

**I B. Tech II Semester Supplementary Examinations, Nov/Dec - 2019****MATHEMATICS-III**

(Com to AE, AME, CE, CSE, IT, EIE, EEE, ME, ECE, Metal E, Min E, E Com E, Agri E, Chem E, PCE, PE)

Time: 3 hours

Max. Marks: 70

Note: 1. Question paper consists of two parts (**Part-A** and **Part-B**)2. Answering the question in **Part-A** is Compulsory3. Answer any **FOUR** Questions from **Part-B****PART -A**

1. a) If  $A = \begin{bmatrix} 123 \\ 246 \\ 4812 \end{bmatrix}$  then find rank of A. (2M)
- b) If 1,2,3 are the Eigen values of matrix A, then Eigen values of  $A^{-1}$ . (2M)
- c) What is the Nature of the quadratic form If 1 0, -1 are Eigen values of form the quadratic form. (2M)
- d) What is an asymptote of the curve? (2M)
- e) Find  $\beta(1,1)$  (2M)
- f) Prove that  $3y^4z^2\bar{i} + z^3x^2\bar{j} - 3x^2y^2\bar{k}$  is a solenoidal vector. (2M)
- g) State Gauss divergence theorem. (2M)

**PART -B**

2. a) Solve the equations  $x + y - 2z + 3w = 0, x - 2y + z - w = 0, 4x + y - 5z + 8w = 0, 5x - 7y + 2z - w = 0$ . (7M)
- b) Solve the system of equations  $x + y + z = 6, x - y + 2z = 5, 3x + y + z = 8, 2x - 2y + 3z = 7$  by Gauss Jordan method. (7M)
3. a) Verify Cayley -Hamilton theorem for  $A = \begin{bmatrix} -1 & 2 & -2 \\ 1 & 2 & 1 \\ -1 & -1 & 0 \end{bmatrix}$  also find  $A^{-1}$  (7M)
- b) Find Rank index and signature of quadratic form  $10x^2 + 2y^2 + 5z^2 - 4xy - 10xz + 6yz$  by orthogonal reduction. (7M)
4. a) Trace the curve  $ay^2 = x^2(a - x)$  (7M)
- b) Find the volume of the sphere  $x^2 + y^2 + z^2 = a^2$  using triple integration. (7M)

5. a) Evaluate  $\int_0^{\infty} x^6 e^{-2x} dx$  (7M)
- b) Show that  $\int_0^{\infty} \frac{x^a}{a^x} dx = \frac{\Gamma(a+1)}{(\log a)^{a+1}} (a > 1)$  (7M)
6. a) if  $\vec{f}$ ,  $\phi$  be differentiable vector and scalar functions respectively, then prove that  $\nabla \cdot (\phi \vec{f}) = (\nabla \phi) \cdot \vec{f} + \phi (\nabla \cdot \vec{f})$  (7M)
- b) Prove that  $\nabla \left( r \nabla \left( \frac{1}{r^3} \right) \right) = \frac{3}{r^4}$  (7M)
7. a) Apply Green's theorem to evaluate  $\oint_C (2xy - x^2) dx + (x^2 + y^2) dy$  where C is bounded by  $y = x^2$  and  $x = y^2$ . (7M)
- b) If  $\vec{F} = 6z \vec{i} + (2x + y) \vec{j} - x \vec{k}$ , then Evaluate  $\iint_S \vec{F} \cdot \hat{n} ds$  where S is the region bounded by the cylinder  $x^2 + y^2 = 9$ ,  $x = 0, y = 0, z = 0$  and  $y = 8$ . (7M)