(2 points each) Circle the best answer:

- (i) The Mohr-failure envelope for a rock as a distinct parabolic curve, which failure model would provide the best capability to predict the failure of the rock.
 - (a) Hoek-Brown
 - (b) von Mises
 - (c) Mohr-Coulomb
- (ii) True or False? A typical range for Poisson ratio in rocks is between $0.2 < \nu < 0.6$
 - (a) True (b) False
- 2 € 0.5
- (iii) Which of the following is not a standard assumption of poroelasticity.
 - (a) There is an interconnected pore system uniformly saturated with fluid.
 - (b) The pore pressure, the total stress acting on the rock externally, and the stresses acting on the grains are statistically defined.
 - (c) The total volume of the pore system is large compared to the volume of the rock.
- (iv) True or False? The elastic behavior of an *isotropic* solid is fully characterized by three independent constants.
 - (a) True
 - (b) False
- (v) True or False? A typical value of Biot's coefficient for petroleum reservoir rocks would be 0.2.
 - (a) True
 - (b) False
- (vi) Which of the following conditions is true in a triaxial compression test for principle stresses, S_1, S_2, S_3
 - (a) $S_1 > S_2 = S_3$
 - (b) $S_1 < S_2 = S_3$
 - (c) $S_1 = S_2 = S_3$
- (vii) So-called cap failure models provide the ability to model
 - (a) inelastic effects occurring for increasing hydrostatic pressure.
 - (b) failure in pure shear.
 - (c) inelastic effects due to slip on crystallographic planes.

(viii) Simplifying the Kirsch equations	at a vertical wellbore	wall, it can be sho	wn that the difference in
minimum and maximum hoop st difference.	ress in the wellbore is	s what factor times	s the horizontal principle
(a) 2			
(b) 4			
(c) 10			
(ix) In a vertical wellbore, we expect b	oreakouts to occur alor	ig the direction of	
(a) S_v .			
(b) S_{Hmax} .			
(c) S_{hmin} .			
(x) For a friction coefficient of $\mu = 0$. principle stresses at around 3.1, the	6 we can estimate both his estimate derives from	ands on the ratio of om what idea?	largest-to-smallest $in\ situ$
(a) Frictional faulting equilibrium			
(b) Conservation of mass			
(c) Tectonic static equilibrium			
(xi) Raising the drilling mud weight a	bove the frac gradient	will lead to	
(a) breakouts.			
(b) drilling induced tensile fractu	res		
(c) washouts.	1009		
	1 1 1 1 1 1 1	lestwicel modical	tivities wellhore breakouts
(xii) Using wellbore imaging technique will have what appearance on the	es such as ultrasonic log e televiewer?	gs or electrical resist	tivities, wendore breakouts
(a) vertical shaded areas			
(b) horizontal shaded areas			
(c) spiraling shaded areas			
(xiii) True or False? A stable wellbore	is defined as one that i	s absent from any b	reakouts.
(a) True			
(b) False			
(xiv) In a vertical wellbore, we expect	drilling induced tensile	e fractures to occur	along the direction of
(a) S_v .			
(b) S_{Hmax} .			
(c) Sharing			

(xv) True or False? In a lower hemispherical projection plot associated with drilling deviated wells, the outermost concentric ring, i.e. the edge of the plot, represents a vertical well.

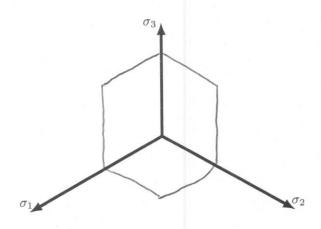
(a) True
(b) False

(4 points each) Short answer:

(i) A displacement field for a one dimensional bar is given as $u(x) = 3x^2$, what is the strain in the bar?

$$\varepsilon(x) = \frac{3x}{2x} = 6x$$

(ii) Sketch a Mohr-Coulomb failure surface in the π -plane on the figure.

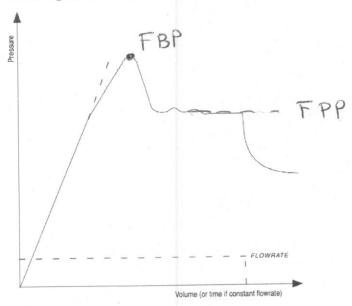


(iii) List two reasons why tensile strength is relatively unimportant in reservoir geomechanics.

1. The tensile strength of rocks is neglible,

2. The in situ stress in the earth is compressive. compressive.

(iv) On the figure below that schematically represents an extended leakoff-test



Label the formation breakdown pressure and the fracture propagation pressure.

(v) You are performing triaxial rock strength tests in the lab. Starting with Hooke's law for an isotropic solid, express volumetric strain in terms of axial and confining stress.

$$\tilde{S} = K \, \mathcal{E}_{VOL} \, \tilde{I} + Z \mu \, \left(\tilde{\mathcal{E}} - \frac{1}{3} \, \mathcal{E}_{VOL} \, \tilde{I} \right) \quad \text{Use} \quad K = \frac{S_{11} + S_{12} + S_{33}}{3 \, \mathcal{E}_{VOL}} = \frac{S_{VOL}}{\tilde{\mathcal{E}}_{VOL}}$$

$$= S_{VOL} \, \tilde{I} + Z \mu \, \left(\tilde{\mathcal{E}} - \frac{1}{3K} \, S_{VOL} \, \tilde{I} \right) \quad S_{olive} \quad \text{for} \quad \tilde{\mathcal{E}}_{vol}$$

$$\tilde{\mathcal{E}} = \frac{1}{Z \mu} \left(\tilde{S} - S_{OL} \, \tilde{I} \right) + \frac{1}{3K} \, S_{VOL} \, \tilde{I}$$

$$\tilde{\mathcal{E}} = \left[\frac{\mathcal{E}_{I}}{\mathcal{E}_{I}} \right] \quad \mathcal{E}_{I} = \left[\frac{\mathcal{E}_{I}}{\mathcal{E}_{I}} \right] \quad \mathcal{E}_{I} = \frac{1}{Z \mu} \left(\sigma_{I} - S_{VOL} \right) + \frac{1}{3K} \, S_{VOL} = \frac{1}{Z \mu} \, \sigma_{I} + \left(\frac{1}{3K} - \frac{1}{Z \mu} \right) \, S_{VOL}$$

$$\mathcal{E}_{I} = \frac{1}{Z \mu} \left(\sigma_{I} - S_{VOL} \right) + \frac{1}{3K} \, S_{VOL} = \frac{1}{Z \mu} \, \sigma_{I} + \left(\frac{1}{3K} - \frac{1}{Z \mu} \right) \, S_{VOL}$$

$$\mathcal{E}_{I} = \frac{1}{Z \mu} \left(\sigma_{I} - S_{VOL} \right) + \frac{1}{3K} \, S_{VOL} = \frac{1}{Z \mu} \, \sigma_{I} + \left(\frac{1}{3K} - \frac{1}{Z \mu} \right) \, S_{VOL}$$

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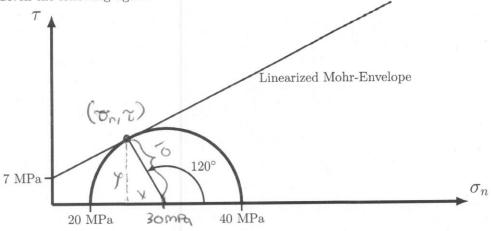
$$\mathcal{E}_{VOL} = \mathcal{E}_{1} + \mathcal{E}_{2} + \mathcal{E}_{3} = \mathcal{E}_{1} + 2\mathcal{E}_{2}$$

$$\mathcal{E}_{VOL} = \frac{1}{2\mu} \left(\sigma_{1} + 2\sigma_{2} \right) + \left(\frac{2}{9\kappa} + \frac{1}{3\mu} \right) \left(\sigma_{1} + 2\sigma_{2} \right)$$

$$= \left(\frac{5}{6\mu} + \frac{2}{9\kappa} \right) \left(\sigma_{1} + 2\sigma_{2} \right)$$

(10 points)

Given the following figure:



Estimate the unconfined compressive strength of the material.

$$X = 10 \cos 60 = 5$$
 $Y = 10 \sin 60 = 5\sqrt{3}$
 $T = 5\sqrt{3}$
 $T = 5\sqrt{3}$
 $T = 5\sqrt{3}$
 $T = 5\sqrt{3} - 7 = 0.0664$
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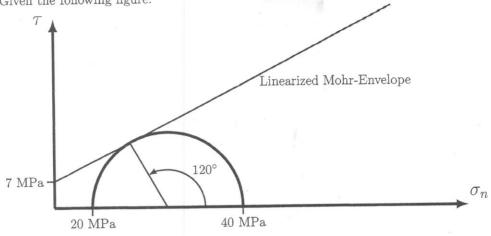
$$G = 2 (S_0) \left[\sqrt{\mu^2 + 1} + 0.0664 \right] =$$

$$\approx 2 (7) \left[\sqrt{0.0664 + 1} + 0.0664 \right] \approx 14.96$$

$$G \approx 15 \text{ MPa}$$

(10 points)

Given the following figure:



Estimate the unconfined compressive strength of the material.

Alternatively, if you interpret 120° as 2B

$$\beta = \frac{\pi}{4} + \frac{1}{2} \tan^{3} \mu$$

$$\tan \left(2\beta - \frac{\pi}{2}\right) = \mu = \frac{1}{3} \approx 0.577 \approx 0.58$$

$$G = 25, \left[\sqrt{\mu^{2}-1}\right] + \mu = 24.24$$

$$\left[\cos 24\right] \text{ MPa}$$

(15 points) Lab strength tests on dry rock samples, i.e. no pore fluid, with peak shear strength values have been fit to the linear relationship $S_1 = 22.8 \text{ MPa} + 4.12 \text{ MPa} S_3$. What is the unconfined compressive strength C_0 and internal friction coefficient μ_I for this rock.

$$C_0 = 22.8 \text{ mPa}$$
 $n = 4.12$
 $M_J = \frac{n-1}{2\sqrt{n}} = \frac{4.12-1}{2\sqrt{4.12}} \approx 0.76 \% 557$
 $M_J \approx 0.77$

(15 points) The reservoir conditions around a vertical well are as follows: The vertical stress is 58 MPa and the minimum horizontal stress is 48 MPa. Given laboratory measurements $\lambda_p = 0.75$, $C_0 = 35$ MPa, $\mu_I = 1.0$ and tensile strength T = 2 MPa, determine the wellbore pressure, P_m that will cause simultaneous initiation of breakouts and tensile fractures. You can ignore temperature effects.

Hint: Tensile fractures will occur when the hoop stress is more tensile that the tensile strength of the rock. Recall that λ_p is the ratio of pore pressure to overburden stress.

At wellbore wall:

$$G_{\Theta\Theta}^{min} = 3G_{Hmin} - G_{Hmex} - \Delta P = -T$$

$$= 3(S_{Hmin} - P_p) - S_{Hmex} + P_p - (P_m - P_p)$$

$$= 3S_{Hmin} - S_{Hmex} + P_p - P_m = -T$$

$$\Rightarrow P_m = 3S_{Hmin} - S_{Hmex} + P_p + T \quad (\triangle)$$

$$P_{m} = \frac{-C_{0} - 4P_{p} + P_{p}q + 8S_{hmin} + 3T}{4 + q} = \frac{-C_{0} + \lambda S_{v}(q - 4) + 8S_{hmin} + 3T}{4 + q}$$

$$P_{m} = \frac{-35 + (0.75)(58)(5.82 - 4) + 8(48) + 3(2)}{4 + (5.82)} \approx 44,2122$$

≈ 44 MPa

(15 points) The reservoir conditions around a vertical well are as follows: The vertical stress is 58 MPa and the minimum horizontal stress is 48 MPa. Given laboratory measurements $\lambda_p = 0.75$, $C_0 = 35$ MPa, $\mu_I = 1.0$ and tensile strength T = 2 MPa, determine the wellbore pressure, P_m that will cause simultaneous initiation of breakouts and tensile fractures. You can ignore temperature effects.

Hint: Tensile fractures will occur when the hoop stress is more tensile that the tensile strength of the rock. Recall that λ_p is the ratio of pore pressure to overburden stress.

Alternatively,

$$S_{Hmax} = \frac{(o + 2P_p + \Delta P + \Delta P^{+} \Delta P^{$$