## Functional Programming – Series 6b

In this series of exercises we will write a type checker for expressions.

Exercise 1. Given are embedded languages for expressions and for types:

$$\begin{aligned} \textbf{data} \ \textit{Expr} &= \textit{Const Int} \\ &\mid \textit{Var String} \\ &\mid \textit{BinOp String Expr Expr} \\ &\mid \textit{App Expr Expr} \end{aligned}$$

$$\mathbf{data} \ \mathit{Type} = \mathit{IntType} \\ | \mathit{FunType} \ \mathit{Type} \ \mathit{Type} \ \mathit{Type}$$

Define a function

$$typeOf::Env \rightarrow Expr \rightarrow Type$$

Here, the *environment Env* contains the types of elementary variables and functions, denoted by *Strings*. It is defined as follows:

$$\mathbf{type}\; Env = [(String, \mathit{Type})]$$

The environment should contain type for at least the operations +, \*, -, where these operations are indicated as strings "+", etcetera.

**Exercise 2.** Extend the embedded languages above with an expression for *if-the-else*, and adapt the types where approprite. The environment now should contain operations && and || for booleans as well.

**Exercise 3.** Extend the expressions and types with 2-tuples and 3-tuples.

**Exercise 4.** Add lambda expressions to your language, where a lambda expression contains the types of the formal parameters, in the following form:

where a is a type.

**Remark.** Note that above no *type variables* are requested. That would require *substitution* and *unification*, which is at this moment not requested.