

# Introduction to Programming

## Lab Session 3

(With material from the ETH Zurich course “Introduction to Programming”)

September 6, 2016



## In this Lab

- ▶ Understanding contracts: preconditions, postconditions (a second attempt)
- ▶ Exercises on class invariant.

## Contracts

# Precondition (from the previous lab)

Property that a feature imposes on clients:

# Precondition (from the previous lab)

Property that a feature imposes on clients:

*square\_root (x: REAL): REAL*

-- Returns the square root number of 'x'

# Precondition (from the previous lab)

Property that a feature imposes on clients:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'

**require**

*x*\_positive:  $x \geq 0$

# Precondition (from the previous lab)

Property that a feature imposes on clients:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'

**require**

x\_positive:  $x \geq 0$

A feature without a **require** clause is always applicable, as if the precondition reads

**require**

always\_ok: **True**

## Precondition principle

A *client* calling a feature must make sure that the *precondition* holds before the call.



## Precondition principle

A *client* calling a feature must make sure that the *precondition* holds before the call.

A client that calls a feature without satisfying its precondition is faulty (*buggy*) software.

# Postcondition (from the previous lab)

Property that a feature guarantees on termination

## Postcondition (from the previous lab)

Property that a feature guarantees on termination

*square\_root (x: REAL): REAL*

-- Returns the square root number of 'x'

# Postcondition (from the previous lab)

Property that a feature guarantees on termination

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'

**require**

*x*\_positive:  $x \geq 0$

# Postcondition (from the previous lab)

Property that a feature guarantees on termination

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'

**require**

*x*\_positive:  $x \geq 0$

**ensure**

result\_value:  $x = \mathbf{Result} * \mathbf{Result}$

# Postcondition (from the previous lab)

Property that a feature guarantees on termination

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'

**require**

*x\_positive*:  $x \geq 0$

**ensure**

*result\_value*:  $x = \mathbf{Result} * \mathbf{Result}$

A feature without an **ensure** clause always satisfies its postcondition, as if the postcondition reads

**ensure**

*always\_ok*: **True**

# Postcondition principle

## Postcondition principle

A feature must make sure that, if its precondition held at the beginning of its execution, its *postcondition* will hold at the end.

# Postcondition principle

## Postcondition principle

A feature must make sure that, if its precondition held at the beginning of its execution, its *postcondition* will hold at the end.

A feature that fails to ensure its postcondition is *buggy* software.



# Precondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

# Precondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**do**

-- to implement later

...

**end**

# Precondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**do**

-- to implement later

...

**end**

The precondition is *True*

# Precondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**do**

-- to implement later

...

**end**

The precondition is *True*: it is too weak. It accepts incorrect values (give me an example), together with all correct ones

# Precondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**do**

-- to implement later

...

**end**

The precondition is *True*: it is too weak. It accepts incorrect values (give me an example), together with all correct ones: the precondition is *complete* and *unsound*.

## Precondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

## Precondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

correct\_x:  $x > 10$

**do**

-- to implement later

...

**end**

## Precondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

correct\_x:  $x > 10$

**do**

-- to implement later

...

**end**

The precondition is too strong.



## Precondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

correct\_x:  $x > 10$

**do**

-- to implement later

...

**end**

The precondition is too strong. It accepts all correct values, but not all the possible correct values (give me an example)

## Precondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

correct\_x:  $x > 10$

**do**

-- to implement later

...

**end**

The precondition is too strong. It accepts all correct values, but not all the possible correct values (give me an example): the precondition is *incomplete* and *sound*.

## Precondition example (attempt 3)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

## Precondition example (attempt 3)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

x\_positive:  $x \geq 0$

**do**

-- to implement later

...

**end**

## Precondition example (attempt 3)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x\_positive*:  $x \geq 0$

**do**

-- to implement later

...

**end**

The precondition is *complete* and *sound*.

# Postcondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

x\_positive:  $x \geq 0$

**do**

-- to implement later

**end**

# Postcondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

x\_positive:  $x \geq 0$

**do**

-- to implement later

**end**

The postcondition is *True*

# Postcondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x\_positive*:  $x \geq 0$

**do**

-- to implement later

**end**

The postcondition is *True*: it is too weak. It guarantees all the correct values, but not all of the guaranteed values are correct (give me an example)



# Postcondition example (attempt 1)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x\_positive*:  $x \geq 0$

**do**

-- to implement later

**end**

The postcondition is *True*: it is too weak. It guarantees all the correct values, but not all of the guaranteed values are correct (give me an example): the postcondition is *incomplete* and *sound*.

## Postcondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x*\_positive: *x*  $\geq$  0

**do**

-- to implement later

**ensure**

result\_ok: **Result**  $\geq$  10

**end**

## Postcondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x*\_positive:  $x \geq 0$

**do**

-- to implement later

**ensure**

result\_ok: **Result**  $\geq 10$

**end**

The postcondition is too strong

## Postcondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x*\_positive:  $x \geq 0$

**do**

-- to implement later

**ensure**

result\_ok: **Result**  $\geq 10$

**end**

The postcondition is too strong. does not guarantee all the correct values (give me an example), but the ones it does guarantee are correct

## Postcondition example (attempt 2)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

*x*\_positive:  $x \geq 0$

**do**

-- to implement later

**ensure**

result\_ok: **Result**  $\geq 10$

**end**

The postcondition is too strong. does not guarantee all the correct values (give me an example), but the ones it does guarantee are correct : *complete* and *unsound*.

## Postcondition example (attempt 3)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

x\_positive:  $x \geq 0$

**do**

-- to implement later

**ensure**

result\_ok: **Result** \* **Result** = *x*

**end**

## Postcondition example (attempt 3)

Add pre- and postconditions to:

*square\_root* (*x*: *REAL*): *REAL*

-- Returns the square root number of 'x'.

**require**

x\_positive:  $x \geq 0$

**do**

-- to implement later

**ensure**

result\_ok: **Result** \* **Result** = *x*

**end**

The postcondition *complete* and *sound*.

# (Un)sound and (in)complete pre/post-conditions

Let  $P$  and  $Q$  be two assertions.



# (Un)sound and (in)complete pre/post-conditions

Let  $P$  and  $Q$  be two assertions.

If a feature needs  $P$ , then:

- ▶ if  $Q \Rightarrow P$ , then  $Q$  is said to be a *sound* precondition; otherwise  $Q$  is said to be an *unsound* precondition;
- ▶ if  $P \Rightarrow Q$ , then  $Q$  is said to be a *complete* precondition; otherwise  $Q$  is said to be an *incomplete* precondition.

# (Un)sound and (in)complete pre/post-conditions

Let  $P$  and  $Q$  be two assertions.

If a feature needs  $P$ , then:

- ▶ if  $Q \Rightarrow P$ , then  $Q$  is said to be a *sound* precondition;  
otherwise  $Q$  is said to be an *unsound* precondition;
- ▶ if  $P \Rightarrow Q$ , then  $Q$  is said to be a *complete* precondition;  
otherwise  $Q$  is said to be an *incomplete* precondition.

If a feature ensures  $P$ , then:

- ▶ if  $P \Rightarrow Q$ , then  $Q$  is said to be a *sound* postcondition;  
otherwise  $Q$  is said to be an *unsound* postcondition;
- ▶ if  $Q \Rightarrow P$ , then  $Q$  is said to be a *complete* postcondition;  
otherwise  $Q$  is said to be an *incomplete* postcondition.

# Example

**feature**

*f (x: REAL): REAL*

**require**

*x  $\geq$  0*

**do**

**Result** := *x.power (2)*

**ensure**

**Result**  $\geq$  0

**end**

Then:

# Example

**feature**

*f (x: REAL): REAL*

**require**

*x >= 0*

**do**

**Result** := *x.power (2)*

**ensure**

**Result** >= 0

**end**

Then:

- ▶ the assertion  $x > 0$  is

# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;

# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;
- ▶ the assertion  $x > -5$  is

# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;
- ▶ the assertion  $x > -5$  is an *unsound* and *complete* precondition and a *sound* and *incomplete* postcondition;

# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;
- ▶ the assertion  $x > -5$  is an *unsound* and *complete* precondition and a *sound* and *incomplete* postcondition;
- ▶ the assertion  $x < -5$  is



# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;
- ▶ the assertion  $x > -5$  is an *unsound* and *complete* precondition and a *sound* and *incomplete* postcondition;
- ▶ the assertion  $x < -5$  is an *unsound* and *incomplete* precondition and an *unsound* and *incomplete* postcondition;

# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;
- ▶ the assertion  $x > -5$  is an *unsound* and *complete* precondition and a *sound* and *incomplete* postcondition;
- ▶ the assertion  $x < -5$  is an *unsound* and *incomplete* precondition and an *unsound* and *incomplete* postcondition;
- ▶ the assertion  $x \geq 0$  is

# Example

**feature**

$f(x: \text{REAL}): \text{REAL}$

**require**

$x \geq 0$

**do**

**Result**  $:= x.\text{power}(2)$

**ensure**

**Result**  $\geq 0$

**end**

Then:

- ▶ the assertion  $x > 0$  is a *sound* and *incomplete* precondition and an *unsound* and *complete* postcondition;
- ▶ the assertion  $x > -5$  is an *unsound* and *complete* precondition and a *sound* and *incomplete* postcondition;
- ▶ the assertion  $x < -5$  is an *unsound* and *incomplete* precondition and an *unsound* and *incomplete* postcondition;
- ▶ the assertion  $x \geq 0$  is a *sound* and *complete* precondition and a *sound* and *complete* postcondition.

# Class invariant

Property that is true of the current object at any *observable* point

# Class invariant

Property that is true of the current object at any *observable* point

```
class BANK_ACCOUNT
```

```
...
```

```
    balance: INTEGER
```

```
        -- 'balance' of the account
```

```
...
```

# Class invariant

Property that is true of the current object at any *observable* point

```
class BANK_ACCOUNT
```

```
...
```

```
    balance: INTEGER
```

```
        -- 'balance' of the account
```

```
...
```

**invariant**

*balance\_no\_negative: balance  $\geq 0$*

# Class invariant

Property that is true of the current object at any *observable* point

```
class BANK_ACCOUNT
```

```
...
```

```
    balance: INTEGER
```

```
        -- 'balance' of the account
```

```
...
```

```
    invariant
```

```
        balance_no_negative: balance >= 0
```

A class without an **invariant** clause has a trivial invariant

```
    invariant
```

```
        always_ok: True
```

# Class invariant principle

## Class invariant principle

A *class invariant* must hold as soon as an object is created, then before and after the execution of any of the class features available to its clients.



# Class invariant principle

## Class invariant principle

A *class invariant* must hold as soon as an object is created, then before and after the execution of any of the class features available to its clients.

A class that fails to ensure its invariants is *buggy* software.

## Exercises

Exercises can be found in: <https://drive.google.com/open?id=0B1GMHm59JFjqY0ZFauFJLU5IeEE>.

Thank you!