

My thought process,

First time when I read the problem, the thing that clicked in my brain \rightarrow

$f(\text{start position, prevHouseColor}) \{$

$\text{minCost} = \text{MAX_VALUE};$

$\text{for}(\dots) \{$

$\text{minCost} = \min(\text{minCost, cost of color } k \text{ for this house + } f(\text{start position} + 1, \text{color } k))$

$\}$ \rightarrow total states = $(n \times k)$

\rightarrow no of total colors

\downarrow no of total houses

And in each state we are iterating over k colors.

$(n \cdot k) \times k = O(nk^2)$ state

Then I saw a follow up \rightarrow

Can you do it in $O(nk)$.

\Downarrow

This got me thinking can I use iterative dp instead.

P.T.D

For, during recursion, we say that the house which we colour first does not matter, just adjacent color should not be the same.

So we did $dp(i, j)$

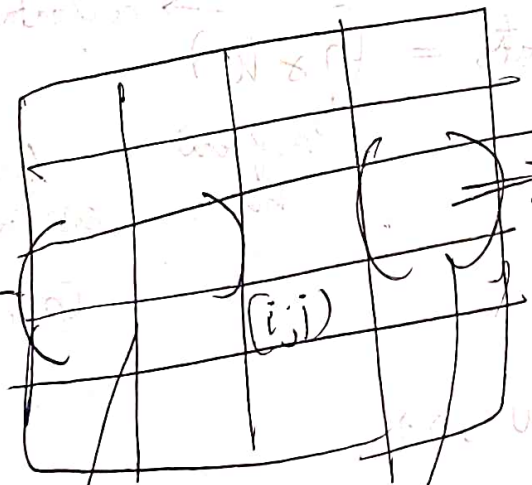
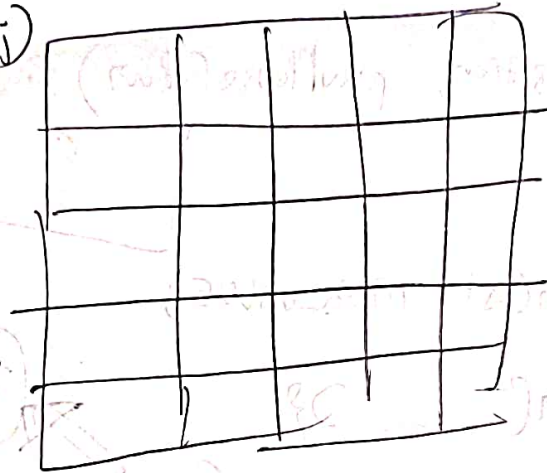
~~$dp(i, j)$~~

$dp(i, j)$

↓
tells one, what is

the minimum cost to

paint house i , with color j , given all the $(i-1)$ are painted, and we have tried all the colors for that house



(this row is already evaluated)

For house i to have color j , house $(i-1)$ cannot have color j .

it can have any color $(0 - j - 1)$ or $(j + 1 \text{ to } k - 1)$

We have to find the minimum of both,

and

$$dp[i][j] = \min(\text{cost}[i][j] +$$

$$\min(dp[0][j], \dots, dp[j-1], dp[j+1], \dots, dp[k-1]))$$

(consider $dp[i-1][j]$)