

Please check the examination details below before entering your candidate information

Candidate surname		Other names	
Centre Number		Candidate Number	
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**Pearson Edexcel Level 3 GCE**

**Tuesday 11 June 2024**

Afternoon (Time: 2 hours)	Paper reference	<b>9MA0/02</b>
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**Mathematics**

**Advanced**

**PAPER 2: Pure Mathematics 2**

<b>You must have:</b> Mathematical Formulae and Statistical Tables (Green), calculator	Total Marks
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**Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 15 questions in this question paper. The total mark for this paper is 100.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

Turn over ►

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1.

$$y = 4x^3 - 7x^2 + 5x - 10$$

(a) Find in simplest form

(i)  $\frac{dy}{dx}$

(ii)  $\frac{d^2y}{dx^2}$

(3)

(b) Hence find the exact value of  $x$  when  $\frac{d^2y}{dx^2} = 0$ 

(2)



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Question 1 continued

Lined area for writing the answer to Question 1.

(Total for Question 1 is 5 marks)



2. Jamie takes out an interest-free loan of £8100

Jamie makes a payment every month to pay back the loan.

Jamie repays £400 in month 1, £390 in month 2, £380 in month 3, and so on, so that the amounts repaid each month form an arithmetic sequence.

- (a) Show that Jamie repays £290 in month 12 (1)

After Jamie's  $N$ th payment, the loan is completely paid back.

- (b) Show that  $N^2 - 81N + 1620 = 0$  (2)

- (c) Hence find the value of  $N$ . (2)



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Question 2 continued

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(Total for Question 2 is 5 marks)



3. The point  $P(3, -2)$  lies on the curve with equation  $y = f(x)$ ,  $x \in \mathbb{R}$

Find the coordinates of the point to which  $P$  is mapped when the curve with equation  $y = f(x)$  is transformed to the curve with equation

(i)  $y = f(x - 2)$

(ii)  $y = f(2x)$

(iii)  $y = 3f(-x) + 5$

(4)



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Question 3 continued

Lined area for writing the answer to Question 3.

(Total for Question 3 is 4 marks)



4. A sequence  $u_1, u_2, u_3, \dots$  is defined by

$$u_{n+1} = ku_n - 5$$

$$u_1 = 6$$

where  $k$  is a positive constant.

Given that  $u_3 = -1$

- (a) show that

$$6k^2 - 5k - 4 = 0 \quad (2)$$

- (b) Hence

- (i) find the value of  $k$ ,

- (ii) find the value of  $\sum_{r=1}^3 u_r$  (3)





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Question 4 continued

Lined area for writing the answer to Question 4.

(Total for Question 4 is 5 marks)



5. Given that  $\theta$  is small and in radians, use the small angle approximations to find an approximate numerical value of

$$\frac{\theta \tan 2\theta}{1 - \cos 3\theta}$$

(3)



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Question 5 continued

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(Total for Question 5 is 3 marks)



6.

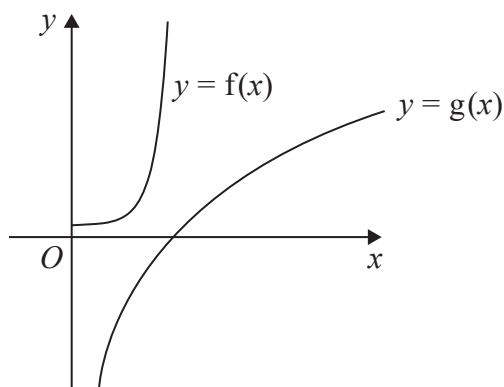


Figure 1

Figure 1 shows a sketch of the curves with equations  $y = f(x)$  and  $y = g(x)$  where

$$f(x) = e^{4x^2 - 1} \quad x > 0$$

$$g(x) = 8 \ln x \quad x > 0$$

(a) Find

(i)  $f'(x)$

(ii)  $g'(x)$

(2)

Given that  $f'(x) = g'(x)$  at  $x = \alpha$

(b) show that  $\alpha$  satisfies the equation

$$4x^2 + 2 \ln x - 1 = 0$$

(2)

The iterative formula

$$x_{n+1} = \sqrt{\frac{1 - 2 \ln x_n}{4}}$$

is used with  $x_1 = 0.6$  to find an approximate value for  $\alpha$

(c) Calculate, giving each answer to 4 decimal places,

(i) the value of  $x_2$

(ii) the value of  $\alpha$

(3)



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Question 6 continued

Lined area for writing the answer to Question 6.



Question 6 continued

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Question 6 continued

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(Total for Question 6 is 7 marks)



7.

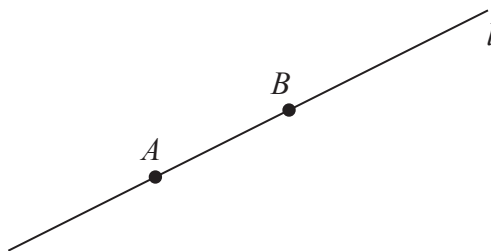


Figure 2

Figure 2 shows a sketch of the straight line  $l$ .

Line  $l$  passes through the points  $A$  and  $B$ .

Relative to a fixed origin  $O$

- the point  $A$  has position vector  $2\mathbf{i} - 3\mathbf{j} + 5\mathbf{k}$
- the point  $B$  has position vector  $5\mathbf{i} + 6\mathbf{j} + 8\mathbf{k}$

(a) Find  $\vec{AB}$

(1)

Given that a point  $P$  lies on  $l$  such that

$$|\vec{AP}| = 2|\vec{BP}|$$

(b) find the possible position vectors of  $P$ .

(4)





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Question 7 continued

Lined area for writing the answer to Question 7.

(Total for Question 7 is 5 marks)



8.

**In this question you must show all stages of your working.****Solutions relying entirely on calculator technology are not acceptable.**

(a) Prove that

$$\frac{1}{\operatorname{cosec} \theta - 1} + \frac{1}{\operatorname{cosec} \theta + 1} \equiv 2 \tan \theta \sec \theta \quad \theta \neq (90n)^\circ, n \in \mathbb{Z} \quad (3)$$

(b) Hence solve, for  $0 < x < 90^\circ$ , the equation

$$\frac{1}{\operatorname{cosec} 2x - 1} + \frac{1}{\operatorname{cosec} 2x + 1} = \cot 2x \sec 2x$$

Give each answer, in degrees, to one decimal place.

(4)



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Question 8 continued

Lined area for writing the answer to Question 8.



Question 8 continued

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Question 8 continued

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(Total for Question 8 is 7 marks)

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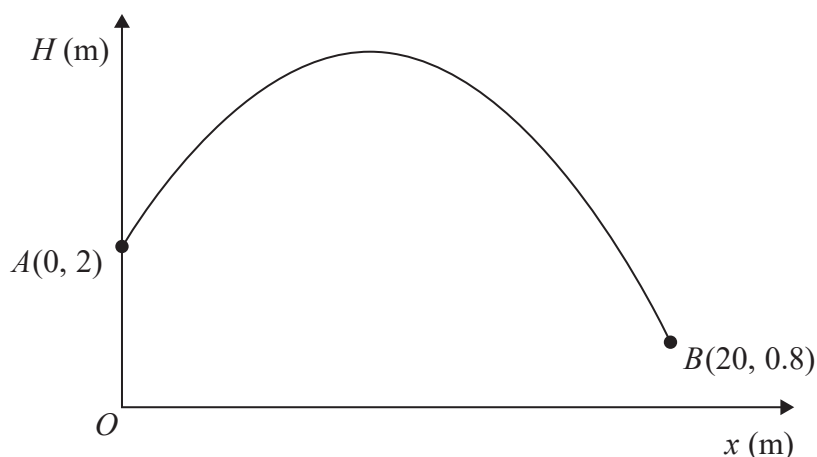


Figure 3

The graph in Figure 3 shows the path of a small ball.

The ball travels in a vertical plane above horizontal ground.

The ball is thrown from the point represented by  $A$  and caught at the point represented by  $B$ .

The height,  $H$  metres, of the ball above the ground has been plotted against the horizontal distance,  $x$  metres, measured from the point where the ball was thrown.

With respect to a fixed origin  $O$ , the point  $A$  has coordinates  $(0, 2)$  and the point  $B$  has coordinates  $(20, 0.8)$ , as shown in Figure 3.

The ball reaches its maximum height when  $x = 9$

A quadratic function, linking  $H$  with  $x$ , is used to model the path of the ball.

(a) Find  $H$  in terms of  $x$ . (4)

(b) Give one limitation of the model. (1)

Chandra is standing directly under the path of the ball at a point 16 m horizontally from  $O$ .

Chandra can catch the ball if the ball is less than 2.5 m above the ground.

(c) Use the model to determine if Chandra can catch the ball. (2)

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Question 9 continued

Lined area for writing the answer to Question 9.



Question 9 continued

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Question 9 continued

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(Total for Question 9 is 7 marks)





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Question 10 continued

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(Total for Question 10 is 6 marks)



11.

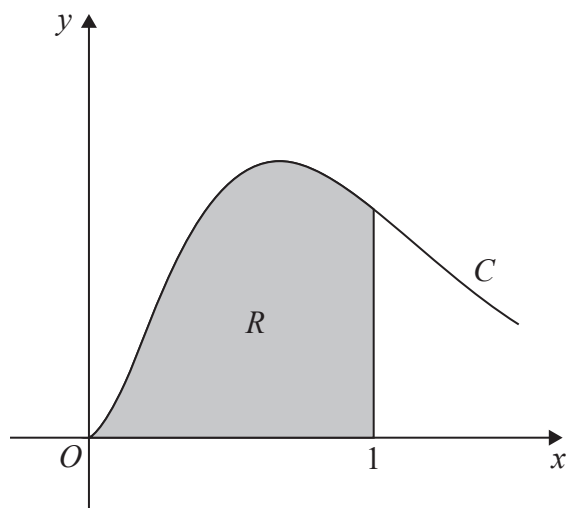


Figure 5

**In this question you must show all stages of your working.**

**Solutions relying entirely on calculator technology are not acceptable.**

Figure 5 shows a sketch of part of the curve  $C$  with equation

$$y = 8x^2e^{-3x} \quad x \geq 0$$

The finite region  $R$ , shown shaded in Figure 5, is bounded by

- the curve  $C$
- the line with equation  $x = 1$
- the  $x$ -axis

Find the exact area of  $R$ , giving your answer in the form

$$A + Be^{-3}$$

where  $A$  and  $B$  are rational numbers to be found.

(5)



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Question 11 continued

Lined area for writing the answer to Question 11.



Question 11 continued

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Question 11 continued

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(Total for Question 11 is 5 marks)



12. (a) Express  $\frac{1}{V(25 - V)}$  in partial fractions. (2)

The volume,  $V$  microlitres, of a plant cell  $t$  hours after the plant is watered is modelled by the differential equation

$$\frac{dV}{dt} = \frac{1}{10}V(25 - V)$$

The plant cell has an initial volume of 20 microlitres.

- (b) Find, according to the model, the time taken, in minutes, for the volume of the plant cell to reach 24 microlitres. (5)
- (c) Show that

$$V = \frac{A}{e^{-kt} + B}$$

where  $A$ ,  $B$  and  $k$  are constants to be found. (3)

The model predicts that there is an upper limit,  $L$  microlitres, on the volume of the plant cell.

- (d) Find the value of  $L$ , giving a reason for your answer. (2)





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Question 12 continued

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Question 12 continued

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Question 12 continued

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(Total for Question 12 is 12 marks)



13. The world human population,  $P$  billions, is modelled by the equation

$$P = ab^t$$

where  $a$  and  $b$  are constants and  $t$  is the number of years after 2004

Using the estimated population figures for the years from 2004 to 2007, a graph is plotted of  $\log_{10} P$  against  $t$ .

The points lie approximately on a straight line with

- gradient 0.0054
- intercept 0.81 on the  $\log_{10} P$  axis

(a) Estimate, to 3 decimal places, the value of  $a$  and the value of  $b$ .

(4)

In the context of the model,

- (b) (i) interpret the value of the constant  $a$ ,  
(ii) interpret the value of the constant  $b$ .

(2)

(c) Use the model to estimate the world human population in 2030

(2)

(d) Comment on the reliability of the answer to part (c).

(1)



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Question 13 continued

Lined area for writing the answer to Question 13.



Question 13 continued

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Question 13 continued

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(Total for Question 13 is 9 marks)



14. The circle  $C_1$  has equation

$$x^2 + y^2 - 6x + 14y + 33 = 0$$

(a) Find

- (i) the coordinates of the centre of  $C_1$
- (ii) the radius of  $C_1$

(3)

A different circle  $C_2$

- has centre with coordinates  $(-6, -8)$
- has radius  $k$ , where  $k$  is a constant

Given that  $C_1$  and  $C_2$  intersect at 2 distinct points,

(b) find the range of values of  $k$ , writing your answer in set notation.

(5)





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Question 14 continued

Lined area for writing the answer to Question 14.



Question 14 continued

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Question 14 continued

Lined area for writing the answer to Question 14.

(Total for Question 14 is 8 marks)



**15.** The curve  $C$  has equation

$$(x + y)^3 = 3x^2 - 3y - 2$$

- (a) Find an expression for  $\frac{dy}{dx}$  in terms of  $x$  and  $y$ .

The point  $P(1, 0)$  lies on  $C$ .

- (b) Show that the normal to  $C$  at  $P$  has equation

$$y = -2x + 2 \quad (2)$$

- (c) Prove that the normal to  $C$  at  $P$  does **not** meet  $C$  again.

You should use algebra for your proof and make your reasoning clear. (5)

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Question 15 continued

Lined area for writing the answer to Question 15.



Question 15 continued

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Question 15 continued

Lined area for writing the answer to Question 15.



**Question 15 continued**

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**(Total for Question 15 is 12 marks)**

**TOTAL FOR PAPER IS 100 MARKS**

