6.S085 Statistics for Research Projects

IAP 2014

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Lecture 8: January 30

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Correction from last time: Kruskal-Wallis non-parametric ANOVA

Noise distribution needs to be the same across data points (need not be Gaussian)

 H_0 : median of all groups is the same

8.1 Machine Learning and Predictive Analytics

Code Blue Example

Recall: how many predicted "positive" / how many there were positive

False positive: how many predicted "positive" incorrectly

8.2 Supervised Learning vs. Unsupervised Learning

Supervised:

- data is labeled
- want to predict label for new point
- Example: email spam classification
 - Training data: emails labeled (manually as spam/notspam)
 - Test data: new emails (want to classify as spam/notspam)

Unsupervised:

- data is not labeled
- want to find structure in the data

Notes:

- Features matter a lot!
- When we can't predict well, generally it's because we don't have good features
- Good features give huge performance gains vs. specifics of what ML algorithm is used

8.3 Supervised Learning

Two approaches: one is probabilistic, the other is not

8.3.1 Probabilistic

Specify a probabilistic model that we assume data is actually generated from

Naive Bayes (probabilistic model) for email spam classification

Idea: specify how an email's features are are generated.

- 1. Flip a biased coin: If H, new email is spam. If T, new email is not spam
- 2. Generate each feature value independently, dependending on whether email is spam/ham

Notice model has parameters!

5 Numbers

- 1. Prob(email is spam)
- 2. Prob("asks for password" is True |spam), Prob("mentions Nigerian prince" |spam)
- 3. Prob("asks for password" is True |notspam), Prob("mentions Nigerian prince" |notspam)

Training: Estimate these parameters

Testing: Prob(spam|new email)

Use Bayes' Rule:

$$P(A|B) = \frac{P(B|A)P(A)}{P(B)}$$

New email: (True, True,?)

Want:

P(SPAM|(TRUE, TRUE, ?))

 $= \frac{P((\text{TRUE}, \text{TRUE}, ?)|\text{SPAM})P(\text{SPAM})}{P((\text{TRUE}, \text{TRUE}, ?)|\text{SPAM})P(\text{SPAM}) + P(|\text{HAM})P(\text{HAM})}$