

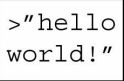


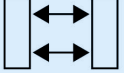
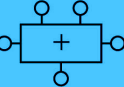
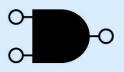
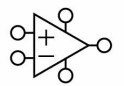
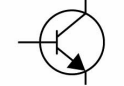

Chapter 5

Digital Design and Computer Architecture, 2nd Edition

David Money Harris and Sarah
L. Harris

Chapter 5 :: Topics

- **Introduction**
- **Arithmetic Circuits**
- **Number Systems**
- **Sequential Building Blocks**
- **Memory Arrays**
- **Logic Arrays**

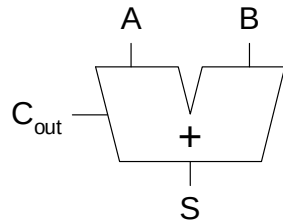
Application Software	
Operating Systems	
Architecture	
Micro-architecture	
Logic	
Digital Circuits	
Analog Circuits	
Devices	
Physics	

Introduction

- **Digital building blocks:**
 - Gates, multiplexers, decoders, registers, arithmetic circuits, counters, memory arrays, logic arrays
- **Building blocks demonstrate hierarchy, modularity, and regularity:**
 - Hierarchy of simpler components
 - Well-defined interfaces and functions
 - Regular structure easily extends to different sizes
- **Will use these building blocks in Chapter 7 to build microprocessor**

1-Bit Adders

Half Adder

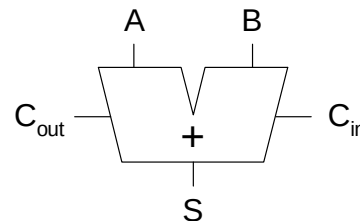


A	B	C_{out}	S
0	0		
0	1		
1	0		
1	1		

$$S =$$

$$C_{out} =$$

Full Adder



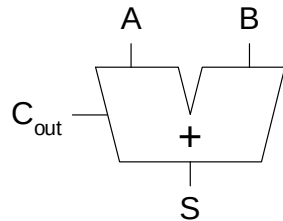
C_{in}	A	B	C_{out}	S
0	0	0		
0	0	1		
0	1	0		
0	1	1		
1	0	0		
1	0	1		
1	1	0		
1	1	1		

$$S =$$

$$C_{out} =$$

1-Bit Adders

Half Adder

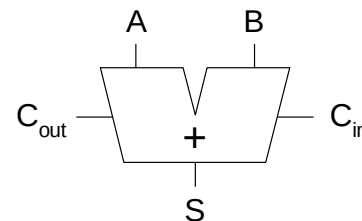


A	B	C_{out}	S
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

$$S = A \oplus B$$

$$C_{out} = A \cdot B$$

Full Adder



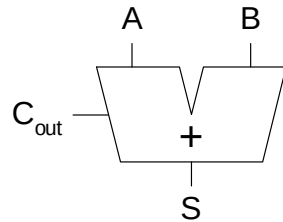
C_{in}	A	B	C_{out}	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

$$S = A \oplus B \oplus C_{in}$$

$$C_{out} = A \cdot B + (A \oplus B) \cdot C_{in}$$

1-Bit Adders

Half Adder

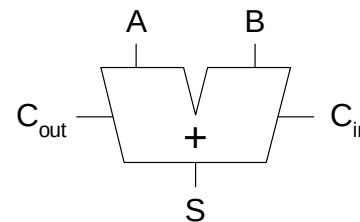


A	B	C_{out}	S
0	0	0	0
0	1	0	1
1	0	0	1
1	1	1	0

$$S = A \oplus B$$

$$C_{out} = AB$$

Full Adder



C_{in}	A	B	C_{out}	S
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

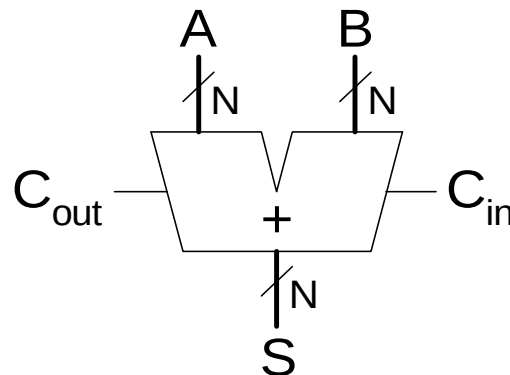
$$S = A \oplus B \oplus C_{in}$$

$$C_{out} = AB + AC_{in} + BC_{in}$$

Multibit Adders (CPAs)

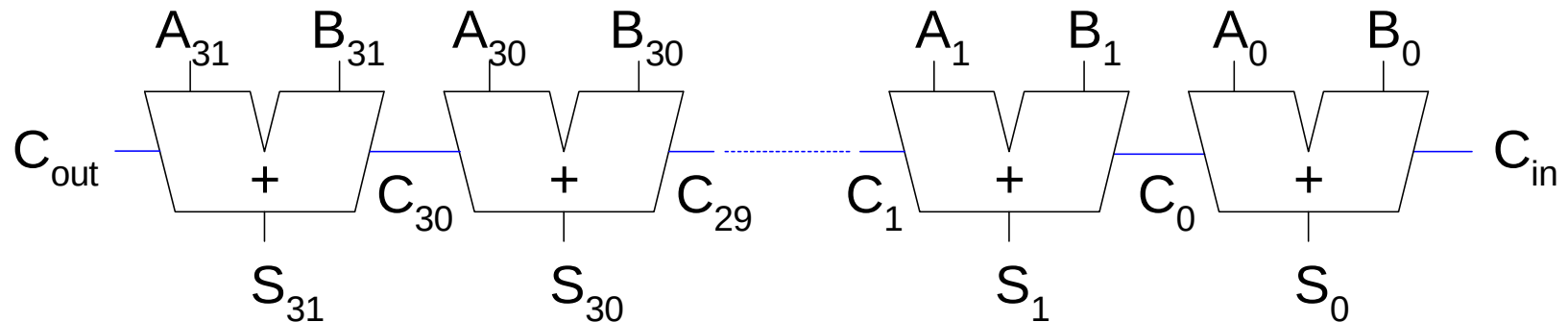
- Types of carry propagate adders (CPAs):
 - Ripple-carry (slow)
 - Carry-lookahead (fast)
 - Prefix (faster)
- Carry-lookahead and prefix adders faster for large adders but require more hardware

Symbol



Ripple-Carry Adder

- Chain 1-bit adders together
- Carry ripples through entire chain
- Disadvantage: **slow**



Ripple-Carry Adder Delay

$$t_{\text{ripple}} = Nt_{FA}$$

where t_{FA} is the delay of a 1-bit full adder

Carry-Lookahead Adder

- Compute carry out (C_{out}) for k -bit blocks using *generate* and *propagate* signals
- **Some definitions:**
 - Column i produces a carry out by either *generating* a carry out or *propagating* a carry in to the carry out
 - Generate (G_i) and propagate (P_i) signals for each column:
 - Column i will generate a carry out if A_i AND B_i are both 1.

$$G_i = A_i B_i$$

- Column i will propagate a carry in to the carry out if A_i OR B_i is 1.

$$P_i = A_i + B_i$$

- The carry out of column i (C_i) is:

$$C_i = A_i B_i + (A_i + B_i) C_{i-1} = G_i + P_i C_{i-1}$$

Carry-Lookahead Addition

- **Step 1:** Compute G_i and P_i for all columns
- **Step 2:** Compute G and P for k -bit blocks
- **Step 3:** C_{in} propagates through each k -bit propagate/generate block

Carry-Lookahead Adder

- **Example:** 4-bit blocks ($G_{3:0}$ and $P_{3:0}$) :

$$G_{3:0} = G_3 + P_3 (G_2 + P_2 (G_1 + P_1 G_0))$$

$$P_{3:0} = P_3 P_2 P_1 P_0$$

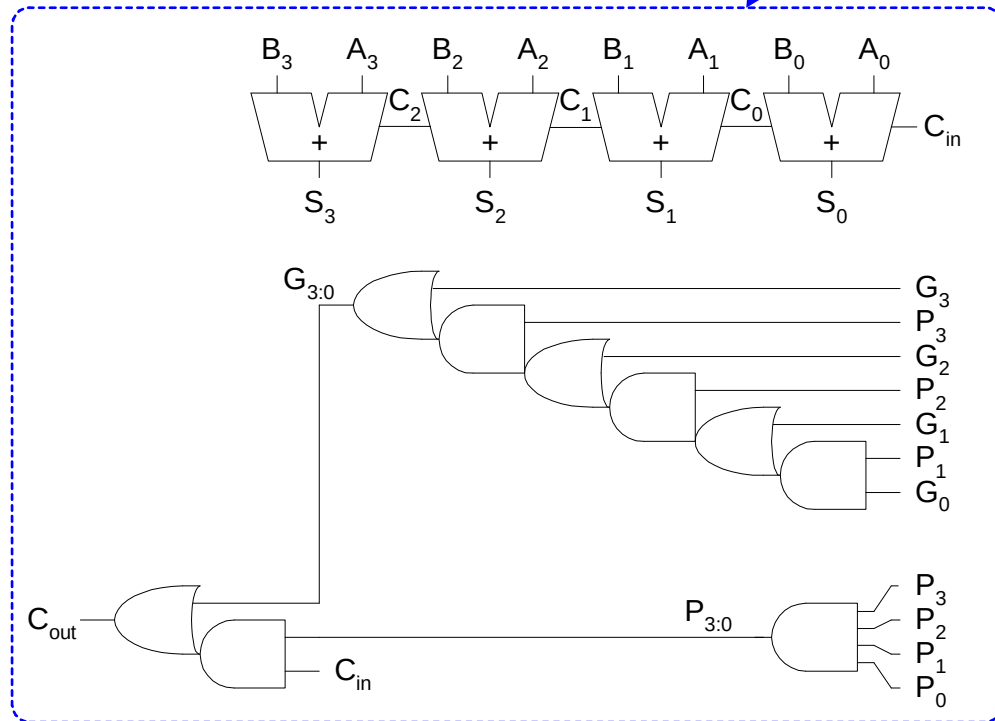
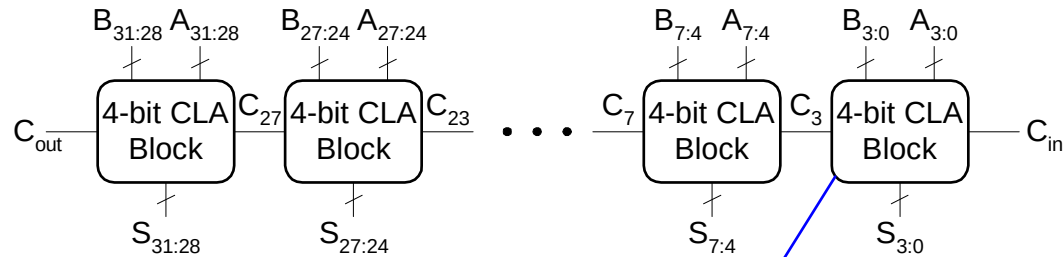
- **Generally,**

$$G_{i:j} = G_i + P_i (G_{i-1} + P_{i-1} (G_{i-2} + P_{i-2} G_j))$$

$$P_{i:j} = P_i P_{i-1} P_{i-2} P_j$$

$$C_i = G_{i:j} + P_{i:j} C_{j-1}$$

32-bit CLA with 4-bit Blocks



Carry-Lookahead Adder

For N -bit CLA with k -bit blocks:

$$t_{CLA} = t_{pg} + t_{pg_block} + (N/k - 1)t_{AND_OR} + kt_{FA}$$

- t_{pg} : delay to generate all P_i, G_i
- t_{pg_block} : delay to generate all $P_{i:j}, G_{i:j}$
- t_{AND_OR} : delay from C_{in} to C_{out} of final AND/OR gate in k -bit CLA block

An N -bit carry-lookahead adder is generally much faster than a ripple-carry adder for $N > 16$

Prefix Adder

- Computes carry in (C_{i-1}) for each column, then computes sum:

$$S_i = (A_i \mathbin{\text{Å}} B_i) \mathbin{\text{Å}} C_i$$

- Computes G and P for 1-, 2-, 4-, 8-bit blocks, etc. until all G_i (carry in) known
- $\log_2 N$ stages

Prefix Adder

- Carry in either *generated* in a column or *propagated* from a previous column.
- Column -1 holds C_{in} , so

$$G_{-1} = C_{in}, P_{-1} = 0$$

- Carry in to column i = carry out of column $i-1$:

$$C_{i-1} = G_{i-1:-1}$$

$G_{i-1:-1}$: generate signal spanning columns $i-1$ to -1

- Sum equation:

$$S_i = (A_i \mathbin{\mathbf{\text{Å}}} B_i) \mathbin{\mathbf{\text{Å}}} G_{i-1:-1}$$

- **Goal:** Quickly compute $G_{0:-1}, G_{1:-1}, G_{2:-1}, G_{3:-1}, G_{4:-1}, G_{5:-1}, \dots$ (called *prefixes*)



Prefix Adder

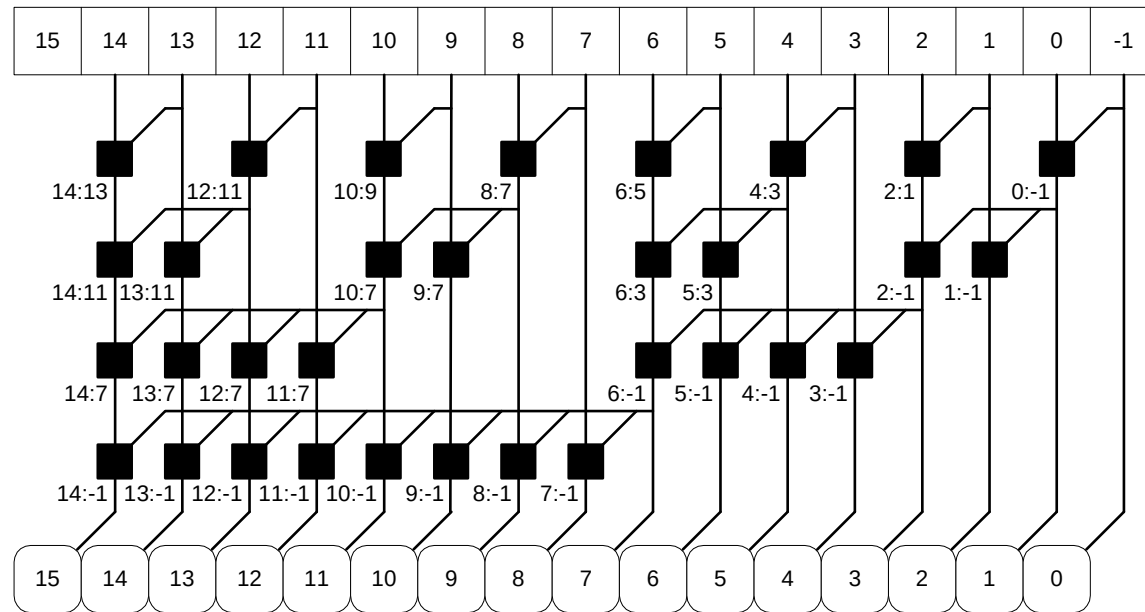
- Generate and propagate signals for a block spanning bits $i:j$:

$$G_{i:j} = G_{i:k} + P_{i:k} G_{k-1:j}$$

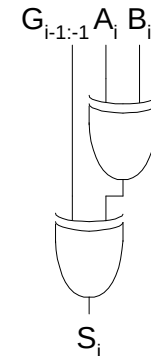
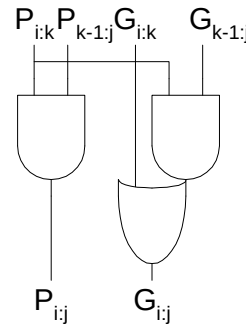
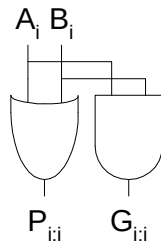
$$P_{i:j} = P_{i:k} P_{k-1:j}$$

- In words:
 - **Generate:** block $i:j$ will generate a carry if:
 - upper part ($i:k$) generates a carry or
 - upper part propagates a carry generated in lower part ($k-1:j$)
 - **Propagate:** block $i:j$ will propagate a carry if *both* the upper and lower parts propagate the carry

Prefix Adder Schematic



Legend



Prefix Adder Delay

$$t_{PA} = t_{pg} + \log_2 N(t_{pg_prefix}) + t_{XOR}$$

- t_{pg} : delay to produce $P_i G_i$ (AND or OR gate)
- t_{pg_prefix} : delay of black prefix cell (AND-OR gate)

Adder Delay Comparisons

Compare delay of: 32-bit ripple-carry, carry-lookahead, and prefix adders

- CLA has 4-bit blocks
- 2-input gate delay = 100 ps; full adder delay = 300 ps

Adder Delay Comparisons

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- CLA has 4-bit blocks
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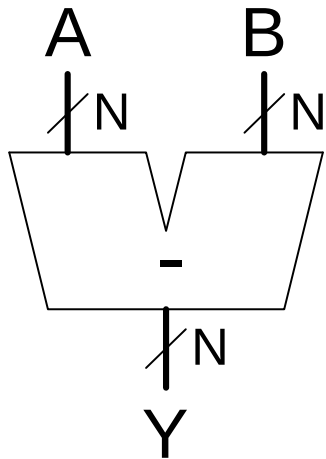
$$t_{\text{ripple}} = Nt_{FA} = 32(300 \text{ ps})$$
$$= \mathbf{9.6 \text{ ns}}$$

$$t_{CLA} = t_{pg} + t_{pg_block} + (N/k - 1)t_{AND_OR} + kt_{FA}$$
$$= [100 + 600 + (7)200 + 4(300)] \text{ ps}$$
$$= \mathbf{3.3 \text{ ns}}$$

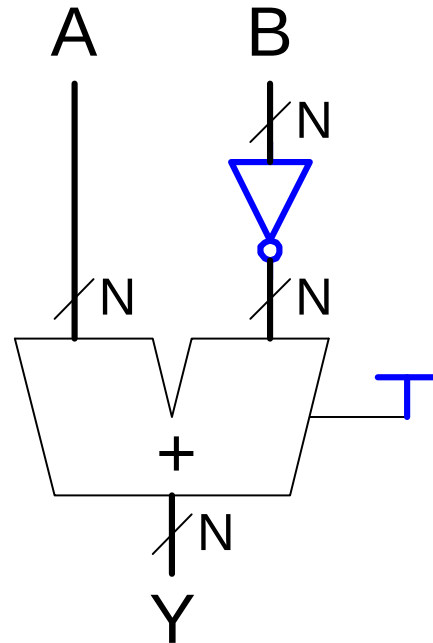
$$t_{PA} = t_{pg} + \log_2 N(t_{pg_prefix}) + t_{XOR}$$
$$= [100 + \log_2 32(200) + 100] \text{ ps}$$
$$= \mathbf{1.2 \text{ ns}}$$

Subtractor

Symbol

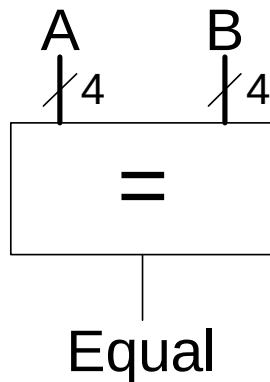


Implementation

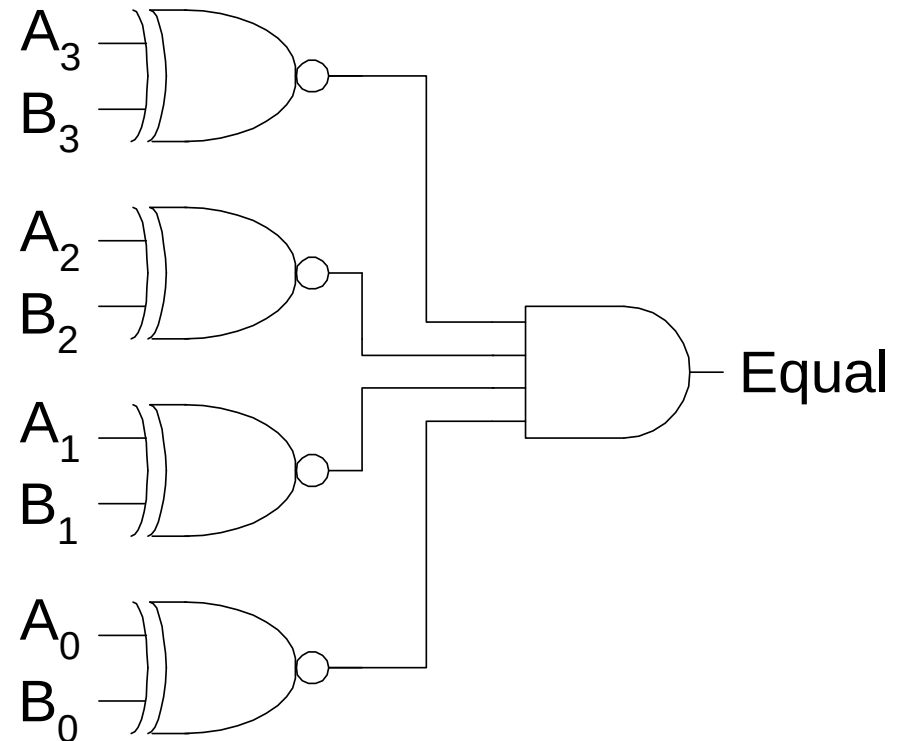


Comparator: Equality

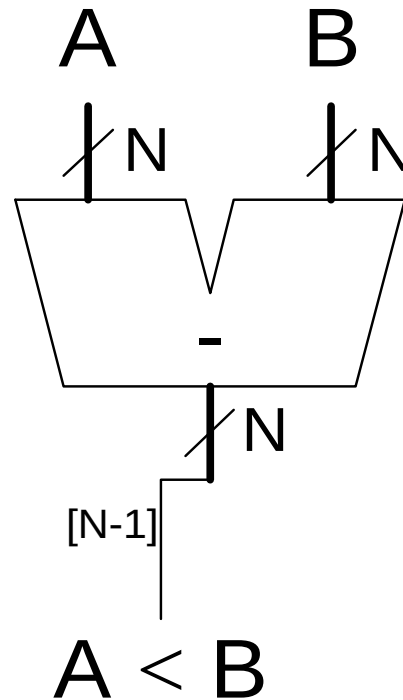
Symbol



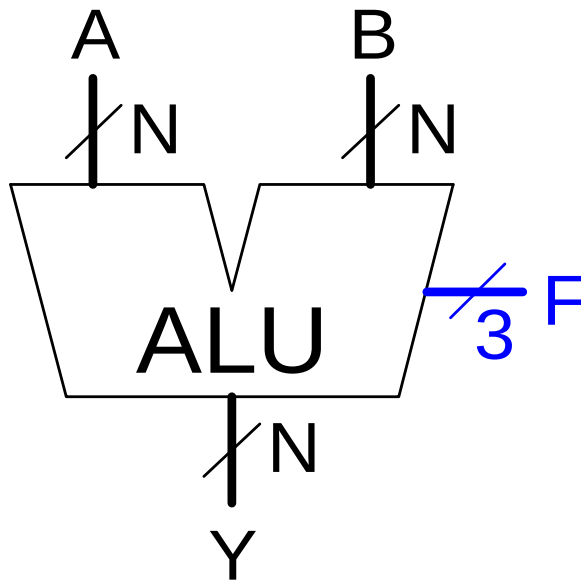
Implementation



Comparator: Less Than

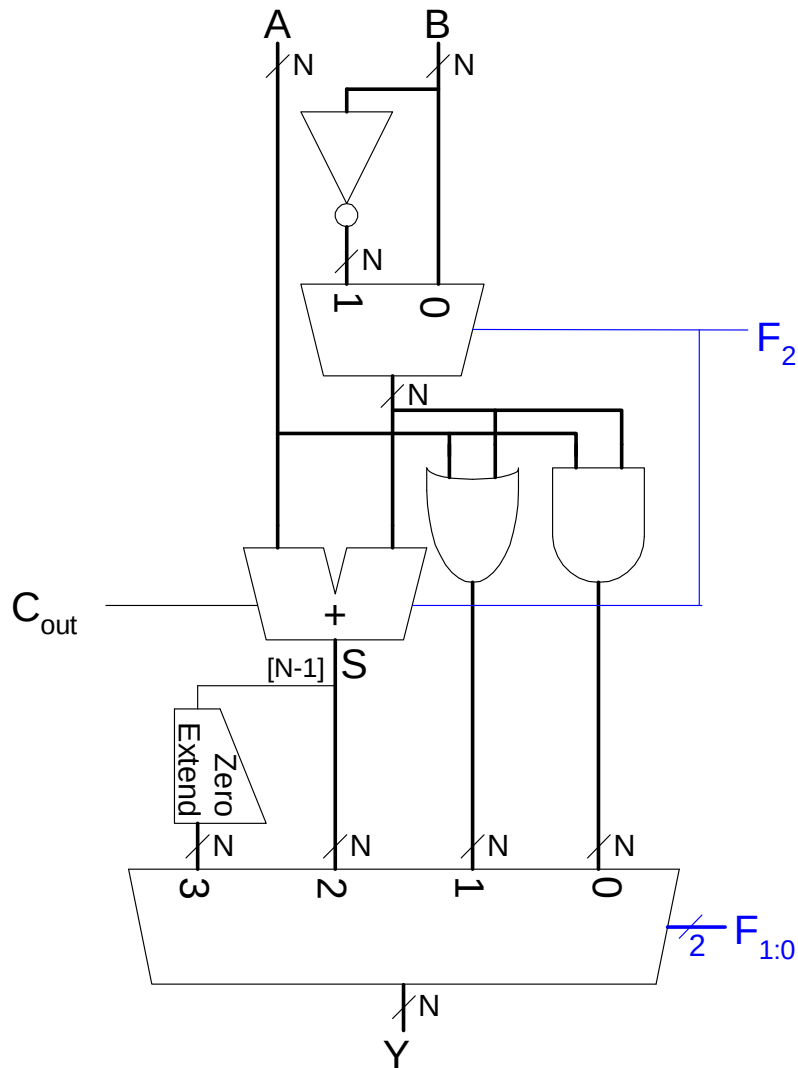


Arithmetic Logic Unit (ALU)



$F_{2:0}$	Function
000	$A \& B$
001	$A B$
010	$A + B$
011	not used
100	$A \& \sim B$
101	$A \sim B$
110	$A - B$
111	SLT

ALU Design



$F_{2:0}$	Function
000	A & B
001	A B
010	A + B
011	not used
100	A & $\sim B$
101	A $\sim B$
110	A - B
111	SLT

Adder Delay Comparisons

Compare delay of: 32-bit ripple-carry, carry-lookahead, and prefix adders

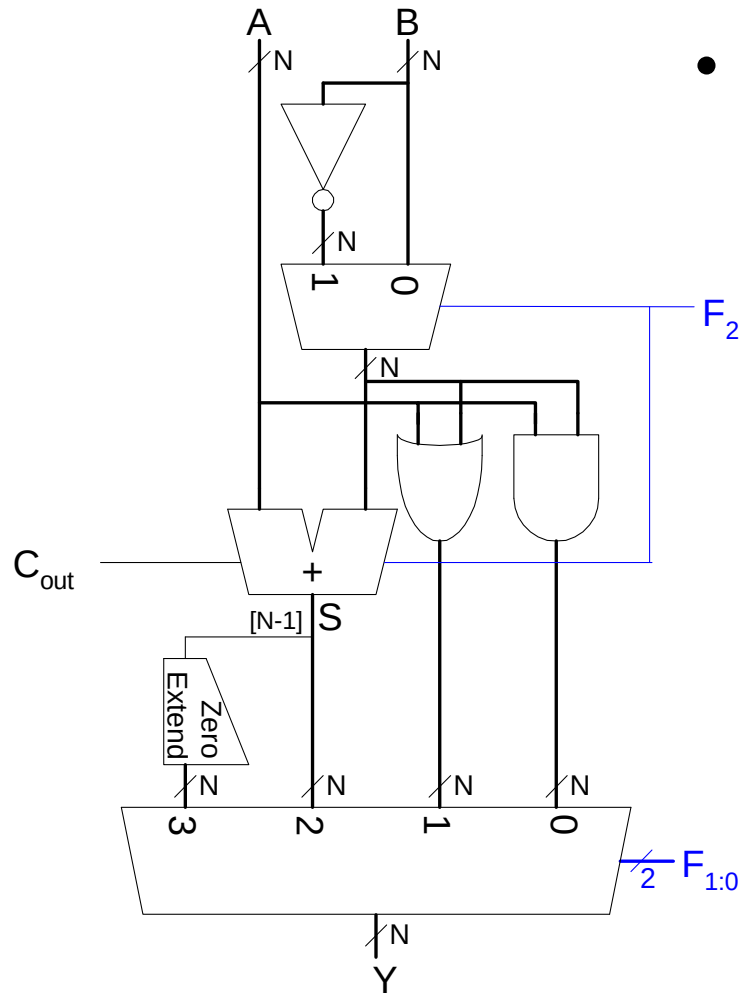
- CLA has 4-bit blocks
- 2-input gate delay = 100 ps; full adder delay = 300 ps

$$t_{\text{ripple}} = Nt_{FA} = 32(300 \text{ ps})$$
$$= \mathbf{9.6 \text{ ns}}$$

$$t_{CLA} = t_{pg} + t_{pg_block} + (N/k - 1)t_{AND_OR} + kt_{FA}$$
$$= [100 + 600 + (7)200 + 4(300)] \text{ ps}$$
$$= \mathbf{3.3 \text{ ns}}$$

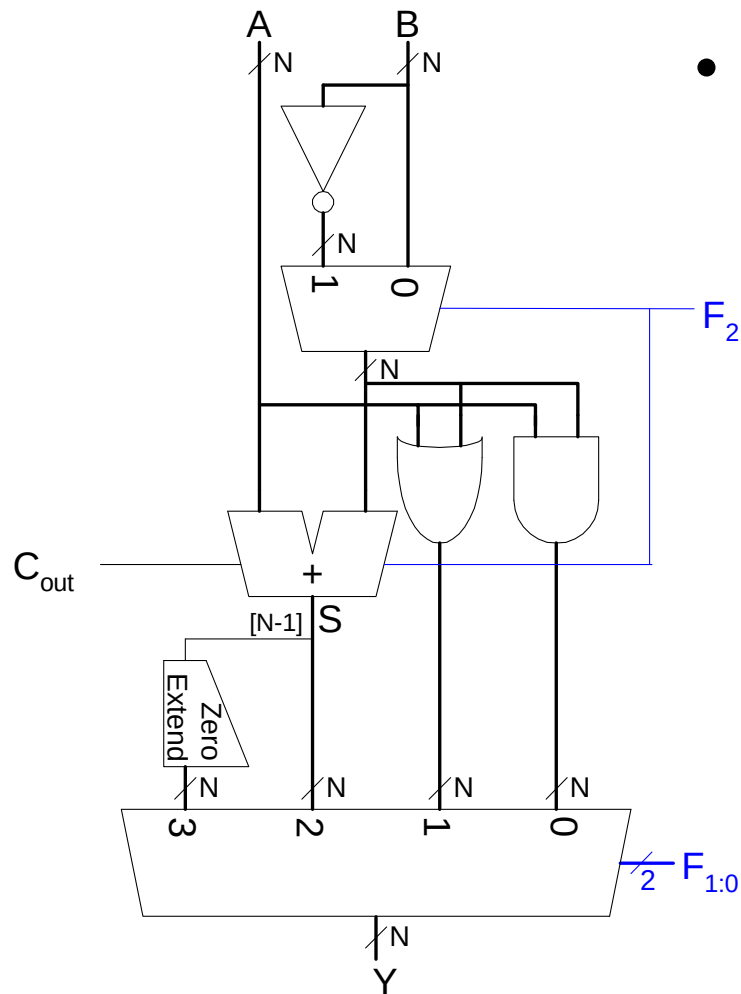
$$t_{PA} = t_{pg} + \log_2 N(t_{pg_prefix}) + t_{XOR}$$
$$= [100 + \log_2 32(200) + 100] \text{ ps}$$
$$= \mathbf{1.2 \text{ ns}}$$

Set Less Than (SLT)



- Configure 32-bit ALU for SLT operation: $A = 25$ and $B = 32$

Set Less Than (SLT)



- Configure 32-bit ALU for SLT operation: $A = 25$ and $B = 32$
 - $A < B$, so Y should be 32-bit representation of 1 (0x00000001)
 - $F_{2:0} = 111$
 - $F_2 = 1$ (adder acts as subtractor), so $25 - 32 = -7$
 - -7 has 1 in the most significant bit ($S_{31} = 1$)
 - $F_{1:0} = 11$ multiplexer selects $Y = S_{31}$ (zero extended) = 0x00000001.

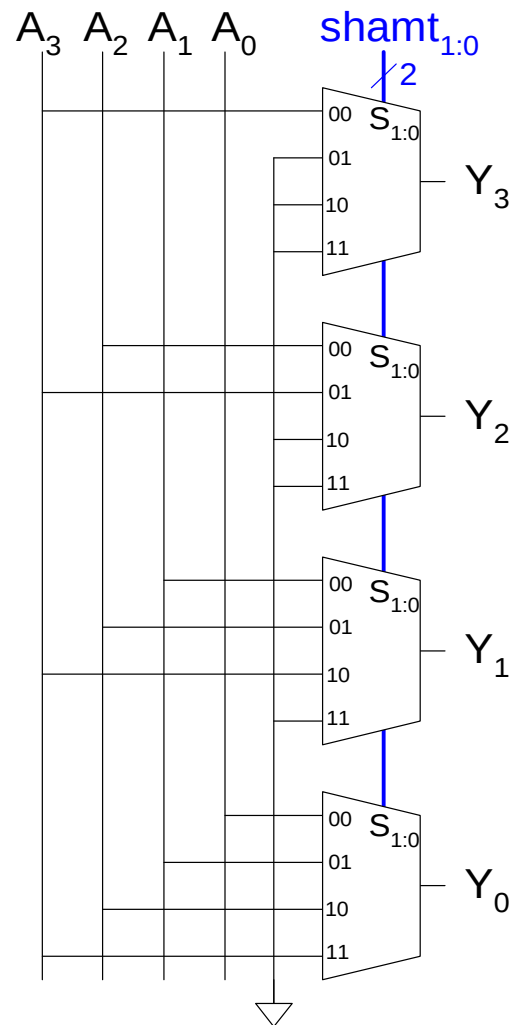
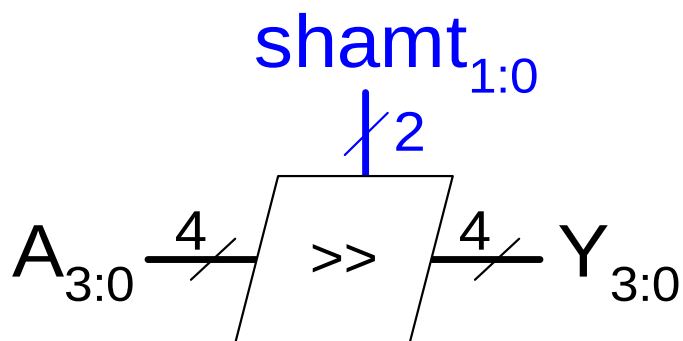
Shifters

- **Logical shifter:** shifts value to left or right and fills empty spaces with 0's
 - Ex: $11001 \gg 2 =$
 - Ex: $11001 \ll 2 =$
- **Arithmetic shifter:** same as logical shifter, but on right shift, fills empty spaces with the old most significant bit (msb).
 - Ex: $11001 \ggg 2 =$
 - Ex: $11001 \lll 2 =$
- **Rotator:** rotates bits in a circle, such that bits shifted off one end are shifted into the other end
 - Ex: $11001 \text{ ROR } 2 =$
 - Ex: $11001 \text{ ROL } 2 =$

Shifters

- **Logical shifter:**
 - Ex: $11001 \gg 2 = 00110$
 - Ex: $11001 \ll 2 = 00100$
- **Arithmetic shifter:**
 - Ex: $11001 \ggg 2 = 11110$
 - Ex: $11001 \lll 2 = 00100$
- **Rotator:**
 - Ex: $11001 \text{ ROR } 2 = 01110$
 - Ex: $11001 \text{ ROL } 2 = 00111$

Shifter Design



Shifters as Multipliers,

- $A \ll N = A \times 2^N$
 - **Example:** $00001 \ll 2 = 00100$ ($1 \times 2^2 = 4$)
 - **Example:** $11101 \ll 2 = 10100$ ($-3 \times 2^2 = -12$)
- $A \gg N = A \div 2^N$
 - **Example:** $01000 \gg 2 = 00010$ ($8 \div 2^2 = 2$)
 - **Example:** $10000 \gg 2 = 11100$ ($-16 \div 2^2 = -4$)

Multipliers

- **Partial products** formed by multiplying a single digit of the multiplier with multiplicand
- **Shifted** partial products **summed** to form result

$$\begin{array}{r}
 230 \\
 \times 42 \\
 \hline
 460 \\
 + 920 \\
 \hline
 9660
 \end{array}$$

$$230 \times 42 = 9660$$

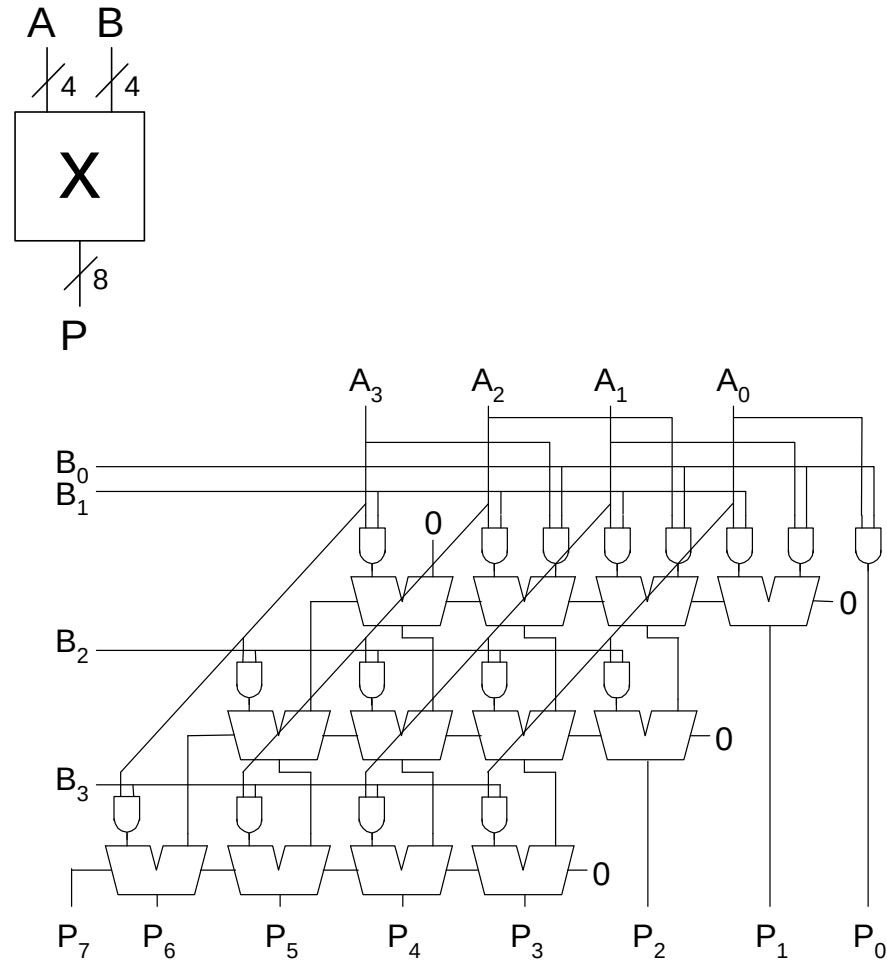
multiplicand
 multiplier
 partial
 products
 result

$$\begin{array}{r}
 0101 \\
 \times 0111 \\
 \hline
 0101 \\
 0101 \\
 0101 \\
 + 0000 \\
 \hline
 0100011
 \end{array}$$

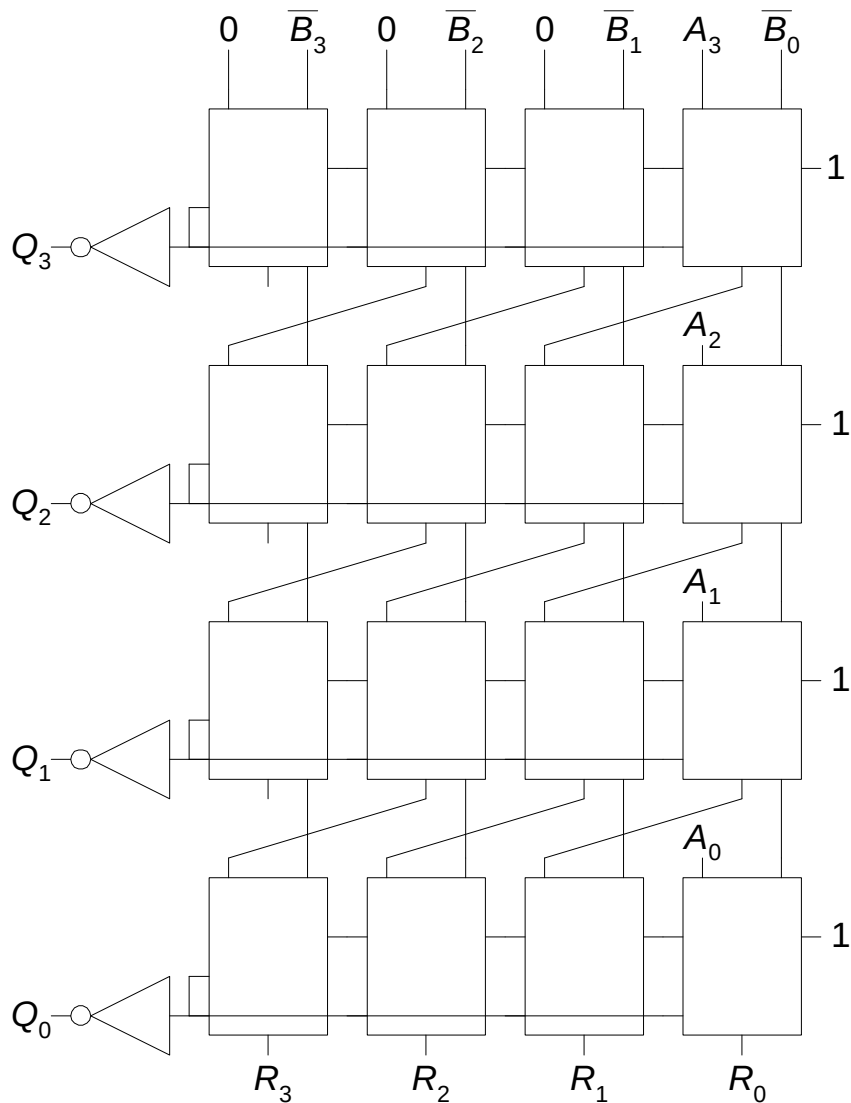
$$5 \times 7 = 35$$

4 x 4 Multiplier

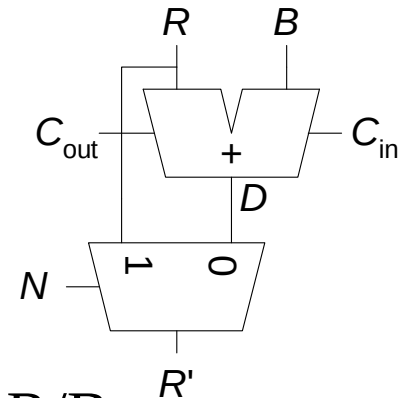
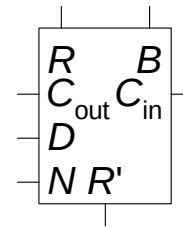
$$\begin{array}{r}
 \begin{array}{cccc}
 & A_3 & A_2 & A_1 & A_0 \\
 \times & B_3 & B_2 & B_1 & B_0 \\
 \hline
 & A_3B_0 & A_2B_0 & A_1B_0 & A_0B_0 \\
 & A_3B_1 & A_2B_1 & A_1B_1 & A_0B_1 \\
 & A_3B_2 & A_2B_2 & A_1B_2 & A_0B_2 \\
 + & A_3B_3 & A_2B_3 & A_1B_3 & A_0B_3 \\
 \hline
 P_7 & P_6 & P_5 & P_4 & P_3 & P_2 & P_1 & P_0
 \end{array}
 \end{array}$$



4 x 4 Divider



Legend



$$A/B = Q + R/B$$

Algorithm:

$$R' = 0$$

for $i = N-1$ to 0

$$R = \{R' \ll 1, A_i\}$$

$$D = R - B$$

if $D < 0$, $Q_i = 0$, $R' = R$

else $Q_i = 1$, $R' = D$

$$R' = R$$



Number Systems

- Numbers we can represent using binary representations
 - **Positive numbers**
 - Unsigned binary
 - **Negative numbers**
 - Two's complement
 - Sign/magnitude numbers
- What about **fractions**?

Numbers with Fractions

- Two common notations:
 - **Fixed-point:** binary point fixed
 - **Floating-point:** binary point floats to the right of the most significant 1

Fixed-Point Numbers

- 6.75 using 4 integer bits and 4 fraction bits:

01101100

0110.1100

$$2^2 + 2^1 + 2^{-1} + 2^{-2} = 6.75$$

- Binary point is implied
- The number of integer and fraction bits must be agreed upon beforehand

Fixed-Point Number

- Represent 7.5_{10} using 4 integer bits and 4 fraction bits.

Fixed-Point Number

- Represent 7.5_{10} using 4 integer bits and 4 fraction bits.

01111000

Signed Fixed-Point

- **Representations:**
 - Sign/magnitude
 - Two's complement
- **Example:** Represent -7.5_{10} using 4 integer and 4 fraction bits
 - **Sign/magnitude:**
 - **Two's complement:**

Signed Fixed-Point

- **Representations:**
 - Sign/magnitude
 - Two's complement
- **Example:** Represent -7.5_{10} using 4 integer and 4 fraction bits

- **Sign/magnitude:**

11111000

- **Two's complement:**

1. +7.5: 01111000

2. Invert bits: 10000111

3. Add 1 to lsb: + 1

 10001000

Floating-Point Numbers

- Binary point floats to the right of the most significant 1
- Similar to decimal scientific notation

- For example, write 273_{10} in scientific notation:

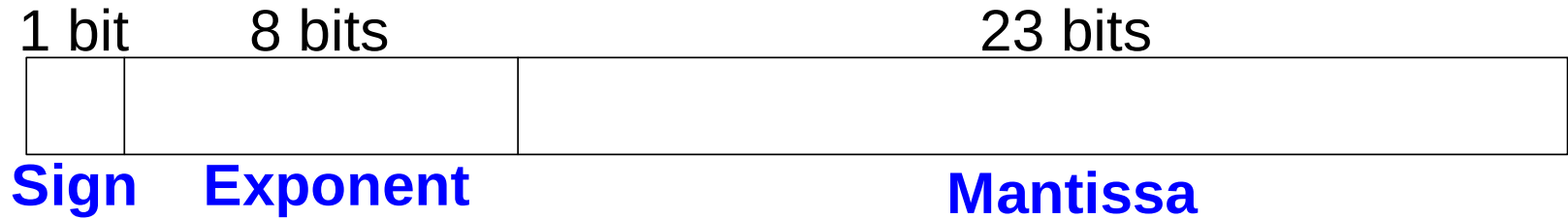
$$273 = 2.73 \times 10^2$$

- In general, a number is written in scientific notation as:

$$\pm M \times B^E$$

- M = mantissa
- B = base
- E = exponent
- In the example, $M = 2.73$, $B = 10$, and $E = 2$

Floating-Point Numbers



- **Example:** represent the value 228_{10} using a 32-bit floating point representation

We show three versions –final version is called the **IEEE 754 floating-point standard**

Floating-Point

1. Convert decimal to binary (**don't reverse steps 1 & 2!**):

$$228_{10} = 11100100_2$$

2. Write the number in “binary scientific notation”:

$$11100100_2 = 1.11001_2 \times 2^7$$

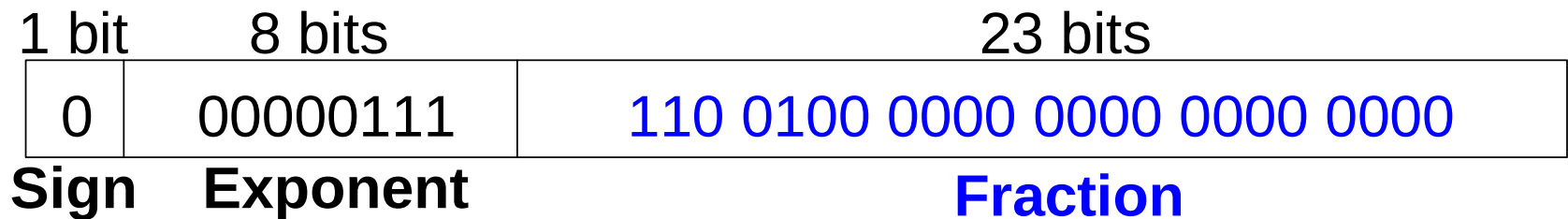
3. Fill in each field of the 32-bit floating point number:

- The sign bit is positive (0)
- The 8 exponent bits represent the value 7
- The remaining 23 bits are the mantissa

1 bit	8 bits	23 bits
0	00000111	11 1001 0000 0000 0000 0000
Sign	Exponent	Mantissa

Floating-Point

- First bit of the mantissa is always 1:
 - $228_{10} = 11100100_2 = \mathbf{1.11001} \times 2^7$
- So, no need to store it: *implicit leading 1*
- Store just fraction bits in 23-bit field



Floating-Point

- *Biased exponent*: bias = 127 (01111111_2)

- Biased exponent = bias + exponent

- Exponent of 7 is stored as:

$$127 + 7 = 134 = 0x10000110_2$$

- The **IEEE 754 32-bit floating-point representation** of 228_{10}

1 bit	8 bits	23 bits
0	10000110	110 0100 0000 0000 0000 0000
Sign	Biased Exponent	Fraction

Floating-Point Example

Write -58.25_{10} in floating point (IEEE 754)

Floating-Point Example

Write -58.25_{10} in floating point (IEEE 754)

1. Convert decimal to binary:

$$58.25_{10} = 111010.01_2$$

2. Write in binary scientific notation:

$$1.1101001 \times 2^5$$

3. Fill in fields:

Sign bit: 1 (negative)

8 exponent bits: $(127 + 5) = 132 = 10000100_2$

23 fraction bits: 110 1001 0000 0000 0000 0000

1 bit	8 bits	23 bits
1	100 0010 0	110 1001 0000 0000 0000 0000
Sign	Exponent	Fraction

in hexadecimal: 0xC2690000

Floating-Point: Special

Number	Sign	Exponent	Fraction
0	X	00000000	00000000000000000000000000000000
∞	0	11111111	00000000000000000000000000000000
$-\infty$	1	11111111	00000000000000000000000000000000
NaN	X	11111111	non-zero

Floating-Point Precision

- **Single-Precision:**
 - 32-bit
 - 1 sign bit, 8 exponent bits, 23 fraction bits
 - bias = 127
- **Double-Precision:**
 - 64-bit
 - 1 sign bit, 11 exponent bits, 52 fraction bits
 - bias = 1023

Floating-Point: Rounding

- **Overflow:** number too large to be represented
- **Underflow:** number too small to be represented
- **Rounding modes:**
 - Down
 - Up
 - Toward zero
 - To nearest
- **Example:** round 1.100101 (1.578125) to only 3 fraction bits
 - Down: 1.100
 - Up: 1.101
 - Toward zero: 1.100
 - To nearest: 1.101 (1.625 is closer to 1.578125 than 1.5 is)

Floating-Point Addition

1. Extract exponent and fraction bits
2. Prepend leading 1 to form mantissa
3. Compare exponents
4. Shift smaller mantissa if necessary
5. Add mantissas
6. Normalize mantissa and adjust exponent if necessary
7. Round result
8. Assemble exponent and fraction back into floating-point format

Floating-Point Addition

Add the following floating-point numbers:

0x3FC00000

0x40500000

Floating-Point Addition

1. Extract exponent and fraction bits

1 bit	8 bits	23 bits
0	01111111	100 0000 0000 0000 0000 0000
Sign	Exponent	Fraction
1 bit	8 bits	23 bits
0	10000000	101 0000 0000 0000 0000 0000
Sign	Exponent	Fraction

For first number (N1): $S = 0, E = 127, F = .1$

For second number (N2): $S = 0, E = 128, F = .101$

2. Prepend leading 1 to form mantissa

N1: 1.1

N2: 1.101

Floating-Point Addition

3. Compare exponents

$127 - 128 = -1$, so shift N1 right by 1 bit

4. Shift smaller mantissa if necessary

shift N1's mantissa: $1.1 \gg 1 = 0.11$ ($\times 2^1$)

5. Add mantissas

$$\begin{array}{r} 0.11 \times 2^1 \\ + 1.101 \times 2^1 \\ \hline 10.011 \times 2^1 \end{array}$$

Floating Point Addition

6. **Normalize mantissa and adjust exponent if necessary**

$$10.011 \times 2^1 = 1.0011 \times 2^2$$

7. **Round result**

No need (fits in 23 bits)

8. **Assemble exponent and fraction back into floating-point format**

$$S = 0, E = 2 + 127 = 129 = 10000001_2, F = 001100..$$

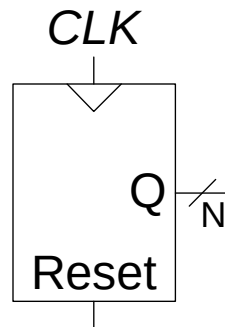
1 bit	8 bits	23 bits
0	10000001	001 1000 0000 0000 0000 0000
Sign	Exponent	Fraction

in hexadecimal: **0x40980000**

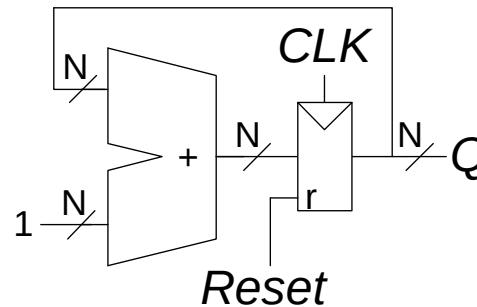
Counters

- Increments on each clock edge
- Used to cycle through numbers. For example,
 - 000, 001, 010, 011, 100, 101, 110, 111, 000, 001...
- Example uses:
 - Digital clock displays
 - Program counter: keeps track of current instruction executing

Symbol



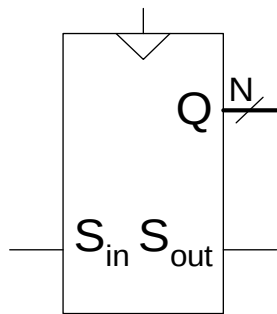
Implementation



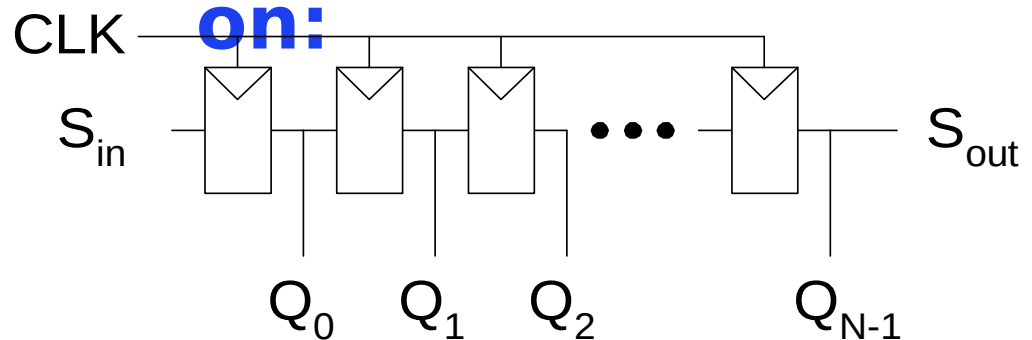
Shift Registers

- Shift a new bit in on each clock edge
- Shift a bit out on each clock edge
- *Serial-to-parallel converter*: converts serial input (S_{in}) to parallel output ($Q_{0:N-1}$)

Symbol:

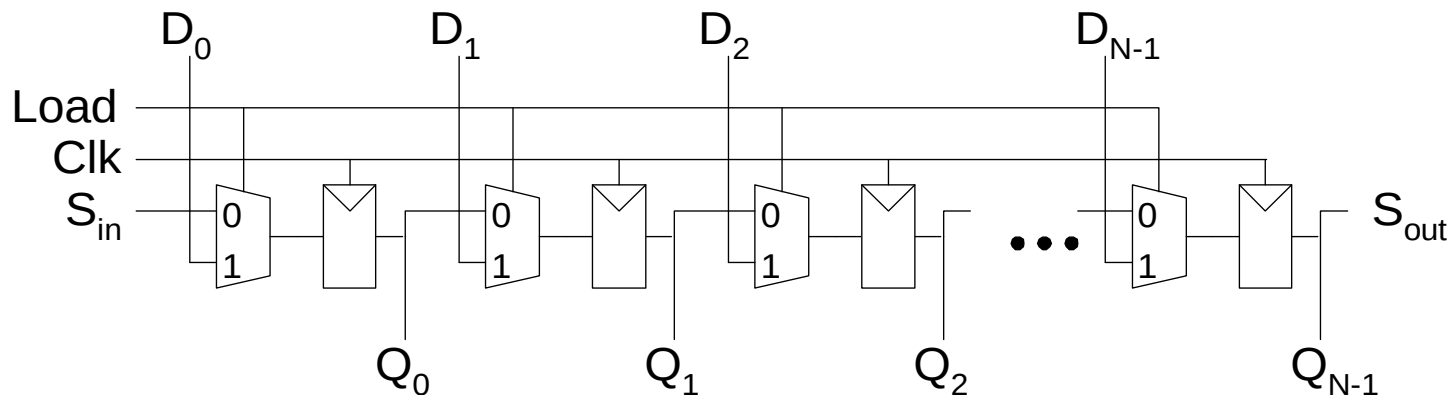


Implementation:



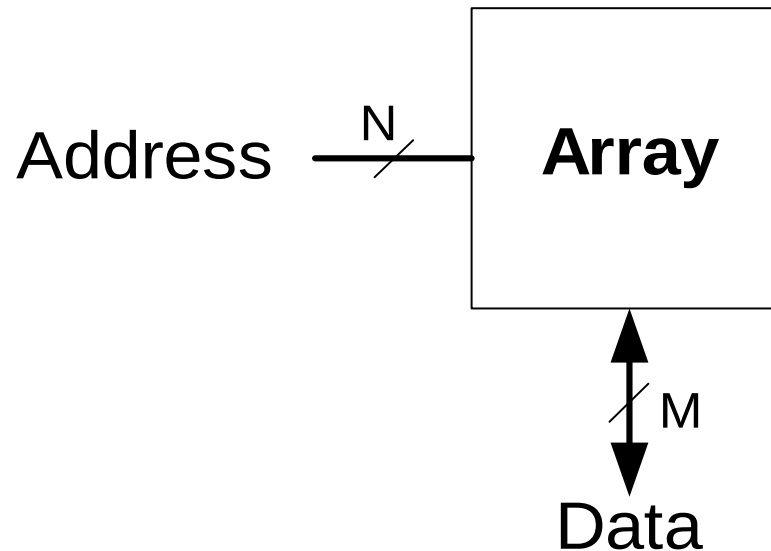
Shift Register with Parallel

- When $Load = 1$, acts as a normal N -bit register
- When $Load = 0$, acts as a shift register
- Now can act as a *serial-to-parallel converter* (S_{in} to $Q_{0:N-1}$) or a *parallel-to-serial converter* ($D_{0:N-1}$ to S_{out})



Memory Arrays

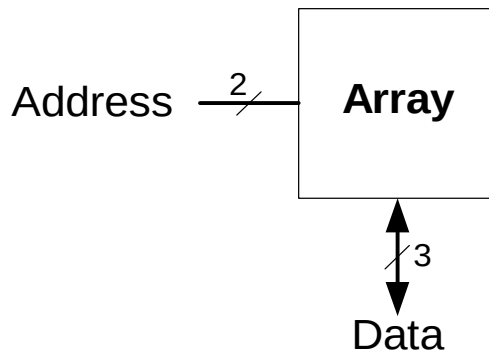
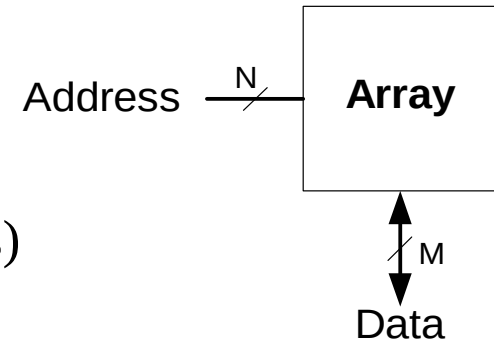
- Efficiently store large amounts of data
- 3 common types:
 - Dynamic random access memory (DRAM)
 - Static random access memory (SRAM)
 - Read only memory (ROM)
- M -bit data value read/ written at each unique N -bit address



ENOUGH FOR
TODAY!

Memory Arrays

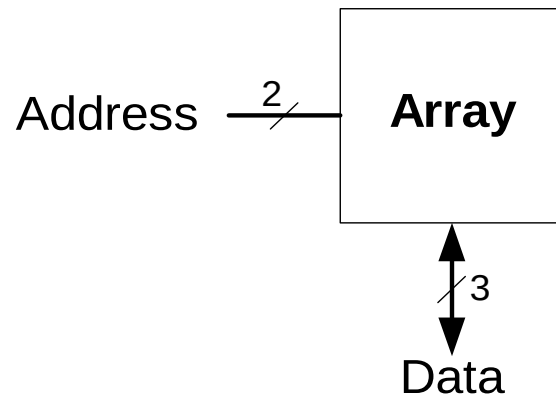
- 2-dimensional array of bit cells
- Each bit cell stores one bit
- N address bits and M data bits:
 - 2^N rows and M columns
 - **Depth**: number of rows (number of words)
 - **Width**: number of columns (size of word)
 - **Array size**: depth \times width = $2^N \times M$



Address	Data			
11	0	1	0	<div style="display: flex; align-items: center;"> ↑ depth ↓ </div>
10	1	0	0	
01	1	1	0	
00	0	1	1	
				<div style="display: flex; align-items: center;"> ← width → </div>

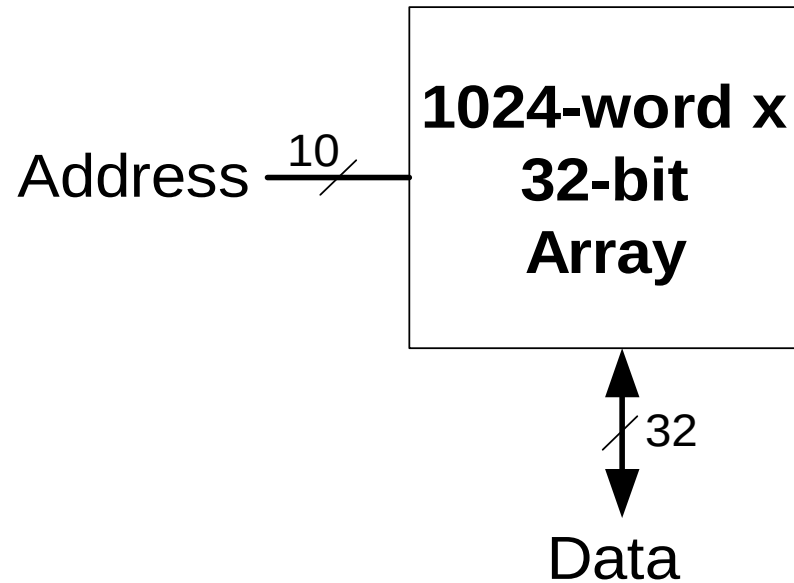
Memory Array Example

- $2^2 \times 3$ -bit array
- Number of words: 4
- Word size: 3-bits
- For example, the 3-bit word stored at address 10 is 100

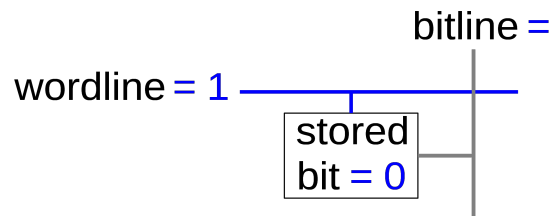
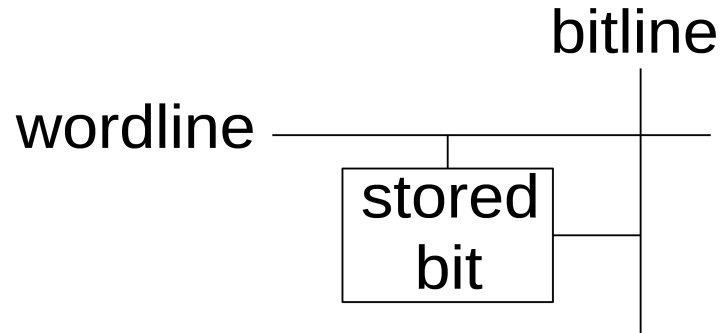


Address	Data			
11	0	1	0	depth ↑ ↓
10	1	0	0	
01	1	1	0	
00	0	1	1	
	width ←→			

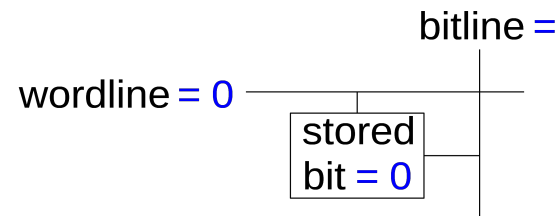
Memory Arrays



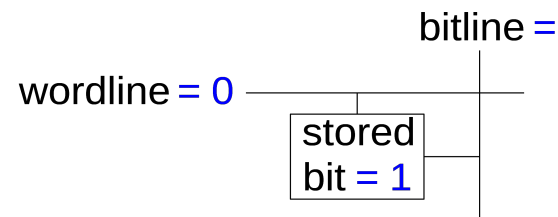
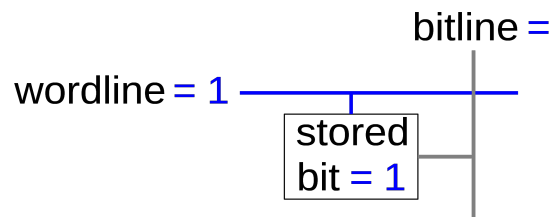
Memory Array Bit Cells



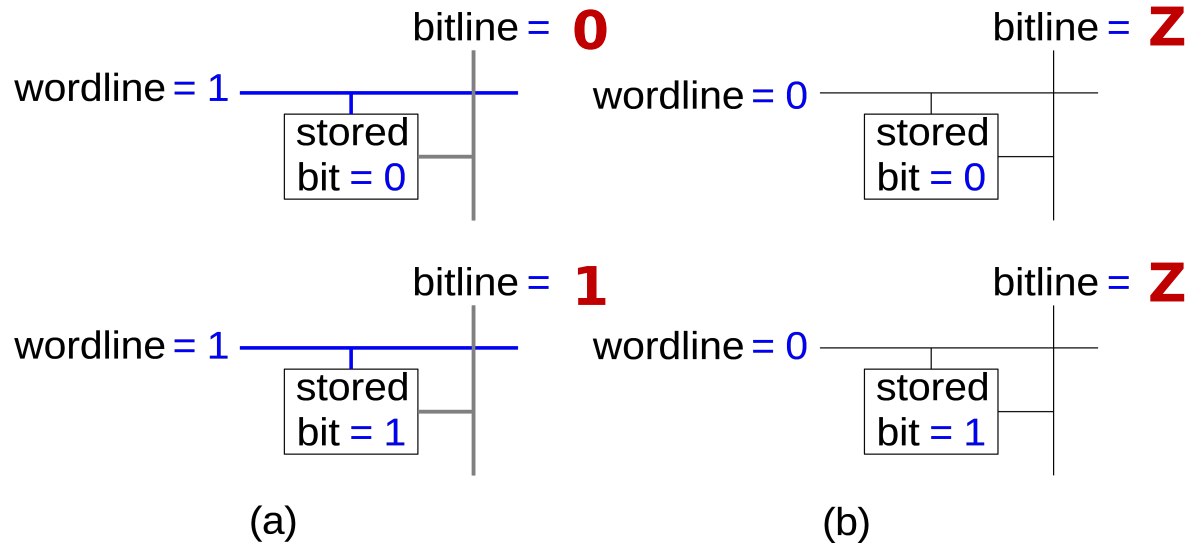
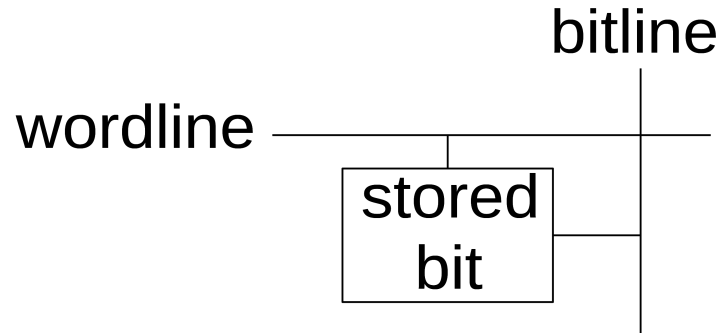
(a)



(b)



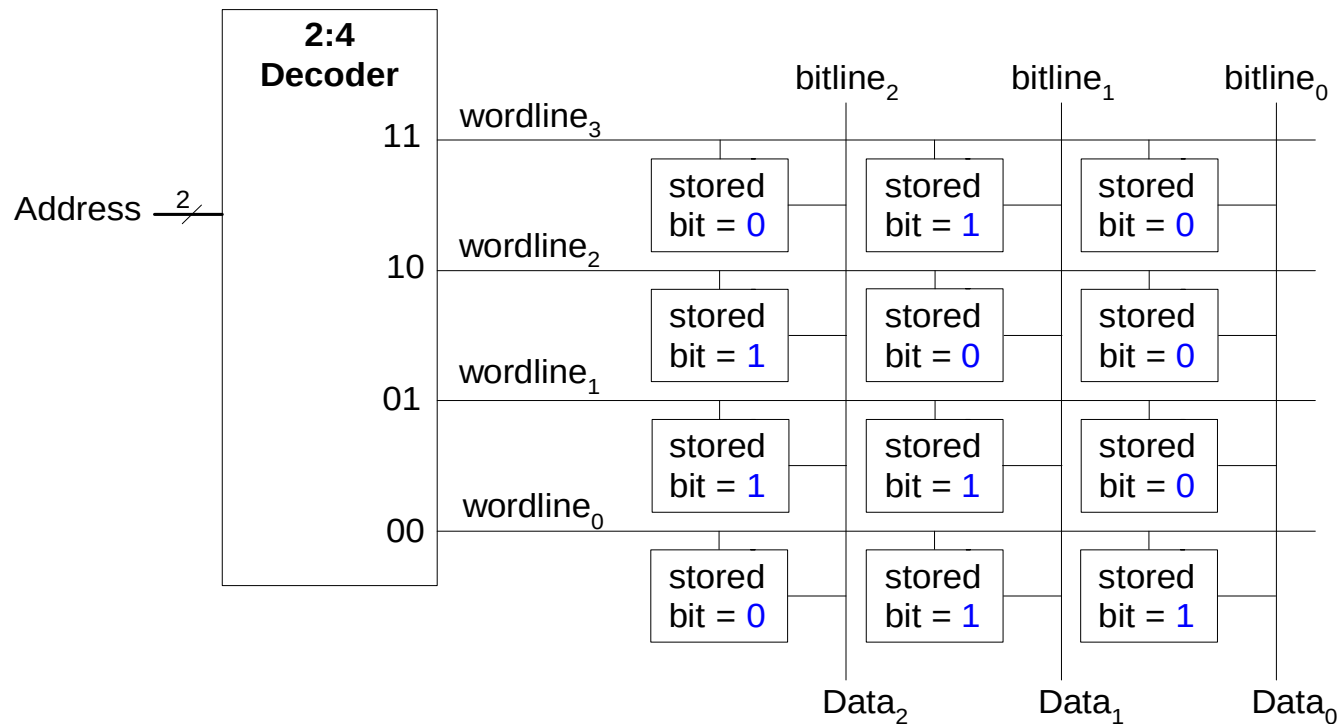
Memory Array Bit Cells



Memory Array

- **Wordline:**

- like an enable
- single row in memory array read/written
- corresponds to unique address
- only one wordline HIGH at once



Types of Memory

- Random access memory (RAM): **volatile**
- Read only memory (ROM): **nonvolatile**

RAM: Random Access

- **Volatile:** loses its data when power off
- Read and written quickly
- Main memory in your computer is RAM (DRAM)

Historically called *random* access memory because any data word accessed as easily as any other (in contrast to sequential access memories such as a tape recorder)

ROM: Read Only Memory

- **Nonvolatile:** retains data when power off
- Read quickly, but writing is impossible or slow
- Flash memory in cameras, thumb drives, and digital cameras are all ROMs

Historically called *read only* memory because ROMs were written at manufacturing time or by burning fuses. Once ROM was configured, it could not be written again. This is no longer the case for Flash memory and other types of ROMs.

Types of RAM

- **DRAM** (Dynamic random access memory)
- **SRAM** (Static random access memory)
- Differ in how they store data:
 - DRAM uses a capacitor
 - SRAM uses cross-coupled inverters

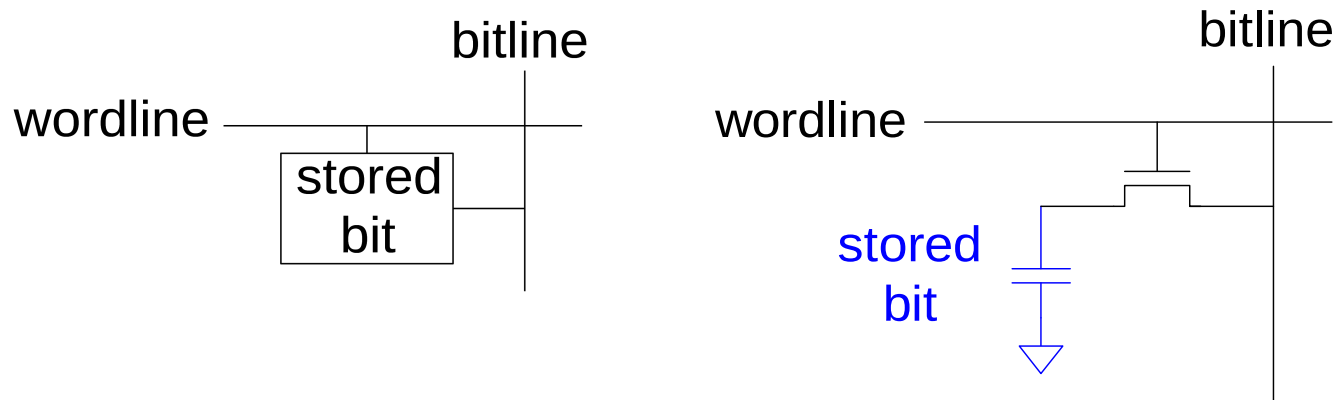
Robert Dennard, 1932 -

- Invented DRAM in 1966 at IBM
- Others were skeptical that the idea would work
- By the mid-1970's DRAM in virtually all computers

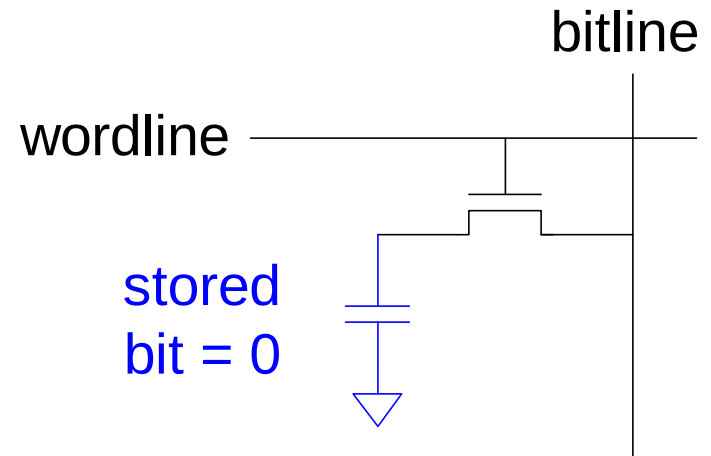
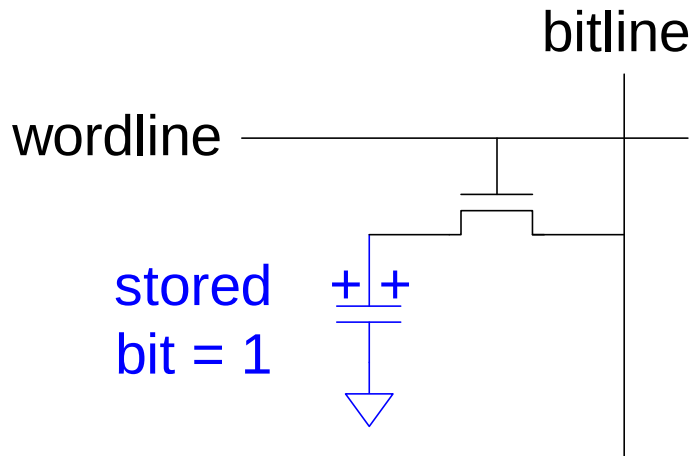


DRAM

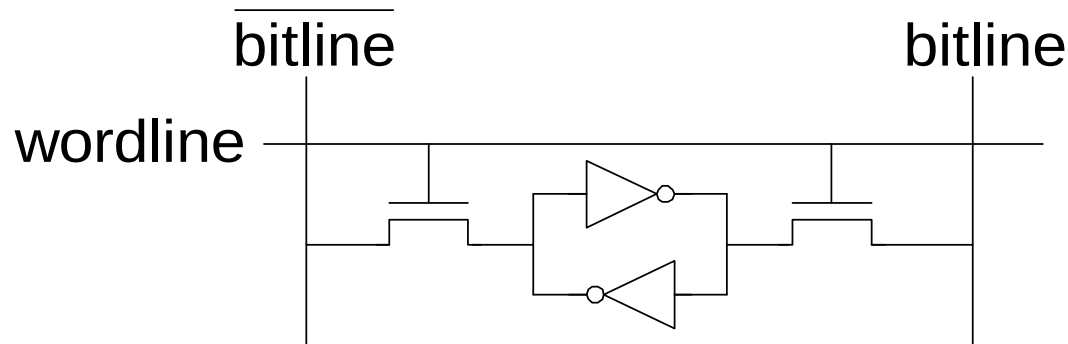
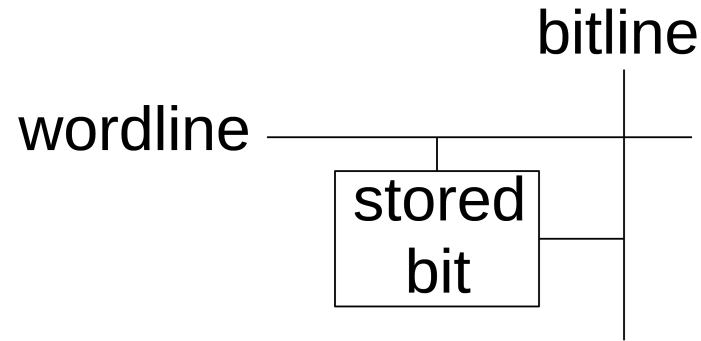
- Data bits stored on capacitor
- *Dynamic* because the value needs to be refreshed (rewritten) periodically and after read:
 - Charge leakage from the capacitor degrades the value
 - Reading destroys the stored value



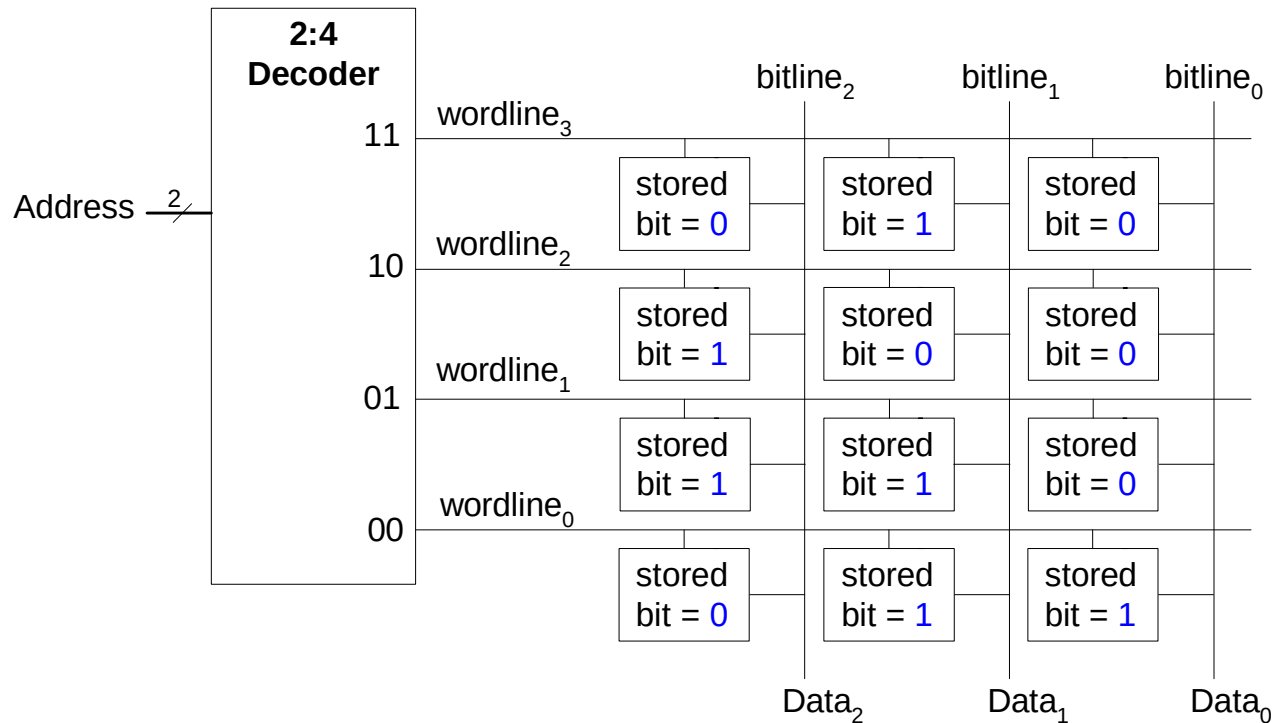
DRAM



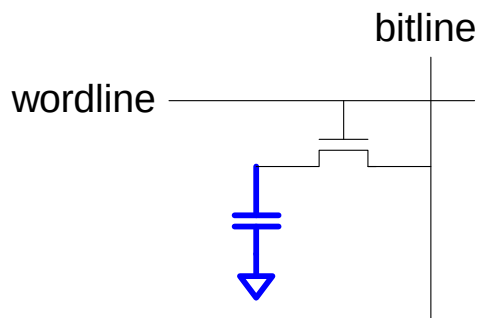
SRAM



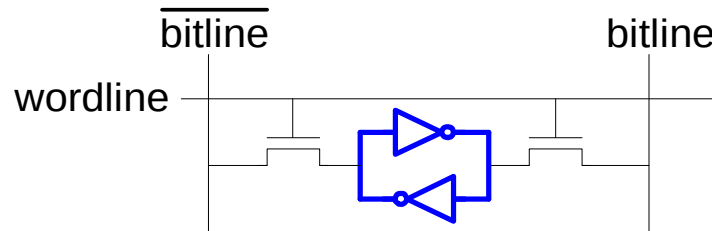
Memory Arrays Review



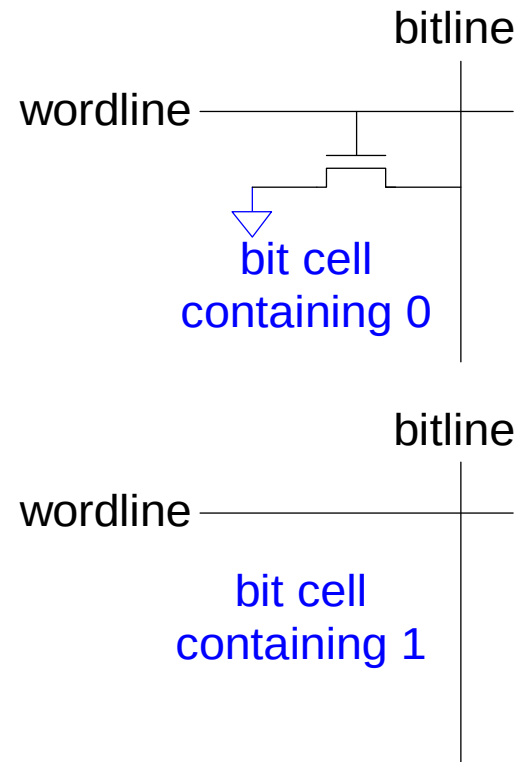
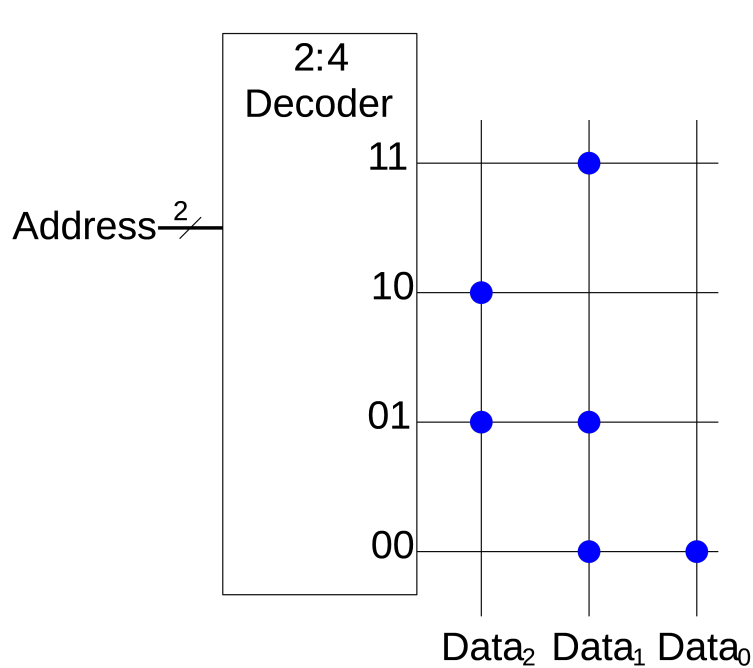
DRAM bit cell:



SRAM bit cell:



ROM: Dot Notation

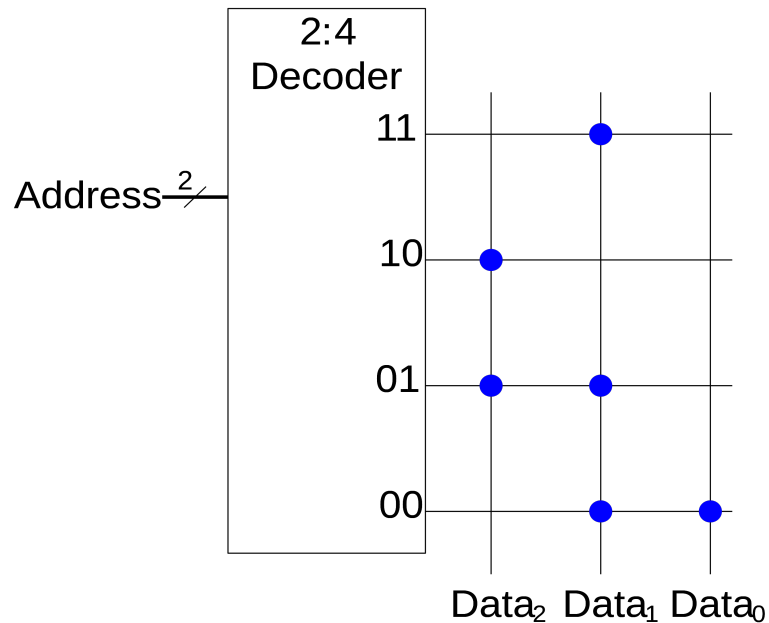


Fujio Masuoka, 1944 -

- Developed memories and high speed circuits at Toshiba, 1971-1994
- Invented Flash memory as an unauthorized project pursued during nights and weekends in the late 1970's
- The process of erasing the memory reminded him of the flash of a camera
- Toshiba slow to commercialize the idea; Intel was first to market in 1988
- Flash has grown into a \$25 billion per year market

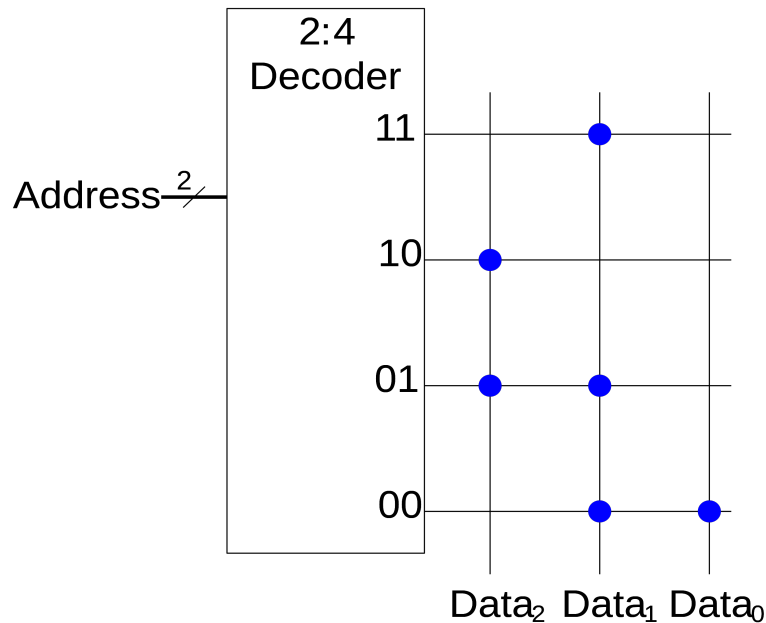


ROM Storage



Address	Data			depth ↑ ↓
11	0	1	0	
10	1	0	0	
01	1	1	0	
00	0	1	1	
			width ←→	

ROM Logic



$$Data_2 = A_1 \bar{A}_0$$

$$A_0$$

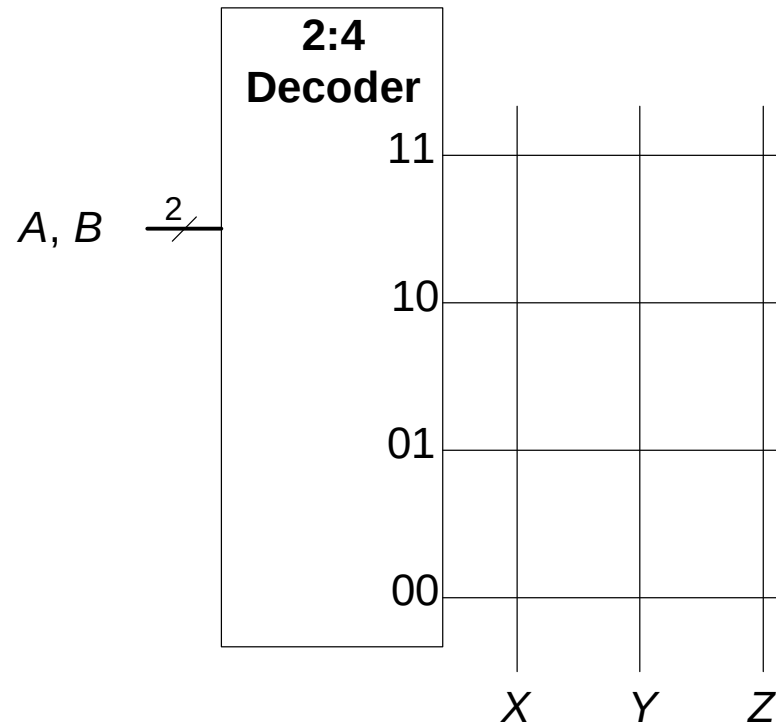
$$Data_1 = \bar{A}_1 + A_0$$

$$Data_0 = A_1 A_0$$

Example: Logic with ROMs

Implement the following logic functions using a $2^2 \times 3$ -bit ROM:

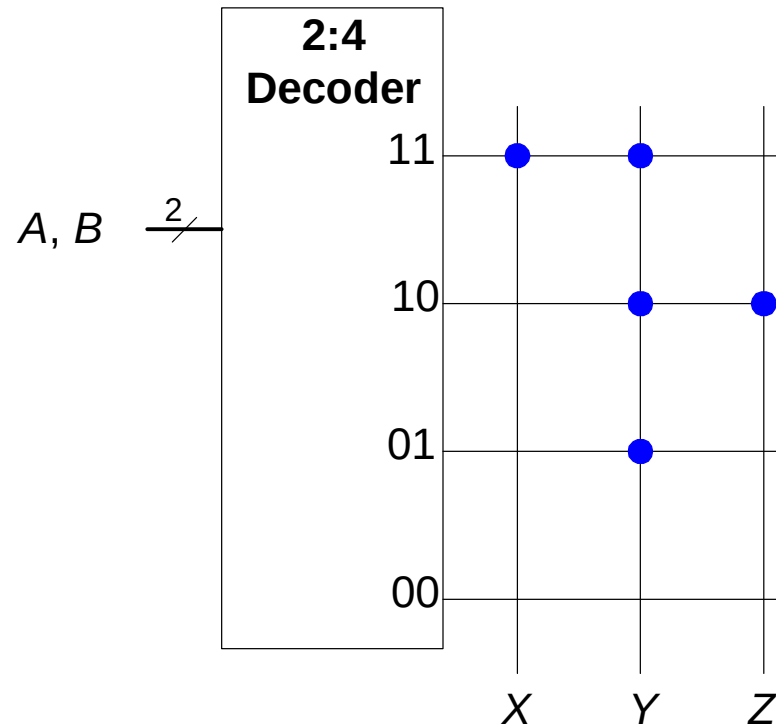
- $X = AB$
- $Y = A + B$
- $Z = A \overline{B}$



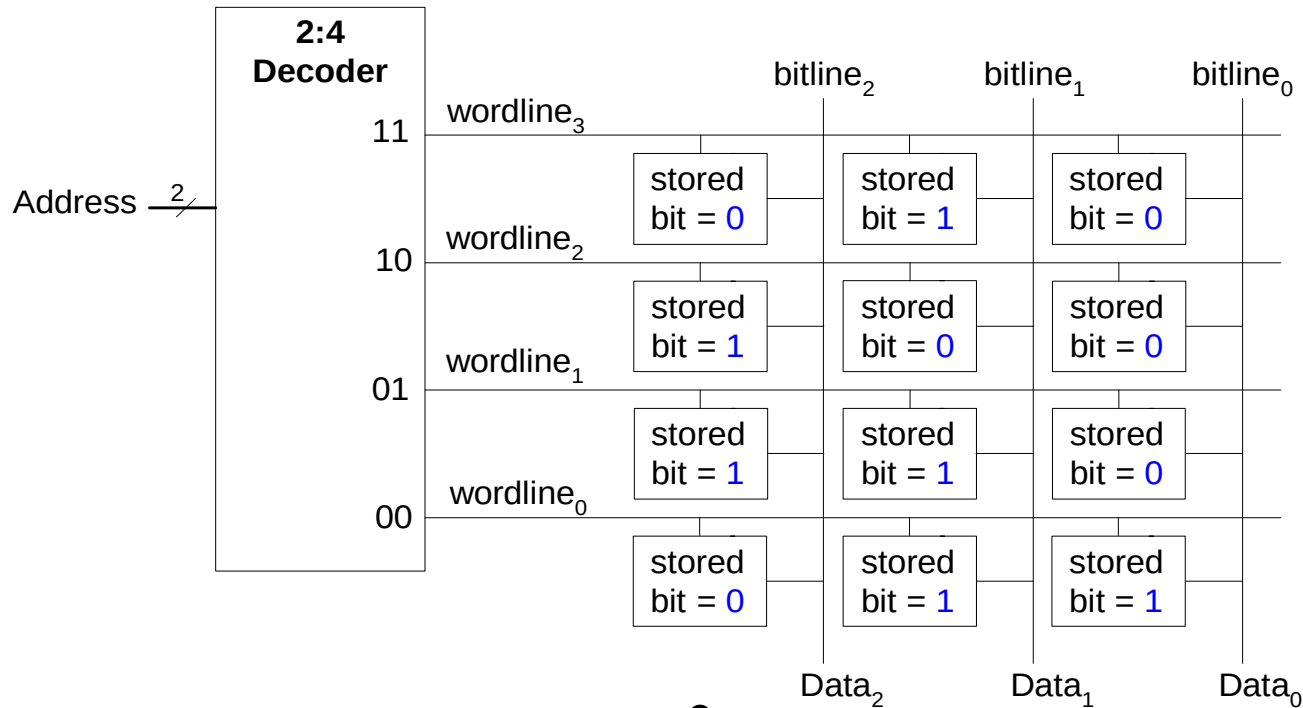
Example: Logic with ROMs

Implement the following logic functions using a $2^2 \times 3$ -bit ROM:

- $X = AB$
- $Y = A + B$
- $Z = A\overline{B}$



Logic with Any Memory



$$Data_2 = A_1 \text{ AND } A_0$$

$$A_0$$

$$Data_1 = A_1 +$$

$$A_0$$

Logic with Memory Arrays

Implement the following logic functions using a $2^2 \times 3$ -bit memory array:

- $X = AB$
- $Y = A + B$
- $Z = A \overline{B}$

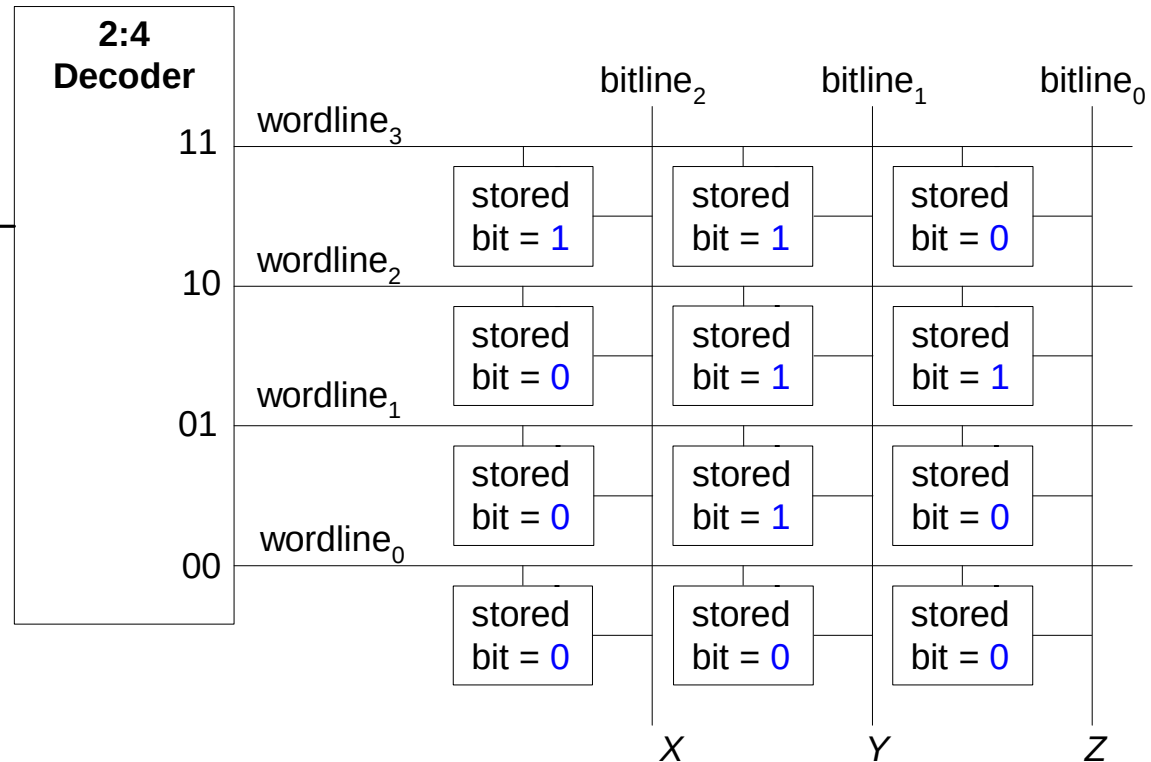
Logic with Memory Arrays

Implement the following logic functions using a $2^2 \times 3$ -bit memory array:

- $X = AB$
- $Y = A + B$
- $Z = A \overline{B}$

A, B

$\frac{2}{\text{bit}}$

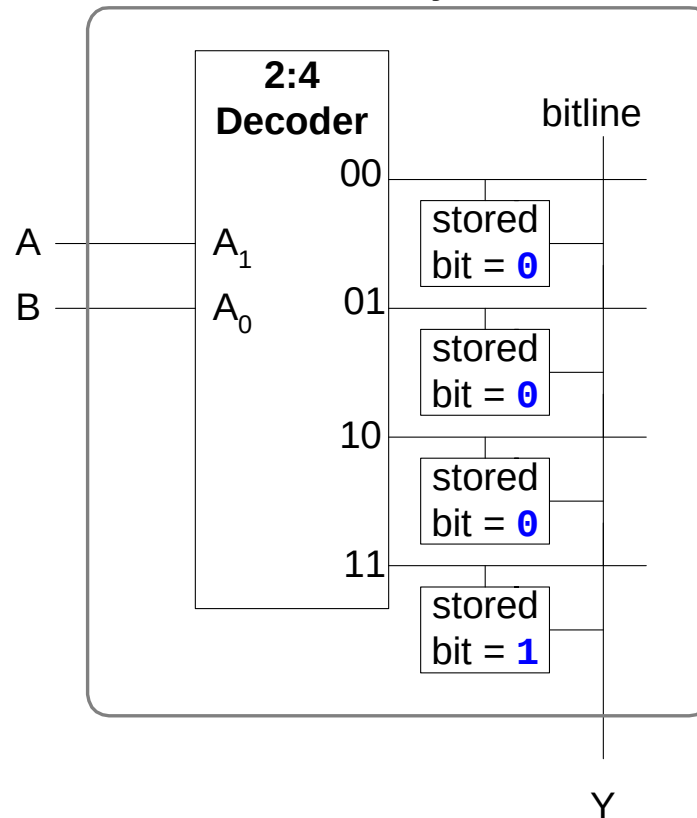


Logic with Memory Arrays

Called *lookup tables* (LUTs): look up output at each input combination (address)

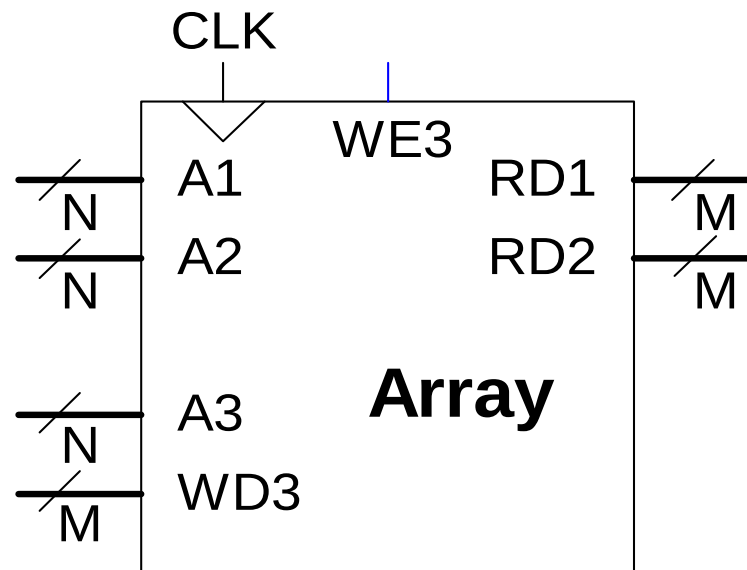
Truth Table		
A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

4-word x 1-bit Array



Multi-ported Memories

- **Port:** address/data pair
- 3-ported memory
 - 2 read ports (A1/RD1, A2/RD2)
 - 1 write port (A3/WD3, WE3 enables writing)
- **Register file:** small multi-ported memory



SystemVerilog Memory

```
// 256 x 3 memory module with one read/write port
module dmem( input  logic      clk, we,
             input  logic [7:0] a,
             input  logic [2:0] wd,
             output logic [2:0] rd);

    logic [2:0] RAM[255:0];

    assign rd = RAM[a];

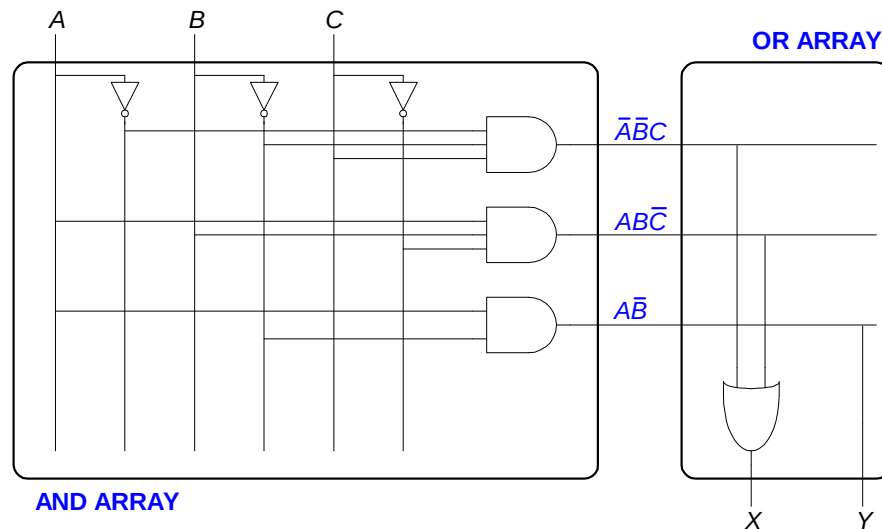
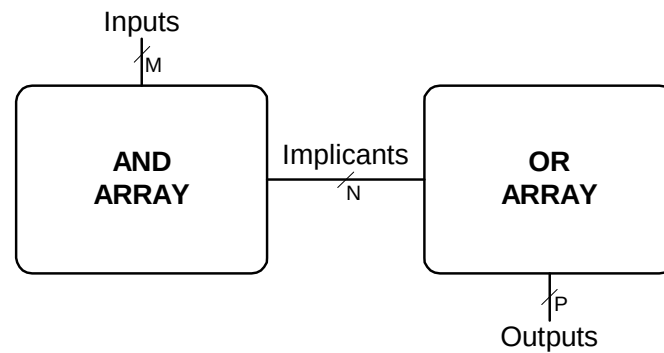
    always @(posedge clk)
        if (we)
            RAM[a] <= wd;
endmodule
```

Logic Arrays

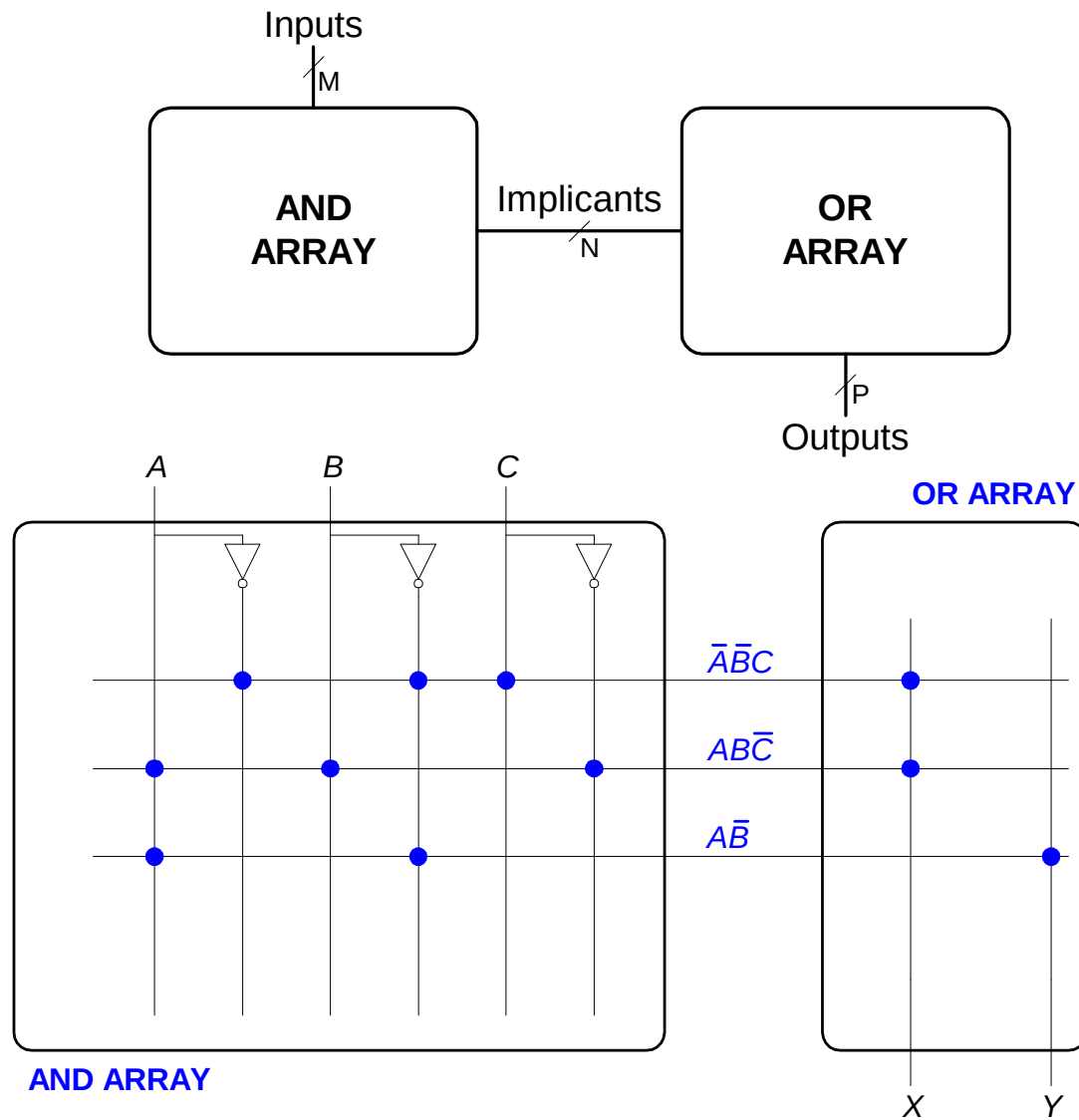
- **PLAs** (Programmable logic arrays)
 - AND array followed by OR array
 - Combinational logic only
 - Fixed internal connections
- **FPGAs** (Field programmable gate arrays)
 - Array of Logic Elements (LEs)
 - Combinational and sequential logic
 - Programmable internal connections

PLAs

- $X = \bar{A}\bar{B}C + ABC\bar{C}$
- $Y = A\bar{B}$



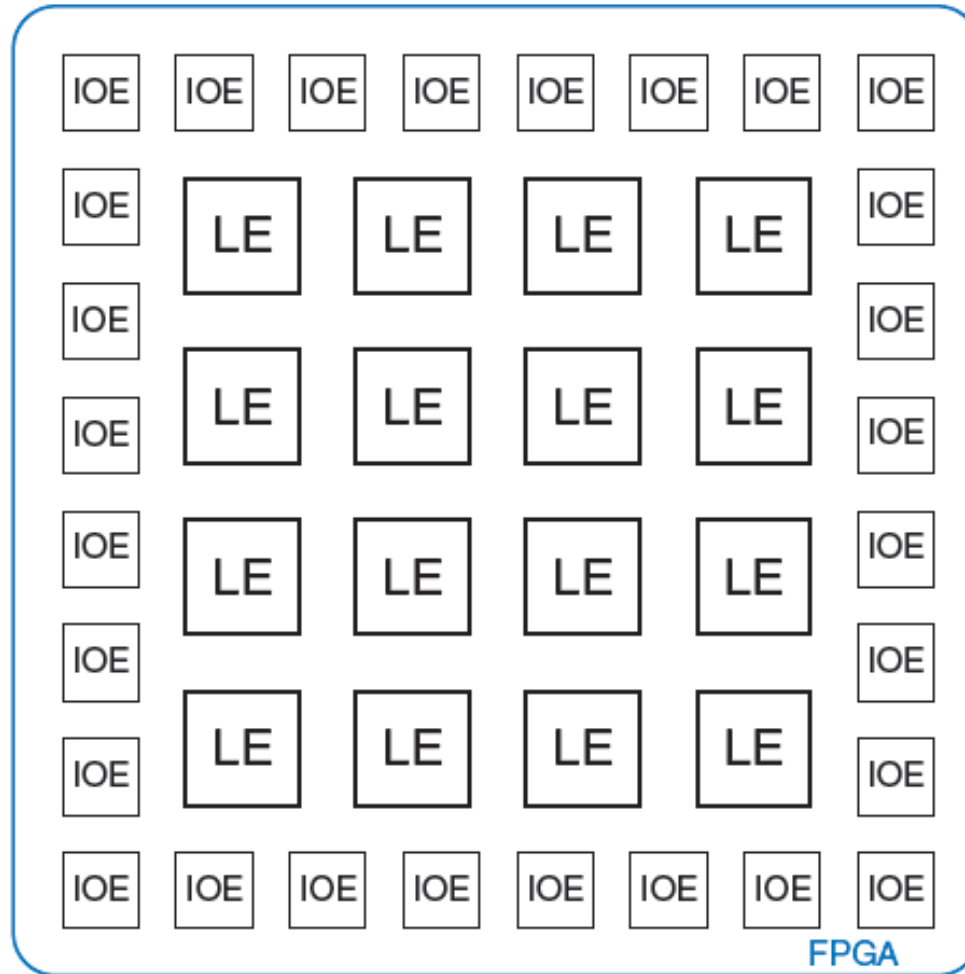
PLAs: Dot Notation



FPGA: Field Programmable

- Composed of:
 - **LEs** (Logic elements): perform logic
 - **IOEs** (Input/output elements): interface with outside world
 - **Programmable interconnection:** connect LEs and IOEs
 - Some FPGAs include other building blocks such as multipliers and RAMs

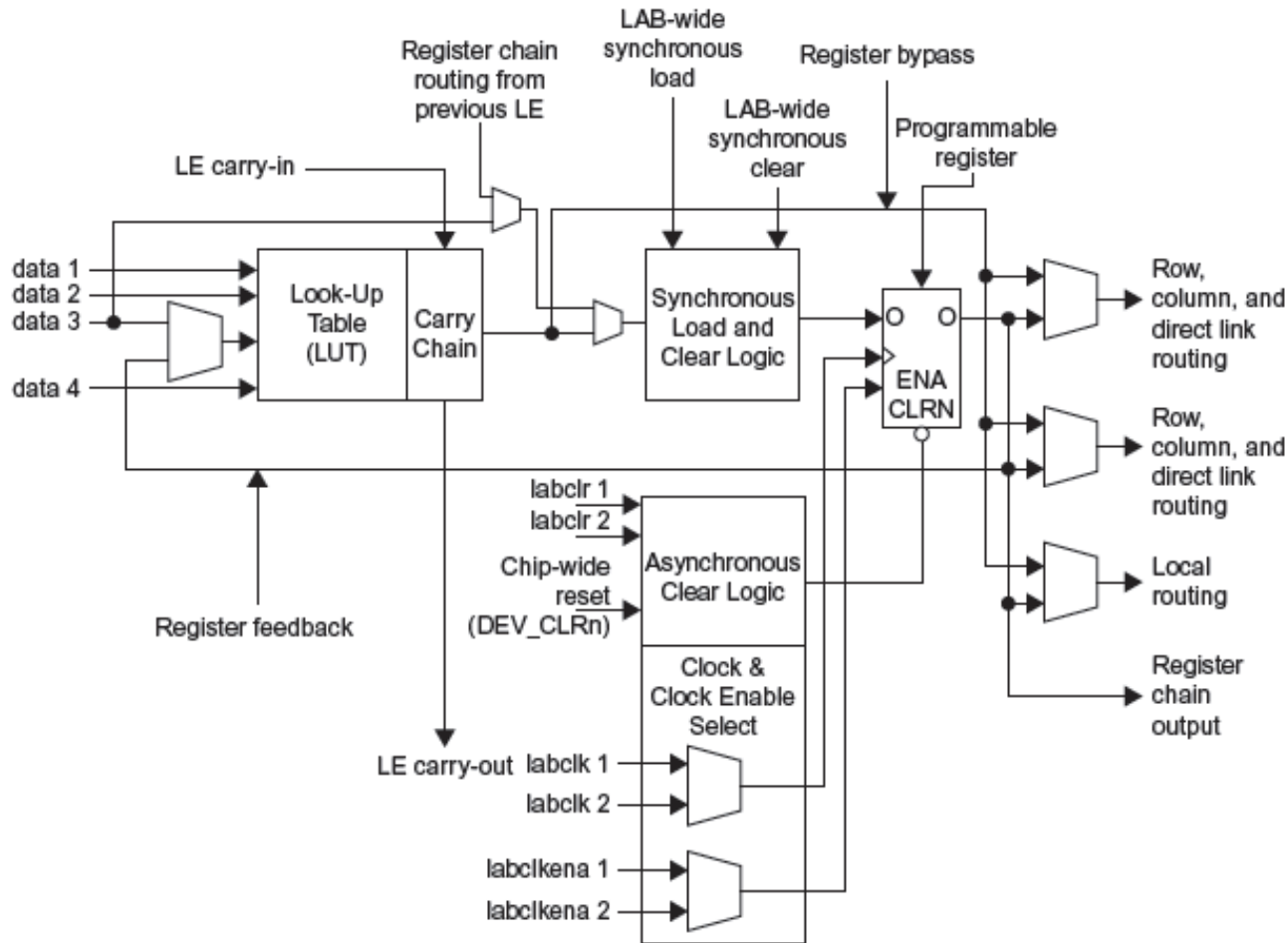
General FPGA Layout



LE: Logic Element

- Composed of:
 - **LUTs** (lookup tables): perform combinational logic
 - **Flip-flops**: perform sequential logic
 - **Multiplexers**: connect LUTs and flip-flops

Altera Cyclone IV LE



Altera Cyclone IV LE

- The Altera Cyclone IV LE has:
 - 1 four-input LUT
 - 1 registered output
 - 1 combinational output

LE Configuration Example

Show how to configure a Cyclone IV LE to perform the following functions:

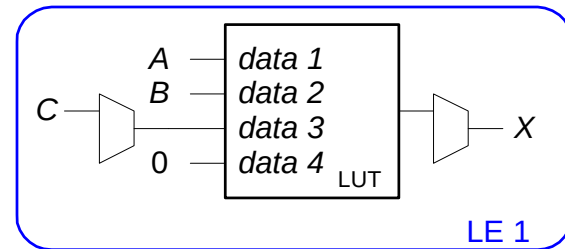
- $X = \overline{A}\overline{B}C + A\overline{B}C$
- $Y = A\overline{B}$

LE Configuration Example

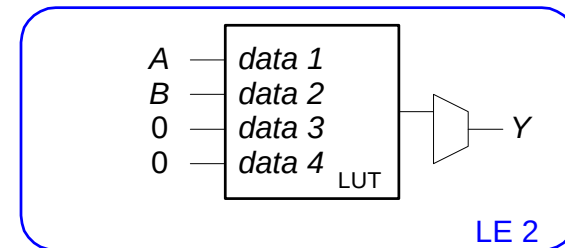
Show how to configure a Cyclone IV LE to perform the following functions:

- $X = \overline{A}\overline{B}C + A\overline{B}C$
- $Y = A\overline{B}$

(A) data 1	(B) data 2	(C) data 3	data 4	(X) LUT output
0	0	0	X	0
0	0	1	X	1
0	1	0	X	0
0	1	1	X	0
1	0	0	X	0
1	0	1	X	0
1	1	0	X	1
1	1	1	X	0



(A) data 1	(B) data 2	data 3	data 4	(Y) LUT output
0	0	X	X	0
0	1	X	X	0
1	0	X	X	1
1	1	X	X	0



FPGA Design Flow

Using a CAD tool (such as Altera's Quartus II)

- **Enter the design** using schematic entry or an HDL
- **Simulate** the design
- **Synthesize** design and map it onto FPGA
- **Download the configuration** onto the FPGA
- **Test** the design