, and  $B$  is Neandertal, and we set  $a = 0.026$ ,  $c = 0.036$ ,  $d = 0.068$ ,  $e + f + g = 0.33$ ,  $\alpha = 0.975$  (reasonable parameter values based on previous work), then we compute the expected value of  $f_2(C, A)$  to be 0.127. Using the same equation but  $\alpha = 1$  (no Neandertal admixture), we get  $f_2 = 0.130$ :

$$E[f_3(C; A, B)] = (c - a)(c - b).$$

If population  $C$  is admixed, there is a negative term in the expected value of  $f_3(C; A, B)$ , which arises because the genetic drift paths  $C \rightarrow A$  and  $C \rightarrow B$  can take opposite directions through the deepest part of the tree. The observation of a negative value provides unambiguous evidence of population mixture in the history of population  $C$ :

$$E[f_4(A, E; D, C)] = (a - e)(d - c).$$

The expected value of  $f_4(A, E; D, C)$  can be computed from the overlap of drifts  $A \rightarrow E$  and  $D \rightarrow C$ . Here there are two possible paths for  $D \rightarrow C$ , with weights  $\alpha$  and  $\beta$ , resulting in two graphs whose expected contribution to  $f_4$  are 0 and  $-\alpha g$  so that  $E[f_4] = -\alpha g$ . Thus, by taking the ratio of the  $f_4$ -statistics for a population that is admixed and one where  $\alpha$  is equal to 1, we have an estimate of  $\alpha$ .

### Appendix C: Mathematical Analysis of $F_3$

In the article we use  $a'$  for population allele frequencies in a population  $A$  and  $a$  for sample frequencies. Here we switch notation and write  $a, b, c, \dots$ , for population frequencies in  $A, B, C, \dots$ .

We consider three populations  $A, B, C$  with a root population  $R$ , and consider  $F_3 = E[(c - a)(c - b)]$  under various ascertainment schemes.

**Theorem 1.** *Assuming that genetic drift is neutral, no backmutation, and no recurrent mutations and that  $A, B, C$  have a simple phylogeny, with no mixing events, then under the following ascertainments,*

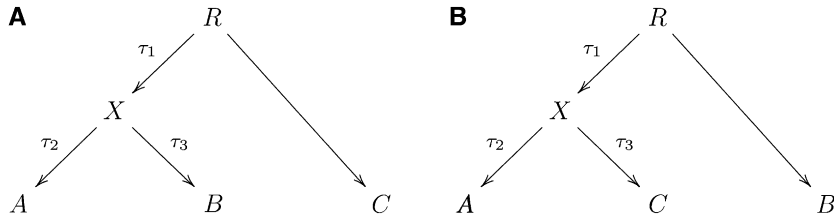
$$F_3(C; A, B) = E[(c - a)(c - b)] \geq 0,$$

1. *no ascertainment, such as in sequence data,*
2. *ascertainment in an outgroup, which split from  $R$  more remotely than  $A, B, C$ ,*
3. *ascertainment by finding a heterozygote in a single individual of  $\{A, B, C\}$ , where we also assume the population of  $R$  is in mutation-drift equilibrium so that the probability that a polymorphic derived allele with population frequency  $r \propto 1/r$  Ewens (1963).*

*Proof.* The first two cases are clear, since drift on edges of the tree rooted at  $R$  are orthogonal. This is the situation discussed at length in the main article. The case where we ascertain that a heterozygote is more complicated and our discussion involves some substantial algebra, which we carried out with Maple.

First consider the tree shown in Figure C1A. Here we show drift distances on the diffusion scale for  $R \rightarrow X, X \rightarrow A, X \rightarrow C$ . So, for example, the probability that two random alleles of  $A$  have a most recent common ancestor (MRCA) more ancient than  $X$  is  $e^{-\tau_2}$ . We let allele frequencies in  $A, B, C, X, R$  be  $a, b, c, x, r$ , respectively. If we ascertain in  $C$ , then  $E[r - a] = E[r - b] = 0$ , and  $E[(r - a)(r - b)] = E[(r - x)^2] \geq 0$ . The case of ascertainment in  $A$  is more complex: Write  $E_0$  for the expectation simply assuming  $R$  is polymorphic and in mutation-drift equilibrium. Then  $E[(c - a)(c - b)]$  under ascertainment of a heterozygote in  $A$  is given by

$$E[(c - a)(c - b)] = \frac{E_0[(c - a)(c - b)a(1 - a)]}{E_0[a(1 - a)]}. \quad (\text{A1})$$



**Figure C1** (A) Appendix C, Theorem 1. (B) Appendix C, Theorem 2.

Thus it is necessary and sufficient to show  $E_0[(c - a)(c - b)a(1 - a)] \geq 0$ :

$$\begin{aligned} E[(c - a)(c - b)] &= E[(r - c)^2] + E[(r - c)(c - b)] \\ &\quad + E[(r - c)(c - a)] + E[(r - a)(r - b)] \\ &= E[(r - c)^2] + E[(r - a)(r - b)]. \end{aligned}$$

So it is enough to prove  $E[(r - a)(r - b)] \geq 0$ . But

$$\begin{aligned} E[(r - a)(r - b)] &= E[(r - x)^2] + E[(r - x)(x - b)] \\ &\quad + E[(r - x)(x - a)] + E[(x - a)(x - b)] \\ &= E[(r - x)(x - a)]. \end{aligned}$$

Let  $K(p, q; \tau)$  be the transition function of the Wright–Fisher diffusion so that for  $0 < p, q < 1$

$$K(p, q; \tau) = P(X(0) = q | X(-\tau) = p),$$

where  $X(\tau)$  is the allele frequency at time  $\tau$  on the diffusion time scale.

We make extensive use of Kimura's theorem giving an explicit representation of  $K$ .

**Theorem 2 (Kimura 1955).**

$$K(x, y; t) = x(1 - x) \sum_{i=0}^{\infty} \frac{J_i^{1,1}(x) J_i^{1,1}(y)}{\text{Num}_i^{1,1}} e^{-\lambda(i)t}, \quad (\text{A2})$$

where  $J_i$  are explicit polynomials (Jacobi or Gegenbauer polynomials) orthogonal on the unit interval with respect to the function  $w(x) = x(1 - x)$ .  $\text{Num}_i$  are normalization constants with

$$\int_0^1 x(1 - x) J_i(x) J_j(x) dx = \delta_{ij} \text{Num}_i$$

and  $\lambda(i)$  is given by

$$\lambda(i) = \frac{(i + 1)(i + 2)}{2}. \quad (\text{A3})$$

We need to show that

$$\begin{aligned} T &= E_0[(r - x)(x - a)a(1 - a)] \\ &= \int_0^1 \int_0^1 \int_0^1 1/r K(r, x; \tau_1) K(x, a, \tau_2) (r - x)(x - a)a(1 - a) dr dx da \geq 0. \end{aligned}$$

We deal with polynomials in  $\{e^{-\tau_i} i = 1, 2, 3\}$ . To simplify the notation set,

$$u = e^{-\tau_1}$$

$$v = e^{-\tau_2}$$

$$w = e^{-\tau_3}.$$

Using Kimura's theorem and the orthogonality of Jacobi polynomials, this integral can be expressed in closed form.

We consider ascertainment of a heterozygote in  $A$ . Now calculation shows that

$$T = \frac{vu(1-u)Q}{120},$$

where  $Q = 5 + 3v^2 + u(5 + 3v^2) - 2v^2(u^2 + u^3 + u^4)$ .

Noting that  $0 \leq v, u \leq 1$ ,

$$Q \geq 5 + 3v^2 + u(5 - 3v^2) \geq 0.$$

Next consider the tree shown in Figure C1B. First suppose we ascertain a heterozygote in  $A$ ,

$$E[(c-a)(c-b)] = E[(c-x)^2] + E[(x-a)(x-r)]$$

and so we want to show

$$T = E_0[(x-a)(x-r)a(1-a)] \geq 0.$$

A similar calculation to that above shows that

$$120T = vu(1-u)(1-v)(v+1)(2u^3 + 4u^2 + 6u + 3) \geq 0,$$

as required. Next suppose we ascertain a heterozygote in  $C$ . We now want to show

$$T = E_0[(c-x)(c-r)c(1-c)] \geq 0.$$

We find

$$120T = wv(1-v)Q,$$

where

$$Q = 3(1+v) + 5u^2(1+v) - 2u^5v^2(1+v+v^2).$$

We need to show  $Q \geq 0$ . Expanding  $Q$  into monomials with coefficients  $\pm 1$  there are six negative terms, each of which can be paired with a positive term of lower degree.

This completes the proof.

Summarizing, our three-population test is rigorous if there is ascertainment in an outgroup only (or no ascertainment as in sequence data). It also is rigorous with a variety of other simple ascertainment. Further in practice, on commercial SNP arrays, highly significant false positives do not seem to arise as we show in Table 5.

## Appendix D: Simulations to Test $f$ -Statistic Methodology

To test the robustness of our  $f$ -statistic methodology, we carried out coalescent simulations of five populations related according to Figure 4, using *ms* (Hudson 2002).

Our simulations involved specifying six dates:

1.  $t_{\text{admix}}$ : Date of admixture between populations  $B'$  and  $C'$ .
2.  $t_{BB'}$ : Date of divergence of populations  $B$  and  $B'$ .
3.  $t_{CC'}$ : Date of divergence of populations  $C$  and  $C'$ .
4.  $t_{ABB'}$ : Date of divergence of population  $A$  from the  $B, B'$  clade.
5.  $t_{ABB'CC'}$ : Date of divergence of the  $A, B, B'$  and  $C, C'$  clades.
6.  $t_O$ : Date of divergence of the  $A, B, B', C, C'$  clade and the outgroup  $O$ .

We assumed that all populations were constant in size in the periods between when they split, with the following diploid sizes:

1.  $N_X$ : Size in the ancestry of population  $X$ .
2.  $N_{B'}$ : Size in the ancestry of population  $B''$ .
3.  $N_B$ : Size in the ancestry of population  $B$ .

4.  $N_{C'}$ : Size in the ancestry of population  $C'$ .
5.  $N_C$ : Size in the ancestry of population  $C$ .
6.  $N_O$ : Size in the recent ancestry of the outgroup  $O$ .
7.  $N_{BB'}$ : Size in the common ancestry of  $B$  and  $B'$ .
8.  $N_{CC'}$ : Size in the common ancestry of  $C$  and  $C'$ .
9.  $N_{ABB'}$ : Size in the common ancestry of  $A$ ,  $B$ , and  $B'$ .
10.  $N_{ABB'CC'}$ : Size in the common ancestry of  $A$ ,  $B$ ,  $B'$ ,  $C$ , and  $C'$ .
11.  $N_{ABB'CC'O}$ : Size in the common ancestry of all populations.

We picked population sizes, times, and  $F_{st}$  to approximately match empirical data for

A: Adygei, West Eurasian  
 B: French, West Eurasian  
 C: Han, East Asian  
 X: Uyghur, Admixed  
 Y: Yoruba, Outgroup

Thus, our baseline simulations correspond to a roughly plausible scenario for some of the genetic history of Eurasia, with Yoruba serving as an outgroup. We then varied parameters, as well as ascertainment of SNPs, and explored how this affected the observed values from simulation.

In Table 1 we show baseline demographic parameters, as well as several alternatives that each involved varying a single parameter compared with the baseline. Each alternate parameter set was separately assessed by simulation (including different SNP ascertainment).

Table 1 shows the results. We find that:

- $F_{st}$ -statistics change as expected depending on SNP ascertainment and demographic history.
- The consistency of  $D$ -statistics with 0 in the absence of admixture is robust to SNP ascertainment. Substantially nonzero values are observed only when the test population is admixed ( $X$ ) and not when it is unadmixed ( $B$ ).
- $f_3$ -statistics are negative when the test population is admixed ( $X$ ) except for high population-specific drift, which masks the signal as expected. Statistics are always positive when the test population is unadmixed ( $B$ ), regardless of ascertainment.

Thus, these simulations show that inferences about history based on the  $f$ -statistics are robust to ascertainment process as we argued in the main text on theoretical grounds.

# GENETICS

**Supporting Information**

<http://www.genetics.org/lookup/suppl/doi:10.1534/genetics.112.145037/-/DC1>

## **Ancient Admixture in Human History**

**Nick Patterson, Priya Moorjani, Yontao Luo, Swapan Mallick, Nadin Rohland, Yiping Zhan,  
Teri Genschoreck, Teresa Webster, and David Reich**

# File S1

## Technical details of a SNP array optimized for population genetics

Yontao Lu, Nick Patterson, Yiping Zhan, Swapan Mallick and David Reich

### Overview

One of the promises of studies of human genetic variation is to learn about human history and also to learn about natural selection.

Array genotyping of hundreds of thousands of SNPs simultaneously—using a technology that produces high fidelity data with an error rate of  $\sim 0.1\%$ —is in theory a powerful tool for these studies. However, a limitation of all SNP arrays that have been available to date is that the SNPs have been chosen in a complicated way for the purpose of medical genetics, biasing their frequencies so that it is challenging to make reliable population genetic inferences. In general, the way that SNPs have been chosen for arrays is so complicated that it has been effectively impossible to model the ascertainment strategy and thus to correct for the bias.

This technical note describes the design, validation, and manufacture of an array consisting of SNPs all ascertained in a clearly documented way. We anticipate that this will provide a useful resource for the community interested in learning about history and natural selection. We hope that this array will be genotyped in many different cohorts, as has been done, for example, in the Marshfield panel where approximately 800 microsatellites have been genotyped in diverse populations<sup>1,2,3,4,5</sup>. By establishing a common set of simply ascertained SNPs that have been genotyped in diverse populations, it should be possible to learn about human history not only in individual studies, but also through meta-analysis.

The array is designed as a union of 13 different SNP panels. In our experience, a few tens of thousands of SNPs is enough to produce powerful inferences about history with regard to summary statistics like measurements of  $F_{ST}$ . Thus, it is better for many analyses to have (for example) 13 sets of tens to hundreds of thousands of SNPs each with its own ascertainment strategy than a single set of 600,000 SNPs. We have included a particularly large number of SNPs from particularly interesting ascertainment—discovery in the two chromosomes of a single San Bushman, a single Yoruba West African, a single French, a single Han Chinese, and a single Papuan—as for some analyses like scans of selection it is valuable to have dense data sets of hundreds of thousands of SNPs. All SNPs chosen for the array were selected from sites in the genome that have read coverage from Neandertals, Denisovans, and chimpanzees, allowing users of the array to compare data from modern humans to archaic hominins and apes.

This array is not ideal for gene mapping, since: (i) No attempt has been made to tag common variation genome-wide. (ii) There are gaps in the genome where no homologous sequence is available from chimpanzee. (iii) Unlike many existing arrays, we have not oversampled SNPs in the vicinity of genes, or adjusting SNP density in order to fully tag haplotypes. Instead we simply sampled SNPs in proportion to their genomic density as discovered by sequencing.

The array is being made commercially available by Affymetrix. Importantly, the academic collaborators who have been involved in the design will not benefit from sales of the array (they

will not receive any financial compensation from Affymetrix). The CEPH-Human Genome Diversity Project (CEPH-HGDP) samples that were genotyped during the course of the project will not be used for any commercial purposes. Affymetrix deposited the genotypes of unrelated CEPH-HGDP samples, collected as part of the array development, into the CEPH-HGDP database on August 12, 2011, more than six months before commercial release of the array (in Spring 2012), and this genotyping data is freely available to the public.

### Design strategy for the 13 panels

#### (Panels 1-12) Discovery of heterozygous sites within 12 individuals of known ancestry

The first 12 SNP ascertainment strategies are based on the idea of the Keinan, Mullikin et al. Nature Genetics 2007 paper<sup>6</sup>. That paper takes advantage of the fact that by discovering SNPs in a comparison of two chromosomes from the same individual of known ancestry, and then genotyping in a larger panel of samples from the same population, one can learn about history in a way that is not affected by the frequency of the SNP in human populations. In particular, even though we may miss a substantial proportion of real SNPs in the individual (false-negatives), and even if a substantial proportion of discovered SNP are false-positives, we expect that the inferences about history using SNPs discovered in this way will be as accurate as what would be obtained using SNPs identified from deep sequencing with perfect readout of alleles.

To understand why false-negative SNPs should not bias inferences, we note that if a SNP is truly heterozygous in the individual in whom we are trying to discover it, there is exactly one copy of the ancestral allele and exactly one copy of the derived allele. Thus, conditional on the SNP being heterozygous in the discovery individual, its probability of being discovered is not further affected by whether it has a high or low minor allele frequency in the population. This contrasts with ascertainment strategies that discover SNPs in more than one individual, where there is always a real (and extremely difficult to quantify) bias toward missing rarer variants. By genotyping SNPs discovered in this way, and making a simple  $p(1-p)$  correction for discovery in two chromosomes (where  $p$  is the minor allele frequency), one can obtain an unbiased reconstruction of the allele frequency distribution in the population.

An important feature of this SNP discovery strategy is that false-positive SNPs (for example, due to sequencing error, mapping error, segmental duplications or copy number variation) are not expected to substantially bias inferences. The reason is that we have validated all candidate SNPs by genotyping them using a different technology, and we have required the genotypes to match the individuals in whom they were discovered. Thus, we expect to have a negligible proportion of false-positive SNPs on the final array.

This procedure has produced 12 panels of uniformly discovered SNPs, which can be used for allele frequency spectrum analysis. There is some overlap of SNPs across panels. Importantly, we have separately determined validation status for the SNPs in each panel, and have only used SNPs that validate in the same sample in which they were discovered. Thus, we have not biased toward SNPs with a high minor allele frequency, or that are polymorphic across multiple populations, which might be expected to have a higher chance of validation if we did not perform the validation in each discovery sample independently.



(Panel 13) SNPs where a randomly chosen San allele is derived relative to an archaic hominin. A 13<sup>th</sup> ascertainment strategy used alignments of three genomes: chimpanzee, Denisova (an archaic hominin from southern Siberia for whom there is 1.9× genome sequence coverage<sup>7</sup>), and San. We examined sites where we had ≥1-fold coverage of Denisova, and ≥3-fold coverage of San. We made an allele call for each individual by majority rule, randomly selecting an allele when there was a tie (this means that we are effectively sampling one of two haplotypes in the individual, and the allele call is not expected to be being biased if the individual is heterozygous at that site). We placed on the array the subset of sites where San is derived relative to both Denisova and chimpanzee, in this case requiring agreement between the Denisova and chimpanzee allele. These are sites that likely arose due to mutations in the last million years.

We chose to use San rather than another modern human for building this panel because there is evidence that the San are approximately symmetrically related to all other present-day humans<sup>8</sup>. Panel 13 is also the only one with SNPs from chromosome X (all the other panels are based on SNPs discovered in males), and thus this panel permits X-autosome comparisons.

### Description of the sequencing data and filtering used in SNP ascertainment

The sequencing data that we use for identifying candidate SNPs has been described in two recent papers: Green et al. 2010<sup>9</sup> and Reich et al. 2010<sup>7</sup>. The data were all generated in the Max Planck Institute in Leipzig using Illumina Genome Analyzer IIx (GAIIx) sequencing instruments via protocols that are described in refs. 9 and 7 (Table 1). Population genetic analyses for ref. 7 were carried out on the very data file that was used to select SNPs for the array.

**Table 1: Characteristics of the sequencing data we are using for SNP ascertainment**

Name	Identifier	Sequenced by	Genomic coverage*	Cutoff† A (Pr)	Cutoff† C (Pr)	Cutoff† G (Pr)	Cutoff† T (Pr)
Han	HGDP00778	Green 2010	3.8	16 (0.489)	14 (0.239)	17 (0.003)	15 (0.11)
Papuan1	HGDP00542	Green 2010	3.6	13 (0.051)	10 (0.119)	15 (0.434)	13 (0.880)
Yoruba	HGDP00927	Green 2010	4.3	17 (0.692)	14 (0.440)	18 (0.562)	16 (0.985)
San	HGDP01029	Green 2010	5.9	17 (0.830)	15 (0.914)	18 (0.649)	16 (0.877)
French	HGDP00521	Green 2010	4.4	17 (0.317)	16 (0.985)	18 (0.024)	17 (0.515)
Mbuti	HGDP00456	Reich 2010	1.2	17 (0.041)	14 (0.504)	17 (0.704)	16 (0.379)
Karitiana	HGDP00998	Reich 2010	1.1	18 (0.210)	14 (0.126)	17 (0.147)	17 (0.589)
Sardinian	HGDP00665	Reich 2010	1.3	19 (0.789)	15 (0.302)	18 (0.474)	17 (0.200)
Bougainville	HGDP00491	Reich 2010	1.5	18 (0.810)	14 (0.288)	17 (0.445)	16 (0.291)
Cambodian	HGDP00711	Reich 2010	1.7	18 (0.717)	14 (0.303)	17 (0.331)	16 (0.398)
Mongolian	HGDP01224	Reich 2010	1.4	18 (0.371)	15 (0.789)	17 (0.051)	16 (0.090)
Papuan2	HGDP00551	Reich 2010	1.4	17 (0.188)	14 (0.661)	17 (0.932)	16 (0.885)
Neandertal	Vindija.3.bones	Green 2010	1.3	27 (0.428)	26 (0.049)	27 (0.308)	27 (0.579)
Denisova	Phalanx	Reich 2010	1.9	40 (1.000)	40 (1.000)	40 (1.000)	40 (1.000)

\* Genomic coverage is calculated for the modern humans as (# of reads mapping to chimpanzee) × (read length which is 76bp for Green et al. 2010 and 101bp for Reich et al. 2010) × (0.95 as we filtered out the 5% of the lowest quality data) / (2.8 Gb). For the archaic hominins we report the coverage from the abstracts of Green et al. 2010 and Reich et al. 2010.

† For each base used in SNP discovery, we give the quality score cutoff and probability of acceptance at that cutoff (parentheses). The cutoffs are chosen to filter out the data of the lowest 5% quality for each nucleotide class (SI 6; Reich et al. 2010).

The 12 modern human samples are all from the CEPH-HGDP panel. A valuable feature of this panel is that DNA for all samples is available on request on a cost-recovery basis for researchers who wish to carry out further sequencing and genotyping analysis on these samples for the purpose of research into human population history<sup>8,10</sup>. Five of the samples (San, Yoruba, Han, French and a Papuan) were sequenced by Green et al. 2010 using Illumina paired-end 76bp reads<sup>9</sup>, while the remaining 7 (Mbuti, Sardinian, Karitiana, Mongolian, Cambodian, Bougainville, and a second Papuan) were sequenced by Reich et al. 2010 using Illumina paired-end 101bp reads<sup>7</sup>. All reads from all 12 samples were mapped to chimpanzee (*PanTro2*). To filter the sequence data for analysis, we used a similar procedure as described in Reich et al. 2010<sup>7</sup>, removing the lowest quality of 5% of nucleotides on a sample and nucleotide-specific basis to maximize the amount of sequencing data available for analysis. After this procedure, we had 3.6-5.9× coverage for the 5 samples and 1.1-1.7× for the 7 samples (Table 1).

We also used data from 4 ancient DNA samples to aid our choice of SNPs. To represent Neandertals, we used a pool of sequences from 3 bones from Vindija Cave in Croatia (Vi33.16, Vi33.25 and Vi33.26) for which we had 1.3× genome coverage altogether<sup>9</sup>. To represent Denisovans, we used data from a finger bone (fifth distal manual phalanx) from the Altai mountains of southern Siberia, with 1.9× coverage<sup>7</sup>.

#### All reads are mapped to chimpanzee and a chimpanzee allele is available

We mapped sequencing reads from modern and ancient genomes to the chimpanzee reference sequence (*PanTro2*) to avoid biases toward one present-day human group more than another.

#### We filtered out reads with a substantial probability of poor mapping

Each read that we analyzed had a mapping quality score (MAPQ) that reflects the confidence of its mapping to *PanTro2*. Based on empirical exploration of the usefulness of the scores, which were generated by either the ANFO or BWA software, we only used reads that had MAPQ of at least 90 for Neandertal (ANFO mapping), 37 for Denisova (BWA), and 60 for present-day humans (BWA). We also rejected reads if the alignment to the chimpanzee resulted in any insertion/deletion difference. This filter was applied in addition to the filtering of Table 1.

#### Filtering of sites with $\geq 2$ alleles not matching chimp across the humans used for SNP discovery.

At a small proportion of sites, we observe more than one non-ancestral allele in the individual sequencing data used for SNP discovery. Such sites cannot be due to a single historical mutation. Instead, the data must reflect at least two mutations or sequencing errors. We filter out such sites.

For a very small fraction of sites, we found that the derived allele is *different* depending on which human is used in SNP discovery (these are potentially triallelic SNPs in the population, although they are not triallelic in the discovery individual). We keep such sites in our list of SNPs for designing, and use multiple probe sets to assay such SNPs.

The raw data file that emerges from this process is available on the “orchestra” Harvard Medical School filesystem at: /groups/reich/CLEAN\_SNP\_ARRAY/rawsnps and is freely available from David Reich on request (a README file is in the same directory at rawsnps\_readme) (Table 2). For brevity, this file only lists the 2,173,116 SNPs where 2 copies of the derived and 1 copy of the ancestral allele are observed a hominin; these are the only SNPs that are candidates for inclusion. Thus, it is an abbreviated version of a larger file used in analyses for ref. 7.

### Filtering the nucleotide calls of the lowest reliability

- (a) We do not use nucleotides for which there is no valid nucleotide call for chimpanzee.
- (b) For Neandertals, we do not use nucleotides within 5 nucleotides of either end of the reads, because of the elevated rate of ancient DNA degradation errors that we empirically observe.
- (c) For Denisova, we do not use nucleotides within 1 nucleotide of either end of the read.
- (d) For both Neandertals and Denisova, we do not use nucleotides with sequence quality  $<40$ .
- (e) For present-day humans, we do not use nucleotides with sequence quality  $<T_{ij}$ , where  $T_{ij}$  is a threshold chosen such that half of nucleotides generated from individual  $i$  and of allele class  $j$  ( $j = A, C, G, T$ ) are less than this value. For nucleotides that have exactly a quality score of  $T_{ij}$ , we randomly choose ones to eliminate such that exactly 5% are dropped (note that this differs from the 50% used in Reich et al. 2010). The cutoffs used are presented in Table 1.
- (f) For the “Papuan1” individual from ref. 9 (HGDP00542), the sequencer had a high error rate at position 34 (41 on the reverse strand). We excluded data from position 34 for this individual.

**Table 2: Datafiles summarizing the SNP ascertainment for the population genetics array**

File name	Readme	Description	Entries
rawsnps	rawsnps_readme	This file contains all sites where there are at least 2 copies of a derived allele and 1 copy of the ancestral allele in 12 present-day humans, 3 Neandertals, and Denisova, and further filtered to be candidates for inclusion in the SNP array.	2, 173,116
ascertained	ascertained_readme	This file contains all SNPs chosen in any ascertainment panel (there are a few hundred that are triallelic and we list them on different lines, so the number of unique SNPs is 1,812,990).	1,813,579
screening	screening_readme	This file contains all probesets we considered for screening array design, as well as the metrics for prioritization and indicator variables indicating whether they were chosen. If chosen, a column indicates the genotyping outcome, and whether the SNP was taken forward to the production array.	3,882,158

Note: These files can be found in the Harvard Medical School orchestra filesystem at /groups/reich/CLEAN\_SNP\_ARRAY/.

### **1,353,671 SNPs for testing on an Affymetrix Axiom™ screening array**

#### 1,812,990 candidate SNPs discovered in 13 different ascertainment panels

We used the following algorithm to choose candidate SNPs for validating on the array.

- (a) We mapped all reads used for SNP discovery to the chimpanzee reference sequence, *PanTro2*, without using data from the human reference sequence at all for read mapping. This was important to avoid biases due to the ancestry of the human reference sequence.
- (b) We rediscovered all SNPs *de novo*, blinding ourselves to any prior information about whether the sites were polymorphic in present-day humans.
- (c) At all SNPs, we required coverage from at least 1 Neandertal read and at least 1 Denisova read. This is expected to result in bias toward locations of the genome where the ancient DNA tends to be better preserved or the sequencing technology tends to work better. However, there is no reason why it would be expected to result in a bias in allele frequencies toward one

modern human population more than another (as all Neandertal and Denisova reads are mapped to chimpanzee, and no modern human data influences the mapping). The availability of data from archaic hominins from each of the SNPs on our array should be of value for some types of population genetic analysis. (For a handful of sites, the Denisova and Neandertal alleles may not be the same as those seen in present-day humans, but we nevertheless considered these sites to be covered by Denisova and Neandertal as we were concerned that not doing so could introduce bias. Users can treat such sites how they wish.)

- (d) All A/T and C/G polymorphisms were excluded, since genotyping these SNPs requires twice the number of probes using the Axiom™ technology. Thus, removing them increases the number of SNPs we can include on a single array. Removing these SNPs has the additional benefit that it eliminates any strand ambiguity. (Illumina arrays do not genotype A/T or C/G SNPs, either.) However, it also had the disadvantage that A/T and C/G SNPs constitute the one class of SNPs that is believed to be immune to biased gene conversion. Thus, in population genetic analyses of the data generated from the array, it will be important to assess whether inferences are potentially explained by biased gene conversion.
- (e) For the SNPs for panels 1-12 (candidate heterozygotes in an individual of known ancestry), we required the observation of at least 2 copies of the derived (non-chimpanzee) and at least 1 copy of the ancestral allele in the studied person (Reich et al. 2010; SI 6). We did not include chromosome X SNPs from these panels as the 12 individuals were all male.
- (f) For the SNPs in panel 13 (derived in San relative to Denisova), we restricted to sites where we had  $\geq 3$ -fold read coverage of San and  $\geq 1$ -fold read coverage of Denisova.

A complication in choosing SNPs discovered in two individuals is that both the San and Denisova individuals are diploid. What we want is to have a panel of SNPs ascertained by comparing a single haploid Denisovan and a single haploid San chromosome, but if we are not careful, we are going to be biased toward the SNPs that are fixed differences. For example, if we accepted only SNPs where all Denisova reads matched chimpanzee and all San reads were derived, then we would bias against SNPs that were truly heterozygous.

To obtain data of the type that would be expected from sampling a single haploid Denisovan and a single haploid San chromosome, we picked the allele that was seen more often in each sample to represent that sample (if there was a tie in terms of the number of reads supporting each allele, we chose one allele at random). In this way, we are picking one of the two chromosomes from each individual (at random), and hence we are effectively sampling a haploid chromosome despite having diploid data. An additional benefit of using the majority rule is that we are also increasing the quality and reliability of the allele call, such that we expect a larger proportion of these SNPs to be real than in panels 1-12.

From the SNPs discovered in this way, we restrict our analysis to sites where Denisova matches the chimpanzee allele and where San is derived (we throw away sites where San is ancestral and Denisova is derived). The reason for this is that this is the only subset of SNPs that we can experimentally validate. To validate these SNPs, we can genotype the San individual and require the observation of an allele that differs from chimpanzee. In contrast, we cannot validate sites where San is ancestral and Denisova is derived, since the Denisova sample is extremely limited and does not provide enough for genotyping assays.

Some of the SNPs from panels 1-13 overlap. Thus, while the sum of the number of SNPs in each panel is 2,581,282, the number of unique SNPs is only 1,812,990. However, the fact that a SNP is

present in more than one panel does not mean that it has a higher likelihood of being validated for the array for a given ascertainment strategy. For SNP identified in more than one panel, we designed a single probe to test the SNP, but we assessed its validation status separately for each panel to avoid bias toward more easily validating more polymorphic SNPs (see below).

The perl script used for choosing SNPs is on the “orchestra” Harvard Medical School filesystem at: /groups/reich/CLEAN\_SNP\_ARRAY/newformat\_affypick.pl (available on request from David Reich). The output file is at /groups/reich/CLEAN\_SNP\_ARRAY/ascertained (available on request from David Reich). This list contains a single entry for each unique SNP, with the exception of triallelic sites that have multiple designs (thus, there are 1,813,579 entries rather than 1,812,990). A readme file is at /groups/reich/CLEAN\_SNP\_ARRAY/ascertained\_readme (available on request from David Reich) (Table 2). The number of SNPs that we selected using each strategy is summarized in Table 3.

**Table 3: Ascertainment of SNPs for panels 1-13**

Panel no.	Ascertainment	Sample ID	Genomic coverage	# SNPs found	# SNPs placed on screening array	# SNPs that validate on screening array	# SNPs that validate on final array
1	French	HGDP00521	4.4	333,492	241,707	123,574	111,970
2	Han	HGDP00778	3.8	281,819	204,841	87,515	78,253
3	Papuan1	HGDP00542	3.6	312,941	232,408	56,518	48,531
4	San	HGDP01029	5.9	548,189	401,052	185,066	163,313
5	Yoruba	HGDP00927	4.3	412,685	302,413	136,759	124,115
6	Mbuti	HGDP00456	1.2	39,178	28,532	14,435	12,162
7	Karitiana	HGDP00998	1.1	12,449	8,535	3,619	2,635
8	Sardinian	HGDP00665	1.3	40,826	29,358	15,260	12,922
9	Melanesian	HGDP00491	1.5	51,237	36,392	17,723	14,988
10	Cambodian	HGDP00711	1.7	53,542	38,399	20,129	16,987
11	Mongolian	HGDP01224	1.4	35,087	24,858	12,872	10,757
12	Papuan2	HGDP00551	1.4	40,996	29,305	14,739	12,117
13	Denisova-San	Den-HGDP01029	-	418,841	308,210	166,422	151,435
<i>Unique SNPs</i>				<i>1,812,990</i>	<i>1,354,003</i>	<i>599,175</i>	<i>542,399</i>
<i>Unique probe designs</i>				<i>1,941,079</i>	<i>1,385,672</i>	<i>605,069</i>	<i>546,581</i>

#### 1,941,079 unique flanking sequences corresponding to the 1,812,990 unique SNPs

To ensure clean SNP ascertainment, we followed a rigorous procedure whereby the flanking sequence assay for each SNP were chosen only based on sequencing data from chimpanzee and the modern human sample used in SNP ascertainment. Thus, while some SNPs were discovered in multiple panels, we did not use this information in probe design. We used the simple rules below to pick a probe, and if the optimal design was different depending on the sample in which the SNP was ascertained, we used more than one probe for the SNP.

For each SNP in each of the 13 ascertainment panels, we specified 71 base pair (bp) flanking sequences that would be used for probe designing as follows:

(a) *Ancestral and derived allele are specified based on the individuals used in SNP ascertainment.*

For each SNP in each panel, we specified the ancestral and derived alleles based on the two

alleles observed in SNP ascertainment, defining as “ancestral” the allele that matched chimpanzee. SNPs within any ascertainment panel almost always had two observed alleles, since we filtered out sites with three or more. However, for SNPs that were discovered in multiple panels, we performed the specification of the ancestral and derived allele independently, and thus for a small fraction of sites, there was a different derived allele depending on the ascertainment panel (even if flanking sequence were sometimes identical).

- (b) *Flanking sequence is specified entirely based on the modern sample used for SNP discovery.* For initial probe design, we provided 35 bp of flanking sequence on either side of the SNP. We started with 71 bp of sequence from the chimpanzee genome, *PanTro2*, centered on the SNP. To decrease the number of mismatches between the flanking sequence and any human that might be analyzed using the array, we “humanized” the flanking sequence based on the modern sample used for SNP discovery (importantly, only the discovery sample is used for the humanization of the sequence, and so the ancestry of other samples cannot bias results).

Specifically, for each of panels 1-13, we took all reads from the modern human used in SNP ascertainment that mapped to the flanking nucleotide. Where 100% of reads disagreed with *PanTro2*, we edited the flanking sequence to reflect that in the ascertainment sample. Otherwise, we kept the chimpanzee allele. An example is:

“acctggctccagGgccagcagctccgtcaAggtcc[G/A]ctgcatgaaactgatgaagggaggggcaccaggcg”. Here, capital [G/A] indicates the [chimp/alternate allele] at the SNP and other capital letters indicate bases edited from the chimpanzee reference to match the ascertainment sample. For ascertainment panel 13 (Denisova ancestral and a randomly chosen San allele derived), we did not use the Denisova genome in primer editing. Instead, we edited the sequence to match San whenever San consistently had a non-chimpanzee allele at all reads overlapping the site.

Because the steps above sometimes result in different flanking sequences for the same nucleotide (depending on the particular sequencing reads from the sample used in SNP ascertainment), we were left with more unique flanking sequences (n=1,941,079) than unique SNPs (n=1,812,991).

#### Procedure used to choose 1,385,671 oligonucleotide probes for the screening array

With the list of 1,951,079 flanking sequences, we needed to design oligonucleotide probes, or “probesets”, for a screening array. We blinded ourselves to prior knowledge about which probes worked in previous assays using the Axiom™ technology, since doing so would expected to lead to a higher validation success rate for probes that have been previously tried on SNP arrays (introducing complex biases). For the same reason, we did not modify probe design based on using information in databases about polymorphism in flanking sequence. The only two types of information that were used in probe design were the physical chemistry considerations of which probes are expected to work well, and mapping information to the *PanTro2* chimp genome. All the metrics used are in a file on the “orchestra” Harvard Medical School filesystem /groups/reich/CLEAN\_SNP\_ARRAY/probesets, available on request from David Reich (Table 2). Details of the filtering procedure that we applied are as follows:

- (a) *We first identified 3,882,158 candidate probesets (two 30mers for each flanking sequence)*

For each of the 1,941,079 flanking sequences, it is possible to design two probesets corresponding to the 30 bp 5’ or 3’ direction of the SNP. We use the shorthand “red” to designate the 5’ probe and “green” to designate the 3’ probe, always referenced relative to the positive strand of the chimpanzee genome sequence *PanTro2* (Figure 1).



(b) *We next restricted analysis to 2,294,760 probesets predicted to have greater success*

Of the 3,882,158 candidate probesets (2 for each of 1,941,079 flanking sequences), we computed metrics that based on past experience were useful for predicting the success of genotyping. The values of the metrics are in /groups/reich/CLEAN\_SNP\_ARRAY/probesets (see probesets\_readme), available on request from David Reich. We applied the following filters to winnow the list to 2,294,760:

- (i) *Removing probesets that map to multiple positions in chimpanzee.*
- (ii) *Best BLAT hit to PanTro2 is much better than the second-best hit.* We used BLAT to map each 35 bp flanking sequence to *PanTro2*. We required a minimum of 33 bp of alignment, and required the difference between the first and second hits to be >5.
- (iii) *16mers within the probeset are relatively unique.* For each candidate 30 bp probeset, we examined each unique 16mer in a sliding window along the sequence (15 in all), and counted the number of exact matches in *PanTro2*. We defined “16mer-max” as the maximum number of exact matches seen for any of these 16-mers. In the experience of Affymetrix scientists who have worked on the Axiom™ technology, non-specific binding is unlikely when 16mer-max is small. We required “16mer-max” <110.
- (iv) *No runs of 4 G’s.* When more than 4 consecutive Gs stack up into quartets, hybridization tends to be compromised. We filtered out probes that had runs of 4 G’s (or 4 C’s),
- (v) *Terminal 5mer is not complemented elsewhere in the probeset.* We required the 5’ terminal 5mer to not have a reverse complement elsewhere in the probeset sequence, to minimize the tendency toward inter/intra probe annealing during hybridization, which in previous experience with the Axiom™ technology could cause a lower success rate.
- (vi) *Number of G and C nucleotides is >5.* We required that >5 of the nucleotides were either G or C. Previous experience suggests that probesets with extremely low G or C usually do not work well for hybridization assays.

(c) *A list of 1,477,155 probesets after eliminating redundancy*

For flanking sequences where both candidate probesets passed the filters above, we chose the probeset that was deemed more likely to succeed based on having a lower value of “16mer-max” metric. When both probesets had the same value of “16mer-max”, we used a random number generator to choose. This resulted in 1,525,604 candidate probesets.

Even after representing each flanking sequence by no more than one probeset, the resulting list contained 48,449 duplicative entries. This occurred when the same SNP (and probeset) had been independently selected in more than one of the 13 ascertainment panels. In such cases, the 71bp flanking sequence obtained as described above could be distinct for multiple SNP ascertainments, but sub-strings could be identical, so that it could happen that the 30mer that was selected to represent the SNP was identical. We therefore merged these probes to eliminate redundancy, leaving us with 1,477,155 unique probesets.

Our naming scheme for probesets contains a binary string of 13 characters providing the ascertainment information for that probe. Because we merged some probesets, we created a new ascertainment code called “asc.new”. This was generated by applying a bitwise-or operation to the binary strings of 13 characters corresponding to the ascertainment information for the redundant probes.

(d) *A final list of 1,385,672 probes that were placed on the screening array*

The 1,477,155 probes that passed our filters were more than could fit into the screening array. Thus, we ranked all the probes based on their “16mer-max” score, breaking ties using a random number generator (lower values have a higher rank). After this ranking, all probes had “16mer-max” of no more than 110, and we were left with 1,385,672 probes.

## Design, genotyping, and analysis of screening array

### Design of the screening array

We designed two arrays to screen these 1.39 million probesets (0.69 million probesets fit onto a single screening array). To minimize bias, we randomized the probes with respect to which one of the 2 screening arrays was used to test them. We also used standard chip design strategies that are applied at Affymetrix for determining probe location in each screen design. The number of SNPs from each panel placed on the screening arrays is presented in Table 3.

The probesets used in the screening array are named like [chr]\_[pos]\_[alleles]\_[asc.new]\_[strand], with the 5 data fields indicating *PanTro2* chromosome / *PanTro2* physical position / ancestral-derived alleles, and the 13 bit binary string indicating the ascertainment panels in which the SNP was discovered, and the strand (f=forward or r=reverse compared to *PanTro2*).

### Genotyping the screening array

Three 96-well plates of samples were genotyped on the 2 screening arrays in early 2011, with the goals of (a) deciding if each SNP passes quality control criteria and can be taken forward to the production array, and (b) generating useful data for preliminary population genetic analysis.

*Validation plate #1:* The goal of validation plate #1 was to genotype the same 12 modern human samples that were used in SNP discovery and in which the derived allele was observed, and to validate that we observe an allele at these samples that is distinct from the ancestral allele seen in primates. There was a high level of redundancy on the plate:

- Each of the 12 modern human samples was genotyped 6 times (six different wells)
- The chimpanzee and bonobo were each genotyped 6 times
- The gorilla and orangutan were each genotyped 4 times

The position of each sample on the plate (except for the upper right 4 wells which were left empty for control samples) was assigned using a random number generator.

*Validation plates #2 and #3:* We also took advantage of the screening array to genotype 2 plates of samples from CEPH-HGDP populations. We genotyped 184 samples from the same populations that were used in SNP discovery, consisting of French (n=28), Han (n=27), Papuan (n=17), San (n=6), Yoruba (n=21), Mbuti (n=13), Karitiana (n=13), Sardinian (n=28), Melanesian (n=11), Cambodian (n=10) and Mongola (n=10). Analysis of the data allowed us to perform further validation of the SNPs on the array, and also to assess whether useful population genetic analyses can be generated from these genotyping data.



### Determining which SNPs “validated”

All samples were genotyped using the Axiom™ Assay 2.0 and genotype calls were made using the apt-probeset-genotype program in the Affymetrix Power Tools (APT) package<sup>11</sup> (the apt-probeset-genotype program is integrated in the Genotyping Console (GTC) version 4.1 software<sup>12</sup>, which also provides visualization tools). Both programs use the Axiom™ GT1 algorithm to call genotypes. The algorithm adapts pre-positioned clusters to the data using a probability-based method. Clustering is carried out in two dimensions, log ratio ( $\log_2(A) - \log_2(B)$ ) and size ( $\log_2(A + B)/2$ ). The algorithm derives from BRLMM-P<sup>13,14</sup>, which clusters in a single signal-contrast dimension, and is tuned to the signal characteristics of the Axiom™ assay.

To avoid ascertainment bias, only the sample used for SNP discovery, chimpanzees and bonobos, were used to assign a validation status to each candidate SNP for each of the 13 ascertainment panels. After an initial inspection of the data from Validation Plate #1, we chose not to use the data from the gorilla and orangutan as part of validation. This is because for a substantial fraction of SNPs, the signal intensities were different for one or both alleles in the apes than in humans, which we hypothesized was due to differences in the flanking DNA sequence under the primers. This occurred most often in gorilla and orangutan, and is expected to confound the genotyping algorithm, and thus we restricted to chimpanzees and bonobos.

We used a separate procedure for deciding whether a SNP was validated for ascertainment panels 1-12 (SNPs discovered as a heterozygote in a single modern human) or in ascertainment panel 13 (SNPs where San was derived and Denisova was ancestral). Table 4 summarizes the number of SNPs that validate in one, two, or all three genotyping runs.

**Table 4: Results of genotyping on the screening array**

Panel	Ascertainment	Sample ID	Screened SNPs	Validated in 3 runs	Validated in 2 runs	Validated in 1 run
1	French	HGDP00521	241,707	94,139	12,283	17,700
2	Han	HGDP00778	204,841	66,885	8,341	12,780
3	Papuan1	HGDP00542	232,408	43,622	5,308	8,000
4	San	HGDP01029	401,052	139,689	18,266	27,648
5	Yoruba	HGDP00927	302,413	103,670	13,542	20,017
6	Mbuti	HGDP00456	28,532	11,123	1,499	1,950
7	Karitiana	HGDP00998	8,535	2,839	326	511
8	Sardinian	HGDP00665	29,358	11,555	1,630	2,232
9	Melanesian	HGDP00491	36,392	13,626	1,769	2,527
10	Cambodian	HGDP00711	38,399	15,606	1,954	2,772
11	Mongolian	HGDP01224	24,858	9,890	1,312	1,824
12	Papuan2	HGDP00551	29,305	11,256	1,464	2,181
13	Denisova-San	Den-HGDP01029	308,210	107,708	26,280	32,845
<i>Unique probesets</i>			<i>1,385,391</i>	<i>455,942</i>	<i>82,978</i>	<i>110,248</i>

### *Panels 1-12 (SNPs ascertained as a heterozygote in a single modern human)*

We performed the ascertainment three times by carrying out three genotyping runs: once using only the 6 chimpanzee replicates to represent the apes, once using only the 6 bonobo replicate, and once using both chimpanzee and bonobo, a total of 12 *Pan* samples.

- a) We required that all 6 human replicates are called heterozygous and all apes homozygous.

- b) We required that the homozygous cluster and heterozygous cluster were well resolved in the clustering space, referred to as “A vs. M space”. M and A are defined as

$$M = \left[ \log_2 \left( A_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) - \log_2 \left( B_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) \right]$$

$$A = \left[ \log_2 \left( A_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) + \log_2 \left( B_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) \right] / 2$$

Based on the experience of Affymetrix scientists with the Axiom™ 2.0 Assay, five conditions were required to be satisfied to ensure that the clusters were well resolved in clustering space. Using the definitions “hetero”=samples called heterozygous, “homo”=samples called homozygous, “std”=standard error, and “abs”=absolute value, the 5 conditions that we required to be met to consider a SNP as validated were:

- (i)  $\text{mean}(M_{\text{hetero}}) \in (-1, 1)$  and  $\text{mean}(M_{\text{homo}}) \in (-\infty, -1] \text{ or } [1, +\infty)$
  - (ii)  $\text{mean}(A_{\text{hetero}}) - 2 \times \text{std}(A_{\text{hetero}}) > \text{mean}(A_{\text{homo}}) - 2 \times \text{std}(A_{\text{homo}})$
  - (iii)  $\text{mean}(A_{\text{hetero}}) \geq 8.5$
  - (iv)  $\Delta_{\text{sep}} \geq 5$ , where  $\Delta_{\text{sep}}$  is computed using the following formula
 
$$\Delta_{\text{sep}} = \text{abs} \left( \frac{\text{mean}(M_{\text{homo}}) - \text{mean}(M_{\text{hetero}})}{[\text{std}(M_{\text{homo}}) + \text{std}(M_{\text{hetero}})]/2} \right)$$
  - (v)  $\text{abs}(\text{mean}(M_{\text{hetero}}) - \text{mean}(M_{\text{homo}})) > 1$
- c) We required that the chimpanzee and bonobo agree at least partially in their genotype calls, for SNPs where a call was made in at least one of the three genotyping runs. The goal was to exclude SNPs that completely disagreed between chimpanzees and bonobos, which would imply that the ancestral allele determination was unreliable at these sites.

*Panel 13 (SNPs where San was derived and Denisova was ancestral)*

SNPs were considered as “validated” for panel 13 if they passed the following validation criteria:

- a) All six San replicates were called heterozygote or derived homozygotes, and all ape replicates were called ancestral homozygotes.
- b) SNPs in chromosome X were not in pseudoautosomal regions (PARs) and were called as homozygous derived in the San individual.
  - (i) PARs were determined by converting coordinates of the human PARs (Build36) to *PanTro2* using the liftOver program from the UCSC genome browser.
  - (ii) The San sample is a male, so SNPs in this chromosome are expected to be homozygotes.
- c) The following three criteria were required to be met to make sure that the clusters were located around expected locations and well separated (that is, they were well resolved)
  - (i)  $\text{mean}(M_{\text{ape}_{\text{homo}}}) \in (-\infty, -1] \text{ or } [1, +\infty)$
  - (ii)  $\text{mean}(A_{\text{ape}_{\text{homo}}}) \geq 9.5$
  - (iii)  $\text{std}(M_{\text{ape}_{\text{homo}}}) < 0.45$
- d) For a SNP passing the above criteria in any one of three genotyping runs, we required that the chimpanzee and bonobo genotypes, compared across runs, did not completely disagree.

For autosomal SNPs in Panel 13, the true genotype for San replicates could be either heterozygote or derived homozygote. To avoid potential bias that might cause either heterozygous or derived

homozygous genotypes to be validated at a higher rate, we did not apply any metrics involving measuring the coherence of the heterozygous or derived homozygous clusters. Thus, the criteria used for Panel 13 are looser than the other 12 panels, which we expect will minimize the potential for ascertainment bias at the cost of lowering the validation rate of SNPs.

#### *Filtering of SNPs based on the genotyping of 184 samples on Validation Plates #2 and #3*

Up to this point, all decisions about which SNPs were considered to be validated were based entirely on the results of genotyping Validation Plate #1 on the screening array. As these decisions were only based on data from apes and the human sample used in SNP discovery, this is a perfectly clean strategy from the point of view of SNP ascertainment.

In practice on inspection of the genotyping results for Validation Plates #2 and #3, we found that a small fraction of SNPs that passed the validation filters described above were completely heterozygous in modern humans, or nearly so. This is unexpected based on population genetic considerations, and suggests that these SNPs overlap segmental duplications (which we did not screen out from our array in the interests of having a completely unbiased ascertainment procedure). An observation of more than half of individuals being heterozygous is unexpected at a true SNP. In an unstructured population for a SNP of frequency  $p$ , the expected proportion of heterozygous genotypes is  $2p(1-p)$ , which is at most 0.5, and the expected rate of heterozygous genotypes is less than this for a structured population.

We therefore implemented a further filter where for each SNP, we computed its frequency across all of the  $N$  modern humans on Validation Plates #2 and #3 that successfully genotyped ( $N \geq 184$ ). We then counted the observed number of heterozygous genotypes  $het_{obs}$  versus the conservative expectation of  $het_{exp} = Np_{het}$ , where  $p_{het} = 2p(1-p)$  (here,  $p$  is the empirical frequency of the derived allele,  $(het_{obs} + 2(\text{number of homozygous genotypes})/2N)$ ). By dividing the difference between the observed and the expected number of heterozygous genotypes by the binomially distributed standard error, we can compute an approximately normally distributed Z-score:

$$Z = \frac{het_{obs} - het_{exp}}{\sqrt{Np_{het}(1 - p_{het})}}$$

We filtered out SNPs for which  $Z > 5$ , which is expected to remove at most a fraction  $3.0 \times 10^{-7}$  of true SNPs by chance. This removed 1,932 additional SNPs.

#### *Summary of results of the validation genotyping*

A total of 605,069 unique probesets (599,175 unique SNPs) were validated by the screen. The numbers of validated SNPs in each panel is listed in Table 3.

#### **Taking forward SNPs to a final production array**

All of the 605,069 probesets that passed the validation criteria after genotyping on the screening array were tiled on the final production array. In addition to those 605,069 “Human Origins” SNPs, a set of 87,044 “Compatibility” SNPs were also tiled on the final production array, choosing from a set of 8.8 million SNPs that had previously been validated using the Axiom 2.0<sup>TM</sup> genotyping assay. Among those SNPs, there are 2,091 non-PAR chromosome Y SNPs, 259 mitochondrial SNPs, and 84,694 SNPs that overlap between the Affymetrix SNP Array 6.0 and Illumina 650Y array. No A/T or C/G SNPs were selected for the Compatibility SNPs, as they take up more space on the array (two probes for each SNP), so that excluding them thus allowed us to

maximize information from the array. For the 84,694 nuclear SNPs, we increased the value of the SNPs by maximizing the fraction that were also genotyped on the Affymetrix SNP Array 5.0 (78.5%), that were covered by sequencing from Neandertal (53.9%) and Denisova (64.7%), and for which a chimpanzee allele was available (nearly 100%).

### Validation of the final SNP array through genotyping of 952 CEPH-HGDP samples

We attempted to genotype 952 CEPH-HGDP samples that were previously determined to be unrelated up to second degree relatives<sup>15</sup>. This genotyping had three goals:

(a) *Round 2 validation: Evaluating the performance of every SNP in the final product array*

Although all of the SNPs that were tiled on the final product array had previously been validated in screening arrays, there is variability in how an assay performs on a real product. Hence after manufacturing the final SNP array, we genotyped 952 unrelated CEPH-HGDP samples (including the 12 modern human samples used in SNP ascertainment) using the final product array. We used these data to create a list of SNPs that had gone through two rounds of validation and would be robust for genotyping.

(b) *Building up prior distributions for SNP calling*

The Axiom™ GT1 algorithm makes more accurate genotype calling for a SNP if it has prior distributions for the 3 genotype clusters (AA, AB, and BB) based on data (by default, the Axiom™ GT1 algorithm uses the generic prior distributions of the 3 clusters, which is just a best guess). Because the CEPH-HGDP panel has such a large number of samples from diverse ancestries, we expect to observe clusters from all 3 genotypes for most SNPs. This allows us to construct prior distributions that could be used for SNP calling in other projects.

(c) *Creating a dataset that will be useful for population genetics*

The genotyping of the unrelated CEPH-HGDP samples has the benefit that it creates a dataset that will be widely available to the population genetics community. Users who wish to genotype samples that they are interested in on this array, will be able to merge the data that they collect with data collected on the CEPH-HGDP samples, to enable a richer comparison of genetic variation in one region to worldwide variation.

**Table 5. Eighteen HGDP samples that did not pass quality control**

Identifier	Population	Reason removed
HGDP00009	Brahui	Failed DQC
HGDP00708	Colombian	<97% genotype call rate
HGDP01266	Mozabite	<97% genotype call rate
HGDP01267	Mozabite	<97% genotype call rate
HGDP01403	Adygei	<97% genotype call rate
HGDP00885	Russian	<97% genotype call rate
HGDP00886	Russian	<97% genotype call rate
HGDP00795	Orcadian	<97% genotype call rate
HGDP00804	Orcadian	<97% genotype call rate
HGDP00746	Palestinian	<99% concordance with Illumina 650Y data
HGDP00326	Kalash	<99% concordance with Illumina 650Y data
HGDP00274	Kalash	<99% concordance with Illumina 650Y data
HGDP00304	Kalash	<99% concordance with Illumina 650Y data
HGDP00309	Kalash	<99% concordance with Illumina 650Y data
HGDP01361	Basque	<99% concordance with Illumina 650Y data
HGDP00710	Colombian	<99% concordance with Illumina 650Y data
HGDP01376	Basque	<99% concordance with Illumina 650Y data
HGDP01009	Karitiana	anomalous ancestry relative to others in group

### Filtering out 18 samples that did not genotype reliably

After assaying all 952 samples, we filtered to 934 samples as follows (Table 5):

- (a) We filtered out 9 samples that did not pass standard Axiom™ 2.0 Array QC metrics: a “DQC” score (chip-level quality metric) and a call rate score. This suggests problems such as low input DNA amount, contamination of DNA samples, or technical issues with hybridization. These 9 samples were excluded from the genotyping calling.
- (b) We excluded an additional 9 samples based on their genotype patterns. Of these, 8 were excluded because there was a greater than 1% genotype discrepancy between our current data and earlier data from the Illumina 650Y array genotyped on the same samples **Error! Bookmark not defined.** We also excluded HGDP01009, an individual that our data (as well as analyses of previous datasets) suggests is a sample whose ancestry is an outlier relative to others from the Karitiana group, suggesting a history of recent gene flow with other Native American populations.

### Special filters applied to chromosome X and Y data

Chromosome X occurs in only a single copy in men but in two copies in women. Chromosome Y occurs only in men. This means that SNPs on these chromosomes need to be treated differently from autosomal SNPs; for chromosome X we genotyped males and females separately, and for chromosome Y we only genotyped males. For males, we required that genotypes on both chromosome X and Y were always homozygous.

### Filtering out additional probesets based on the genotyping of the final array

Not all probesets tiled onto the final array performed well enough to produce reliable results. We filtered out a total of 58,488 additional probesets by sequentially applying the seven criteria listed in Table 6. Three of the criteria used in Table 6 require more detailed explanation.

**Table 6. Phase 2 validation (determining probesets for which we report genotypes)**

Order	Filter	Removed	Definition
1	SNP call rate $\geq 95\%$	23,476	(no. of called samples) / (no. of genotyped samples = 943)
2	Concordance	31,415	For panels 1-12, the SNP must be heterozygous in the sample used in ascertainment (for panel 13, heterozygous or derived homozygous).
3	het_rate > 5	79	This is the same metric used in SNP validation
4	het_offset > -0.5	892	See below for explanation
5	resolution score $\geq 3.6$	2,450	See below for explanation
6	chrX annotation	94	Panel 13 SNPs that are <i>PanTro2</i> chrX but not <i>hg18</i> chrX are removed.
7	chrX SNPs separate males and females	82	See below for explanation
Total removed by all filters		58,488	

**het\_offset:** Using the definition of “A vs. M space” described in the discussion of the screening array filters, we defined a quantity called *het\_offset* that measures whether the heterozygous genotype is appropriately intermediate between the homozygous clusters. For a probeset with three observed genotype clusters (AA, AB, and BB), it is defined as

$$\text{het\_offset: } \text{mean}(M_{AB}) - \frac{\text{mean}(M_{AA}) + \text{mean}(M_{BB})}{2}$$

For a probeset with one observed homozygous and one heterozygous cluster, it is defined as:

$$het\_offset: mean(M_{AB}) - mean(M_{AA|BB})$$

For other situations, *het\_offset* is not used as a filter.

resolution score: This is again defined in the M space of the “A vs M space”, and it measures how well the heterozygous cluster separates from the homozygous cluster(s). We define:

$$resolution = \frac{abs(mean(M_{homo}) - mean(M_{hetero}))}{sd(M_{homo}) + sd(M_{hetero})} \times 2$$

For a probeset with three observed genotype clusters (AA, AB, and BB), the resolution score is defined as:  $\min(resolution_{AA-AB}, resolution_{BB-AB})$ . For a probeset with one observed homozygous cluster and one observed heterozygous cluster, the resolution score is the resolution between two clusters. For other situations, the resolution score is NA.

chromosome X SNPs separate males and females: It was found that for some chromosome X SNPs, female samples and male samples formed distinct genotype clusters. Such cases most likely are not real chromosome X SNPs. One possible explanation for this pattern is SNPs derived from fixed differences between homologous chromosome X and chromosome Y sequences<sup>15,16</sup>. We removed chromosome X SNPs that meet all of the following criteria

1. All called male samples have the same genotype call
2. Greater than 85% of called female samples have the same genotype call and there are at most 2 different called genotypes for females
3. The distance between the male genotype cluster center and the major female genotype cluster center is at least 0.8 units in the M genotype clustering space.

The number of final validated SNPs is given in the final column of Table 7, and this is the set of SNPs for which we publically released data for 934 unrelated CEPH-HGDP samples on August 12, 2011. Table 7 summarizes the SNPs on the final product array.

**Table 7. Summary of SNPs in the final array**

Category	number of probesets	number of SNPs
Human Origins	546,581	542,399
Chromosome Y	2,091	2,091
Mitochondrial DNA	259	259
Compatibility	84,694	84,694
<i>Total</i>	<i>633,625</i>	<i>629,443</i>

Upon commercial release of the array, Affymetrix is planning to release user-friendly software that will facilitate SNP calling using each of the ascertainment panels. Users who are interested in any particular ascertainment will open up one of 14 available folders of files (the first 13 corresponding to the SNPs in each ascertainment, and the 14<sup>th</sup> corresponding to all SNPs together). Users will then be able to use that folder (which will include ascertainment-panel specific priors) to call genotypes relevant to any given ascertainment panel.

The genotyping data on the 934 unrelated CEPH-HGDP samples that we collected as part of this project has been made freely available without restriction to the community by depositing the data into the CEPH-HGDP database on August 12, 2011 ([http://ftp.cephb.fr/hgdp\\_suppl0/](http://ftp.cephb.fr/hgdp_suppl0/)). There are no restrictions on using these data and publishing papers based on these data.

In addition to the dataset of 934 CEPH-HGDP samples that we released on August 12, 2011, we have also carried out further filtering to create a dataset of 828 samples that might be more useful for some population genetic analyses. This dataset, which is the one that we used for the analyses of population history reported in the present paper, is available for downloading from the Reich laboratory website ([http://genetics.med.harvard.edu/reich/Reich\\_Lab/Welcome.html](http://genetics.med.harvard.edu/reich/Reich_Lab/Welcome.html)). To generate this dataset, we started with the dataset that was released to the CEPH-HGDP website on August 12, 2011, and then carried out population-specific Principal Component Analysis to identify individual samples that are outliers with respect to their own populations (consistent with admixture with other populations without the last few generation). These individuals were then filtered out of the dataset, allowing us to analyze data from a homogeneous population sample. Table 8 lists the number of samples from each population before and after the filtering.

**Table 8. Number of CEPH-HGDP samples in each of the two datasets reported here**

Population	Region	Aug. 12 2011	Further filtering
BantuKenya	Africa	11	10
BantuSouthAfrica	Africa	8	6
BiakaPygmy	Africa	23	20
Mandenka	Africa	22	20
Mbuti*	Africa	13	12
Mozabite	Africa	27	25
San*	Africa	6	5
Yoruba*	Africa	22	22
Cambodian*	East Asia	10	10
Dai	East Asia	10	10
Daur	East Asia	9	7
Han*	East Asia	34	33
Han-NChina	East Asia	10	10
Hezhen	East Asia	9	9
Japanese	East Asia	29	28
Lahu	East Asia	8	7
Miao	East Asia	10	10
Mongola*	East Asia	10	8
Naxi	East Asia	9	7
Oroqen	East Asia	9	8
She	East Asia	10	10
Tu	East Asia	10	9
Tujia	East Asia	10	9
Uygur	East Asia	10	9
Xibo	East Asia	9	7
Yakut	East Asia	25	23
Yi	East Asia	10	10

Population	Region	Aug. 12 2011	Further filtering
Adygei	West Eurasia	17	15
Basque	West Eurasia	22	20
Bedouin	West Eurasia	46	38
Druze	West Eurasia	42	32
French*	West Eurasia	28	27
Italian	West Eurasia	13	11
Orcadian	West Eurasia	13	13
Palestinian	West Eurasia	45	34
Russian	West Eurasia	23	22
Sardinian*	West Eurasia	28	27
Tuscan	West Eurasia	8	7
Balochi	South Asia	24	21
Brahui	South Asia	24	22
Burusho	South Asia	25	24
Hazara	South Asia	22	17
Kalash	South Asia	19	18
Makrani	South Asia	25	22
Pathan	South Asia	24	22
Sindhi	South Asia	24	22
Colombian	America	5	4
Karitiana*	America	13	8
Maya	America	21	18
Pima	America	14	11
Surui	America	8	6
Melanesian*	Oceania	11	9
Papuan*	Oceania	17	14

\* Indicates a population used in SNP ascertainment. Analysis of data from these populations should remove the individual used in SNP discovery, as they have highly biased SNP genotypes (all heterozygotes) relative to others in the same group.

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- <sup>12</sup> Genotyping Console:  
[http://www.affymetrix.com/browse/level\\_seven\\_software\\_products\\_only.jsp?productId=131535&categoryId=35625#1\\_1](http://www.affymetrix.com/browse/level_seven_software_products_only.jsp?productId=131535&categoryId=35625#1_1)
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[http://www.affymetrix.com/support/technical/whitepapers/dmet\\_plus\\_algorithm\\_whitepaper\\_v1.pdf](http://www.affymetrix.com/support/technical/whitepapers/dmet_plus_algorithm_whitepaper_v1.pdf) (pdf, 292 KB)
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# File S1

## Technical details of a SNP array optimized for population genetics

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### Overview

One of the promises of studies of human genetic variation is to learn about human history and also to learn about natural selection.

Array genotyping of hundreds of thousands of SNPs simultaneously—using a technology that produces high fidelity data with an error rate of ~0.1%—is in theory a powerful tool for these studies. However, a limitation of all SNP arrays that have been available to date is that the SNPs have been chosen in a complicated way for the purpose of medical genetics, biasing their frequencies so that it is challenging to make reliable population genetic inferences. In general, the way that SNPs have been chosen for arrays is so complicated that it has been effectively impossible to model the ascertainment strategy and thus to correct for the bias.

This technical note describes the design, validation, and manufacture of an array consisting of SNPs all ascertained in a clearly documented way. We anticipate that this will provide a useful resource for the community interested in learning about history and natural selection. We hope that this array will be genotyped in many different cohorts, as has been done, for example, in the Marshfield panel where approximately 800 microsatellites have been genotyped in diverse populations<sup>1,2,3,4,5</sup>. By establishing a common set of simply ascertained SNPs that have been genotyped in diverse populations, it should be possible to learn about human history not only in individual studies, but also through meta-analysis.

The array is designed as a union of 13 different SNP panels. In our experience, a few tens of thousands of SNPs is enough to produce powerful inferences about history with regard to summary statistics like measurements of  $F_{ST}$ . Thus, it is better for many analyses to have (for example) 13 sets of tens to hundreds of thousands of SNPs each with its own ascertainment strategy than a single set of 600,000 SNPs. We have included a particularly large number of SNPs from particularly interesting ascertainment—discovery in the two chromosomes of a single San Bushman, a single Yoruba West African, a single French, a single Han Chinese, and a single Papuan—as for some analyses like scans of selection it is valuable to have dense data sets of hundreds of thousands of SNPs. All SNPs chosen for the array were selected from sites in the genome that have read coverage from Neandertals, Denisovans, and chimpanzees, allowing users of the array to compare data from modern humans to archaic hominins and apes.

This array is not ideal for gene mapping, since: (i) No attempt has been made to tag common variation genome-wide. (ii) There are gaps in the genome where no homologous sequence is available from chimpanzee. (iii) Unlike many existing arrays, we have not oversampled SNPs in the vicinity of genes, or adjusting SNP density in order to fully tag haplotypes. Instead we simply sampled SNPs in proportion to their genomic density as discovered by sequencing.

The array is being made commercially available by Affymetrix. Importantly, the academic collaborators who have been involved in the design will not benefit from sales of the array (they

will not receive any financial compensation from Affymetrix). The CEPH-Human Genome Diversity Project (CEPH-HGDP) samples that were genotyped during the course of the project will not be used for any commercial purposes. Affymetrix deposited the genotypes of unrelated CEPH-HGDP samples, collected as part of the array development, into the CEPH-HGDP database on August 12, 2011, more than six months before commercial release of the array (in Spring 2012), and this genotyping data is freely available to the public.

### Design strategy for the 13 panels

#### (Panels 1-12) Discovery of heterozygous sites within 12 individuals of known ancestry

The first 12 SNP ascertainment strategies are based on the idea of the Keinan, Mullikin et al. Nature Genetics 2007 paper<sup>6</sup>. That paper takes advantage of the fact that by discovering SNPs in a comparison of two chromosomes from the same individual of known ancestry, and then genotyping in a larger panel of samples from the same population, one can learn about history in a way that is not affected by the frequency of the SNP in human populations. In particular, even though we may miss a substantial proportion of real SNPs in the individual (false-negatives), and even if a substantial proportion of discovered SNP are false-positives, we expect that the inferences about history using SNPs discovered in this way will be as accurate as what would be obtained using SNPs identified from deep sequencing with perfect readout of alleles.

To understand why false-negative SNPs should not bias inferences, we note that if a SNP is truly heterozygous in the individual in whom we are trying to discover it, there is exactly one copy of the ancestral allele and exactly one copy of the derived allele. Thus, conditional on the SNP being heterozygous in the discovery individual, its probability of being discovered is not further affected by whether it has a high or low minor allele frequency in the population. This contrasts with ascertainment strategies that discover SNPs in more than one individual, where there is always a real (and extremely difficult to quantify) bias toward missing rarer variants. By genotyping SNPs discovered in this way, and making a simple  $p(1-p)$  correction for discovery in two chromosomes (where  $p$  is the minor allele frequency), one can obtain an unbiased reconstruction of the allele frequency distribution in the population.

An important feature of this SNP discovery strategy is that false-positive SNPs (for example, due to sequencing error, mapping error, segmental duplications or copy number variation) are not expected to substantially bias inferences. The reason is that we have validated all candidate SNPs by genotyping them using a different technology, and we have required the genotypes to match the individuals in whom they were discovered. Thus, we expect to have a negligible proportion of false-positive SNPs on the final array.

This procedure has produced 12 panels of uniformly discovered SNPs, which can be used for allele frequency spectrum analysis. There is some overlap of SNPs across panels. Importantly, we have separately determined validation status for the SNPs in each panel, and have only used SNPs that validate in the same sample in which they were discovered. Thus, we have not biased toward SNPs with a high minor allele frequency, or that are polymorphic across multiple populations, which might be expected to have a higher chance of validation if we did not perform the validation in each discovery sample independently.

(Panel 13) SNPs where a randomly chosen San allele is derived relative to an archaic hominin. A 13<sup>th</sup> ascertainment strategy used alignments of three genomes: chimpanzee, Denisova (an archaic hominin from southern Siberia for whom there is 1.9× genome sequence coverage<sup>7</sup>), and San. We examined sites where we had ≥1-fold coverage of Denisova, and ≥3-fold coverage of San. We made an allele call for each individual by majority rule, randomly selecting an allele when there was a tie (this means that we are effectively sampling one of two haplotypes in the individual, and the allele call is not expected to be being biased if the individual is heterozygous at that site). We placed on the array the subset of sites where San is derived relative to both Denisova and chimpanzee, in this case requiring agreement between the Denisova and chimpanzee allele. These are sites that likely arose due to mutations in the last million years.

We chose to use San rather than another modern human for building this panel because there is evidence that the San are approximately symmetrically related to all other present-day humans<sup>8</sup>. Panel 13 is also the only one with SNPs from chromosome X (all the other panels are based on SNPs discovered in males), and thus this panel permits X-autosome comparisons.

### Description of the sequencing data and filtering used in SNP ascertainment

The sequencing data that we use for identifying candidate SNPs has been described in two recent papers: Green et al. 2010<sup>9</sup> and Reich et al. 2010<sup>7</sup>. The data were all generated in the Max Planck Institute in Leipzig using Illumina Genome Analyzer IIx (GAIIx) sequencing instruments via protocols that are described in refs. 9 and 7 (Table 1). Population genetic analyses for ref. 7 were carried out on the very data file that was used to select SNPs for the array.

**Table 1: Characteristics of the sequencing data we are using for SNP ascertainment**

Name	Identifier	Sequenced by	Genomic coverage*	Cutoff† A (Pr)	Cutoff† C (Pr)	Cutoff† G (Pr)	Cutoff† T (Pr)
Han	HGDP00778	Green 2010	3.8	16 (0.489)	14 (0.239)	17 (0.003)	15 (0.11)
Papuan1	HGDP00542	Green 2010	3.6	13 (0.051)	10 (0.119)	15 (0.434)	13 (0.880)
Yoruba	HGDP00927	Green 2010	4.3	17 (0.692)	14 (0.440)	18 (0.562)	16 (0.985)
San	HGDP01029	Green 2010	5.9	17 (0.830)	15 (0.914)	18 (0.649)	16 (0.877)
French	HGDP00521	Green 2010	4.4	17 (0.317)	16 (0.985)	18 (0.024)	17 (0.515)
Mbuti	HGDP00456	Reich 2010	1.2	17 (0.041)	14 (0.504)	17 (0.704)	16 (0.379)
Karitiana	HGDP00998	Reich 2010	1.1	18 (0.210)	14 (0.126)	17 (0.147)	17 (0.589)
Sardinian	HGDP00665	Reich 2010	1.3	19 (0.789)	15 (0.302)	18 (0.474)	17 (0.200)
Bougainville	HGDP00491	Reich 2010	1.5	18 (0.810)	14 (0.288)	17 (0.445)	16 (0.291)
Cambodian	HGDP00711	Reich 2010	1.7	18 (0.717)	14 (0.303)	17 (0.331)	16 (0.398)
Mongolian	HGDP01224	Reich 2010	1.4	18 (0.371)	15 (0.789)	17 (0.051)	16 (0.090)
Papuan2	HGDP00551	Reich 2010	1.4	17 (0.188)	14 (0.661)	17 (0.932)	16 (0.885)
Neandertal	Vindija.3.bones	Green 2010	1.3	27 (0.428)	26 (0.049)	27 (0.308)	27 (0.579)
Denisova	Phalanx	Reich 2010	1.9	40 (1.000)	40 (1.000)	40 (1.000)	40 (1.000)

\* Genomic coverage is calculated for the modern humans as (# of reads mapping to chimpanzee) × (read length which is 76bp for Green et al. 2010 and 101bp for Reich et al. 2010) × (0.95 as we filtered out the 5% of the lowest quality data) / (2.8 Gb). For the archaic hominins we report the coverage from the abstracts of Green et al. 2010 and Reich et al. 2010.

† For each base used in SNP discovery, we give the quality score cutoff and probability of acceptance at that cutoff (parentheses). The cutoffs are chosen to filter out the data of the lowest 5% quality for each nucleotide class (SI 6; Reich et al. 2010).

The 12 modern human samples are all from the CEPH-HGDP panel. A valuable feature of this panel is that DNA for all samples is available on request on a cost-recovery basis for researchers who wish to carry out further sequencing and genotyping analysis on these samples for the purpose of research into human population history<sup>8,10</sup>. Five of the samples (San, Yoruba, Han, French and a Papuan) were sequenced by Green et al. 2010 using Illumina paired-end 76bp reads<sup>9</sup>, while the remaining 7 (Mbuti, Sardinian, Karitiana, Mongolian, Cambodian, Bougainville, and a second Papuan) were sequenced by Reich et al. 2010 using Illumina paired-end 101bp reads<sup>7</sup>. All reads from all 12 samples were mapped to chimpanzee (*PanTro2*). To filter the sequence data for analysis, we used a similar procedure as described in Reich et al. 2010<sup>7</sup>, removing the lowest quality of 5% of nucleotides on a sample and nucleotide-specific basis to maximize the amount of sequencing data available for analysis. After this procedure, we had 3.6-5.9× coverage for the 5 samples and 1.1-1.7× for the 7 samples (Table 1).

We also used data from 4 ancient DNA samples to aid our choice of SNPs. To represent Neandertals, we used a pool of sequences from 3 bones from Vindija Cave in Croatia (Vi33.16, Vi33.25 and Vi33.26) for which we had 1.3× genome coverage altogether<sup>9</sup>. To represent Denisovans, we used data from a finger bone (fifth distal manual phalanx) from the Altai mountains of southern Siberia, with 1.9× coverage<sup>7</sup>.

#### All reads are mapped to chimpanzee and a chimpanzee allele is available

We mapped sequencing reads from modern and ancient genomes to the chimpanzee reference sequence (*PanTro2*) to avoid biases toward one present-day human group more than another.

#### We filtered out reads with a substantial probability of poor mapping

Each read that we analyzed had a mapping quality score (MAPQ) that reflects the confidence of its mapping to *PanTro2*. Based on empirical exploration of the usefulness of the scores, which were generated by either the ANFO or BWA software, we only used reads that had MAPQ of at least 90 for Neandertal (ANFO mapping), 37 for Denisova (BWA), and 60 for present-day humans (BWA). We also rejected reads if the alignment to the chimpanzee resulted in any insertion/deletion difference. This filter was applied in addition to the filtering of Table 1.

#### Filtering of sites with $\geq 2$ alleles not matching chimp across the humans used for SNP discovery.

At a small proportion of sites, we observe more than one non-ancestral allele in the individual sequencing data used for SNP discovery. Such sites cannot be due to a single historical mutation. Instead, the data must reflect at least two mutations or sequencing errors. We filter out such sites.

For a very small fraction of sites, we found that the derived allele is *different* depending on which human is used in SNP discovery (these are potentially triallelic SNPs in the population, although they are not triallelic in the discovery individual). We keep such sites in our list of SNPs for designing, and use multiple probe sets to assay such SNPs.

The raw data file that emerges from this process is available on the “orchestra” Harvard Medical School filesystem at: /groups/reich/CLEAN\_SNP\_ARRAY/rawsnps and is freely available from David Reich on request (a README file is in the same directory at rawsnps\_readme) (Table 2). For brevity, this file only lists the 2,173,116 SNPs where 2 copies of the derived and 1 copy of the ancestral allele are observed a hominin; these are the only SNPs that are candidates for inclusion. Thus, it is an abbreviated version of a larger file used in analyses for ref. 7.

### Filtering the nucleotide calls of the lowest reliability

- (a) We do not use nucleotides for which there is no valid nucleotide call for chimpanzee.
- (b) For Neandertals, we do not use nucleotides within 5 nucleotides of either end of the reads, because of the elevated rate of ancient DNA degradation errors that we empirically observe.
- (c) For Denisova, we do not use nucleotides within 1 nucleotide of either end of the read.
- (d) For both Neandertals and Denisova, we do not use nucleotides with sequence quality  $<40$ .
- (e) For present-day humans, we do not use nucleotides with sequence quality  $<T_{ij}$ , where  $T_{ij}$  is a threshold chosen such that half of nucleotides generated from individual  $i$  and of allele class  $j$  ( $j = A, C, G, T$ ) are less than this value. For nucleotides that have exactly a quality score of  $T_{ij}$ , we randomly choose ones to eliminate such that exactly 5% are dropped (note that this differs from the 50% used in Reich et al. 2010). The cutoffs used are presented in Table 1.
- (f) For the “Papuan1” individual from ref. 9 (HGDP00542), the sequencer had a high error rate at position 34 (41 on the reverse strand). We excluded data from position 34 for this individual.

**Table 2: Datafiles summarizing the SNP ascertainment for the population genetics array**

File name	Readme	Description	Entries
rawsnps	rawsnps_readme	This file contains all sites where there are at least 2 copies of a derived allele and 1 copy of the ancestral allele in 12 present-day humans, 3 Neandertals, and Denisova, and further filtered to be candidates for inclusion in the SNP array.	2, 173,116
ascertained	ascertained_readme	This file contains all SNPs chosen in any ascertainment panel (there are a few hundred that are triallelic and we list them on different lines, so the number of unique SNPs is 1,812,990).	1,813,579
screening	screening_readme	This file contains all probesets we considered for screening array design, as well as the metrics for prioritization and indicator variables indicating whether they were chosen. If chosen, a column indicates the genotyping outcome, and whether the SNP was taken forward to the production array.	3,882,158

Note: These files can be found in the Harvard Medical School orchestra filesystem at /groups/reich/CLEAN\_SNP\_ARRAY/.

### **1,353,671 SNPs for testing on an Affymetrix Axiom™ screening array**

#### 1,812,990 candidate SNPs discovered in 13 different ascertainment panels

We used the following algorithm to choose candidate SNPs for validating on the array.

- (a) We mapped all reads used for SNP discovery to the chimpanzee reference sequence, *PanTro2*, without using data from the human reference sequence at all for read mapping. This was important to avoid biases due to the ancestry of the human reference sequence.
- (b) We rediscovered all SNPs *de novo*, blinding ourselves to any prior information about whether the sites were polymorphic in present-day humans.
- (c) At all SNPs, we required coverage from at least 1 Neandertal read and at least 1 Denisova read. This is expected to result in bias toward locations of the genome where the ancient DNA tends to be better preserved or the sequencing technology tends to work better. However, there is no reason why it would be expected to result in a bias in allele frequencies toward one

modern human population more than another (as all Neandertal and Denisova reads are mapped to chimpanzee, and no modern human data influences the mapping). The availability of data from archaic hominins from each of the SNPs on our array should be of value for some types of population genetic analysis. (For a handful of sites, the Denisova and Neandertal alleles may not be the same as those seen in present-day humans, but we nevertheless considered these sites to be covered by Denisova and Neandertal as we were concerned that not doing so could introduce bias. Users can treat such sites how they wish.)

- (d) All A/T and C/G polymorphisms were excluded, since genotyping these SNPs requires twice the number of probes using the Axiom™ technology. Thus, removing them increases the number of SNPs we can include on a single array. Removing these SNPs has the additional benefit that it eliminates any strand ambiguity. (Illumina arrays do not genotype A/T or C/G SNPs, either.) However, it also had the disadvantage that A/T and C/G SNPs constitute the one class of SNPs that is believed to be immune to biased gene conversion. Thus, in population genetic analyses of the data generated from the array, it will be important to assess whether inferences are potentially explained by biased gene conversion.
- (e) For the SNPs for panels 1-12 (candidate heterozygotes in an individual of known ancestry), we required the observation of at least 2 copies of the derived (non-chimpanzee) and at least 1 copy of the ancestral allele in the studied person (Reich et al. 2010; SI 6). We did not include chromosome X SNPs from these panels as the 12 individuals were all male.
- (f) For the SNPs in panel 13 (derived in San relative to Denisova), we restricted to sites where we had  $\geq 3$ -fold read coverage of San and  $\geq 1$ -fold read coverage of Denisova.

A complication in choosing SNPs discovered in two individuals is that both the San and Denisova individuals are diploid. What we want is to have a panel of SNPs ascertained by comparing a single haploid Denisovan and a single haploid San chromosome, but if we are not careful, we are going to be biased toward the SNPs that are fixed differences. For example, if we accepted only SNPs where all Denisova reads matched chimpanzee and all San reads were derived, then we would bias against SNPs that were truly heterozygous.

To obtain data of the type that would be expected from sampling a single haploid Denisovan and a single haploid San chromosome, we picked the allele that was seen more often in each sample to represent that sample (if there was a tie in terms of the number of reads supporting each allele, we chose one allele at random). In this way, we are picking one of the two chromosomes from each individual (at random), and hence we are effectively sampling a haploid chromosome despite having diploid data. An additional benefit of using the majority rule is that we are also increasing the quality and reliability of the allele call, such that we expect a larger proportion of these SNPs to be real than in panels 1-12.

From the SNPs discovered in this way, we restrict our analysis to sites where Denisova matches the chimpanzee allele and where San is derived (we throw away sites where San is ancestral and Denisova is derived). The reason for this is that this is the only subset of SNPs that we can experimentally validate. To validate these SNPs, we can genotype the San individual and require the observation of an allele that differs from chimpanzee. In contrast, we cannot validate sites where San is ancestral and Denisova is derived, since the Denisova sample is extremely limited and does not provide enough for genotyping assays.

Some of the SNPs from panels 1-13 overlap. Thus, while the sum of the number of SNPs in each panel is 2,581,282, the number of unique SNPs is only 1,812,990. However, the fact that a SNP is

present in more than one panel does not mean that it has a higher likelihood of being validated for the array for a given ascertainment strategy. For SNP identified in more than one panel, we designed a single probe to test the SNP, but we assessed its validation status separately for each panel to avoid bias toward more easily validating more polymorphic SNPs (see below).

The perl script used for choosing SNPs is on the “orchestra” Harvard Medical School filesystem at: /groups/reich/CLEAN\_SNP\_ARRAY/newformat\_affypick.pl (available on request from David Reich). The output file is at /groups/reich/CLEAN\_SNP\_ARRAY/ascertained (available on request from David Reich). This list contains a single entry for each unique SNP, with the exception of triallelic sites that have multiple designs (thus, there are 1,813,579 entries rather than 1,812,990). A readme file is at /groups/reich/CLEAN\_SNP\_ARRAY/ascertained\_readme (available on request from David Reich) (Table 2). The number of SNPs that we selected using each strategy is summarized in Table 3.

**Table 3: Ascertainment of SNPs for panels 1-13**

Panel no.	Ascertainment	Sample ID	Genomic coverage	# SNPs found	# SNPs placed on screening array	# SNPs that validate on screening array	# SNPs that validate on final array
1	French	HGDP00521	4.4	333,492	241,707	123,574	111,970
2	Han	HGDP00778	3.8	281,819	204,841	87,515	78,253
3	Papuan1	HGDP00542	3.6	312,941	232,408	56,518	48,531
4	San	HGDP01029	5.9	548,189	401,052	185,066	163,313
5	Yoruba	HGDP00927	4.3	412,685	302,413	136,759	124,115
6	Mbuti	HGDP00456	1.2	39,178	28,532	14,435	12,162
7	Karitiana	HGDP00998	1.1	12,449	8,535	3,619	2,635
8	Sardinian	HGDP00665	1.3	40,826	29,358	15,260	12,922
9	Melanesian	HGDP00491	1.5	51,237	36,392	17,723	14,988
10	Cambodian	HGDP00711	1.7	53,542	38,399	20,129	16,987
11	Mongolian	HGDP01224	1.4	35,087	24,858	12,872	10,757
12	Papuan2	HGDP00551	1.4	40,996	29,305	14,739	12,117
13	Denisova-San	Den-HGDP01029	-	418,841	308,210	166,422	151,435
<i>Unique SNPs</i>				<i>1,812,990</i>	<i>1,354,003</i>	<i>599,175</i>	<i>542,399</i>
<i>Unique probe designs</i>				<i>1,941,079</i>	<i>1,385,672</i>	<i>605,069</i>	<i>546,581</i>

#### 1,941,079 unique flanking sequences corresponding to the 1,812,990 unique SNPs

To ensure clean SNP ascertainment, we followed a rigorous procedure whereby the flanking sequence assay for each SNP were chosen only based on sequencing data from chimpanzee and the modern human sample used in SNP ascertainment. Thus, while some SNPs were discovered in multiple panels, we did not use this information in probe design. We used the simple rules below to pick a probe, and if the optimal design was different depending on the sample in which the SNP was ascertained, we used more than one probe for the SNP.

For each SNP in each of the 13 ascertainment panels, we specified 71 base pair (bp) flanking sequences that would be used for probe designing as follows:

(a) *Ancestral and derived allele are specified based on the individuals used in SNP ascertainment.*

For each SNP in each panel, we specified the ancestral and derived alleles based on the two

alleles observed in SNP ascertainment, defining as “ancestral” the allele that matched chimpanzee. SNPs within any ascertainment panel almost always had two observed alleles, since we filtered out sites with three or more. However, for SNPs that were discovered in multiple panels, we performed the specification of the ancestral and derived allele independently, and thus for a small fraction of sites, there was a different derived allele depending on the ascertainment panel (even if flanking sequence were sometimes identical).

- (b) *Flanking sequence is specified entirely based on the modern sample used for SNP discovery.* For initial probe design, we provided 35 bp of flanking sequence on either side of the SNP. We started with 71 bp of sequence from the chimpanzee genome, *PanTro2*, centered on the SNP. To decrease the number of mismatches between the flanking sequence and any human that might be analyzed using the array, we “humanized” the flanking sequence based on the modern sample used for SNP discovery (importantly, only the discovery sample is used for the humanization of the sequence, and so the ancestry of other samples cannot bias results).

Specifically, for each of panels 1-13, we took all reads from the modern human used in SNP ascertainment that mapped to the flanking nucleotide. Where 100% of reads disagreed with *PanTro2*, we edited the flanking sequence to reflect that in the ascertainment sample. Otherwise, we kept the chimpanzee allele. An example is:

“acctggctccagGgccagcagctccgtcaAggtcc[G/A]ctgcatgaaactgatgaagggaggggcaccaggcg”. Here, capital [G/A] indicates the [chimp/alternate allele] at the SNP and other capital letters indicate bases edited from the chimpanzee reference to match the ascertainment sample. For ascertainment panel 13 (Denisova ancestral and a randomly chosen San allele derived), we did not use the Denisova genome in primer editing. Instead, we edited the sequence to match San whenever San consistently had a non-chimpanzee allele at all reads overlapping the site.

Because the steps above sometimes result in different flanking sequences for the same nucleotide (depending on the particular sequencing reads from the sample used in SNP ascertainment), we were left with more unique flanking sequences (n=1,941,079) than unique SNPs (n=1,812,991).

#### Procedure used to choose 1,385,671 oligonucleotide probes for the screening array

With the list of 1,951,079 flanking sequences, we needed to design oligonucleotide probes, or “probesets”, for a screening array. We blinded ourselves to prior knowledge about which probes worked in previous assays using the Axiom™ technology, since doing so would be expected to lead to a higher validation success rate for probes that have been previously tried on SNP arrays (introducing complex biases). For the same reason, we did not modify probe design based on using information in databases about polymorphism in flanking sequence. The only two types of information that were used in probe design were the physical chemistry considerations of which probes are expected to work well, and mapping information to the *PanTro2* chimp genome. All the metrics used are in a file on the “orchestra” Harvard Medical School filesystem /groups/reich/CLEAN\_SNP\_ARRAY/probesets, available on request from David Reich (Table 2). Details of the filtering procedure that we applied are as follows:

- (a) *We first identified 3,882,158 candidate probesets (two 30mers for each flanking sequence)*

For each of the 1,941,079 flanking sequences, it is possible to design two probesets corresponding to the 30 bp 5’ or 3’ direction of the SNP. We use the shorthand “red” to designate the 5’ probe and “green” to designate the 3’ probe, always referenced relative to the positive strand of the chimpanzee genome sequence *PanTro2* (Figure 1).





(b) *We next restricted analysis to 2,294,760 probesets predicted to have greater success*

Of the 3,882,158 candidate probesets (2 for each of 1,941,079 flanking sequences), we computed metrics that based on past experience were useful for predicting the success of genotyping. The values of the metrics are in /groups/reich/CLEAN\_SNP\_ARRAY/probesets (see probesets\_readme), available on request from David Reich. We applied the following filters to winnow the list to 2,294,760:

- (i) *Removing probesets that map to multiple positions in chimpanzee.*
- (ii) *Best BLAT hit to PanTro2 is much better than the second-best hit.* We used BLAT to map each 35 bp flanking sequence to *PanTro2*. We required a minimum of 33 bp of alignment, and required the difference between the first and second hits to be >5.
- (iii) *16mers within the probeset are relatively unique.* For each candidate 30 bp probeset, we examined each unique 16mer in a sliding window along the sequence (15 in all), and counted the number of exact matches in *PanTro2*. We defined “16mer-max” as the maximum number of exact matches seen for any of these 16-mers. In the experience of Affymetrix scientists who have worked on the Axiom™ technology, non-specific binding is unlikely when 16mer-max is small. We required “16mer-max” <110.
- (iv) *No runs of 4 G’s.* When more than 4 consecutive Gs stack up into quartets, hybridization tends to be compromised. We filtered out probes that had runs of 4 G’s (or 4 C’s),
- (v) *Terminal 5mer is not complemented elsewhere in the probeset.* We required the 5’ terminal 5mer to not have a reverse complement elsewhere in the probeset sequence, to minimize the tendency toward inter/intra probe annealing during hybridization, which in previous experience with the Axiom™ technology could cause a lower success rate.
- (vi) *Number of G and C nucleotides is >5.* We required that >5 of the nucleotides were either G or C. Previous experience suggests that probesets with extremely low G or C usually do not work well for hybridization assays.

(c) *A list of 1,477,155 probesets after eliminating redundancy*

For flanking sequences where both candidate probesets passed the filters above, we chose the probeset that was deemed more likely to succeed based on having a lower value of “16mer-max” metric. When both probesets had the same value of “16mer-max”, we used a random number generator to choose. This resulted in 1,525,604 candidate probesets.

Even after representing each flanking sequence by no more than one probeset, the resulting list contained 48,449 duplicative entries. This occurred when the same SNP (and probeset) had been independently selected in more than one of the 13 ascertainment panels. In such cases, the 71bp flanking sequence obtained as described above could be distinct for multiple SNP ascertainments, but sub-strings could be identical, so that it could happen that the 30mer that was selected to represent the SNP was identical. We therefore merged these probes to eliminate redundancy, leaving us with 1,477,155 unique probesets.

Our naming scheme for probesets contains a binary string of 13 characters providing the ascertainment information for that probe. Because we merged some probesets, we created a new ascertainment code called “asc.new”. This was generated by applying a bitwise-or operation to the binary strings of 13 characters corresponding to the ascertainment information for the redundant probes.

(d) *A final list of 1,385,672 probes that were placed on the screening array*

The 1,477,155 probes that passed our filters were more than could fit into the screening array. Thus, we ranked all the probes based on their “16mer-max” score, breaking ties using a random number generator (lower values have a higher rank). After this ranking, all probes had “16mer-max” of no more than 110, and we were left with 1,385,672 probes.

## Design, genotyping, and analysis of screening array

### Design of the screening array

We designed two arrays to screen these 1.39 million probesets (0.69 million probesets fit onto a single screening array). To minimize bias, we randomized the probes with respect to which one of the 2 screening arrays was used to test them. We also used standard chip design strategies that are applied at Affymetrix for determining probe location in each screen design. The number of SNPs from each panel placed on the screening arrays is presented in Table 3.

The probesets used in the screening array are named like [chr]\_[pos]\_[alleles]\_[asc.new]\_[strand], with the 5 data fields indicating *PanTro2* chromosome / *PanTro2* physical position / ancestral-derived alleles, and the 13 bit binary string indicating the ascertainment panels in which the SNP was discovered, and the strand (f=forward or r=reverse compared to *PanTro2*).

### Genotyping the screening array

Three 96-well plates of samples were genotyped on the 2 screening arrays in early 2011, with the goals of (a) deciding if each SNP passes quality control criteria and can be taken forward to the production array, and (b) generating useful data for preliminary population genetic analysis.

*Validation plate #1:* The goal of validation plate #1 was to genotype the same 12 modern human samples that were used in SNP discovery and in which the derived allele was observed, and to validate that we observe an allele at these samples that is distinct from the ancestral allele seen in primates. There was a high level of redundancy on the plate:

- Each of the 12 modern human samples was genotyped 6 times (six different wells)
- The chimpanzee and bonobo were each genotyped 6 times
- The gorilla and orangutan were each genotyped 4 times

The position of each sample on the plate (except for the upper right 4 wells which were left empty for control samples) was assigned using a random number generator.

*Validation plates #2 and #3:* We also took advantage of the screening array to genotype 2 plates of samples from CEPH-HGDP populations. We genotyped 184 samples from the same populations that were used in SNP discovery, consisting of French (n=28), Han (n=27), Papuan (n=17), San (n=6), Yoruba (n=21), Mbuti (n=13), Karitiana (n=13), Sardinian (n=28), Melanesian (n=11), Cambodian (n=10) and Mongola (n=10). Analysis of the data allowed us to perform further validation of the SNPs on the array, and also to assess whether useful population genetic analyses can be generated from these genotyping data.

### Determining which SNPs “validated”

All samples were genotyped using the Axiom™ Assay 2.0 and genotype calls were made using the apt-probeset-genotype program in the Affymetrix Power Tools (APT) package<sup>11</sup> (the apt-probeset-genotype program is integrated in the Genotyping Console (GTC) version 4.1 software<sup>12</sup>, which also provides visualization tools). Both programs use the Axiom™ GT1 algorithm to call genotypes. The algorithm adapts pre-positioned clusters to the data using a probability-based method. Clustering is carried out in two dimensions, log ratio ( $\log_2(A) - \log_2(B)$ ) and size ( $\log_2(A + B)/2$ ). The algorithm derives from BRLMM-P<sup>13,14</sup>, which clusters in a single signal-contrast dimension, and is tuned to the signal characteristics of the Axiom™ assay.

To avoid ascertainment bias, only the sample used for SNP discovery, chimpanzees and bonobos, were used to assign a validation status to each candidate SNP for each of the 13 ascertainment panels. After an initial inspection of the data from Validation Plate #1, we chose not to use the data from the gorilla and orangutan as part of validation. This is because for a substantial fraction of SNPs, the signal intensities were different for one or both alleles in the apes than in humans, which we hypothesized was due to differences in the flanking DNA sequence under the primers. This occurred most often in gorilla and orangutan, and is expected to confound the genotyping algorithm, and thus we restricted to chimpanzees and bonobos.

We used a separate procedure for deciding whether a SNP was validated for ascertainment panels 1-12 (SNPs discovered as a heterozygote in a single modern human) or in ascertainment panel 13 (SNPs where San was derived and Denisova was ancestral). Table 4 summarizes the number of SNPs that validate in one, two, or all three genotyping runs.

**Table 4: Results of genotyping on the screening array**

Panel	Ascertainment	Sample ID	Screened SNPs	Validated in 3 runs	Validated in 2 runs	Validated in 1 run
1	French	HGDP00521	241,707	94,139	12,283	17,700
2	Han	HGDP00778	204,841	66,885	8,341	12,780
3	Papuan1	HGDP00542	232,408	43,622	5,308	8,000
4	San	HGDP01029	401,052	139,689	18,266	27,648
5	Yoruba	HGDP00927	302,413	103,670	13,542	20,017
6	Mbuti	HGDP00456	28,532	11,123	1,499	1,950
7	Karitiana	HGDP00998	8,535	2,839	326	511
8	Sardinian	HGDP00665	29,358	11,555	1,630	2,232
9	Melanesian	HGDP00491	36,392	13,626	1,769	2,527
10	Cambodian	HGDP00711	38,399	15,606	1,954	2,772
11	Mongolian	HGDP01224	24,858	9,890	1,312	1,824
12	Papuan2	HGDP00551	29,305	11,256	1,464	2,181
13	Denisova-San	Den-HGDP01029	308,210	107,708	26,280	32,845
<i>Unique probesets</i>			<i>1,385,391</i>	<i>455,942</i>	<i>82,978</i>	<i>110,248</i>

### *Panels 1-12 (SNPs ascertained as a heterozygote in a single modern human)*

We performed the ascertainment three times by carrying out three genotyping runs: once using only the 6 chimpanzee replicates to represent the apes, once using only the 6 bonobo replicate, and once using both chimpanzee and bonobo, a total of 12 *Pan* samples.

- a) We required that all 6 human replicates are called heterozygous and all apes homozygous.

- b) We required that the homozygous cluster and heterozygous cluster were well resolved in the clustering space, referred to as “A vs. M space”. M and A are defined as

$$M = \left[ \log_2 \left( A_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) - \log_2 \left( B_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) \right]$$

$$A = \left[ \log_2 \left( A_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) + \log_2 \left( B_{\text{allele}_{\text{signal}_{\text{intensity}}}} \right) \right] / 2$$

Based on the experience of Affymetrix scientists with the Axiom™ 2.0 Assay, five conditions were required to be satisfied to ensure that the clusters were well resolved in clustering space. Using the definitions “hetero”=samples called heterozygous, “homo”=samples called homozygous, “std”=standard error, and “abs”=absolute value, the 5 conditions that we required to be met to consider a SNP as validated were:

- (i)  $\text{mean}(M_{\text{hetero}}) \in (-1, 1)$  and  $\text{mean}(M_{\text{homo}}) \in (-\infty, -1] \text{ or } [1, +\infty)$
  - (ii)  $\text{mean}(A_{\text{hetero}}) - 2 \times \text{std}(A_{\text{hetero}}) > \text{mean}(A_{\text{homo}}) - 2 \times \text{std}(A_{\text{homo}})$
  - (iii)  $\text{mean}(A_{\text{hetero}}) \geq 8.5$
  - (iv)  $\Delta_{\text{sep}} \geq 5$ , where  $\Delta_{\text{sep}}$  is computed using the following formula
 
$$\Delta_{\text{sep}} = \text{abs} \left( \frac{\text{mean}(M_{\text{homo}}) - \text{mean}(M_{\text{hetero}})}{[\text{std}(M_{\text{homo}}) + \text{std}(M_{\text{hetero}})]/2} \right)$$
  - (v)  $\text{abs}(\text{mean}(M_{\text{hetero}}) - \text{mean}(M_{\text{homo}})) > 1$
- c) We required that the chimpanzee and bonobo agree at least partially in their genotype calls, for SNPs where a call was made in at least one of the three genotyping runs. The goal was to exclude SNPs that completely disagreed between chimpanzees and bonobos, which would imply that the ancestral allele determination was unreliable at these sites.

*Panel 13 (SNPs where San was derived and Denisova was ancestral)*

SNPs were considered as “validated” for panel 13 if they passed the following validation criteria:

- a) All six San replicates were called heterozygote or derived homozygotes, and all ape replicates were called ancestral homozygotes.
- b) SNPs in chromosome X were not in pseudoautosomal regions (PARs) and were called as homozygous derived in the San individual.
  - (i) PARs were determined by converting coordinates of the human PARs (Build36) to *PanTro2* using the liftOver program from the UCSC genome browser.
  - (ii) The San sample is a male, so SNPs in this chromosome are expected to be homozygotes.
- c) The following three criteria were required to be met to make sure that the clusters were located around expected locations and well separated (that is, they were well resolved)
  - (i)  $\text{mean}(M_{\text{ape}_{\text{homo}}}) \in (-\infty, -1] \text{ or } [1, +\infty)$
  - (ii)  $\text{mean}(A_{\text{ape}_{\text{homo}}}) \geq 9.5$
  - (iii)  $\text{std}(M_{\text{ape}_{\text{homo}}}) < 0.45$
- d) For a SNP passing the above criteria in any one of three genotyping runs, we required that the chimpanzee and bonobo genotypes, compared across runs, did not completely disagree.

For autosomal SNPs in Panel 13, the true genotype for San replicates could be either heterozygote or derived homozygote. To avoid potential bias that might cause either heterozygous or derived

homozygous genotypes to be validated at a higher rate, we did not apply any metrics involving measuring the coherence of the heterozygous or derived homozygous clusters. Thus, the criteria used for Panel 13 are looser than the other 12 panels, which we expect will minimize the potential for ascertainment bias at the cost of lowering the validation rate of SNPs.

#### *Filtering of SNPs based on the genotyping of 184 samples on Validation Plates #2 and #3*

Up to this point, all decisions about which SNPs were considered to be validated were based entirely on the results of genotyping Validation Plate #1 on the screening array. As these decisions were only based on data from apes and the human sample used in SNP discovery, this is a perfectly clean strategy from the point of view of SNP ascertainment.

In practice on inspection of the genotyping results for Validation Plates #2 and #3, we found that a small fraction of SNPs that passed the validation filters described above were completely heterozygous in modern humans, or nearly so. This is unexpected based on population genetic considerations, and suggests that these SNPs overlap segmental duplications (which we did not screen out from our array in the interests of having a completely unbiased ascertainment procedure). An observation of more than half of individuals being heterozygous is unexpected at a true SNP. In an unstructured population for a SNP of frequency  $p$ , the expected proportion of heterozygous genotypes is  $2p(1-p)$ , which is at most 0.5, and the expected rate of heterozygous genotypes is less than this for a structured population.

We therefore implemented a further filter where for each SNP, we computed its frequency across all of the  $N$  modern humans on Validation Plates #2 and #3 that successfully genotyped ( $N \geq 184$ ). We then counted the observed number of heterozygous genotypes  $het_{obs}$  versus the conservative expectation of  $het_{exp} = Np_{het}$ , where  $p_{het} = 2p(1-p)$  (here,  $p$  is the empirical frequency of the derived allele,  $(het_{obs} + 2(\text{number of homozygous genotypes})/2N)$ ). By dividing the difference between the observed and the expected number of heterozygous genotypes by the binomially distributed standard error, we can compute an approximately normally distributed Z-score:

$$Z = \frac{het_{obs} - het_{exp}}{\sqrt{Np_{het}(1 - p_{het})}}$$

We filtered out SNPs for which  $Z > 5$ , which is expected to remove at most a fraction  $3.0 \times 10^{-7}$  of true SNPs by chance. This removed 1,932 additional SNPs.

#### *Summary of results of the validation genotyping*

A total of 605,069 unique probesets (599,175 unique SNPs) were validated by the screen. The numbers of validated SNPs in each panel is listed in Table 3.

#### **Taking forward SNPs to a final production array**

All of the 605,069 probesets that passed the validation criteria after genotyping on the screening array were tiled on the final production array. In addition to those 605,069 “Human Origins” SNPs, a set of 87,044 “Compatibility” SNPs were also tiled on the final production array, choosing from a set of 8.8 million SNPs that had previously been validated using the Axiom 2.0<sup>TM</sup> genotyping assay. Among those SNPs, there are 2,091 non-PAR chromosome Y SNPs, 259 mitochondrial SNPs, and 84,694 SNPs that overlap between the Affymetrix SNP Array 6.0 and Illumina 650Y array. No A/T or C/G SNPs were selected for the Compatibility SNPs, as they take up more space on the array (two probes for each SNP), so that excluding them thus allowed us to

maximize information from the array. For the 84,694 nuclear SNPs, we increased the value of the SNPs by maximizing the fraction that were also genotyped on the Affymetrix SNP Array 5.0 (78.5%), that were covered by sequencing from Neandertal (53.9%) and Denisova (64.7%), and for which a chimpanzee allele was available (nearly 100%).

### Validation of the final SNP array through genotyping of 952 CEPH-HGDP samples

We attempted to genotype 952 CEPH-HGDP samples that were previously determined to be unrelated up to second degree relatives<sup>15</sup>. This genotyping had three goals:

(a) *Round 2 validation: Evaluating the performance of every SNP in the final product array*

Although all of the SNPs that were tiled on the final product array had previously been validated in screening arrays, there is variability in how an assay performs on a real product. Hence after manufacturing the final SNP array, we genotyped 952 unrelated CEPH-HGDP samples (including the 12 modern human samples used in SNP ascertainment) using the final product array. We used these data to create a list of SNPs that had gone through two rounds of validation and would be robust for genotyping.

(b) *Building up prior distributions for SNP calling*

The Axiom™ GT1 algorithm makes more accurate genotype calling for a SNP if it has prior distributions for the 3 genotype clusters (AA, AB, and BB) based on data (by default, the Axiom™ GT1 algorithm uses the generic prior distributions of the 3 clusters, which is just a best guess). Because the CEPH-HGDP panel has such a large number of samples from diverse ancestries, we expect to observe clusters from all 3 genotypes for most SNPs. This allows us to construct prior distributions that could be used for SNP calling in other projects.

(c) *Creating a dataset that will be useful for population genetics*

The genotyping of the unrelated CEPH-HGDP samples has the benefit that it creates a dataset that will be widely available to the population genetics community. Users who wish to genotype samples that they are interested in on this array, will be able to merge the data that they collect with data collected on the CEPH-HGDP samples, to enable a richer comparison of genetic variation in one region to worldwide variation.

**Table 5. Eighteen HGDP samples that did not pass quality control**

Identifier	Population	Reason removed
HGDP00009	Brahui	Failed DQC
HGDP00708	Colombian	<97% genotype call rate
HGDP01266	Mozabite	<97% genotype call rate
HGDP01267	Mozabite	<97% genotype call rate
HGDP01403	Adygei	<97% genotype call rate
HGDP00885	Russian	<97% genotype call rate
HGDP00886	Russian	<97% genotype call rate
HGDP00795	Orcadian	<97% genotype call rate
HGDP00804	Orcadian	<97% genotype call rate
HGDP00746	Palestinian	<99% concordance with Illumina 650Y data
HGDP00326	Kalash	<99% concordance with Illumina 650Y data
HGDP00274	Kalash	<99% concordance with Illumina 650Y data
HGDP00304	Kalash	<99% concordance with Illumina 650Y data
HGDP00309	Kalash	<99% concordance with Illumina 650Y data
HGDP01361	Basque	<99% concordance with Illumina 650Y data
HGDP00710	Colombian	<99% concordance with Illumina 650Y data
HGDP01376	Basque	<99% concordance with Illumina 650Y data
HGDP01009	Karitiana	anomalous ancestry relative to others in group

### Filtering out 18 samples that did not genotype reliably

After assaying all 952 samples, we filtered to 934 samples as follows (Table 5):

- (a) We filtered out 9 samples that did not pass standard Axiom™ 2.0 Array QC metrics: a “DQC” score (chip-level quality metric) and a call rate score. This suggests problems such as low input DNA amount, contamination of DNA samples, or technical issues with hybridization. These 9 samples were excluded from the genotyping calling.
- (b) We excluded an additional 9 samples based on their genotype patterns. Of these, 8 were excluded because there was a greater than 1% genotype discrepancy between our current data and earlier data from the Illumina 650Y array genotyped on the same samples **Error! Bookmark not defined.** We also excluded HGDP01009, an individual that our data (as well as analyses of previous datasets) suggests is a sample whose ancestry is an outlier relative to others from the Karitiana group, suggesting a history of recent gene flow with other Native American populations.

### Special filters applied to chromosome X and Y data

Chromosome X occurs in only a single copy in men but in two copies in women. Chromosome Y occurs only in men. This means that SNPs on these chromosomes need to be treated differently from autosomal SNPs; for chromosome X we genotyped males and females separately, and for chromosome Y we only genotyped males. For males, we required that genotypes on both chromosome X and Y were always homozygous.

### Filtering out additional probesets based on the genotyping of the final array

Not all probesets tiled onto the final array performed well enough to produce reliable results. We filtered out a total of 58,488 additional probesets by sequentially applying the seven criteria listed in Table 6. Three of the criteria used in Table 6 require more detailed explanation.

**Table 6. Phase 2 validation (determining probesets for which we report genotypes)**

Order	Filter	Removed	Definition
1	SNP call rate $\geq 95\%$	23,476	(no. of called samples) / (no. of genotyped samples = 943)
2	Concordance	31,415	For panels 1-12, the SNP must be heterozygous in the sample used in ascertainment (for panel 13, heterozygous or derived homozygous).
3	het_rate > 5	79	This is the same metric used in SNP validation
4	het_offset > -0.5	892	See below for explanation
5	resolution score $\geq 3.6$	2,450	See below for explanation
6	chrX annotation	94	Panel 13 SNPs that are <i>PanTro2</i> chrX but not <i>hg18</i> chrX are removed.
7	chrX SNPs separate males and females	82	See below for explanation
Total removed by all filters		58,488	

**het\_offset:** Using the definition of “A vs. M space” described in the discussion of the screening array filters, we defined a quantity called *het\_offset* that measures whether the heterozygous genotype is appropriately intermediate between the homozygous clusters. For a probeset with three observed genotype clusters (AA, AB, and BB), it is defined as

$$\text{het\_offset: } \text{mean}(M_{AB}) - \frac{\text{mean}(M_{AA}) + \text{mean}(M_{BB})}{2}$$

For a probeset with one observed homozygous and one heterozygous cluster, it is defined as:

$$het\_offset: mean(M_{AB}) - mean(M_{AA|BB})$$

For other situations, *het\_offset* is not used as a filter.

**resolution score:** This is again defined in the M space of the “A vs M space”, and it measures how well the heterozygous cluster separates from the homozygous cluster(s). We define:

$$resolution = \frac{abs(mean(M_{homo}) - mean(M_{hetero}))}{sd(M_{homo}) + sd(M_{hetero})} \times 2$$

For a probeset with three observed genotype clusters (AA, AB, and BB), the resolution score is defined as:  $\min(resolution_{AA-AB}, resolution_{BB-AB})$ . For a probeset with one observed homozygous cluster and one observed heterozygous cluster, the resolution score is the resolution between two clusters. For other situations, the resolution score is NA.

**chromosome X SNPs separate males and females:** It was found that for some chromosome X SNPs, female samples and male samples formed distinct genotype clusters. Such cases most likely are not real chromosome X SNPs. One possible explanation for this pattern is SNPs derived from fixed differences between homologous chromosome X and chromosome Y sequences<sup>15,16</sup>. We removed chromosome X SNPs that meet all of the following criteria

1. All called male samples have the same genotype call
2. Greater than 85% of called female samples have the same genotype call and there are at most 2 different called genotypes for females
3. The distance between the male genotype cluster center and the major female genotype cluster center is at least 0.8 units in the M genotype clustering space.

The number of final validated SNPs is given in the final column of Table 7, and this is the set of SNPs for which we publically released data for 934 unrelated CEPH-HGDP samples on August 12, 2011. Table 7 summarizes the SNPs on the final product array.

**Table 7. Summary of SNPs in the final array**

Category	number of probesets	number of SNPs
Human Origins	546,581	542,399
Chromosome Y	2,091	2,091
Mitochondrial DNA	259	259
Compatibility	84,694	84,694
<i>Total</i>	<i>633,625</i>	<i>629,443</i>

Upon commercial release of the array, Affymetrix is planning to release user-friendly software that will facilitate SNP calling using each of the ascertainment panels. Users who are interested in any particular ascertainment will open up one of 14 available folders of files (the first 13 corresponding to the SNPs in each ascertainment, and the 14<sup>th</sup> corresponding to all SNPs together). Users will then be able to use that folder (which will include ascertainment-panel specific priors) to call genotypes relevant to any given ascertainment panel.



The genotyping data on the 934 unrelated CEPH-HGDP samples that we collected as part of this project has been made freely available without restriction to the community by depositing the data into the CEPH-HGDP database on August 12, 2011 ([http://ftp.cephb.fr/hgdp\\_suppl0/](http://ftp.cephb.fr/hgdp_suppl0/)). There are no restrictions on using these data and publishing papers based on these data.

In addition to the dataset of 934 CEPH-HGDP samples that we released on August 12, 2011, we have also carried out further filtering to create a dataset of 828 samples that might be more useful for some population genetic analyses. This dataset, which is the one that we used for the analyses of population history reported in the present paper, is available for downloading from the Reich laboratory website ([http://genetics.med.harvard.edu/reich/Reich\\_Lab/Welcome.html](http://genetics.med.harvard.edu/reich/Reich_Lab/Welcome.html)). To generate this dataset, we started with the dataset that was released to the CEPH-HGDP website on August 12, 2011, and then carried out population-specific Principal Component Analysis to identify individual samples that are outliers with respect to their own populations (consistent with admixture with other populations without the last few generation). These individuals were then filtered out of the dataset, allowing us to analyze data from a homogeneous population sample. Table 8 lists the number of samples from each population before and after the filtering.

**Table 8. Number of CEPH-HGDP samples in each of the two datasets reported here**

Population	Region	Aug. 12 2011	Further filtering
BantuKenya	Africa	11	10
BantuSouthAfrica	Africa	8	6
BiakaPygmy	Africa	23	20
Mandenka	Africa	22	20
Mbuti*	Africa	13	12
Mozabite	Africa	27	25
San*	Africa	6	5
Yoruba*	Africa	22	22
Cambodian*	East Asia	10	10
Dai	East Asia	10	10
Daur	East Asia	9	7
Han*	East Asia	34	33
Han-NChina	East Asia	10	10
Hezhen	East Asia	9	9
Japanese	East Asia	29	28
Lahu	East Asia	8	7
Miao	East Asia	10	10
Mongola*	East Asia	10	8
Naxi	East Asia	9	7
Oroqen	East Asia	9	8
She	East Asia	10	10
Tu	East Asia	10	9
Tujia	East Asia	10	9
Uygur	East Asia	10	9
Xibo	East Asia	9	7
Yakut	East Asia	25	23
Yi	East Asia	10	10

Population	Region	Aug. 12 2011	Further filtering
Adygei	West Eurasia	17	15
Basque	West Eurasia	22	20
Bedouin	West Eurasia	46	38
Druze	West Eurasia	42	32
French*	West Eurasia	28	27
Italian	West Eurasia	13	11
Orcadian	West Eurasia	13	13
Palestinian	West Eurasia	45	34
Russian	West Eurasia	23	22
Sardinian*	West Eurasia	28	27
Tuscan	West Eurasia	8	7
Balochi	South Asia	24	21
Brahui	South Asia	24	22
Burusho	South Asia	25	24
Hazara	South Asia	22	17
Kalash	South Asia	19	18
Makrani	South Asia	25	22
Pathan	South Asia	24	22
Sindhi	South Asia	24	22
Colombian	America	5	4
Karitiana*	America	13	8
Maya	America	21	18
Pima	America	14	11
Surui	America	8	6
Melanesian*	Oceania	11	9
Papuan*	Oceania	17	14

\* Indicates a population used in SNP ascertainment. Analysis of data from these populations should remove the individual used in SNP discovery, as they have highly biased SNP genotypes (all heterozygotes) relative to others in the same group.

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- <sup>12</sup> Genotyping Console:  
[http://www.affymetrix.com/browse/level\\_seven\\_software\\_products\\_only.jsp?productId=131535&categoryId=35625#1\\_1](http://www.affymetrix.com/browse/level_seven_software_products_only.jsp?productId=131535&categoryId=35625#1_1)
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[http://www.affymetrix.com/support/technical/whitepapers/dmet\\_plus\\_algorithm\\_whitepaper\\_v1.pdf](http://www.affymetrix.com/support/technical/whitepapers/dmet_plus_algorithm_whitepaper_v1.pdf) (pdf, 292 KB)
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