

Training data set: Who buys computer?

age	income	student	credit rating	buys computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
31...40	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
31...40	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
31...40	medium	no	excellent	yes
31...40	high	yes	fair	yes
>40	medium	no	excellent	no

$$Info(D) = I(1,5) = -\frac{1}{5} \log\left(\frac{1}{5}\right) - \frac{4}{5} \log\left(\frac{4}{5}\right) = 0.940$$

$$Info_{age}(D) = \frac{5}{5} I(2,3) + \frac{4}{5} I(1,4) + \frac{1}{5} I(3,2) \\ = \frac{5}{5} \left[-\frac{2}{5} \log\left(\frac{2}{5}\right) - \frac{3}{5} \log\left(\frac{3}{5}\right) \right] + \frac{4}{5} \left[-\frac{1}{4} \log\left(\frac{1}{4}\right) - \frac{3}{4} \log\left(\frac{3}{4}\right) \right] + \frac{1}{5} \left[-\frac{3}{2} \log\left(\frac{3}{2}\right) - \frac{2}{2} \log\left(\frac{2}{2}\right) \right] = 0.914$$

$$Info_{income}(D) = \frac{4}{5} I(3,1) + \frac{1}{5} I(1,4) + \frac{1}{5} I(2,3) \\ = \frac{4}{5} \left[-\frac{3}{4} \log\left(\frac{3}{4}\right) - \frac{1}{4} \log\left(\frac{1}{4}\right) \right] + \frac{1}{5} \left[-\frac{1}{1} \log\left(\frac{1}{1}\right) - \frac{3}{1} \log\left(\frac{3}{1}\right) \right] + \frac{1}{5} \left[-\frac{2}{2} \log\left(\frac{2}{2}\right) - \frac{1}{2} \log\left(\frac{1}{2}\right) \right] = 0.911$$

$$Info_{student}(D) = \frac{3}{5} I(2,1) + \frac{1}{5} I(3,4) \\ = \frac{3}{5} \left[-\frac{2}{3} \log\left(\frac{2}{3}\right) - \frac{1}{3} \log\left(\frac{1}{3}\right) \right] + \frac{1}{5} \left[-\frac{3}{4} \log\left(\frac{3}{4}\right) - \frac{1}{4} \log\left(\frac{1}{4}\right) \right] = 0.939$$

$$Info_{credit}(D) = \frac{4}{5} I(1,2) + \frac{1}{5} I(3,3) \\ = \frac{4}{5} \left[-\frac{1}{4} \log\left(\frac{1}{4}\right) - \frac{3}{4} \log\left(\frac{3}{4}\right) \right] + \frac{1}{5} \left[-\frac{3}{3} \log\left(\frac{3}{3}\right) - \frac{2}{3} \log\left(\frac{2}{3}\right) \right] = 0.912$$

$$Gain(age) = 0.940 - 0.914 = 0.026$$

$$Gain(income) = 0.940 - 0.911 = 0.029$$

$$Gain(student) = 0.940 - 0.939 = 0.001$$

$$Gain(credit) = 0.940 - 0.912 = 0.028$$