

III B. Tech I Semester Regular/Supplementary Examinations, March - 2021**SIGNALS AND SYSTEMS**

(Electrical and Electronics Engineering)

Time: 3 hours

Max. Marks: 70

Note: 1. Question Paper consists of two parts (**Part-A** and **Part-B**)2. Answer **ALL** the question in **Part-A**3. Answer any **FOUR** Questions from **Part-B****PART -A****(14 Marks)**

1. a) Define continuous time unit impulse and unit step functions. [2M]
- b) State Parseval's relation for continuous time Fourier transforms. [2M]
- c) What are the effects of sampling rate? [2M]
- d) A signal $x(t)$ has energy E . Calculate the energy of the signal $x(t/2)$. [3M]
- e) If $X(s) = \frac{s+2}{s^2+8s+25}$, find $x(t)$, $t \geq 0$. [3M]
- f) Determine the Z transform of $x(n) = a_n \cos(\omega_0 n)u(n)$. [2M]

PART -B**(56 Marks)**

2. a) Find whether the following signals are periodic or not? If periodic, determine the fundamental period. [7M]
 - i) $x(t) = \cos \frac{\pi}{3} t + \sin \frac{\pi}{4} t$, ii) $x(t) = 3u(t) + 2\sin 2t$.
- b) Show that sinusoidal functions are orthogonal functions. [7M]
3. a) Find the exponential Fourier series representation of the signal $x(t) = \cos^2 t$. [7M]
- b) State and prove the following properties of Fourier transform: [7M]
 - i) Frequency shifting, ii) Differentiation in time.
4. a) State and prove the sampling theorem for low pass signals. [7M]
- b) The signal $x(t) = \cos 5\pi t + 0.3 \cos 10\pi t$ is instantaneously sampled. Find the maximum interval of sampling. [7M]
5. a) Find the convolution of the following signals using graphical method: $x(t) = e^{-3t} u(t)$; $h(t) = u(t-3) - u(t-5)$. [7M]
- b) Sketch and explain characteristics of an ideal Low pass, High pass and Band pass filters. [7M]
6. a) Find the Laplace transform and ROC for the signal $x(t) = e^t \sin 2t$, $t \leq 2$. [7M]
- b) State and prove Time scaling property of Laplace transforms. [7M]
7. a) Prove that the sequence $x(n) = a^n u(n)$ and $x(n) = -a^n u(-n-1)$ have the same $X(z)$ and differ only in ROC. Also plot their ROC. [7M]
- b) Find the inverse Z-transform of $X(z) = \frac{z(z-1)}{(z+1)^3(z+2)^2}$; ROC: $|z| > 2$ [7M]

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**PART -A****(14 Marks)**

1. a) Define power and energy signals. [2M]
- b) What is Fourier spectrum? [2M]
- c) State sampling theorem for band pass signals. [2M]
- d) Compare ESD and PSD. [3M]
- e) Compute the Laplace transform of the signal  $x(t)=te^{-2t} \sin 2t u(t)$  using properties of Laplace transform. [3M]
- f) State initial and final value theorems in Z-transform. [2M]

**PART -B****(56 Marks)**

2. a) Find the even and odd parts of the signal  $x(t) = e^{-2t} \cos(t)$ . [7M]
- b) A rectangular function  $f(t)$  is defined by [7M]
 
$$f(t) = 1 \text{ for } 0 < t < \pi$$

$$-1 \text{ for } \pi < t < 2\pi$$

Approximate this function by a waveform  $\sin(t)$  over the interval  $(0, 2\pi)$  such that mean square error is minimum.
3. a) Obtain the exponential Fourier series for the function  $f(t) = A \sin(\omega t)$  over the interval  $0 \leq t \leq \pi$ . Also find the trigonometric Fourier coefficients from exponential Fourier coefficients. [7M]
- b) What is Hilbert transform? How does it differ from other transforms? [7M]
4. a) Explain the effects of under sampling. [7M]
- b) The spectral range of a signal extends from 5.6 MHz to 6.8 MHz. Find the minimum sampling rate and maximum sampling time. [7M]
5. a) For an initially relaxed system, the impulse response  $h(t)$  is given by  $h(t) = [e^{-2t} - e^{-3t}]u(t)$ . Find the excitation  $x(t)$  to produce an output  $y(t) = t e^{-2t} u(t)$ . [7M]
- b) Obtain the conditions for the distortion less transmission through a system. [7M]
6. a) Write the properties of ROC for Laplace transforms. [7M]
- b) Find the inverse Laplace transform of  $X(s) = -\frac{1000}{s^2 - 100}$  ROC:  $-10 < \text{Re}(s) < 10$ . [7M]
7. a) Find the Inverse Z-transform of the sequence  $X(Z) = \frac{z}{2z^2 - 3z + 1}$ , ROC:  $|z| > 1$  [7M]
- b) Prove that, for causal sequences, the ROC is the exterior of a circle of radius  $r$ . [7M]

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1. a) State the relation between step, ramp and delta functions. [2M]
- b) What is the effect of Hilbert transform? [2M]
- c) When does aliasing occur? How can it be avoided? [2M]
- d) Determine the ESD of a gate function of width  $\tau$  and amplitude A. [3M]
- e) Compute the Laplace transform of the signal  $x(t)=t^2e^{-3t}u(t)$  using properties of Laplace transform. [3M]
- f) Mention the methods of finding the inverse Z-transform. [2M]

**PART -B****(56 Marks)**

2. a) Check linearity and causality of the following systems: [7M]
  - i)  $\frac{d^3y(t)}{dt^3} + 7\frac{d^2y(t)}{dt^2} + 9t\frac{dy(t)}{dt} + y(t) = x^2(t)$
  - ii).  $y(n) = x(n)x(n-2)$ .
- b) Show that the functions  $\sin n\omega_0 t$  and  $\cos m\omega_0 t$  are orthogonal over a complete period for all values of m and n. [7M]
3. a) State and prove the following properties of Fourier transform: [7M]
  - i) time shifting, ii) convolution.
- b) Derive the expressions for the trigonometric Fourier series coefficients. [7M]
4. a) Find the Nyquist rate and Nyquist interval for the following signals: [7M]
  - i)  $x(t) = 2 \text{ sinc}(100\pi t)$ , ii)  $x(t) = -10 \sin(40\pi t) \cos(300\pi t)$ .
- b) Differentiate between natural and flat top sampling methods. [7M]
5. a) Prove that the autocorrelation function of an energy signal and its energy spectral density are Fourier transform pairs. [7M]
- b) Suppose that the signal  $x(t)=u(t+0.5)-u(t-0.5)$  and the signal  $h(t)=e^{j\omega_0 t}$ . Determine a value of  $\omega_0$  which ensures that  $y(0)=0$ , where  $y(t)=x(t)*h(t)$ . [7M]
6. a) Find the Laplace Transform of the signal  $x(t) = e^{-at}u(t)$  and find its ROC. [7M]
- b) If  $X(s) = \frac{s+2}{s^2+8s+25}$ , find  $x(t)$ ,  $t \geq 0$ . [7M]
7. a) Find the Z-transform of the following sequences: [7M]
  - i)  $x(n) = (1 + 2^n + 3^n)u(n)$ , ii)  $y(n) = x(n+1)u(n)$ ,
- b) State and Prove Initial and Final value theorems in z-transform. [7M]

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PART -A**(14 Marks)**

1. a) Show that $\delta(n) = u(n) - u(n-1)$. [2M]
- b) State Dirichlet's conditions. [2M]
- c) Define Nyquist rate and Nyquist interval. [2M]
- d) Prove that $R_{12}(\tau) = R_{21}(-\tau)$. [3M]
- e) Find the Laplace transform and ROC for the signal $x(t) = e^t \sin 2t, t \leq 2$. [3M]
- f) Mention the relationship between s-plane and z-plane. [2M]

PART -B**(56 Marks)**

2. a) Define ramp signal. Illustrate with example. And sketch the following signal [7M]
 $y(t) = r(t) - r(t-2) - r(t-3) + r(t-4)$.
- b) Prove that the complex exponential signals are orthogonal functions. [7M]
3. a) State and explain the significance of Dirichlet's Conditions. [7M]
- b) Find the Fourier transform of the following signals: [7M]
 i) Signum function, ii) Rectangular function.
4. a) Find the Nyquist rate Nyquist interval for the following signals: [7M]
 i) $\text{rect}(300t)$ ii) $-10\sin(40\pi t) \cos(300\pi t)$.
- b) State and explain the sampling theorem for band pass signals. [7M]
5. a) Find the convolution of the signals $x_1(t) = e^{-at}u(t)$; $x_2(t) = e^{-bt}u(t)$ using [7M]
 Fourier transform.
- b) Derive the relation between rise time and bandwidth of a low pass filter. [7M]
6. a) Prove that the signals $x(t) = e^{-at}u(t)$ and $x(t) = -e^{-at}u(-t)$ have the same $X(s)$ and [7M]
 differ only in ROC. Also plot their ROCs.
- b) Obtain the relation between Laplace transform and Fourier transform. [7M]
7. a) Find the z-transform and ROC of [7M]

$$x(n) = 3\left(\frac{5}{7}\right)^n u(n) + 2\left(-\frac{1}{3}\right)^n u(n).$$
- b) Distinguish between Fourier, Laplace, and Z-transform. [7M]
