# CISC 372: Parallel Computing CUDA, part 4

Stephen F. Siegel

Department of Computer and Information Sciences
University of Delaware

#### Matrix multiplication

$$\begin{bmatrix} a_{00} & a_{01} & a_{02} \\ a_{10} & a_{11} & a_{12} \end{bmatrix} \times \begin{bmatrix} b_{00} & b_{01} & b_{02} \\ b_{10} & b_{11} & b_{12} \\ b_{20} & b_{21} & b_{22} \end{bmatrix} =$$

$$\begin{bmatrix} a_{00}b_{00} + a_{01}b_{10} + a_{02}b_{20} & a_{00}b_{01} + a_{01}b_{11} + a_{02}b_{21} & a_{00}b_{02} + a_{01}b_{12} + a_{02}b_{22} \\ a_{10}b_{00} + a_{11}b_{10} + a_{12}b_{20} & a_{10}b_{01} + a_{11}b_{11} + a_{12}b_{21} & a_{10}b_{02} + a_{11}b_{12} + a_{12}b_{22} \end{bmatrix}$$

#### Matrix multiplication: sequential CPU code

See seq/matmul.c.

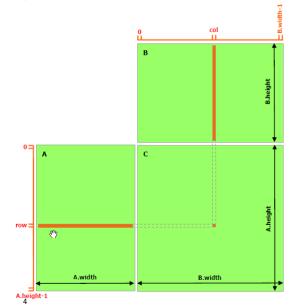
```
 b: n \times l 
 b: l \times m 
 c: n \times m 
 c_{ij} = \sum_{i=1}^{l-1} a_{ik} b_{kj}
```

Time for n=l=m=8000: > 1 hour (512 billion multiplications)

```
for (int i = 0; i < n; i++)
  for (int j = 0; j < m; j++)
    c[i][j] = 0.0;
for (int i = 0; i < n; i++) {
  for (int j = 0; j < m; j++) {
    for (int k = 0; k < 1; k++)
        c[i][j] += a[i][k]*b[k][j];
  }
}</pre>
```

# CUDA: simple matrix multiplication [CUDA Programming Guide 3.2.3]

- $ightharpoonup A: n \times l$
- $\triangleright$  B:  $l \times m$
- $ightharpoonup C: n \times m$
- each thread computes at most one element of c
- $c_{ij} = \sum_{k=0}^{\infty} a_{ik} b_{kj}$



#### Simple matrix multiplication: matmul1.cu: kernel

```
/* Kernel. Multiplies a and b, sticking results into c.
   a is nxl, b is lxm, c is nxm. */
__global__ void multiply(int n, int 1, int m,
                         double * a, double * b, double * c) {
  int i = blockDim.v * blockIdx.v + threadIdx.v;
  int j = blockDim.x * blockIdx.x + threadIdx.x;
  if (i < n && j < m) {
    double result = 0.0:
    for (int k = 0; k < 1; k++)
      result += a[i*l + k] * b[k*m + j]; // a[i][k] * b[k][j];
    c[i*m + j] = result; // c[i][j]
```

- on Beowulf (K40c): Time for n = l = m = 8000: 13.8s.
- can we do better?

#### matmul1.cu: memory analysis

#### Questions?

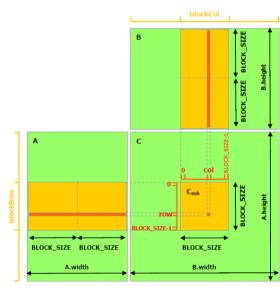
- how many times is each element of a read from global memory?
- how many times is each element of b read from global memory?

#### Answers.

- element  $a_{ik}$  is used in the computation of every element of row i of c:  $c_{i,0,m-1}$
- ightharpoonup hence  $a_{ik}$  is read m times
- $\blacktriangleright$  element  $b_{kj}$  is used in the computation of every element of column j of c:  $c_{0...n-1..i}$
- ightharpoonup hence  $b_{ki}$  is read n times
- reading from global memory is slow!
- can we use shared memory?
- note: you will never be able to fit the whole matrices into shared memory at once!

## Matrix multiplication: using shared memory

- ► *C* is divided into square blocks
- lacktriangle each CUDA block computes one block of C
  - this computation requires one row of blocks from A
  - ightharpoonup and one column of blocks from B
- for s = 0, 1, ...
  - load block s of A's row of blocks into shared memory
  - ▶ load block s of B's column of blocks into shared memory
  - multiply to get partial result
  - accumulate sum of partial results
  - each element of A is loaded m/BLOCK\_SIZE times
  - each element of B is loaded n/BLOCK\_SIZE times



# Using shared memory: matmul2.cu: kernel, part 1: load

```
__global__ void multiply(int n, int l, int m,
                         double * a. double * b. double * c) {
 int i_local = threadIdx.y, j_local = threadIdx.x;
 int i = blockDim.y * blockIdx.y + i_local; // row of c
 int j = blockDim.x * blockIdx.x + j_local; // col of c
 double result = 0.0;
 for (int s = 0; s < 1; s += BLOCK_SIZE) {
   __shared__ double a_s[BLOCK_SIZE][BLOCK_SIZE];
    __shared__ double b_s[BLOCK_SIZE][BLOCK_SIZE];
   // each thread loads its one element of a: a[i][s+j_local]
   if (i < n \&\& s + i_local < 1)
     a_s[i_local][i_local] = a[i*l + s + i_local];
   // each thread loads its one element of b: b[s+i_local][i]
    if (s + i local < l && i < m)
     b_s[i_local][j_local] = b[(s + i_local)*m + j];
   svncthreads():
```

## Using shared memory: matmul2.cu: kernel, part 2: multiply and store

```
// need s + k < 1, i.e., k < 1 - s
 const int k_stop = MIN(BLOCK_SIZE, 1 - s);
 for (int k = 0; k < k_stop; k++)
    if (i < n \&\& j < m)
      result += a_s[i_local][k] * b_s[k][i_local];
 __syncthreads():
if (i < n && i < m)
 c[i*m + j] = result; // c[i][j]
```

 $\blacktriangleright$  on Beowulf (K40c): Time for n=l=m=8000: 4.8s.

#### CUDA: additional concepts

- CUDA events provide a practical way to time things all within CUDA
- multiple devices
  - cudaGetDeviceCount(int \*count)
  - cudaSetDevice(int device)
  - launch a kernel on one device
  - change the device (set device to something else)
  - launch another kernel, repeat

#### Hybrid all the way: MPI+OpenMP+CUDA

To take advantage of all hardware in a modern supercomputer. . .

- use MPI for interprocess communication
- use OpenMP or other threading model for intraprocess (shared memory) concurrency on the CPU
- use CUDA to offload certain computations onto GPGPUs
- ...all in one program!
  - you know how to do each of these separately.
  - here is simple "hello world" example as a template for combining all three forms
  - ▶ hybrid.cu

#### hybrid.cu: MPI+OpenMP+CUDA, part 1: kernel

```
#include <stdio.h>
#include <mpi.h>
#include <omp.h>
#include <assert.h>
__global__ void kernel(int rank) {
 int bid = blockIdx.x;
 int tid = threadIdx.x:
 printf("Hello from block %d, thread %d of the GPU, called by process %d\n",
          bid, tid, rank);
```

- each MPI process will invoke the kernel
- the process will pass its rank (ID) as an argument
- this would be appropriate, for example, with one MPI process and one GPU card per node

#### hybrid.cu: MPI+OpenMP+CUDA, part 2: host code

```
int main (void) {
 int rank, nprocs, required = MPI_THREAD_FUNNELED, provided;
 MPI_Init_thread(&argc, &argv, required, &provided);
 assert(provided == MPI_THREAD_FUNNELED);
 MPI_Barrier(MPI_COMM_WORLD);
 double start = MPI_Wtime();
 MPI_Comm_size(MPI_COMM_WORLD, &nprocs); MPI_Comm_rank(MPI_COMM_WORLD, &rank);
 kernel << 3,4>>> (rank); // 3 blocks, 4 threads per block
#pragma omp parallel shared(rank,nprocs)
   int tid = omp_get_thread_num(), nthreads = omp_get_num_threads();
   printf("Greetings from CPU thread %d/%d of process %d/%d!\n",
           tid. nthreads. rank. nprocs):
 cudaDeviceSvnchronize():
 MPI_Barrier(MPI_COMM_WORLD);
 if (rank == 0) printf("Time: %f\n", MPI_Wtime() - start);
 MPI_Finalize();
```

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#### Makefile

```
NAME = hybrid
ROOT = .../.../..
include $(ROOT)/common.mk
NPROCS = 2
NCORES = 4
all: $(NAME).exec
test: $(NAME).exec
        $(MPIRUN) -n $(NPROCS) -c $(NCORES) --gres=gpu:1 ./$<</pre>
$(NAME).exec: $(NAME).cu Makefile
        nvcc --compiler-options -fopenmp -o $0 --compiler-bindir mpic++ $<
.PHONY: all test
```

#### Run on Beowulf

```
siegel@grendel:~/372/code/src/cuda/hybrid$ make test
nvcc --compiler-options -fopenmp -o hybrid.exec --compiler-bindir mpic++ hybrid.cu
srun --unbuffered -n 2 -c 4 --gres=gpu:1 ./hybrid.exec
Greetings from CPU thread 0/4 of process 0/2!
Greetings from CPU thread 3/4 of process 0/2!
Greetings from CPU thread 2/4 of process 0/2!
Greetings from CPU thread 1/4 of process 0/2!
Hello from block 0, thread 0 of the GPU, called by process 0
Hello from block 0, thread 1 of the GPU, called by process 0
Hello from block 1, thread 3 of the GPU, called by process 0
Greetings from CPU thread 0/4 of process 1/2!
Greetings from CPU thread 2/4 of process 1/2!
Greetings from CPU thread 1/4 of process 1/2!
Greetings from CPU thread 3/4 of process 1/2!
Hello from block 0, thread 0 of the GPU, called by process 1
Hello from block 0, thread 1 of the GPU, called by process 1
Hello from block 1, thread 3 of the GPU, called by process 1
Time: 0.530748
```

#### Bridges SLURM script: hybrid\_p100.sh

```
#!/bin/bash
# 1 node with 4 cores and 1 GPU is requested.
# On this node we run a program with 2 processes, each with 2 threads.
# Each process also invokes, once, a 3x4 GPU kernel.
#SBATCH -p GPU-shared
#SBATCH -t. 00:01:00
#SBATCH -N 1
#SBATCH --ntasks-per-node 4
#SBATCH --gpus=1
# echo commands to stdout
set -x
OMP_NUM_THREADS=2 mpirun -np 2 ./hybrid.exec
```

#### Bridges hybrid output

```
+ OMP NUM THREADS=2
+ mpirun -np 2 ./hybrid.exec
Greetings from CPU thread 0/2 of process 1/2!
Greetings from CPU thread 1/2 of process 1/2!
Hello from block 0, thread 0 of the GPU, called by process 1
Hello from block 0, thread 1 of the GPU, called by process 1
. . .
Hello from block 1, thread 1 of the GPU, called by process 0
Hello from block 1, thread 2 of the GPU, called by process 0
Hello from block 1, thread 3 of the GPU, called by process 0
Time: 0.292469
```