# Tsvstat

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## 1 Introduction

The *tsvtstat* tool can be used to generate a table of summary statistics given a table or stream of tab separated numeric observations.

### 2 Statistics

The formulas used to generate statistics are compatible with those used by common spreadsheets.

#### 2.1 Mean

$$\bar{x} = \sum \frac{x_i}{n}$$

$$\implies \sum x_i = n\bar{x} \tag{1}$$

## 2.2 Sample Variance and Standard Deviation

$$s^{2} = \frac{1}{n-1} \sum_{1}^{n} (x_{i} - \bar{x})^{2}$$
Sample Variance
$$= \frac{1}{n-1} \sum_{1}^{n} (x_{i}^{2} - 2\bar{x}x_{i} + \bar{x}^{2})$$

$$= \frac{1}{n-1} (\sum_{1}^{n} x_{i}^{2} - 2\bar{x} \sum_{1} x_{i} + n\bar{x}^{2})$$

$$= \frac{1}{n-1} (\sum_{1}^{n} x_{i}^{2} - 2n\bar{x}^{2} + n\bar{x}^{2})$$
substitute (1)
$$= \frac{1}{n-1} \sum_{1}^{n} x_{i}^{2} - n\bar{x}^{2})$$

$$s = \sqrt{s^{2}}$$
Sample Variance

#### 2.3 Skewness

$$skew = \frac{n}{(n-1)(n-2)} \sum \frac{(x, -\bar{x})^3}{s^3}$$

$$= \frac{n}{(n-1)(n-2)} \frac{\sum x_i^3 - 3\bar{x} \sum x_i^2 + 2n\bar{x}^3}{s^3}$$
 subst. (3)

$$\sum_{1}^{n} (x_{i} - \bar{x})^{3} = \sum_{1}^{n} (x_{i}^{2} - 2x_{i}\bar{x} + \bar{x}^{2})(x_{i} - \bar{x})$$

$$= \sum_{1}^{n} (x_{i}^{3} - 2x_{i}^{2}\bar{x} + x_{i}\bar{x}^{2} - \bar{x}x_{i}^{2} + 2x_{i}\bar{x}^{2} - \bar{x}^{3})$$

$$= \sum_{1}^{n} (x_{i}^{3} - 3x_{i}^{2}\bar{x} + 3x_{i}\bar{x}^{2} - \bar{x}^{3})$$

$$= \sum_{1}^{n} x_{i}^{3} - 3\bar{x} \sum x_{i}^{2} + 3\bar{x}^{2} \sum x_{i} - n\bar{x}^{3}$$

$$= \sum_{1}^{n} x_{i}^{3} - 3\bar{x} \sum x_{i}^{2} + 3n\bar{x}^{3} - n\bar{x}^{3}$$
 by (1)
$$= \sum_{1}^{n} x_{i}^{3} - 3\bar{x} \sum x_{i}^{2} + 2n\bar{x}^{3}$$
 (3)

#### 2.4 Kurtosis

$$kurt = \frac{n(n+1)}{(n-1)(n-2)(n-3)} \sum_{1}^{n} \frac{(x,-\bar{x})^4}{s^4} - \frac{3(n-1)^2}{(n-2)(n-3)}$$

$$= \frac{n(n+1)}{(n-1)(n-2)(n-3)} \frac{\sum_{1}^{n} x_i^4 - 4\bar{x} \sum_{1}^{n} x_i^3 + 6\bar{x}^2 \sum_{1}^{n} x_i^2 - 3n\bar{x}^4}{s^4} \quad \text{substitute (4)}$$

$$- \frac{3(n-1)^2}{(n-2)(n-3)}$$

excess kurtosis = kurt - 3

$$\sum_{1}^{n} (x_{i} - \bar{x})^{4} = \sum_{1}^{n} (x_{i} - \bar{x})^{3} (x_{i} - \bar{x})$$

$$= \sum_{1}^{n} (x_{i}^{3} - 3x_{i}^{2}\bar{x} + 3x_{i}\bar{x}^{2} - \bar{x}^{3})(x_{i} - \bar{x}) \qquad \text{substitute (2)}$$

$$= \sum_{1}^{n} x_{i}(x_{i}^{3} - 3x_{i}^{2}\bar{x} + 3x_{i}\bar{x}^{2} - \bar{x}^{3}) - \bar{x}(x_{i}^{3} - 3x_{i}^{2}\bar{x} + 3x_{i}\bar{x}^{2} - \bar{x}^{3})$$

$$= \sum_{1}^{n} (x_{i}^{4} - 3x_{i}^{3}\bar{x} + 3x_{i}^{2}\bar{x}^{2} - x_{i}\bar{x}^{3}) - (\bar{x}x_{i}^{3} - 3x_{i}^{2}\bar{x}^{2} + 3x_{i}\bar{x}^{3} - \bar{x}^{4})$$

$$= \sum_{1}^{n} (x_{i}^{4} - 4x_{i}^{3}\bar{x} + 6x_{i}^{2}\bar{x}^{2} - 4x_{i}\bar{x}^{3} + \bar{x}^{4})$$

$$= \sum_{1}^{n} x_{i}^{4} - 4\bar{x} \sum_{1}^{n} x_{i}^{3} + 6\bar{x}^{2} \sum_{1}^{n} x_{i}^{2} - 4\bar{x}^{3} \sum_{1}^{n} x_{i} + n\bar{x}^{4})$$

$$= \sum_{1}^{n} x_{i}^{4} - 4\bar{x} \sum_{1}^{n} x_{i}^{3} + 6\bar{x}^{2} \sum_{1}^{n} x_{i}^{2} - 4n\bar{x}^{4} + n\bar{x}^{4}$$

$$= \sum_{1}^{n} x_{i}^{4} - 4\bar{x} \sum_{1}^{n} x_{i}^{3} + 6\bar{x}^{2} \sum_{1}^{n} x_{i}^{2} - 3n\bar{x}^{4}$$

$$(4)$$