

Training data set: Who buys computer?

age	income	student	credit rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$$\text{Info}(D) = I(1,2) = -\frac{9}{12} \log\left(\frac{9}{12}\right) - \frac{3}{12} \log\left(\frac{3}{12}\right) = 0.940$$

$$\text{Info}_{age}(D) = \frac{5}{12} I(2,3) + \frac{4}{12} I(4,0) + \frac{3}{12} I(3,2)$$

$$= \frac{5}{12} \left[-\frac{3}{5} \log\left(\frac{3}{5}\right) - \frac{2}{5} \log\left(\frac{2}{5}\right) \right] + \frac{4}{12} \left[-\frac{1}{2} \log\left(\frac{1}{2}\right) - \frac{1}{2} \log\left(\frac{1}{2}\right) \right] + \frac{3}{12} \left[-\frac{3}{4} \log\left(\frac{3}{4}\right) - \frac{1}{4} \log\left(\frac{1}{4}\right) \right] = 0.644$$

$$\text{Info}_{income}(D) = \frac{4}{12} I(3,0) + \frac{1}{12} I(4,2) + \frac{7}{12} I(3,2)$$

$$= \frac{4}{12} \left[-\frac{2}{3} \log\left(\frac{2}{3}\right) - \frac{1}{3} \log\left(\frac{1}{3}\right) \right] + \frac{1}{12} \left[-\frac{1}{4} \log\left(\frac{1}{4}\right) - \frac{3}{4} \log\left(\frac{3}{4}\right) \right] + \frac{7}{12} \left[-\frac{3}{4} \log\left(\frac{3}{4}\right) - \frac{1}{4} \log\left(\frac{1}{4}\right) \right] = 0.911$$

$$\text{Info}_{student}(D) = \frac{5}{12} I(1,0) + \frac{3}{12} I(3,4)$$

$$= \frac{5}{12} \left[-\frac{1}{2} \log\left(\frac{1}{2}\right) - \frac{1}{2} \log\left(\frac{1}{2}\right) \right] + \frac{3}{12} \left[-\frac{3}{7} \log\left(\frac{3}{7}\right) - \frac{4}{7} \log\left(\frac{4}{7}\right) \right] = 0.779$$

$$\text{Info}_{credit}(D) = \frac{9}{12} I(1,2) + \frac{3}{12} I(3,2)$$

$$= \frac{9}{12} \left[-\frac{5}{9} \log\left(\frac{5}{9}\right) - \frac{4}{9} \log\left(\frac{4}{9}\right) \right] + \frac{3}{12} \left[-\frac{1}{3} \log\left(\frac{1}{3}\right) - \frac{2}{3} \log\left(\frac{2}{3}\right) \right] = 0.992$$

$$\text{Gain}(\text{age}) = 0.940 - 0.644 = 0.296$$

$$\text{Gain}(\text{income}) = 0.940 - 0.911 = 0.029$$

$$\text{Gain}(\text{student}) = 0.940 - 0.779 = 0.161$$

$$\text{Gain}(\text{credit}) = 0.940 - 0.992 = 0.048$$