

## Codeforces Round #408 (DIV. 2).

Q) You will be given  $n$  cities,  $(n-1)$  edges, represented in the form of a tree. There are  $K$  police stations placed on some cities out of the  $n$  cities.

The condition for a city to be safe is that ~~so~~, that city should have atleast 1 police station at a distance  $K$ . Each edge has weight 1.

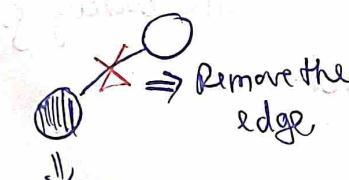


city A --- city B

The city is made in such a way such that all the cities are already safe.

You need to cut the maximum number of edges such that each city is still safe. Even after cutting the edges

A) **Intuition** - Since we know that all the cities are already safe, meaning each city has a police station at a distance  $K$  from it. We can start doing bfs from each of the police stations, and whenever we will see that we are trying to visit an already visited cell, we will remove that branch.



Already visited.

(Proof Wikipedia) Bezout's Identity

in between. This is a theorem that proves that Math function. Form two integers  $(a, b)$  we can find such that  $a \cdot x + b \cdot y = d$ .

If  $\gcd(a, b) = d$ , then there exists integers  $x$  and  $y$  such that  $a \cdot x + b \cdot y = d$ .

This can be extended to larger set of numbers ( $n > 2$ ).

For two integers  $(a, b, c, d, e, f)$  if  $\gcd(a, b, c, d, e, f) = g$ .

then there exist  $n_1, n_2, n_3, n_4, n_5, n_6$  such that  $a \cdot n_1 + b \cdot n_2 + c \cdot n_3 + d \cdot n_4 + e \cdot n_5 + f \cdot n_6 = g$ .

for some  $(n_1, n_2, n_3, n_4, n_5, n_6)$ .

Therefore if a question comes like, that word is gcd - related.

a) Given an array is it possible to use a subset of the array and multiply each of the elements with a separate multiplicand, such that sum of those elements is  $g$ .

b) Basically  $\gcd(a, b, c) = g$ . { For some subset  $(a, b, c)$  in the array }.

You need to find if any such subset exists or not.

Cuz if  $\gcd(a, b, c) = g$

$$a \cdot n_1 + b \cdot n_2 + c \cdot n_3 = g \quad [\text{Bezout's Identity}]$$

## Queue Reconstruction by Height.

- (a) You will be given an array of people  $\text{people} [h_i, k_i]$ ,  
 $h_i$  - denoting the height of the  $i^{\text{th}}$  person.  
 $k_i$  - Number of people left of the person who are taller or equal height.  
Now you need to arrange the sequence in such a manner that the sequence is correct.

Input  $\rightarrow [7, 0], [4, 4], [7, 1], [5, 0], [6, 1], [5, 2]$

Output  $\rightarrow [5, 0], [7, 0], [5, 2], [6, 1], [4, 4], [6, 1]$ .

(Sohn) ~~Explanation~~ Since we have the best data for the output who

(Step 1)  $\rightarrow$  We will sort the data first on the basis of height and then on the basis of 2nd item.

So sorted list becomes like.

$[4, 4], [5, 0], [5, 2], [6, 1], [7, 0], [7, 1]$

We have to fill 5 Blank spaces.

(Step 2)

$[4, 4] \rightarrow$  So 4 numbers are before  $[4, 4]$ ,

Now  $[4, 4] = \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}}$

$[5, 0] \rightarrow$  No number before it  $\rightarrow [5, 0] \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad [4, 4]$

$[5, 2] \rightarrow$  5 blank spaces after it  $\rightarrow \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad \underline{\text{blank}} \quad [4, 4]$

(Final) = (union of all sets) =  $[4, 4] \cup [5, 0] \cup [5, 2]$

## Submask Enumeration

What is a submask of a bitmask?

Let's say a bitmask is  $1011000$ . Then its submasks are  
 $1000000, 1010000, 1001000, 0011000, 0010000,$   
 $0001000$ .

$0101000 \rightarrow$  This is not a submask. The submask will have  
only those bits set which ~~had~~ bits ~~were~~ were originally set  
in the bitmask.

How to generate submasks of the bitmask.

Code:

```

submask = bitmask;
while (submask != 0) {
    submask = (submask - 1) & bitmask;
}

```

Suppose  $\text{bitmask} = 101100$ . Submask =  $101100$  as well.

$(\text{Submask} - 1) \Rightarrow$  Will make the rightmost set bit 0 and make all  
the bits to the right of it as 1.

$$(101100 - 1) = (101011) \& (101100) = (101000)$$

Now suppose you for each bit mask you want to generate their sub masks. Let's try to find out its time complexity.

Let's say one of the bitmasks has  $K$  bits set. Now each of those  $K$  bits have  $2^K$  choices. So  $2^K$  submasks.

Now how many ways out of the  $n$  bits you can choose  $K$  bits.

$\binom{n}{K} \cdot 2^K$ . Now do this for all the  $K$ 's from 0 to  $n$ .

$$\sum_{K=0}^n \binom{n}{K} \cdot 2^K = (2+1)^n = 3^n. O(3^n)$$

Now let's go to a question on the above topic.



### Find Minimum Time to Finish All

Jobs

(Leetcode)

- Q) You will be given an array, and you have to split them into  $K$  non-empty subsets, such that the subset which has the maximum sum is minimized.  $O(K \cdot 3^n)$ .

$$\text{jobs} = [1, 2, 4, 7, 8] \quad K=2$$

$$\text{a)- } (1, 2, 8) \quad (6) \quad (4, 7) \quad \text{Ans}=11.$$

- (A) We will be using Submask Enumeration in this question.

## (BITMASK Approach)

lets say we have a  $dp[i][ ]$  array.

$dp[i][\text{bitmask}] \Rightarrow$  This will tell me that

For the first  $i$  workers, if we distribute

the jobs which are having their bits set in the bitmask,

then

$dp[i][\text{bitmask}] = \text{minimizing the maximum of all the subsets.}$

So we will build our  $dp$  in such a way that

$dp[k][\text{pow}(2, \text{number of jobs})]$  will be holding the final answer.

$n = \text{no of jobs}$

(Step1) Store the answer for 1 worker first

~~for (int i = 0; i < n; i++)~~ for ( $\text{bitmask} = 0$ ;  $\text{bitmask} < (1 \ll n)$ ;  $\text{bitmask}++$ ) {

~~$dp[0][\text{bitmask}] = \text{sum}[\text{bitmask}]$~~



$S = N$

Sum of the jobs which have  
bitmask their bits set

(Step2) Now while adding the ~~bitmask~~ a new worker we will  
use a submask.

Q.T.9

lets assume we have a bitmask 10101.

In the enumeration part we will be generating its submask.

So basically we will try to find.

lets take a submask = 10001

$$dp[i][10101] = \min \left( dp[i][10101], \max \left( \begin{array}{l} dp[i-1][10001], \text{sum}[10101 - 10001] \\ \text{option 1} \quad \quad \quad \text{option 2} \end{array} \right) \right)$$

~~option 1~~  $\Rightarrow$  the submask divided among  $(i-1)$  workers

option 2  $\Rightarrow$  the rest of the jobs  $(i-1)$  (bitmask - submask) given to the  $i^{\text{th}}$  worker.

$$dp[i][\text{bitmask}] = \min \left( dp[i][\text{bitmask}], \max \left( \begin{array}{l} dp[i-1][\text{submask}], \text{sum}[\text{bitmask} - \text{submask}] \\ \text{option 1} \quad \quad \quad \text{option 2} \end{array} \right) \right);$$

Calculate this for all the bitmasks.

## Suffix Array

### Construction and Utility

What is Suffix Array?

Let us say we have a string  $\rightarrow$  banana.

Suffix array is an array which stores the suffixes in the sorted order.

0	1	2	3	4	5
a	n	a	n	a	n

 $\rightarrow$  Listing the suffixes. banana, anana, nana, ana, na, a.

If I sort them, it is stored as

a,	ana,	anana,	banana,	na	nana
5	3	1	0	4	2

$\rightarrow SA$

Suffix Array stores the indices where the suffixes would have started in sorted order.

Now there is a way using which we sort the suffixes.

We sort the whole suffix array in batches.

① First we sort the strings on the basis of 1st character.

② Then we sort it on the basis of first 2 characters.

③ Then first 4 characters.

④ Then first 8 characters.

⑤ And finally first  $2^n$  characters.

How do we do this?

Check out the next page.

Step 1) we create a p array.  $p[100][\text{long string}]$

$p[i][j]$ .  $\rightarrow$  will tell us what is the rank of the suffix  $j$  if all the suffixes are sorted by the first  $2^i$  characters.

so first thing

for ( $i = 0; i < n; i++$ ) {

$$p[0][i] = s[i] - 10^i;$$

3.

random						
A	S	P	O	R	E	N

(Step 2)

We will create a struct called suffix.

Struct suffix {

int first; // to store first few char. won't work  
int second; // to store next few char. won't work  
int index;

};

(Q) You might be wondering why do we need first and second variable.

(A) Because suppose we have  $p[i][j]$ .  $\rightarrow$  calculated for all the suffixes.. That means we have the suffixes sorted by the first  $2^i$  characters.

Now suppose I want to sort calculate  $p[i][j]$ .

So now the first =  $p[i][j]$ , second =  $p[i + \text{pow}(2, i)][j]$

Now if we take a pair  $(\text{first}, \text{second})$ . Then we have

the suffix  $j$ , first  $2^i$  characters.

$$i = 1; j$$

for( $i = 1; i < n; i++$ ) {

$$\text{int next} = \text{pow}(2, i-1);$$

if( $\text{next} > n$ ) break;  $i = \checkmark$

$\Rightarrow (\log N)$

Total is  $O(N(\log N)^2)$

$$t[j].\text{first} = p[i-1][j];$$

$$t[j].\text{second} = j + \text{next} < n \Rightarrow p[i-1][j+next] := -1;$$

$$t[j].\text{index} = j;$$

this sorting can be done in  $O(N) \Rightarrow O(N \log N)$

sort( $t, t+n, \text{comparator}$ );  $\Rightarrow$  Just to sort the suffixes.

Now we want to populate the  $p[ ][ ]$  array with many

for( $j = 0; j < n; j++$ ) {  $\Rightarrow$  this part is basically the condition giving the same ranks to some suffixes. }

$$p[i][t[j].\text{index}] = (j > 0 \text{ and } t[j].\text{first} == t[j-1].\text{first} \text{ and } t[j].\text{second} == t[j-1].\text{second}) ?$$

$$p[i][t[j-1].\text{index}] := j;$$

};

~~Time Complexity~~  $O(\log N)$  complexity.

~~Calculating the LCP~~  $\rightarrow O(\log N)$  complexity.

~~LCP~~: LCP  $\rightarrow$  Longest Common Prefix. Given two suffixes, LCP ~~array~~ will find what is the longest common prefix between these two suffixes.

Step tells us till which point did we sort(i, j).

Code:

int lcp(int i, int j, int n, int step) {  
 if (i == j) return n - i; // All characters are same.  
 if (step >= n) return 0;  
 int return\_value = 0;

for (int k = step; k >= 0; k--) {

if ( $i >= n$  or  $j >= n$ ) {

break;  $i = \text{sorted}[i]$

}  $\rightarrow$  Check which rank matches

if ( $p[k][i] == p[k][j]$ ) {

$\rightarrow$  that means,  $2^k$  characters are matching

return\_value += pow(2, k);

$i += \text{pow}(2, k); \rightarrow$  shifting suffix by

$j += \text{pow}(2, k); \rightarrow$   $2^k$  characters and

do the same for  $j$ .  $\rightarrow$  again compare

if ( $p[k][i] == p[k][j]$ ) {

return return\_value;

}

## ~~LEET CODE~~

Weekly Contest

(MEDIUM)

(Shortest String that contains all the three strings.)

(NEW APPROACH Completely)

(a)

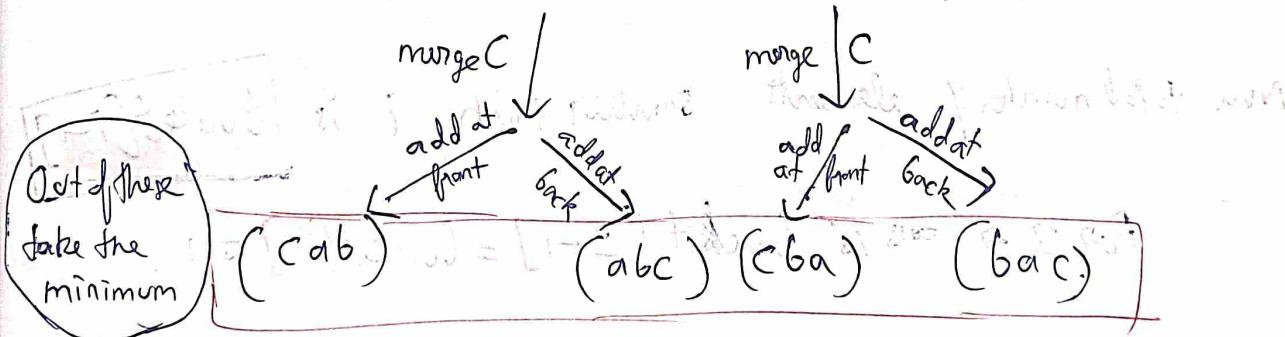
You will be given 3 strings  $a, b, c$ . Your task is to find the minimum length string such that this string contains all the 3 strings,  $(a, b, c)$  as substrings.

(A)

We will have to brute force and manually combine the strings in all possible formats and get the minimum string out of those.

$F(a, b, c) \rightarrow$  In this first we will combine  $(a$  and  $b)$ , and then try to merge  $c$  with it.

merge  $(a, b) \rightarrow (ab)$  or  $ba$ .



Similarly do for.  $F(b, c, a) \rightarrow$  merge  $(b$  and  $c)$  and then try to merge  $a$  with it.

Finally take the minimum of

$F(a, b, c), F(b, c, a), F(a, c, b)$

~~(LEETCODE)~~ ~~O(N^2)~~ ~~< Bucket Sort Algo >~~  
 OR ~~How many~~ Numbers are smaller than the current Number.  
 Given an arr, with  $0 \leq \text{arr}[i] \leq 100$ . For each number  
 tell the count of numbers which are smaller than it in the  
 whole array.

arr →	[	0		1		2		2		3	]
-------	---	---	--	---	--	---	--	---	--	---	---

We will use Bucket sort which is an  $O(N)$

bucket [arr[i]]++
-------------------

bucket →	[			1		2		1				1		1	]
----------	---	--	--	---	--	---	--	---	--	--	--	---	--	---	---

Now do a prefix sum on bucket

0		1		2		3		4		5		6		7		8
---	--	---	--	---	--	---	--	---	--	---	--	---	--	---	--	---

Now total number of elements smaller than  $i$  is  $\boxed{\text{Bucket}[i-1]}$

For  $i=2$  ans is  $\boxed{\text{Bucket}[2-1]} = \boxed{\text{Bucket}[1]}$

## (LEETCODE) Check If It is Possible to Split Array.

You are given an array of length  $n$ , and an integer  $m$ . You need to be able to tell if it is possible to split the array into  $n$ , non-empty arrays.

In each step for splitting the array, the following conditions must hold.

- \* Length of the subarray is 1 or 2.
- \* The sum of elements of the subarray is  $\geq m$ .

(Sln) Method 1.  $O(N^2 \cdot n)$  or  $O(n)$  more steps needed.

Solve this using dynamic programming.

$dp[i][j] \rightarrow$  Will basically tell you if you can split the subarray  $arr[i, i+1, \dots, j]$  inside  $dp(i, j)$ .

Inside  $dp(i, j) \rightarrow$  you can perform all possible splits, and break it into subproblems.  $dp(i, j) \rightarrow dp(i, k) \& dp(k, j)$ .

(Method 2) (#\*) [Amazing Observation].  $O(N)$

If any two consecutive elements have sum  $\geq m$ , then we can split the entire array into single element.

LEETCODE  
CONTEST

Find the Safest Path in the Grid

SEE CODE IMP.

DISCUSS

TOP

You are given a  $N \times N$  matrix. A cell which is empty grid[i][j] = 0 and a cell which is a thief has grid[i][j] = 1.

For a given cell, the safeness factor of the cell is the minimum manhattan distance from any of the thief cells.

After we know the safeness factor of each cell, we need to find the path such that in that path the minimum safeness is maximum. Out of all the paths, you need to choose a path from  $(0,0)$  to  $(n-1, n-1)$  where the minimum safeness is maximum.

Soln

Step 1) You can find the safeness of each cell using Multi-Source BFS. Now for each cell you have safeness factors.

(Method 1) Binary Search

(BFS, DFS)

Step 2

Binary Search + BFS

Time Complexity

( $\log N$ )  $\approx N^2$

(Method 2)

$(\log N^2)(N^2)$

Priority Queue based

Dijkstra

In this we will do a binary search.

choose a mid = (start + end) / 2.

we will insert into the cell

we will check if there's a path

{ safeness of the cell }

that exists such that any cell

{ index of the cell }

we travel has ( $\text{Safeness} \geq \text{mid}$ ).

And manipulate our mid.

(LEETCODE  
CONTEST)

(Length of Longest Valid Substring)

(HARD)

(SLIDING WINDOW)

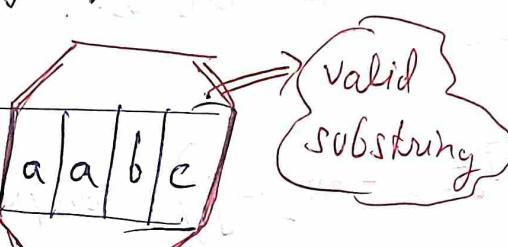
(~~DP~~)

(CODE IN LEFT CODE)

You are given a string word and also given a set of strings  $\rightarrow$  (Forbidden Strings). A string is called Valid if none of its substrings are a part of forbidden set.

We need to print the length of the longest valid substring of which is a part of word.

Example

word = 

forbidden = ["aaa", "cb"]

(Sln) We will be using a sliding window approach on solving the problem.

Observation ①  $\rightarrow$  You see that the maximum length of a forbidden string is 10.  $\rightarrow$  (V.Imp Observation.)

Observation ②  $\rightarrow$

Active Window + (new character).

All the new substrings generated will decide whether this new character can be included in the Active Window.

Now we only care about the substrings generated of length 10.

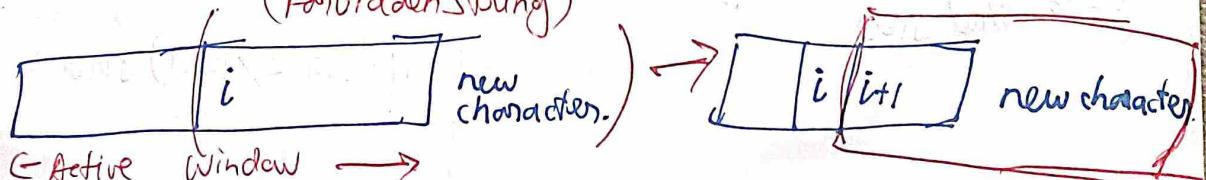
new character,   $\dots$  

(Then Repeat) Till Window goes out (String)  $\leftarrow$  length 10  $\rightarrow$   
(last step)  $\rightarrow$  If the new set of 10 substrings are present in the forbidden Set. Then the window has to be changed.

Suppose.

(Forbidden String)

New Active Window



Premium  
Amazon

Find the Index of Larger Integer // ~~OR OR~~

You are given an integer Array, where all the values are same except that 1 Integer. A single index has a value larger than all the other indexes. You are given a function ~~(\*) \* \*~~

f(l, r, n, y) → which tells us.

{

sum(arr[l] + ... + arr[r]) comparison with

sum(arr[n] + ... + arr[y])

So  $f(l, r, n, y)$  returns 1 → if subarray sum is greater

refers to  $\rightarrow$  if subarray sum is smaller, 0 → if subarray sum is equal.

(Sln)

Binary Search

$O(\log_2 N)$

V. Imp (Cool Trick)

Ternary search

$O(\log_3 N)$

we could use two parts of the array to divide the given array into 3 parts

array

Left

Right

Part1

Part2

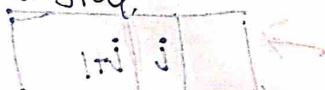
Part3

if  $f(\text{left}, \text{right}) > f(\text{Part1}, \text{Part2})$  then search in Part1

if  $f(\text{left}, \text{right}) < f(\text{Part1}, \text{Part2})$  then search in Part2

else go to that side.

for part1



returning

if  $f(\text{Part2}, \text{Part1}) > f(\text{Part1}, \text{Part2})$  search in Part2.

# (X) V.Imp) (X) Meeting Scheduler (Interval Problem)

(Leetcode Premium)

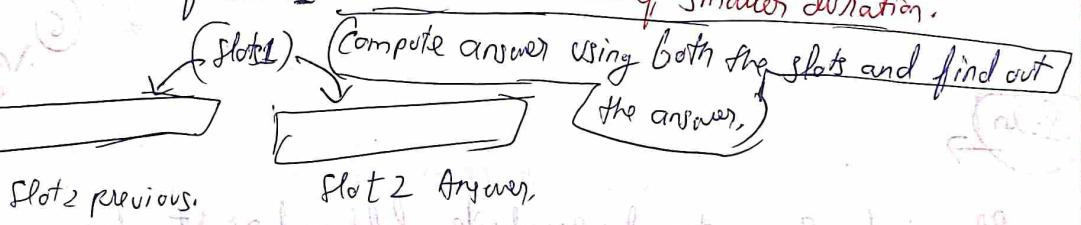
(TIK TOK)

You are given 2 arrays.  $\text{Slots}_1$  and  $\text{Slots}_2$ , and an Integer Duration. You need to find the earliest slot available in which both are available.  $\text{Slots}_1 \rightarrow [ [10, 50], [60, 120], [140, 210] ]$ ,  $\text{Slots}_2 \rightarrow [ [0, 15], [60, 70] ]$  duration  $\rightarrow 8$ .

Ans  $\rightarrow [60, 68]$

(Binary Search)

Solution 1) Sort ( $\text{Slots}_1, \text{Slots}_2$ ). After sorting them loop through each slot of ( $\text{Slots}_1$ ) and using binary search find the slot in  $\text{Slots}_2$  whose start is just greater than or equal to the start of the current slot of  $\text{Slots}_1$ .   
 Corner Case  $\rightarrow$  Filter out slots which are of smaller duration.



(Solution 2)  $\rightarrow$  Priority Queue

~~slot1~~  $\rightarrow$  [ ] [ ] [ ] [ ]

~~slot2~~  $\rightarrow$  [ ] [ ] [ ] [ ]

Since slots of same person won't collide  
So we use ~~use~~ a priority queue.

slot $i$   $\rightarrow$  check for intersection between slot  $i$  and slot  $j$  and pop slot  $i$

(Two Pointer)

slot $1$   $\rightarrow$  [ ] [ ] [ ] [ ]

slot $2$   $\rightarrow$  [ ] [ ] [ ] [ ]

We keep  $i$  and  $j$  and check their compatibility. Out of  $i$  and  $j$  whichever slot has earlier ending time we move it forward. In this case  $i$

Follow up

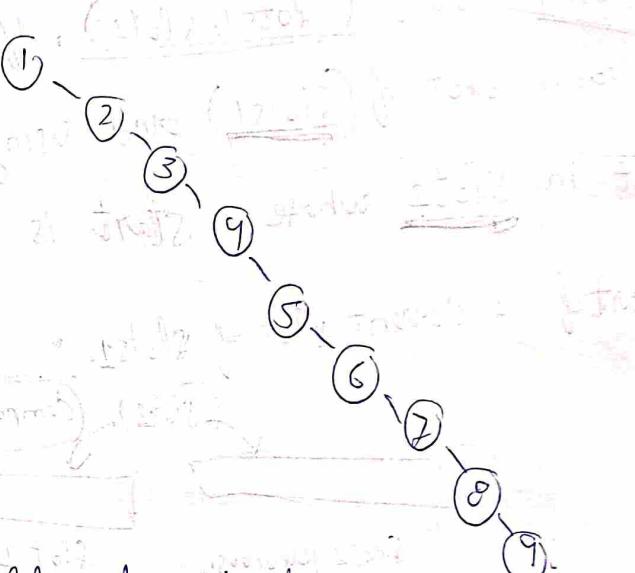
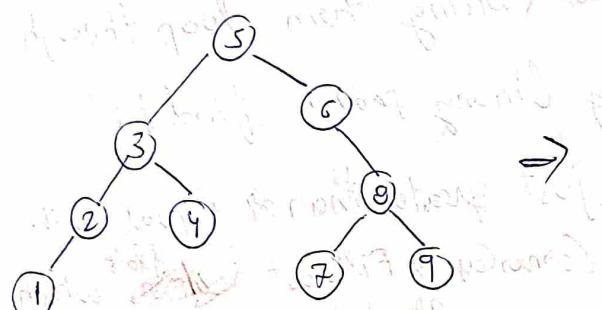
If there are multiple people with multiple slots. Then calculate the same. If not all are available at the same time. Find the slot in which maximum people are available.

[Line Sweep we can use that]  $\rightarrow$  then check for any duration, which duration has maximum people using subarray preffix sum.

(GOOGLE)

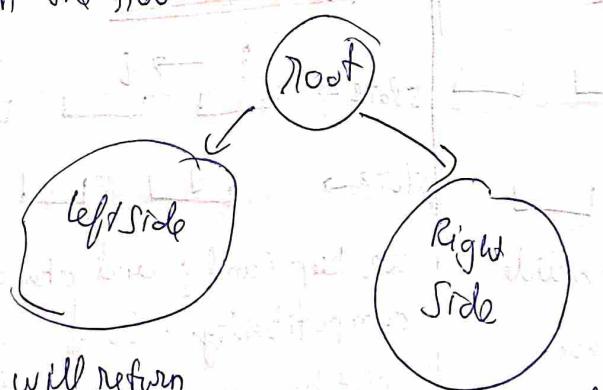
## Increasing Order Search Tree

You are given a binary search tree, rearrange the tree in in-order, so that the leftmost node in the tree becomes the root of the tree and every node has no left child and only right child.



Soln

- Plan is to segment and evaluate left and right trees separately and merge with the Root.



$f(\text{LeftSide})$  will return

Head and tail of the

chain of LeftSubtree. we want to

[full of LeftSubtree chain].

LeftSide • Second  $\rightarrow$  right = Root

root  $\rightarrow$  left = Null

Root  $\rightarrow$  right = RightSide first [Head of RightSubtree chain]

function (Root) {

    LeftSide =  $f(\text{LeftSide})$ .

$f(\text{RightSide})$  will

return the Head and

tail of the chain of

RightSubtree,

Code  $\Rightarrow$  Arg =  $f(\text{root}).\text{first}$ .

pair<TreeNode\*, TreeNode\*> f(TreeNode\* root){

if (root == NULL){

return {NULL, NULL};

}

pair<TreeNode\*, TreeNode\*> leftSide = f(root->left);

if (leftSide.second != NULL){

leftSide.second->right = root; }  $\rightarrow$  leftSide

root->left = NULL;

pair<TreeNode\*, TreeNode\*> rightSide = f(root->right);

root->right = rightSide.first;

TreeNode\* head = root;

TreeNode\* tail = root;

if (leftSide.first == NULL)  $\Rightarrow$  start from the bottom-left;

head = leftSide.first; }  $\Rightarrow$  start from the

if (rightSide.second != NULL){

tail = rightSide.second; }

return {head, tail}; }

(GOOGLE)

# [Robot Room Cleaner]

Q You have been given a robot and you have to use that robot to clean the room. The room has some of its cells blocked, and some cells are empty. Your job is to ~~is to~~. You have been given the Robot → following APIs now you have to write an algo such that the blindfold robot clears the entire room.

turnRight(); → turns the Robot to right by  $90^\circ$ .  
turnLeft(); → turns the Robot to left by  $90^\circ$ .  
move(); → Move in the direction by 1 cell it's facing.  
clean(); → Cleans the current cell in which the robot is present. Returns false if there is a block, true if there isn't.

- Soln
- 1) Idea is to solve it using dfs and backtracking. So basically we will traverse through the grid and check for all possible directions the Robot can travel and we will consequently clean the cell in which we are in.
  - 2) The starting cell we will mark it as  $(0,0)$  and the remaining cells we will mark it relative to this cell.
  - 3) Upon reaching a cell where all the options are blocked or we have already explored all the options we will backtrack to where we originally came from / [basically to a call's method] with

the same orientation. For that we will do the following operation.

turnRight()  $\times$  2 times  $\rightarrow 180^\circ$  to go in reverse.

move()  $\rightarrow \approx 1$  time

turnRight()  $\times$  2 times  $\rightarrow 180^\circ$  to go in original orientation.

directions  $\Rightarrow \{ \{1, 0\}, \{0, -1\}, \{-1, 0\}, \{0, 1\} \}$

setPairs( $\langle$ int, int $\rangle$ , visited);

dfs(int x, int y, int currentOrientation);  
visited[ $\langle$ x, y $\rangle$ ] = 1;  
clean();

### Explanation:

```
for (int i = 1; i <= q; i++) {  
    int new_orientation = (current_orientation + i) % 4;  
    int new_x = x + directions[new_orientation].first;  
    int new_y = y + directions[new_orientation].second;  
    if (!visited[new_x][new_y] and move()) {  
        dfs(new_x, new_y, new_orientation);  
    }  
}
```

Left Say  
current orientation = 3.  
i.e. Upper  $\rightarrow$   $\uparrow$

Robot is facing Up.  
If we do  
 $(3+1=4) \% 4$   
 $= 0$ .

So it becomes Right.

So each time we are  
adding i we are  
basically  
turningRight()

turnRight();  
turnRight();  
move();  
turnRight();  
turnRight();  
Explained in point 3)

## (GOOGLE) Count Fertile Pyramids in a Land.

You will be given a  $n \times m$  grid, where some cells will be 0 and some cells will be 1. You need to count number of pyramids and inverse pyramids that can be formed.

what is a pyramid. lets take a cell  $(i, j)$ . It's considered a pyramid if the height of the pyramid is greater than 1.

$(i, j)$

$\rightarrow$  this is a valid pyramid.

Similarly, inverse you can visualize

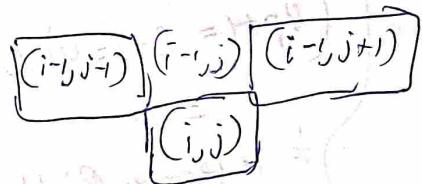
$\rightarrow$  this is a valid pyramid.

$\rightarrow$  this is a valid pyramid.

Soln

\* This is a very simple problem. We will evaluate considering inverse pyramid formation.

Let's say a cell  $(i, j)$  will form a pyramid or not and if it will how many will it form.



\* Condition 1  $\rightarrow$  if  $(\text{grid}[i][j] == 1)$

and  $(\text{grid}[i-1][j-1] == 1)$

then one if height 2 can be reached,

\* Condition 2  $\rightarrow$  Now we have already evaluated results for  $(\text{grid}[i-1][j-1])$  and  $(\text{grid}[i-1][j+1])$  so we know what height pyramids those are forming.

(Step 3)  $\rightarrow$  out of  $\text{grid}[i-1][j-1]$  and  $\text{grid}[i-1][j+1]$  minimum of them will be new height of pyramid.

$$\text{grid}[i][j] = \min(\text{grid}[i-1][j-1], \text{grid}[i-1][j+1]) + 1.$$

Step 4

$\text{ans} += (\text{grid}[i][j] - 1)$  } because number of pyramids with newly introduced will be height-1, since height=1 is invalid.

[Code in LeetCode]

(GOOGLE)

[Code in LeetCode]

[Range Module]

(HARD).

(\*) You are fucked if this question comes in interview.]

- ① A half open interval concept is used here.  $[\text{left}, \text{right}) \rightarrow$  means all real numbers within the interval of  $\text{left} \leq \text{left}$  and less than right.

Now you are given 3 operations.

- 1) addRange ( $\text{int left, int right}) \rightarrow$  Basically you need to add a range  $[\text{left}, \text{right})$  in the set of valid intervals.
- 2) queryRange ( $\text{int left, int right}) \rightarrow$  you have to tell all the real numbers within the interval  $[\text{left}, \text{right})$  are valid or not.
- 3) removeRange ( $\text{int left, int right}) \rightarrow$  You have to mark the range of real numbers between  $[\text{left}, \text{right})$  as invalid.

Sohin

Yes I had the correct intuition behind it.

- \* Well for adding a range, we want to check if the new range is overlapping with any of the existing ranges, and if it does we want to merge it into a whole new range and remove the old range. Basic idea is to have disjoint intervals.

To begin with we will have 4 data structures.

startMap  $\rightarrow$  Mapping of  $s \mapsto e$

endMap  $\rightarrow$  Mapping of  $e \mapsto s$

startSet  $\rightarrow$  all the entries of start

endSet  $\rightarrow$  all the entries of end.

addRange( $s$ ,  $e$ )

\* Step 1) Find the end of an interval which is just greater than or equal to  $s$ .

auto it = endSet.lower\_bound( $s$ );

Evaluation of cases with diff. behavior

(Step 2)

iterate over the endSet map to traverse through intervals.

while ( $it \neq endSet.end()$ ) {

int  $e = *it$ ;

int  $s = endMap[e]$ ;

if ( $e > s$ ) {

if (overlapping) {

removeMapping( $(s, e)$ );

else {

break;  $\Rightarrow$  Since

if ( $e > s$ ) {

$s = e$   $\Rightarrow$  new start

and if no overlap  $\Rightarrow$  new start

rest of the intervals are also greater and

non-overlapping

new start

old interval

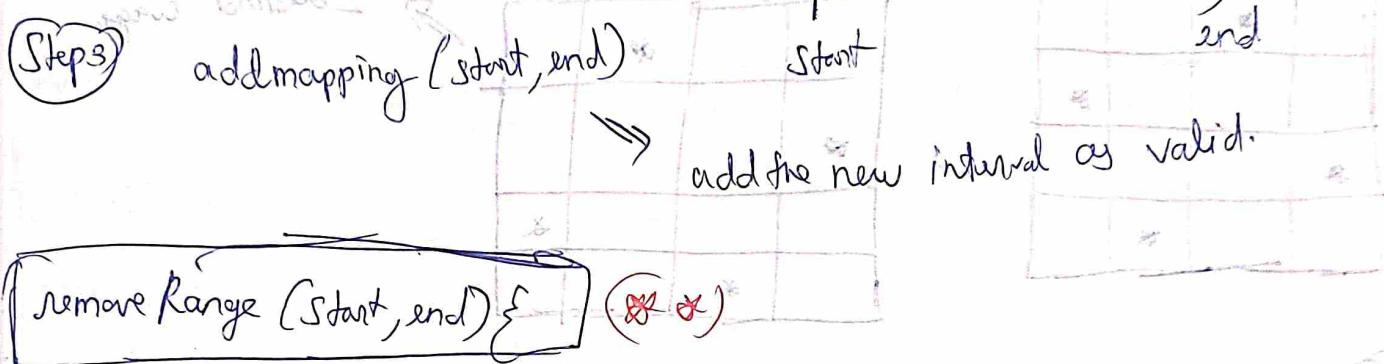
new interval to be added.

start  $\leftarrow e$

end  $\Rightarrow$  start  $\leftarrow e$

start  $\leftarrow e$

$\text{if } (\text{e} > \text{end}) \{$  For the case when  
 end = 0;  
 $\}$  not in range with current interval.  
 $\} \Rightarrow$  close while loop.  
 then extend the new interval.



(Step 2) Find the end of an interval which is strictly greater than start  
 Notice why I used strictly greater, because  $\text{end} = \text{start}$  is already invalid, because it's a half-open interval  $[\text{start}, \text{end})$ .

auto it = endSet.upper\_bound (start);

while (it != endSet.end()) { traversing through the intervals.

int e = \*it;

int s = endMap[e];

it++;

if (overlapping) {

else { completely valid  
removeMapping (start, e) mark it as invalid.

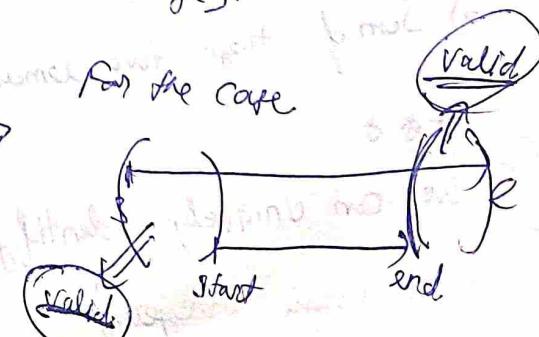
} some reason as mentioned in addRange}.

if (start > s) { mark for the case  
addRange (s, start);

if (e > end) { mark for the case

addRange (end, e);

} close while loop

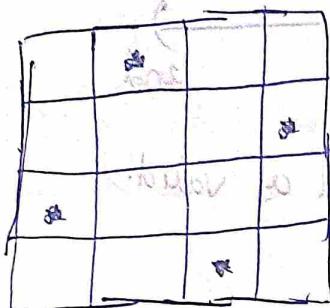


(GOOGLE).

[Important New Concept]  $(N \text{ Queens - II})$   $\rightarrow$  [Code in LeetCode]

- Q) You are being given a chess board, You have to find number of distinct ways in which you can place  $N$  queens in such a way that the queens don't attack each other.

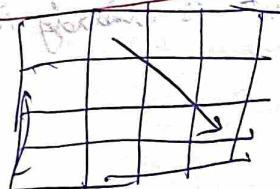
Example.



$\Rightarrow$  2 distinct ways.

Soln) Here I will introduce two important concept of a grid.

1) negative diagonal  $\rightarrow$  if we are travelling in the direction from top-left to bottom-right.



1) Then we can see at the next cell,

row<sub>next</sub> = row<sub>1</sub> and col<sub>next</sub> = col<sub>1</sub>.  
2) Difference between row and col remains same.

$$\text{diff} = (\text{row} - \text{col})$$

2) positive diagonal  $\rightarrow$  if we are travel in the direction from top-right to bottom-right.

1) Then we can see at the next cell, row<sub>next</sub> = row<sub>1</sub> and col<sub>next</sub> = col<sub>1</sub>.

2) Sum of these two remains same  $\Rightarrow$  sum = (row + col).

So we can uniquely identify a neg-diagonal and positive diagonal using a single integer.

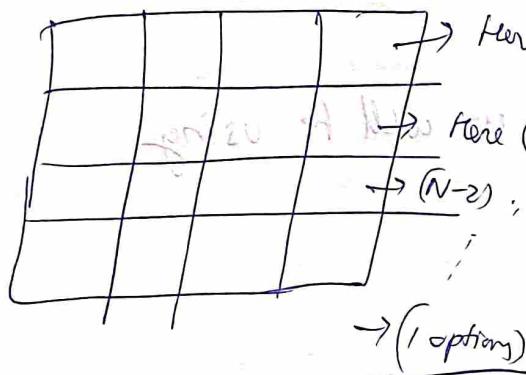
## Logic

We will use back track, and at each row we will be placing queens at each column and check for 3 things

- 1) if this column falls into the visited column list -
  - 2) if this cell falls into negative diagonal visited list -
  - 3) if this cell falls into positive diagonal visited list -

## Complexity Analysis

V-V temp



Here we can try  $N$  different options

After  $(N-1)$  steps, there will be  $N$  cells.

→ For each option we are going over  
No claim.

$$(N \cdot (N-1) \cdot (N-2) \cdots \cdot 1) [N_{\text{options}}] \rightarrow (N! \cdot N)$$

 Google

## Minimum Replacements to Sort the Array

→ You already know the question. The ~~word~~ of the question is, given a number  $X, Y$  such that  $(X > Y)$ . Split  $X$  into various parts such that [sum of the parts =  $Y$ ] and  $\min(\text{parts})$  is maximized.

~~John~~ Let's say  $\{X = 26, Y = 12\}$  - (Case I) ( $X \% Y = 0$ ) then  $\min(\lceil \frac{X}{Y} \rceil, 1) = Y$   
~~(Ex-1)~~ (V. Imp Point) (Case II) If it's not divisible, (Step 1) → Get how many parts it needs to be broken into such that each part is  $\leq Y$ .  $\lceil \frac{X}{Y} \rceil$  [parts  $\leq Y$ ]. After operating

break =  $(x/y) + 1$  . [The +1 is for  $x \% y$  part]

Step 2) Now check what is the maximum number you can fill in those boxes.

~~Result~~  $(\text{Answer}) \times (\text{breaks}) \leq x \Rightarrow (\text{Answer}) \leq \left(\frac{x}{\text{breaks}}\right)$

Imp

Maximum Score of Good Subarray

O(N)

Two Pointers

Greedy

- a) You are given an array of integers and a number K.  
You need to find the maximum possible score of a valid subarray.

See for a subarray  $[num[i], num[i+1], \dots, num[j]]$ .

Score =  $\min(num[i], num[i+1], \dots, num[j]) \times [Length of the subarray]$   
valid subarray  $(i, j)$  such that  $(i \leq K \leq j) \rightarrow$  i.e. index K has to be included always.

(A) The soln is really simple we will be using two pointers to solve this.

Point 1]

Out of the two indices  $i$  &  $j$  whichever we are going to choose length of the new subarray is

going to be same in both the cases.

So out of  $num[K-1]$  and  $num[K+1]$  it's better to choose the larger one.

Point 2] Whether to expand on the left or the right totally depends on which side has greater value, so that it maximizes the minimum of the new subarray.

Code 1h-LeftCode

## (Burst Balloons)

(Dynamic Programming)

Amazing Problem

- Q) You are given  $n$  balloons, indexed from 0 to  $(n-1)$ . Each balloon has number written on it. If you burst  $i^{th}$  balloon, you will get ~~some~~ few coins.   
~~coins = nums[i-1] + nums[i] + nums[i+1]~~ Basically the left & right adjacent coins. But if there are no coins present to the left or right of it, we take coin values to be 1.   
 Find the maximum points you can achieve after bursting all balloons.

(A) Step 1

Let's break the problem into sub problems.

If we choose a sub array  $[i, j]$  and we want to burst the  $k^{th}$  balloon.

So our problem breaks into

Solve  $(i, j)$  =

Solve  $(i, k-1)$

+ solve  $(k+1, j)$ ;   
 [Problem of Bursting  $k^{th}$  balloon first]   
 leftBalloon  $\rightarrow$  num  $[k]$  \* RightBalloon

leftBalloon and RightBalloon  $\rightarrow$  should exist Right,

But we cannot burst the  $k^{th}$  balloon first

solve the subproblem  $(i, k-1)$  because and then

[balloon  $[k-1]$  and balloon  $[k+1]$   $\rightarrow$  are adjacent now]

## (How to solve this Problem)

(\*) Let's say we will ~~prefer~~ burst the  $k^{\text{th}}$  balloon at the last of the subarray  $[i, \dots, j]$ .

(\*\*) So now  $(k-1)^{\text{th}}$  and  $(k+1)^{\text{th}}$  are not adjacent now.

(\*\*\*) So now we solve the subproblem

1) solve  $(i, k-1)$

2) solve  $(k+1, j)$

3) (burst the  $k^{\text{th}}$  balloon of the subarray at the last)

so left balloon =  $\text{num}[i-1]$

so right balloon =  $\text{num}[j+1]$

so solve  $(i, j) = \text{solve}(i, k-1) + \text{solve}(k+1, j)$

so  $\text{num}[i-1] \& \text{num}[k] \& \text{num}[j+1]$

(Google) [CODE IN 24 Game] [Backtracking]

[EERCODE] [INFO2]

Q) You are given 4 cards with values in it. You should arrange the numbers on these cards in a mathematical expression using the operators  $[+, -, *, /]$  to get the value  $target$

Division operator is not integer division, if real division, go to 8

$$3/2 != 1 ; 3/2 = 1.5 \quad (\text{N} \rightarrow \text{I}) \quad \text{middle/lv2 left/lv2}$$

middle/lv2  $\leftarrow [l \rightarrow \text{middle}, r \rightarrow \text{middle}]$

Soln we will be using complete backtracking and complete brute force. Since we are allowed to arrange the numbers here we need not apply operations just on adjacent numbers.

[Implementation is very nice. I was not able to implement. Pls Revise]

Concept of epsilon introduced for double numbers  $\rightarrow \text{epsilon} = \text{pow}(10, -5)$ .

```

void backTrack(vector<double> num) {
    if (num.size() == 1) {
        if (abs(num[0] - target) < epsilon) {
            ans = true;
            return;
        }
    }
    for (int i=0; i<n; i++) {
        for (int j=i+1; j<n; j++) {
            if (i==j) continue;
            double a = num[i];
            double b = num[j];
            Vector<double> newNum;
            for (int k=0; k<n; k++) {
                if (k==i || k==j) {
                    go.push_back(num[k]);
                } else {
                    go.push_back(a(operation)b);
                }
            }
            backTrack(go);
            go.pop_back();
        }
    }
}

```

to compare double variables.

As we keep on modifying the array, for each operation from  $i$  to  $j$ , on the two operands we shrink them to 1 operand.

here we choose which ( $i$  and  $j$ ) to perform operation on. ~~Recurse~~

we populate all the elements except  $i$  and  $j$ .

we push the new operand at last.

# (Count Pairs with XOR in Range)

Greedy

O(N)

BITCODE

Given an array and two integers low and high, return the number of nice pairs. A nice pair  $(i, j)$  of an array is such that  $\text{low} \leq \text{nums}[i] \wedge \text{nums}[j] \leq \text{high}$ .

DP

BITCODE

A) This problem is similar to the problem of find maximum XOR of 2 elements in the array.

Break the problem into 2 parts-

① (a) populate the numbers  $\text{nums}[0] \dots \text{nums}[i-1]$  into the tree, using bits from left to right. Suppose  $10 \rightarrow 1010 \rightarrow$

(b) And at each node we have a  $\text{cnt}$  pointer to keep track that how many numbers have this bitwise prefix.

② For each  $\text{nums}[i]$ , we can traverse the tree and try to check number of elements inserted into the tree whose XOR with  $\text{nums}[i]$  is less than a given number  $K$ .

RmP part

# for (each bit of K) {

i<sup>th</sup> bit of N =  $(N \gg i) \& 1$ ;

if (i<sup>th</sup> bit of K == 1) then

can consider all the numbers whose i<sup>th</sup> bit is same as that of i<sup>th</sup> bit of N. Because that will make XOR = 0 which is less than K.

if (i<sup>th</sup> bit of K == 0) then

$\Rightarrow \text{node} = \text{node} \rightarrow \text{child}[i^{\text{th}} \text{bit of N}]$

$\text{node} = \text{node} \rightarrow \text{child}[i^{\text{th}} \text{bit of N}]$ . we will exceed the value of K.

(GOOGLE) [Maximum Strictly Increasing Cells in a Matrix] (Amazing trick)

(LEETCODE)

d) given a n\*m integer matrix. You can select any cell in the matrix as your starting cell.

From the starting cell you can move to any other cell in the same row or same col, but only if value of the new cell is strictly greater than value in the current cell. Return how many maximum cells you can visit in this way.

Example:

3	1	6
-9	5	7

(Ans 9)

Soln

[Step 1] → Create a map

Map < int, vector<pair<int, int>>

This is going to be used for storing value → positions list [Since there can be duplicate values]

[Step 2] → We are going to start travelling the values in increasing order.

We are going to keep 2 arrays :-

- 1) Row-Max[i] → to store what is the maximum value I can get from ~~i<sup>th</sup> cell~~ now.
- 2) Col-Max[j] → to store what is the maximum value I can get from j<sup>th</sup> col.

Code

```
for (auto it = mp.begin(); it != mp.end(); it++) {
```

```
    for (auto p : it->second) {
```

```
        int i = p.first
```

```
        int j = p.second
```

dpl[i][j] = max(row[i], col[j])

+ 1 } duplicates

in a diff loop

in next page

```
    for (auto p : it->second) { int i = p.first; int j = p.second; }
```

row-max[i] = max(row-max[i], dpl[i][j]);

col-max[j] = max(col-max[j], dpl[i][j]);

lets take the example

0	1	0	1
0	3	1	dp[0][0]
1	3	9	dp[1][0]

(Reason)

Step 1

we start with

$1 \rightarrow (0, 1)$ .

rowMax  $\rightarrow$

0	1
0	0

colMax  $\rightarrow$

0	1
0	0

rowMax  $\rightarrow$

0	1
1	0

colMax  $\rightarrow$

0	1
0	1

Step 2

Next up we update 3. [Duplicates]

Now lets say we update rowMax and colMax after the first 3 is processed itself.

What happens then?

$$dp[0][0] = \max(\text{rowMax}[0], \text{colMax}[0]) + 1 = 2$$

$$\text{rowMax}[0] = \max(\text{rowMax}[0], dp[0][0]) = 2$$

$$\text{colMax}[0] = \max(\text{colMax}[0], dp[0][0]) = 2 \rightarrow \text{Keep this part in mind}$$

Now when we are processing the next 3:

$$dp[0][0] = \max(\text{rowMax}[1], \text{colMax}[0]) + 1 = 3 \rightarrow \text{which is wrong}$$

Because we updated the rowMax and colMax using the first 3. The 2nd (3) is now thinking there is a number smaller than itself on the row or col who can visit the  $\max(\text{rowMax}, \text{colMax})$  cells.

Hence.

First we should find answers of all the Ques (3) and then update row-Max or col-Max.

Hence the 2nd loop.

(~~LFU Cache~~)

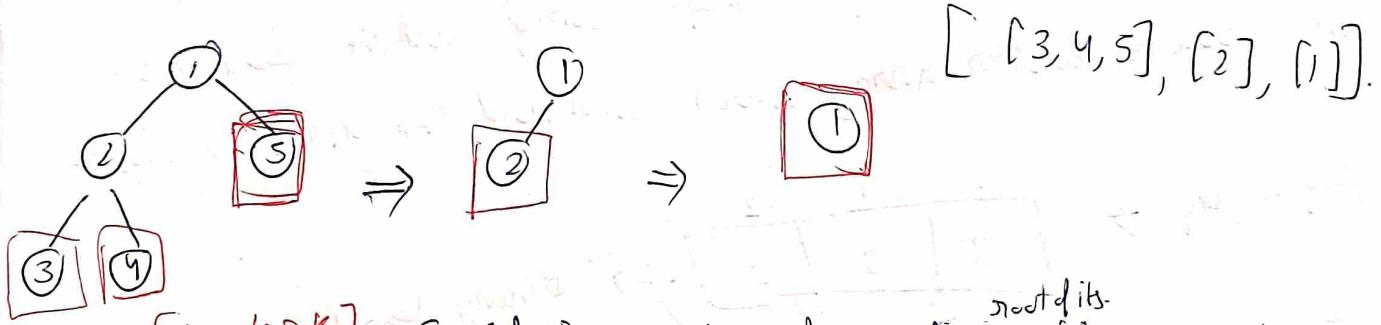
Q) ~~Take all know what a LFU Cache is If you have forgotten go to~~

~~Q~~

(Find leaves of Binary Tree)

Create an unordered map ( $\text{int} \rightarrow \text{vector<int>}$ ) to store level to leaf node map

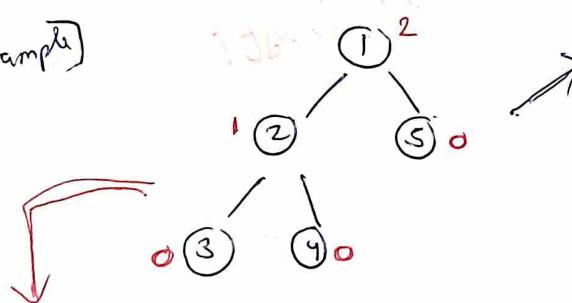
Q) You are given a binary tree, you need to remove leaves at each stage. A new tree will be formed and we need to remove its leaves again. At each step ~~remove~~ store the removed leaves



Sols  $\Rightarrow$  [New truck] Considering each node as the <sup>root of its</sup> subtree we try to calculate its height. The nodes with the same height will be removed.

at the same iteration.

(Example)



$\text{vector<vector<int>} \text{res};$

Code  $\Rightarrow$

```
int dft(  $\text{root}$  ) {
    if ( $\text{root} == \text{NULL}$ ) { return -1; }
    int level = max( dft(  $\text{root} \rightarrow \text{left}$  ), dft(  $\text{root} \rightarrow \text{right}$  ) ) + 1
    res[ level ].push_back(  $\text{root} \rightarrow \text{val}$  );
}
```

$\text{res}[ \text{level} ].push\_back( \text{node} \rightarrow \text{val} )$ ,

(Medium) (RLC Iterator)

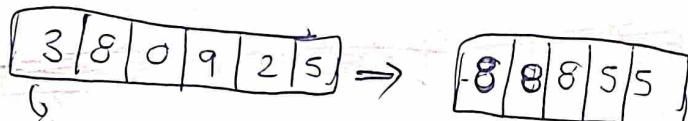
Binary Search Approach

$\mathcal{O}(\log N)$

You will be given an encoded array where

$i \% 2 == 0 \rightarrow$  frequency of the number  
and  $(i+1) \rightarrow$  is the actual number.

→ There is a nest function.

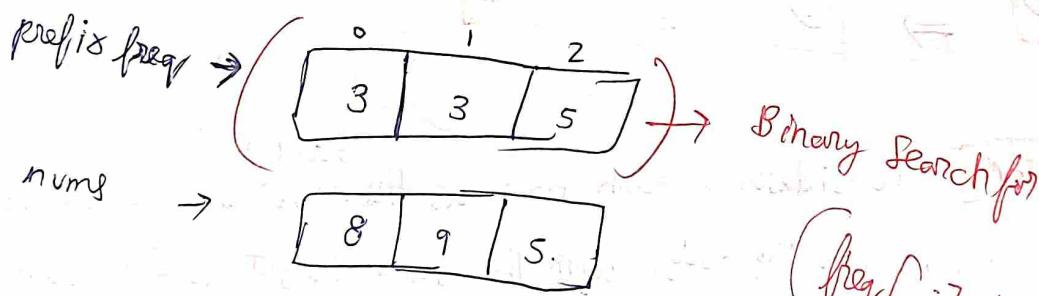


encoding looks something  
like

which tells you to  
extract nest n  
numbers from the array  
and ~~possibly~~ print the  
last number extracted.

Soh

We will be using binary search to solve this problem, we will be using a prefix sum of all the frequencies and created another array which will hold the actual numbers.



Note

$\text{car} = 0$

`int nest(int n){`

check if

$(\text{car} + n) \geq \text{sum of all elements}) \}$  return -1; };

else ↴

Binary search on the prefix freq of  $(\text{car} + n)$  and find the smallest index with that value.

(V.V.V. Hard)

Expression Add Operators

[LeetCode]

Q) You are given a string num, that only contains digits, and an integer target. You need to return all possibilities to insert binary operators '+', '-' and/or '\*' between the digits of num so that the resultant expression evaluates to target value.

Note the operands

cannot have leading zeros.

Example : [num="123", target=6] →

operand can be "0" but  
not "00"

Output → ["1\*2\*3", "1+2+3"]

Beware if you see this  
in interview

Soln

[Code In LeetCode]

This is going to be a crazy solution. Calm your mind before understanding it.

Step 1

Here we will be using the substring generation from [i---j] th subarray

for every recursive iteration we will have a start index.

{ startindex }  
int num = 0

for ( i = startindex; i < s.length(); i++ ) {

if ( i - startindex > 1, and → we don't want leading zeros  
num + = 10 \* num + s[i] - '0';      s[i] == '0' ) break;

string exp = s[ start\_index --- i ]

if ( i + 1 );

⇒ this is how we will be generating  
sub segments

(Step 2) Consider there were only '+' and '-' operators so no problem of using brackets or precedence operators.

In that case -

$$(\star \star \star \star \star) \Rightarrow V.V.Imp$$

Very Simple if only + and - are there

void

f (int i, string path, long result){  
    if (i == originalString.length()) {  
        if (result == target) {  
            path is one of the answer; }  
        return;  
    }

    for (j = i; j < s.length(); j++) {  
        ~~new constString~~ new constString = "";

        if (i == 0) {  
            num = (num + 10) \* s[i];  
            i++;  
        }

Suppose till now  
the expression was

1 - 2 and to be

evaluated expression is

1 - 2 + 3. So

prevNum

needs to be

stored

= prevNum = -2.

f (j+1, choose to add,

path + "

choose to subtract

Path - "constString, result

constString, result + num);

constString, result - num);

new res

= res - prevNum

+ prevNum & (3)

}

}

Step 3) Here we will modify the function to incorporate the multiplication changes.

```
void f(int start, string &s, string path, long result, long prev, int target) {  
    if (start == s.length()) {  
        if (result == target) {  
            ans.push_back(path);  
            return;  
        }  
    }  
  
    string cur = "", num = 0;  
  
    for (int i = start; i < s.length(); i++) {  
        if (i > start) cur += s[i];  
        num = num * 10 + s[i] - '0';  
  
        if (i + 1 < s.length()) {  
            addCase(i + 1, s, path + "+" + cur, result + num, num, target);  
            subtractCase(i + 1, s, path + "-", result - num, num, target);  
            multiplyCase(i + 1, s, path + "*", result - num * num, num, target);  
            divideCase(i + 1, s, path + "/", result / num, num, target);  
        }  
    }  
}
```

For the case  $(1 + 2 \times 3)$  →  $1123$

$\text{prevNum} = 2$   
 $\text{num} = 3$   
 $\text{result} = 1 + 2$

For the case  $(1 - 2 \times 3)$

$\text{prevNum} = -2$   
 $\text{num} = 3$   
 $\text{result} = 1 - 2$

V-Lmp  
(V-Lmp)  
(V-Lmp)  
(V-Lmp)

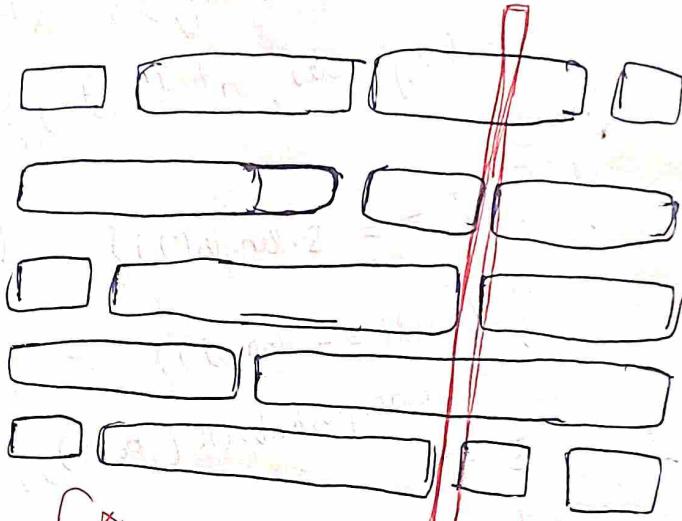
# Brick Wall

(MEDIUM)

- (GEOGEE) (EDGE MARKING APPROACH)
- Q There are bricks filled in front of you, for  $n$  rows. The  $i^{\text{th}}$  row has bricks of width 1.

Eg.

[1	2	2	1]
[3	1	2]	
[1	3	2]	
[2	4	]	
[3	1	2]	
[1	3	1	1]



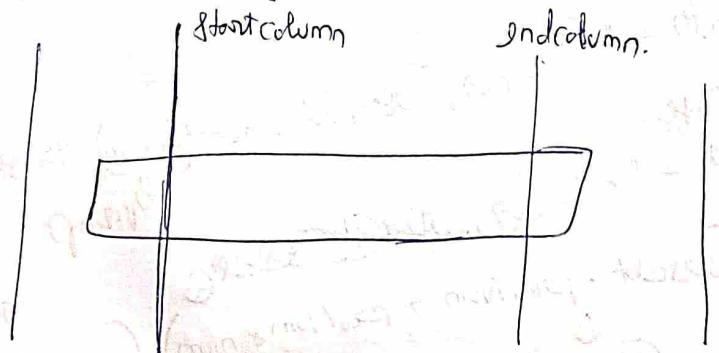
We want to draw a line across the brick wall from top to bottom in such a way that it cuts the least number of bricks.

Soln

there are 2 solutions for this.

[Soln 1] {Line Sweep}

\* We will travel through a row and for every brick we will calculate its starting column and ending column if the brick is covering.



After for each row using prefix sum, we calculate line [startcolumn] ++ line [endcolumn + 1] -- which column has longest gap.

Soln 2

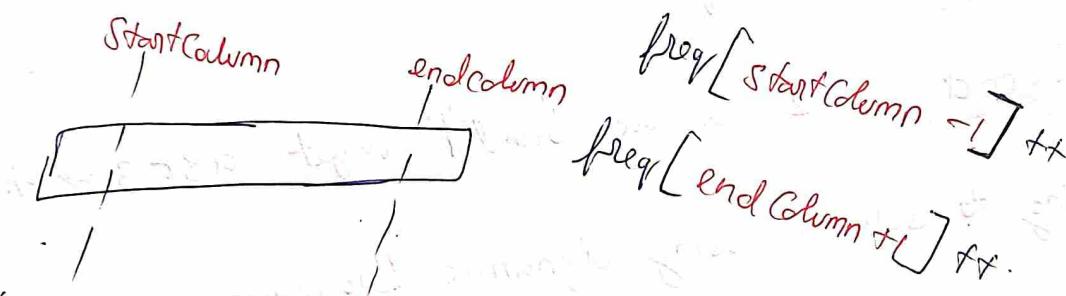
Now the line sweep technique has a problem.

Let's say the  $\text{wall}[i][j] \leq 10^9$  so you cannot ~~store~~

Store the start column or end column in the array

Approach 2

We will use a hashmap to mark the frequency of edges which are not touched.



Now in the after we find what max (freq[i]).

maxEdges = max(freq[i]).  
No of bricks = walls.size() = n.

{Note}  
{Trick}

(Minimum Difference between  
largest and smallest value in 3 moves.)

Q Given an integer array, you can modify almost K numbers to any numbers of your choice. Return the minimum difference you can get after applying the operations between largest and smallest value.

Ans (Possible options) → First sort the array

- 1) discard K smallest numbers → Find ( $A[K] - A[n-1]$ )
- 2) discard (K-1) smallest 1 largest Find ( $A[K-1] - A[n-2]$ )
- 3) discard (K-2) smallest + 2 largest Find ( $A[K-2] - A[n-3]$ )

choose  
minimum of  
these

Q1

(HARD)

(~~DATA STRUCTURE~~)

(String Compression II)

(CODE DN

[LEETCODE])

RLE (Run Length Encoding) is a string compression. Given a string  $s = "aaaabcccd"$ ,  $K=2$ . Notice how for single  $\checkmark$

$RLE = a3b1c3d$  [ Characters we don't append 1. Given an integer  $K$  ~~with~~, you can remove at most  $K$

characters from the string  $s$ . Return the minimum length of RLE encoded string you can form.

A1

$s = "aaabcccd"$   $K=2$  remove "b" and "d" we get  $a3c3 \Rightarrow 9$ .

\* We are going to solve it using dynamic Programming.

\* At each character we have a choice ~~with~~ whether we want to take this character in our string or not.

\* We will keep calculating the length of the RLE ~~at~~ at each index dynamically.

State of dp.

What is the

dp [start] [prevchar] [len] [k] can form given that

for the substring  $s[start, \dots n-1]$

Character of the string  $s[start, \dots n-1]$ , with the  $prevChar$  as the previous  $k$  elements and  $len$  as the length of previous continuous segments and we can still delete.

$f(\text{start}, \text{prevchar}, \text{len}, -K)$

$\text{if } (K < 0) \{ \text{return INT_MAX} \}$  we deleted more than K characters

$\text{if } (\text{start} >= n) \{ \text{return } 0; \}$  we got to the end correctly

$\text{if } (n - \text{start} \leq K) \{ \text{return } 0; \}$  Another optimisation if no characters left  $< K$ . Then we delete all the

$\text{if } (\text{dp}(\text{current state}) != -1) \{ \text{return } \text{dp}(\text{current state}); \}$  characters

We decide to delete  $s[\text{start}]$  and not keep it.

choice 1 =

$f(\text{start} + 1, \text{prevchar}, \text{len}, K - 1);$

$\downarrow$   
prevchar remains same

$\downarrow$   
character has been deleted so  
 $K = K - 1$

We keep the character.

~~choice 2~~ But there are 2 parts.

Point 1  $\rightarrow$  if ( $s[\text{start}] == \text{prevchar}$ )

Same character to the segment has been added

choice 2 = isLengthIncreasing(len+1) +  $f(\text{start} + 1, \text{prevchar}, \text{len} + 1, K)$ .

{This is to check q9 to a10 transition}

Point 2  $\rightarrow$  if ( $s[\text{start}] \neq \text{prevchar}$ )

choice 2 = 1 +  $f(\text{start} + 1, s[\text{start}], 1, K)$ ; length of segment = 1

$\downarrow$  prevchar now becomes  $s[\text{start}]$

this 1 is added

because a new character has been introduced after a long subsegment

Side RDR aaa b  $\Rightarrow$  ab b  $\rightarrow +1$

[HARD]

Finding MK Average

O(logm)

O(1) → calculate MKC

↳ To add a number.

You are given two integers  $m$  and  $K$  and a stream of numbers is flowing. We need to find MK average for this stream.

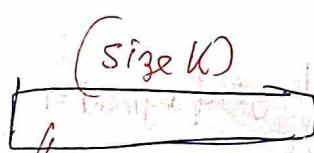
Steps in which MK Average is being calculated.

- If the current no of elements in the stream is less than  $m$  then we return -1.
- if no of elements we have encountered till now is greater than  $m$ ,
  - ① then take the latest  $m$  elements
  - ② Remove the smallest  $K$  elements
  - ③ Remove the largest  $K$  elements
  - ④ Calculate average of the remaining elements

This is the part that we want to check  
Keep in mind latest  $m$  elements

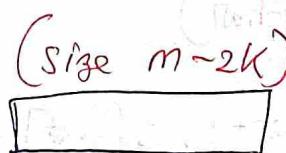
[Sol] we will be using 4 variables.

- ① Queue →  q [This will contain the latest  $m$  items]
- ② 3 multisets.



left

This holds the ~~smallest~~  
 $K$  smallest elements out of  
the latest  $m$  elements.



mid

This holds the  
( $m-2K$ ) next



Right

This holds the  
next  $K$  out of the  
latest  $m$ .

Add Number

if (q.size is less than m) {

push it to the queue.

Push this new number into the 3 multisets.

① push new number into left set

② check if left set size is exceeding in size more than K. if you want to delete the last element of the multiset

If Yes.

st.erase (prev(st.end()))

→ this function will point to iterator previous to st.end()

then take the last element of left set and push it into the mid set.

st.rbegin() → this iterator will take us to the end of the multiset

check if the mid set size is exceeding in size more than  $(m - 2K)$ . ⇒ [update the sum of mid set accordingly]

check if right set size is

If Yes

then take the last element of mid set and push it into the Right set.

5.

Now the condition is that

(q.size == m)

then take q.front

- q.front() has to be popped. = {delete\_element}

and q.push (new) element

{P.T.O}

Now the {delete\_element} needs to be deleted from the

{left, mid or right} set where we want this element to be removed from. So that it is not in one of the latest  $m$  elements.

$n = \text{delete\_element}$

check if  $[^{\star} \text{left.begin()} >= n]$

erase  $\text{left.erase}(n)$

else if  $(^{\star} \text{mid.begin()} >= n)$

erase  $\text{mid.erase}(n)$   
 $\sum -= n$

else  
 $\text{right.erase}(n)$

After erasing from one of the sets we need to do resizing again.

if  $[\text{left.size()} < k]$

$\text{left.insert} (^{\star} \text{mid.begin()})$

$\text{mid.erase} (\text{mid.begin()})$

$\sum -= \text{mid.begin()}$

if  $[\text{mid.size()} < m-2k]$

$\text{mid.insert} (^{\star} \text{right.begin()})$

$\text{right.erase} (\text{right.begin()})$

~~$\sum + = \text{right.begin()}$~~

$\sum + = \text{right.begin()}$

We keep modifying  $\sum$  on the fly

(Amazing trick)

HARD

## Optimize Water Distribution in a Village

GRAPH

[tmp to check why my approach failed]

- ① There are  $n$  houses. For each house  $i$ , we can either build a well inside the house directly or connect the house to a component which has atleast one house where a well is built. You are given an array wells, where  $\text{wells}[i-1]$  gives us the cost to build a well at node  $i$ . Also you are given pipes edges, ~~so~~ where its has  $[\text{house}_1, \text{house}_2, \text{cost}]$ . Basically cost to build a ~~one~~ bidirectional pipe from house $_1$  to house $_2$  has a cost  $\rightarrow$  cost. Find the minimum cost to connect all the edges.

Here we want to use DSU to connect the components

Soln

Approach is that you travel the edges sorted by their [Minimum Spanning Tree]  $\rightarrow$  After connecting all houses to house $(0)$  using wells $[i]$  edge weight. ~~We will travel the edges and add cost.~~

Trick

You assume a house  $0$  which only has water. We consider new pipes to be built from house $(i)$  to house $(0)$ . In the end we want to see while checking a pipe, check node  $v$  and node  $u$ . ~~if the node~~

Step 1

Case 1

If both the nodes have ~~especially~~ no water, then we will assign **well** to the node which has lower well setup cost and connect the edge and mark the other node as **HAS WATER**

Connected have  $0$  in their component or not

Case 2

If both the nodes have water no need to connect

Case 3

If one of the nodes has water, then we simply just connect the node which has no water.

P.T.O

## My Approach

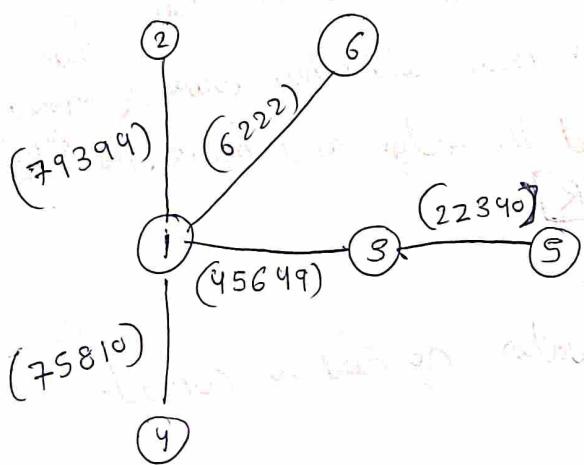
- 1) Sort the nodes by their well setup cost.
- 2) While travelling through the nodes, we want to check if node has water or not.

then using bfs as the source node as the ~~new~~ current node where we built the well. Then start merging edges if the cost to build a well on the new node to be stitched is greater than edge weight then we shall ~~not~~ stitch it.

$\text{cost to stitch} > \text{cost to build well on this node}$

why is this approach wrong?

first case:



well setup cost	
1	4625
2	65696
3	86292
4	68291
5	37147
6	7880

Here if you go by bfs then you will merge heavier weights first

Classical

[Maximum Path Duality]

(Hard) [Leafcode] of a graph.

Complexity Analysis

[Use of Constraints]

Backtracking

Q1 You are given an undirected graph from nodes 0 to  $n-1$ . You are given edges  $[(u_i, v_i, w_i)]$  which tell

$w_i$  is the time required to go from  $[u_i \rightarrow v_i]$  or  $[v_i \rightarrow u_i]$

You are also given an array values, where  $\text{values}[i]$  is the value of the  $i^{\text{th}}$  node. max ~~edges~~  $\rightarrow$  ~~edges~~

You need to tell what is the maximum score you can get while travelling from node 0 and ending at node 0 again within maxTime.

Score is sum of the value[i] of the distinct nodes visited.

Constraints  $\rightarrow$

$$[10 \leq w_i, \text{maxTime} \leq 100]$$

$$n = 1000$$

From each node 4 edges can be connected at most.

A This problem is a game of constraints only.

What if we madly travel around the graph across all edges. With 1 condition, we keep on

adding the edge weights as we keep travelling around the graph.

Step 1  $\rightarrow$  Keep adding edge weights as we travel around the graph and stop traversing as soon as ~~maxTime~~  $\rightarrow$  [time of traversal  $>$  maxTime]

Step 2  $\rightarrow$  keeping a visited array. Note we are not checking the

visited array to see if we want to visit it or not. Rather we are using it as a counter array to keep track that how many times are we visiting it. If it is already visited update its score,  $\rightarrow$  don't add

PTO

## Time Complexity Analysis

→ Base Case → if ( $\text{time travelled} > \text{most time}$ ) return.

④ You see in constraints  $[10 \leq w_i \leq 100]$

So depth of each dfs can be of  $[10 \text{ to } 100]$ .  $[100/10]$ .

(i.e.)  $[\text{most time} / \min(w_i)] \rightarrow \text{worst case}$

and each node has max 4 edge connected to it. So at each depth level we have 4 choices.

So total we are doing  $4 \times 4 \times \dots \times 4$  (i.e.)  $(4^{\text{10}})$   
(10 steps operation)

⑤ And while traversal if you are seeing that the node is ~~is~~ 0.  
then update to maximum score

Similarly we can find the distance as well.

i.e.  $\text{distance}[\text{node}][i] \rightarrow \text{distance from node to its } i^{\text{th}}$  ancestor.

Now if we have this data. Then we can find distance between any two nodes. Node  $(a, b)$ .

$\text{distance}(a) + \text{distance}(\text{LCA}(a, b))$  and

$\text{distance}(b) + \text{distance}(\text{LCA}(a, b))$ .

Amazing concept

Using LCA to find max Edge Weight between

two nodes.

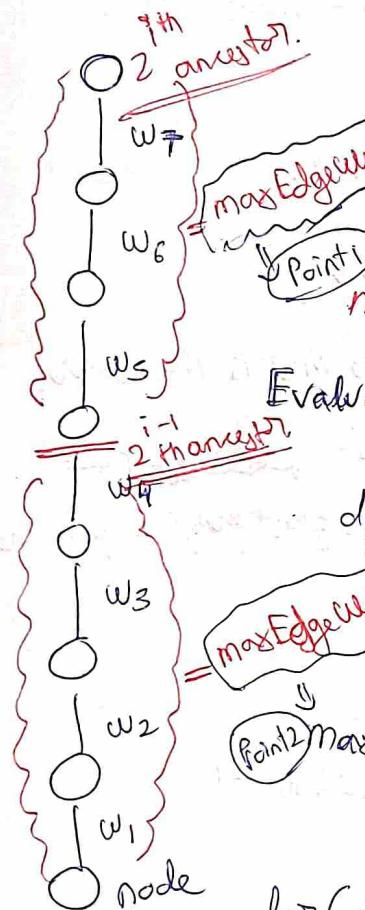
Find any ~~one~~ thing [sum, xor, max] between two nodes.)

This is an amazing concept using LCA. and can be used to find amazing properties between ~~nodes~~ two nodes.

Such as distance,

You can find within nodes as well. Suppose you are asked to solve ~~for~~ of edgeweights between node A and node B?

Now we can store



maxEdgeWeight[node][i]  $\rightarrow$  this tells me the ~~o~~

maximum edgeweight encountered in the path from node to its  $i^{\text{th}}$  ancestor.

Evaluation maxEdgeWeight[node][i] =

dfs(node, parent, edgeWeight) {

    maxEdgeWeight[node][i-1] = UP[node][0] = parent

    Point2 maxEdgeWeight[node][0] = edgeWeight;

    for (~~loop~~ i=1; i < log(i); i++) {

        if (UP[node][i-1] == -1) {

            UP[node][i] = UP[~~node~~][i-1];

        UP[node][i] = UP[UP[node][i-1]][i-1];

    maxEdgeWeight[node][i] = max(maxEdgeWeight[node][i-1],

        maxEdgeWeight[UP[node][i-1]][i-1]);

~~Q or \*~~

## Largest Color Value in Directed Graph.

Dmp

Thought Process of Directed Graphs

(Revise)

- Q) There is a directed graph of  $n$  nodes and  $m$  edges. Nodes from 0 to  $n-1$ . For each node you are given colors. Directed edges are  $s = "abcde"$  which means 

0	1	2	3	4
a	6	c	d	e

 also given.

$$\text{color}[0] = a$$

$$\text{color}[1] = b$$

$$\text{color}[2] = c$$

$$\text{color}[3] = d$$

$$\text{color}[4] = e$$

A path from node  $u$  to node  $v$  is a path if

$u$  to  $v$  is reachable. ~~Also reaches~~

Also for each path there is a score.

$$[v \rightarrow v_1 \rightarrow v_2 \rightarrow v_3 \rightarrow \dots \rightarrow v]$$

which ever colors frequency is maximum, that is the score.

Q) In the path from node  $u$  to node  $v$ , each node has a ~~frequency~~ color. If you count the freq of each color then ~~maximum~~ the highest frequency is the answer.

Note: Return -1 if there is a cycle in the graph

(Step 1) → Detect a cycle. If cycle is there then return -1

(Step 2) Trick is Topological Sort.

Whenever it's a directed graph try to check if it's solvable by topological sort or not

But Now in BFS queue of topsort store an array of length 26, which has the frequency stored.

At each node check ~~the max~~ what is the max of that array

## Few Categories of questions,

→ Upon seeing these type of questions what is the thought process that should come in your mind.

### [Categories I]

#### [Swap to Sort]

Q) Given an array you will be given a condition on which certain indices and certain values are swappable amongst themselves. You want to find the lexicographically smallest array that you can find using these swaps.

A) The first thought that should come to your brain is how you can group the indices which are swappable amongst themselves. ~~Once you have~~ [Note] Don't try to manually sort the values.

Once you have grouped the set of indices into 1 value using D.S.U. Sort only those elements and insert into their respective position.

### (Category II)

#### [Interval swap and Sort]

Q) You will be given intervals  $[\text{start}, \text{end}]$  and you will be asked to how many minimum meetings room will be required.

A) Either used priority-queue or line sweep. To solve this question.

But to solve this using line sweep we will be needing all the start and end,  $[\text{end-start}]$  to be in an array formable range.

### [Category III]

Given a graph and path between two nodes you might be asked to find XOR sum of nodes or max of something within that path.

- (A) Think of LCA and binary Lifting during that. Find ways to calculate things from node(a) to  $LCA(a,b)$  and from node(b) to  $LCA(a,b)$ .

You need to do  
this question  
in  $O(N)$

Longest Consecutive Sequence

(REVERSE)

(V.VIMP) Trick

(Google)

- (Q) What is the longest consecutive sequence of an array

arr  $\rightarrow [100, 4, 200, 1, 3, 2]$

9 1 3 2

are the list of consecutive elements

- (A) Let's walk through the naive approach. Keep a map or hashset of all the numbers present in the array. For each  $num[i]$ , keep doing a +1 and check if  $(num[i]+1)$  is present or not. Then check  $(num[i]+2)$  is present or not. If not then break, else keep increasing the length of the segment.

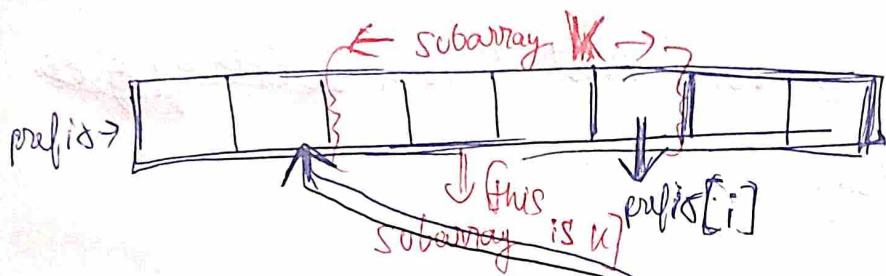
Optimal  $\rightarrow$  The above approach which came to my mind was  $O(N^2)$ . Now there is a slight fix. For every  $num[i]$  just check if  $(num[i]-1)$  is present in the hashset or not. If present then don't evaluate it. If not present, then start evaluating to check if  $num[i]+1$  is present or not then  $(num[i]+2)$  and so on. This way we are only evaluating the start of the sequence.

[Category IV]

this is a way to

Subarray having sum = k

Create a prefix array. Let say  $\{a[i] \leq 10^9\}$



In the map keep  
storing prefix sum  
fill  $\{i\}$ .

Find if there was a occurrence of  $[prefix[i] - k]$

Things to keep in mind while coding

If you have a set which has integers in sorted order.

You want to do an operation of deleting a few numbers from the set.

You might do

while ( $it != st.end()$ ) {

$st.erase(it)$  and  $it++$ }

→ **NULL  
Pointer  
exception**

make sure to move the pointer and then call erase.

while ( $it != st.end()$ ) {

$num = *it;$

$it++;$

$st.erase(num);$

→ **False iterator to the starting number  
will be lost**

## [Minimum Window Substring]

N.B.P

- Q) Given a string S and T. Find the minimum contiguous substring ~~subset~~ of S, such that T is a ~~substring~~ subsequence of the substring.

i.e. T can be generated using the subsequence of the substring of S.

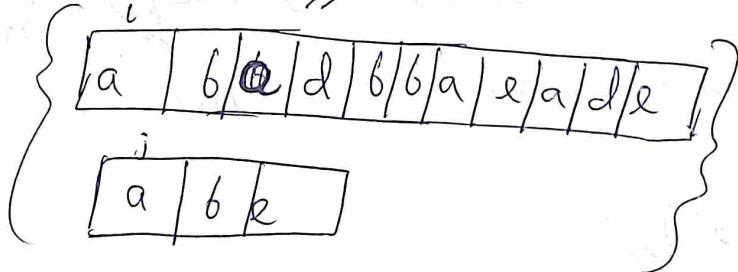
- A) Idea behind the solution: [Sliding window]

S → a b b d b b a e a d e  
T → a b e

(Similar Questions)

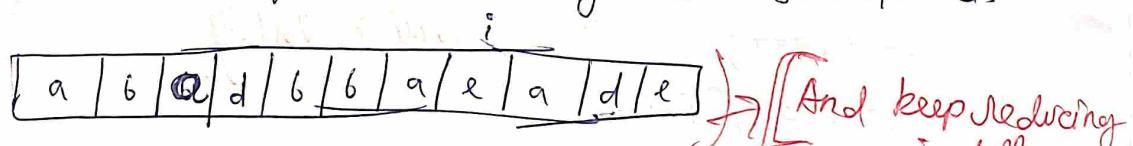
keep two pointers *i* & *j* as we do normally

Step 1

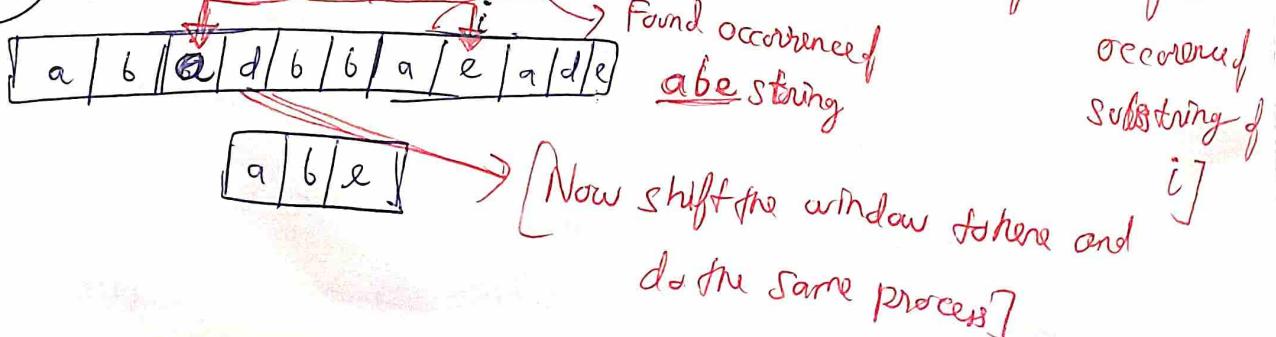


Step 2

Now suppose at *i* we found that string T is a subsequence.



Step 3



Now shift the window further and do the same process]

~~Category Question~~ Category Question.

~~Google~~ Google [Maximum Performance of a Team]

~~Vikas~~ Vikas

way of thinking these questions

You are given two arrays of size  $n$ . Speed and Efficiency. Speed[i] and Efficiency[i] represent speed and efficiency of the  $i^{\text{th}}$  Engineer. We can choose at most  $K$  Engineers such that the team's performance is maximum.

Team's Performance =  $(\text{Sum of the speed of all Engineers}) \times \text{minimum Efficiency of all those Engineers}$

~~How to do these kinds of problems?~~ ↗ [Use Min Heap for this] → [try to think of these questions in this manner]

~~Thought process~~ ↗ Step 1 [Sort the Engineers by their decreasing Efficiencies] ↗ Try to think of it as if you are considering a particular Efficiency as minimum at the moment. (Sorted in descending order)

Step 2 Let's say we are choosing at most  $K$  Engineers such that minimum efficiency is  $E_3$ .

E →	$E_1$	$E_2$	$E_3$	$E_4$	$E_5$	$E_6$	$E_7$
S →	$S_1$	$S_2$	$S_3$	$S_4$	$S_5$	$S_6$	$S_7$

Range

Step 3 Now we have to choose at most  $K$  such speeds. Within the given range and pop the minimum speed out of the current and insert the new speed.