

Vehicle-Track Interaction & Dynamics

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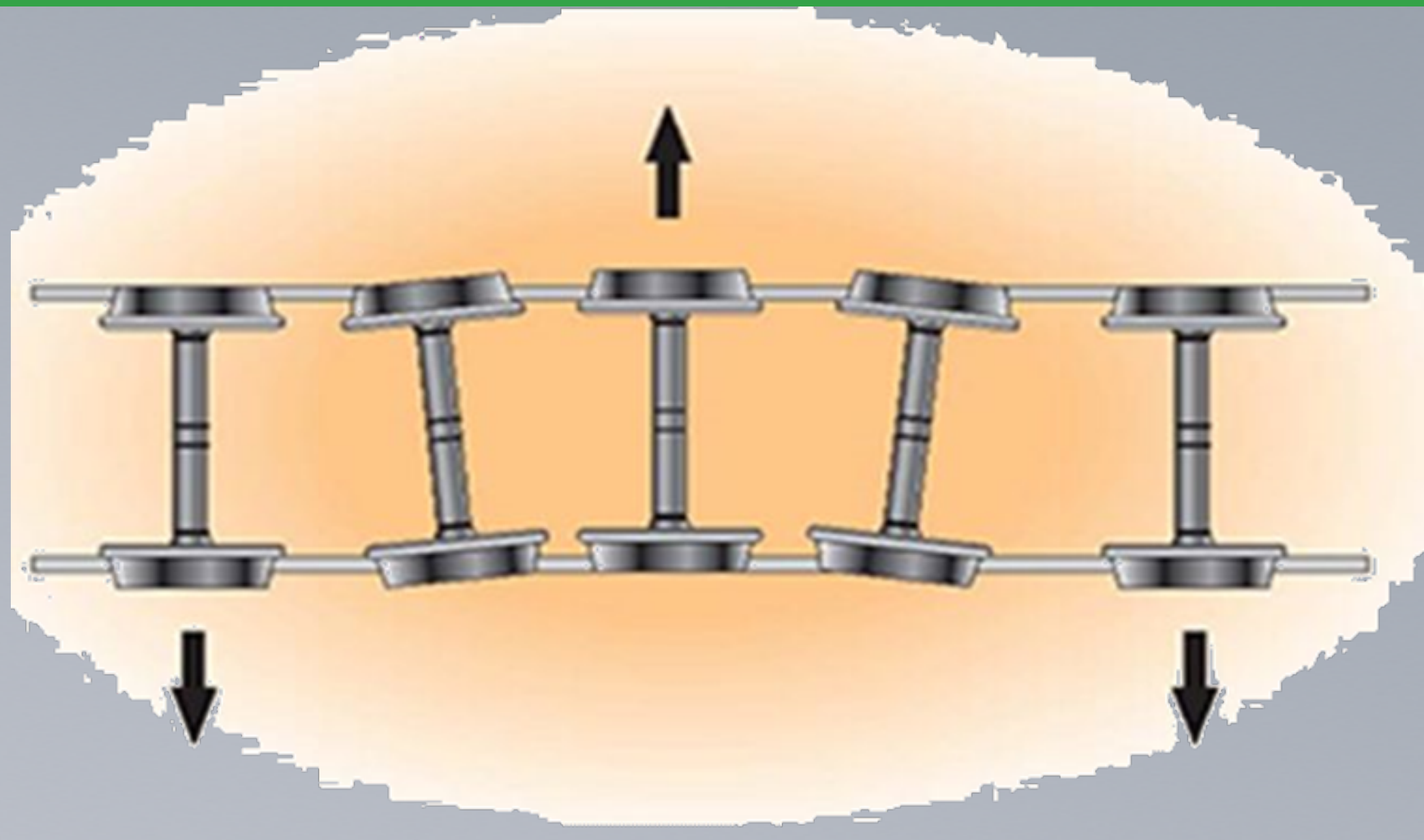


PEARL MILESTONE SPONSOR

PRINCIPLES COURSE



JUNE 10-12,
2025



WRI2025HH

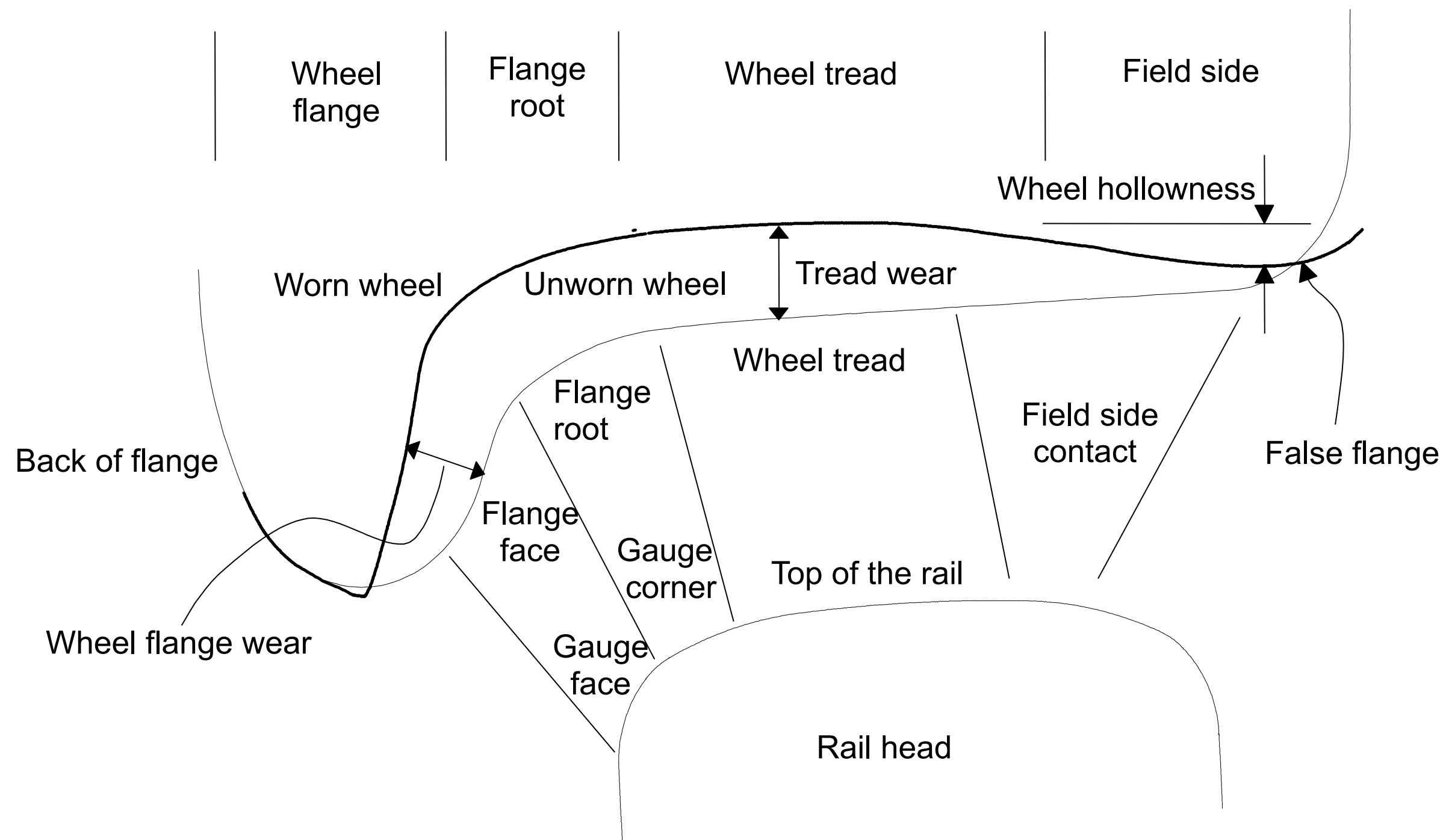


Agenda

1. Vehicle steering, stability, and curving forces
2. Wheel-rail profile design and performance
3. Vehicle-track interaction derailment mechanisms and risk assessment
 - a. Wheel climb
 - b. Rail rollover



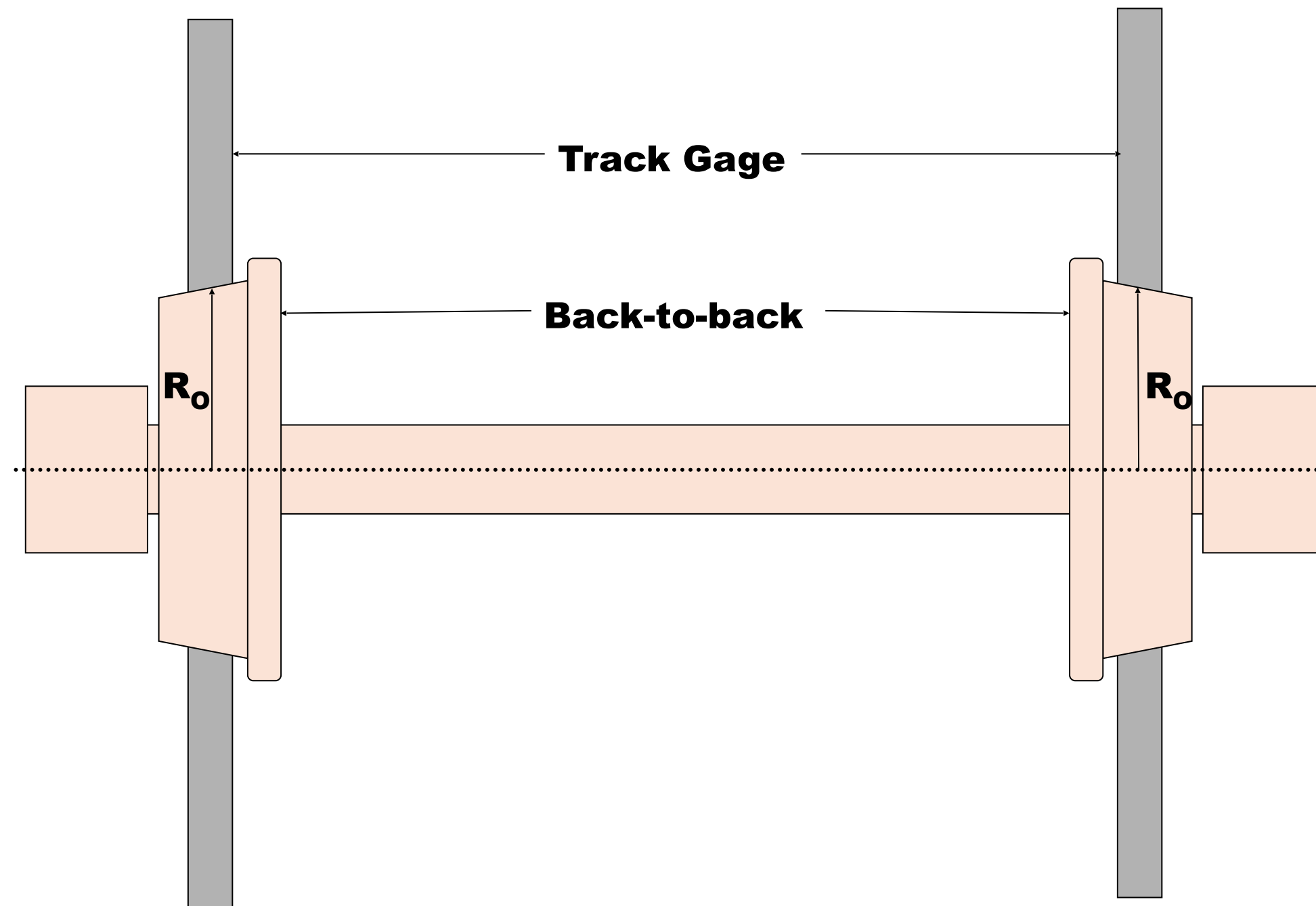
Terminology



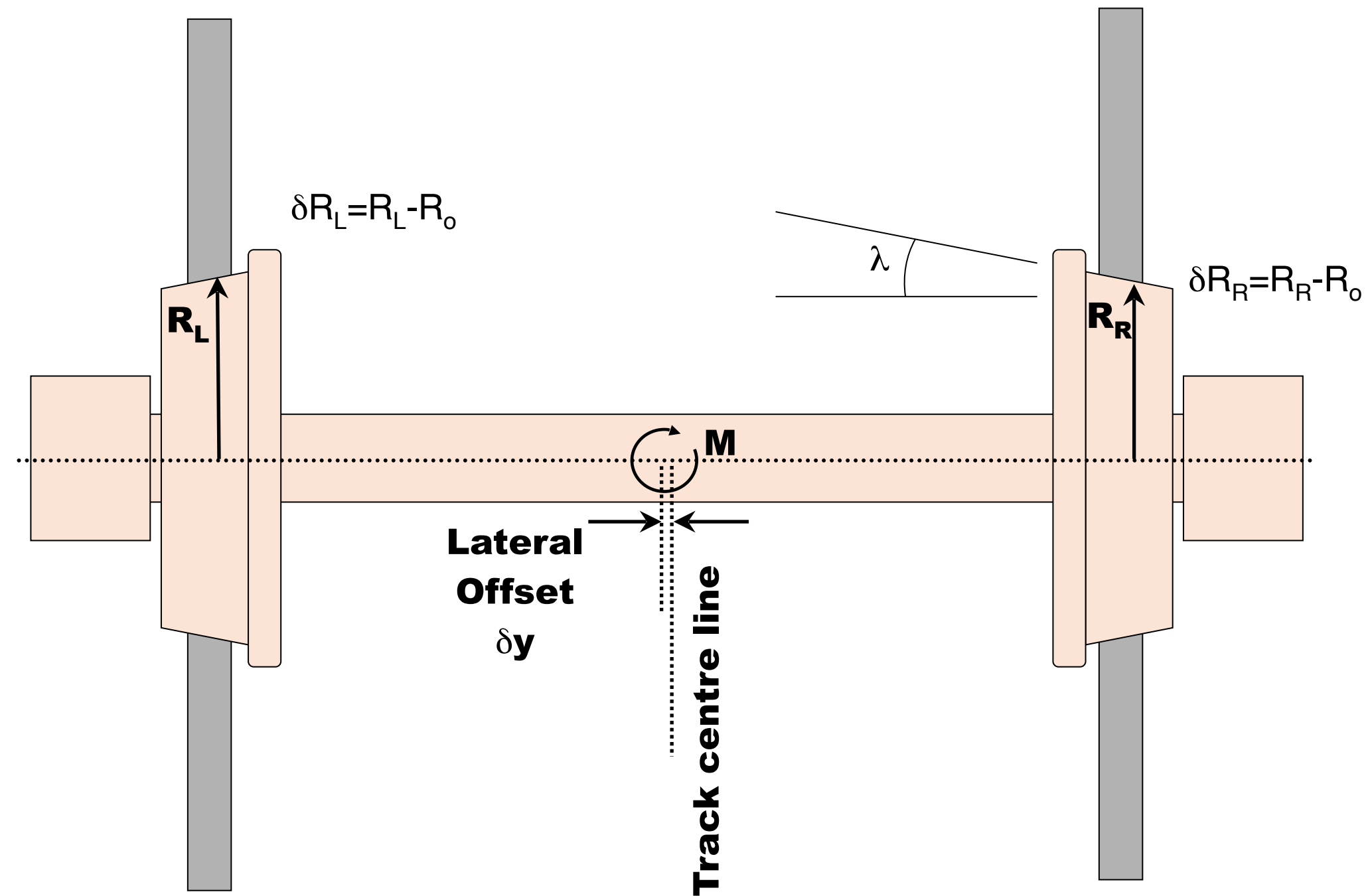


WHEELSET & VEHICLE STEERING

The Free Rolling Wheelset

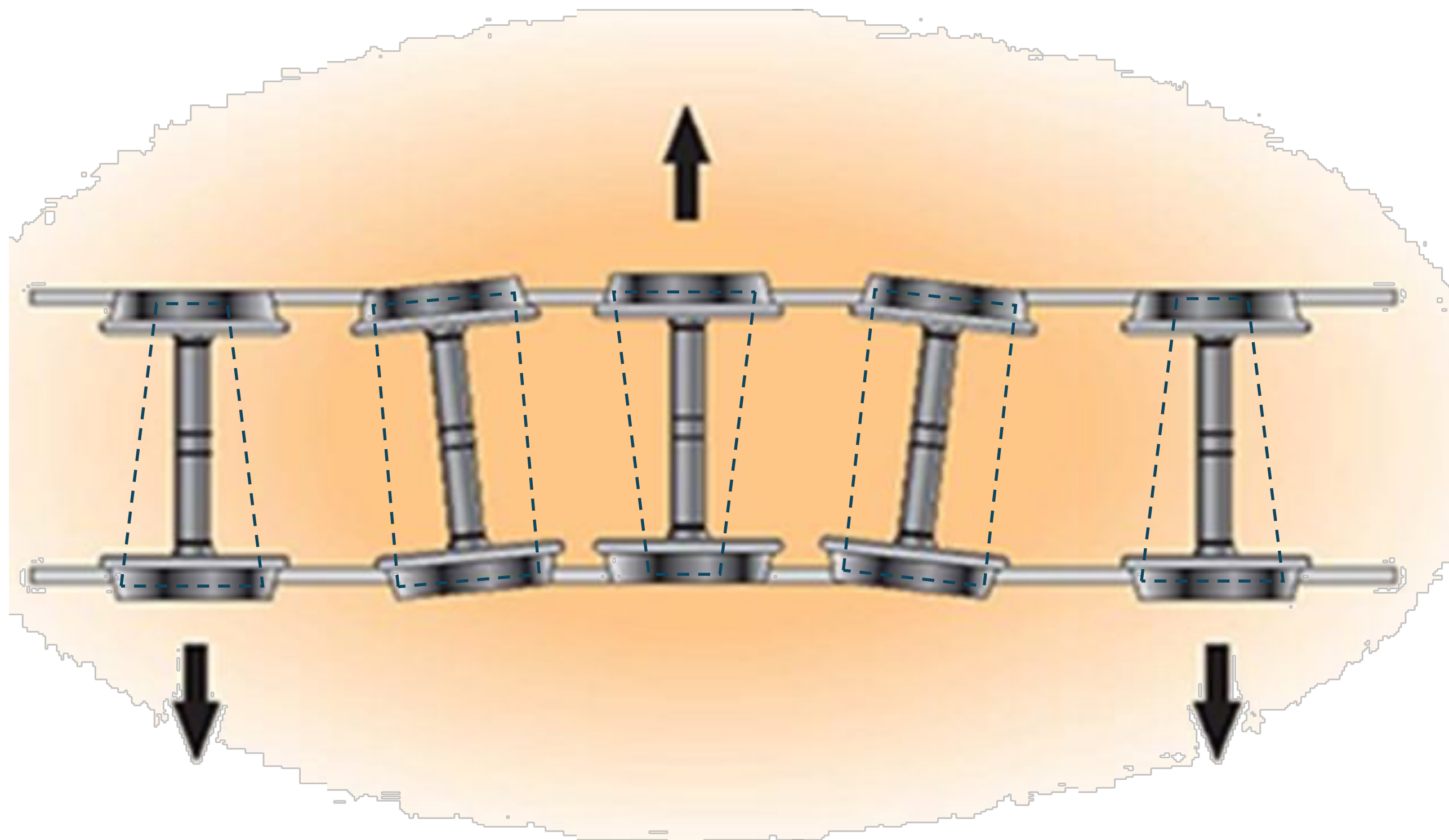


The Free Rolling Wheelset

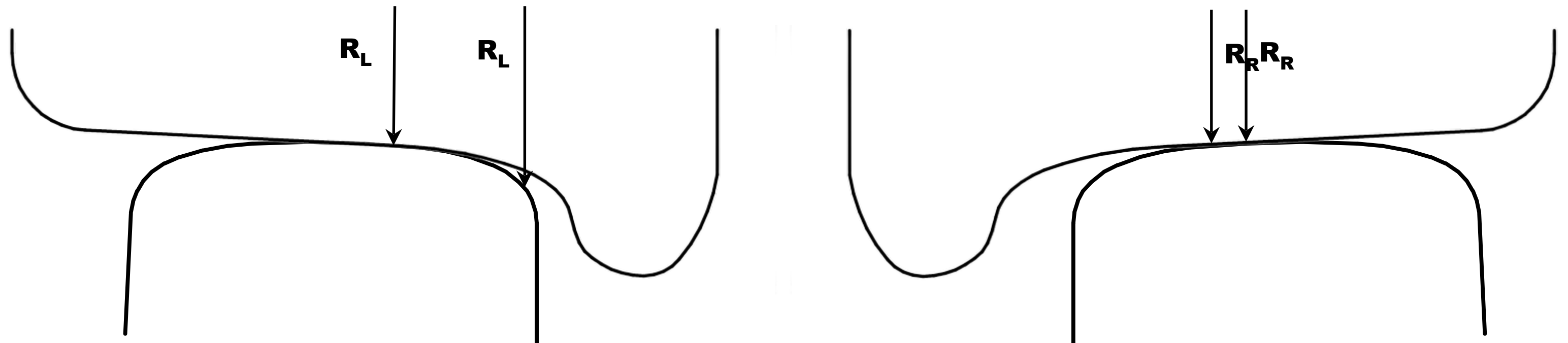
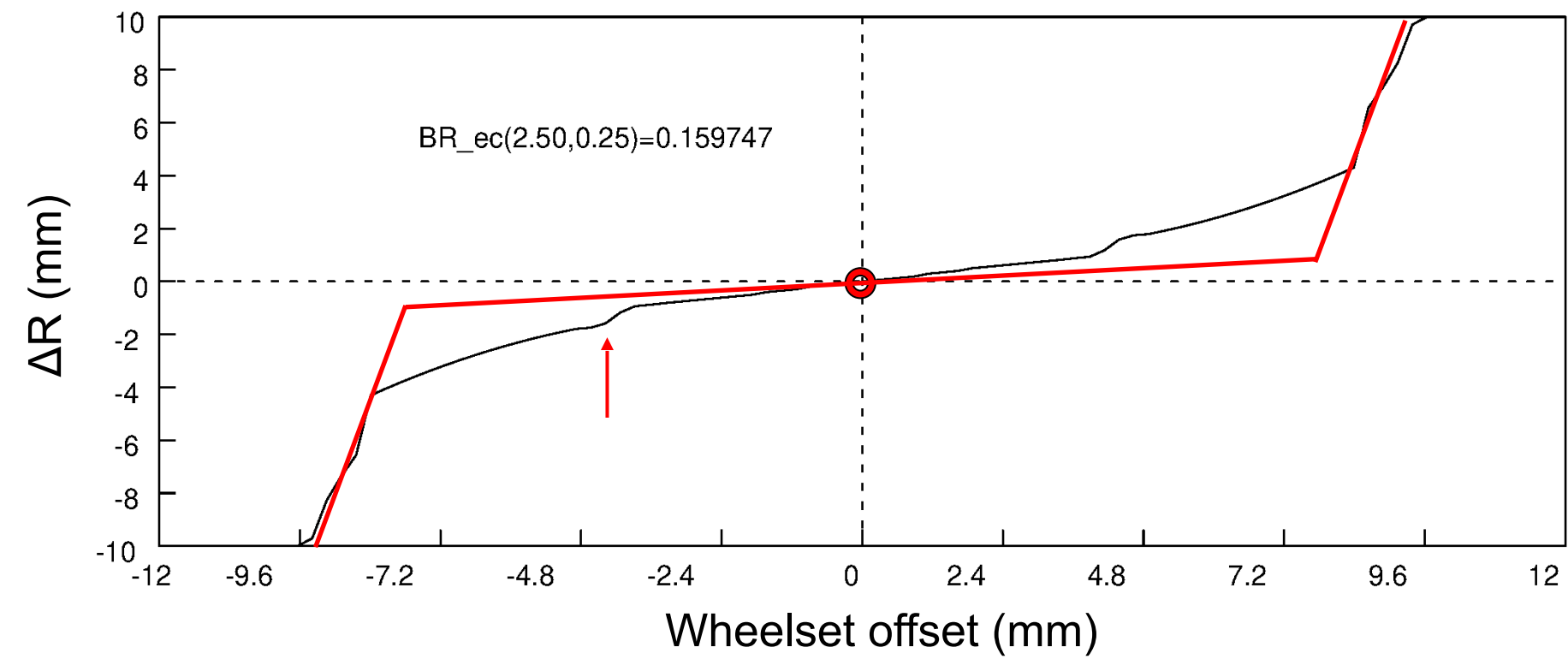




The Free Wheelset - Hunting



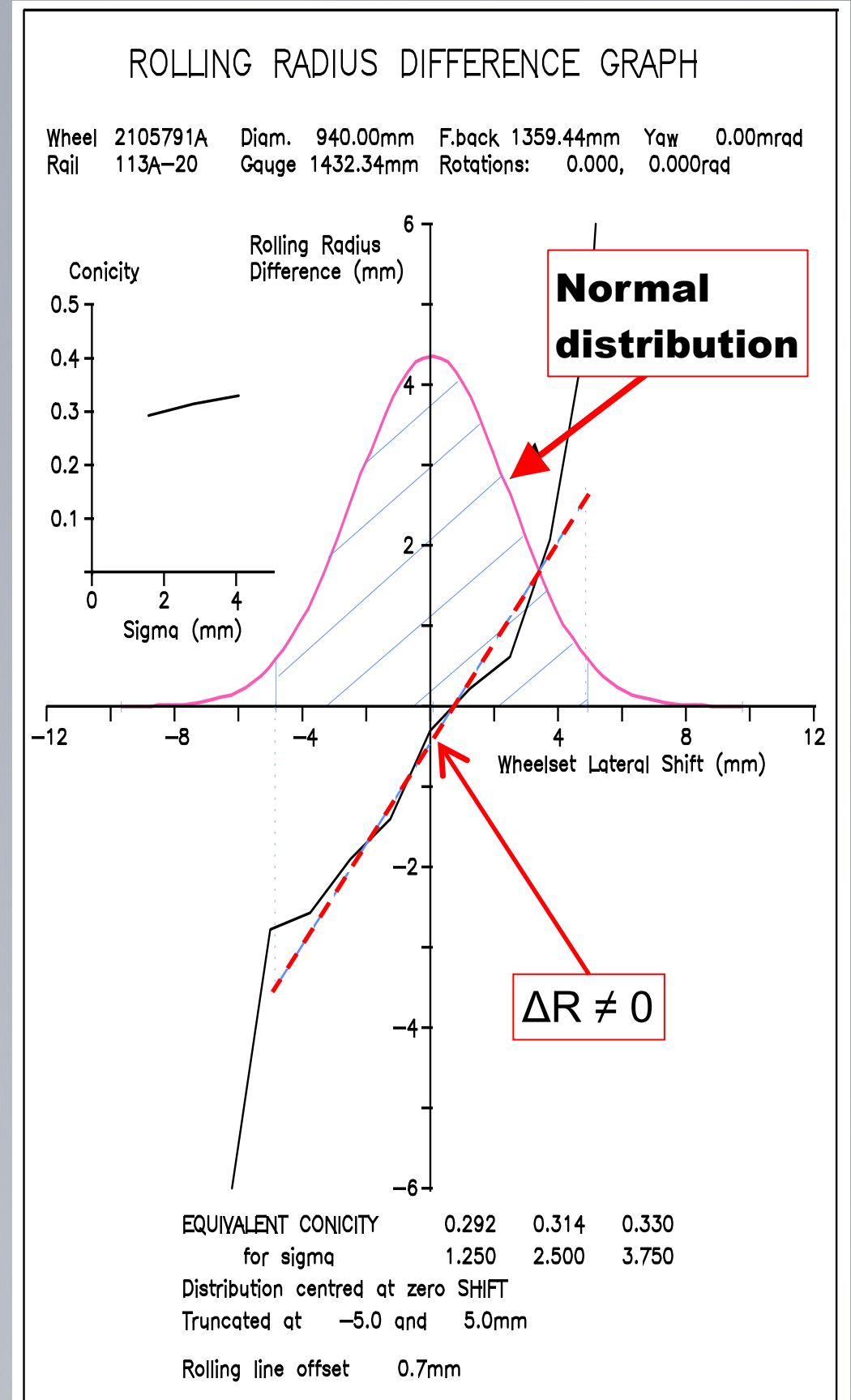
Conicity



Equivalent Conicity from the ΔR Plot

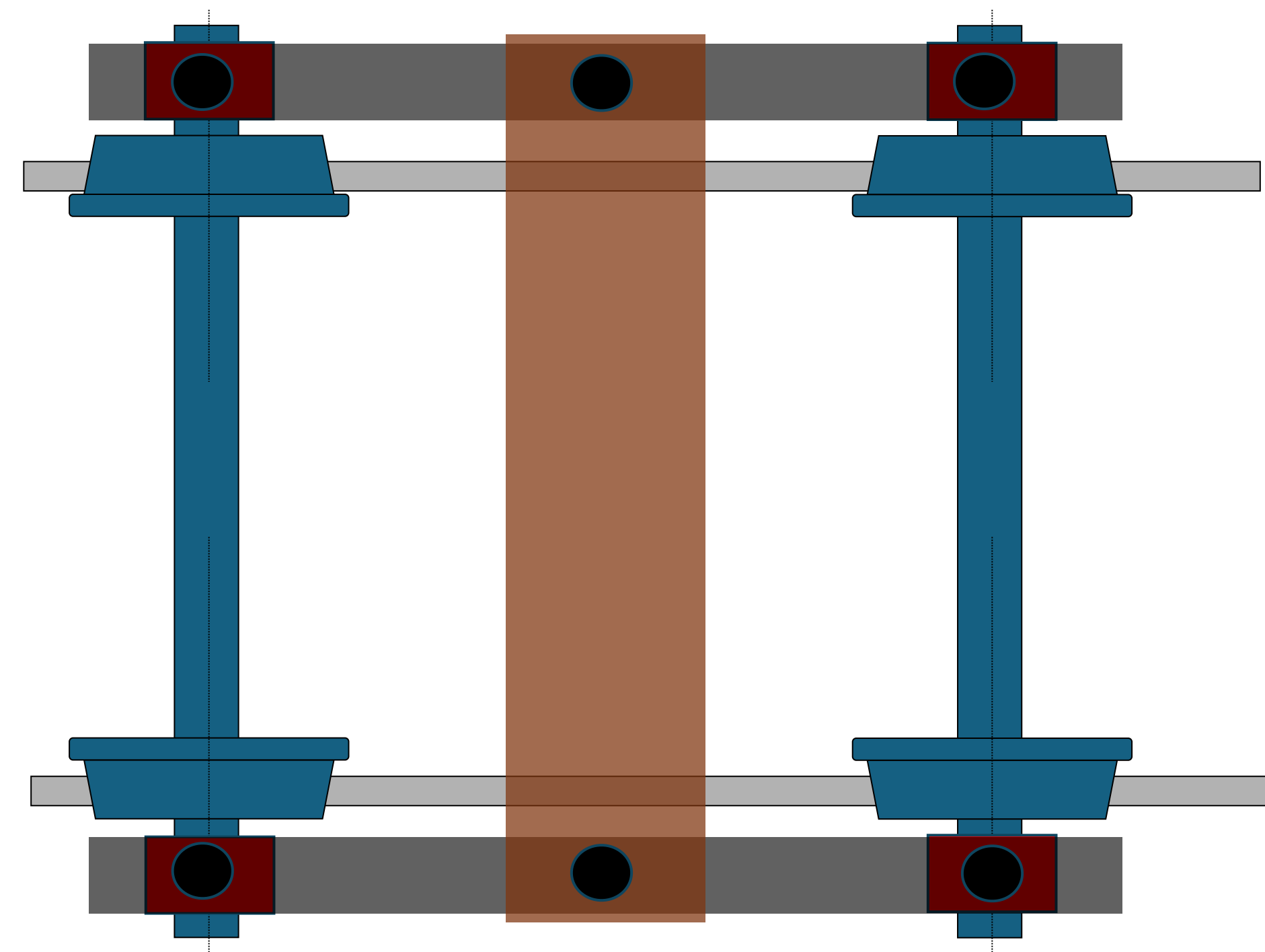
- British Rail derivation

$$\lambda_e = \frac{1}{2} \int \frac{N(y)(r_R - r_L)}{y} dy$$





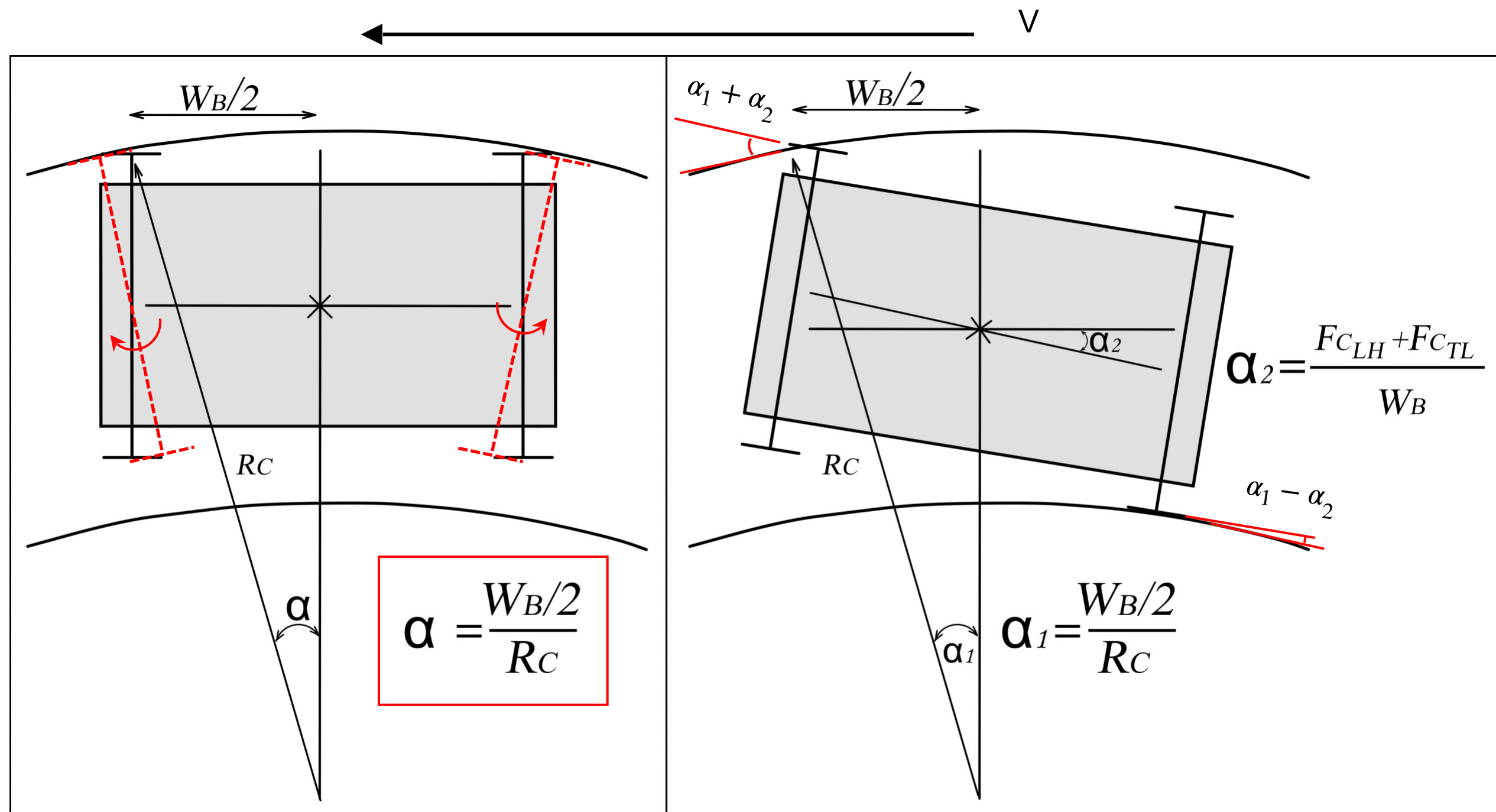
A Truck Can Provide Stability



- Bearing**
- Side frame**
- Bolster**
- Damping and stiffness**

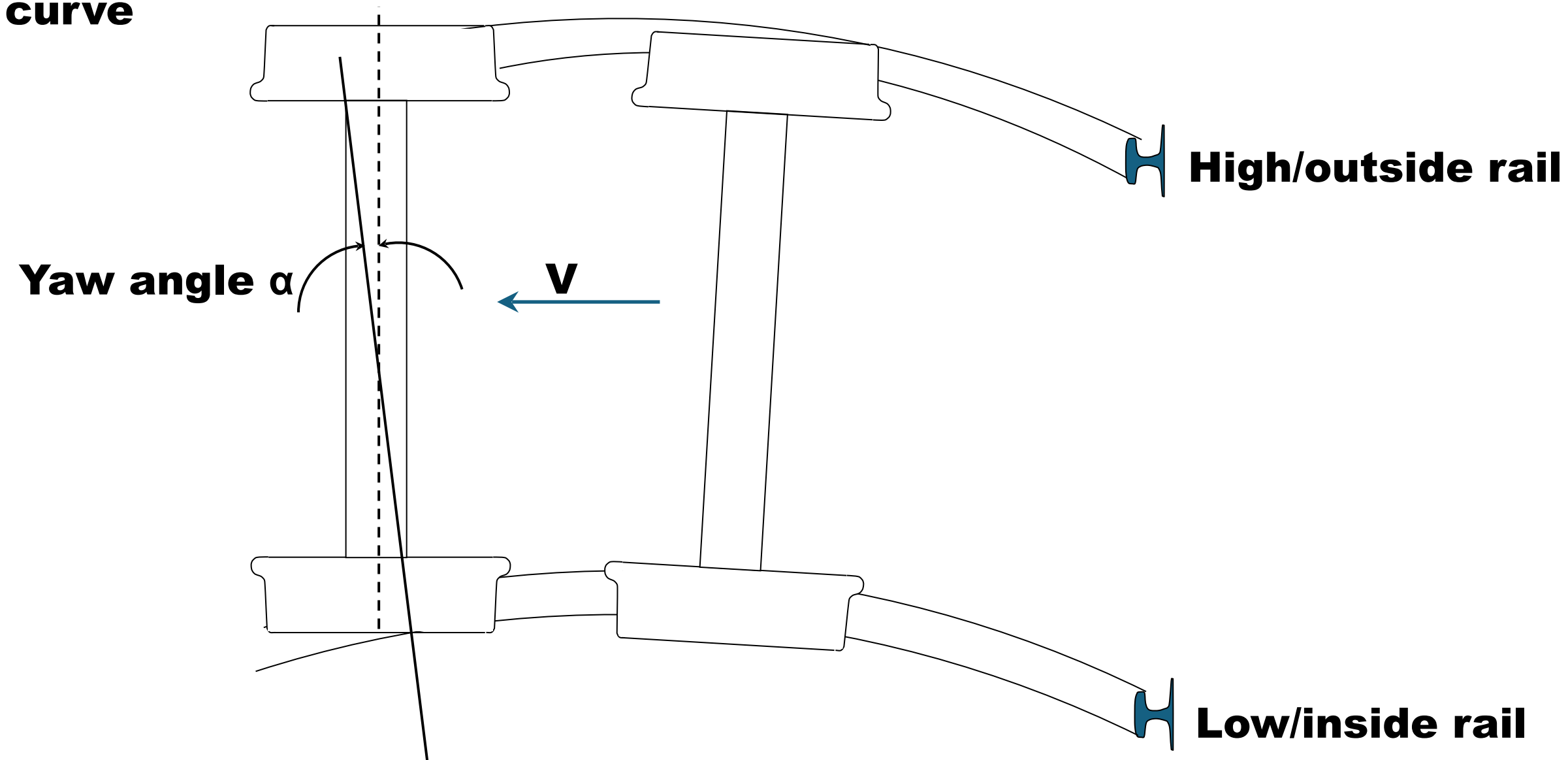


The Yaw Angle

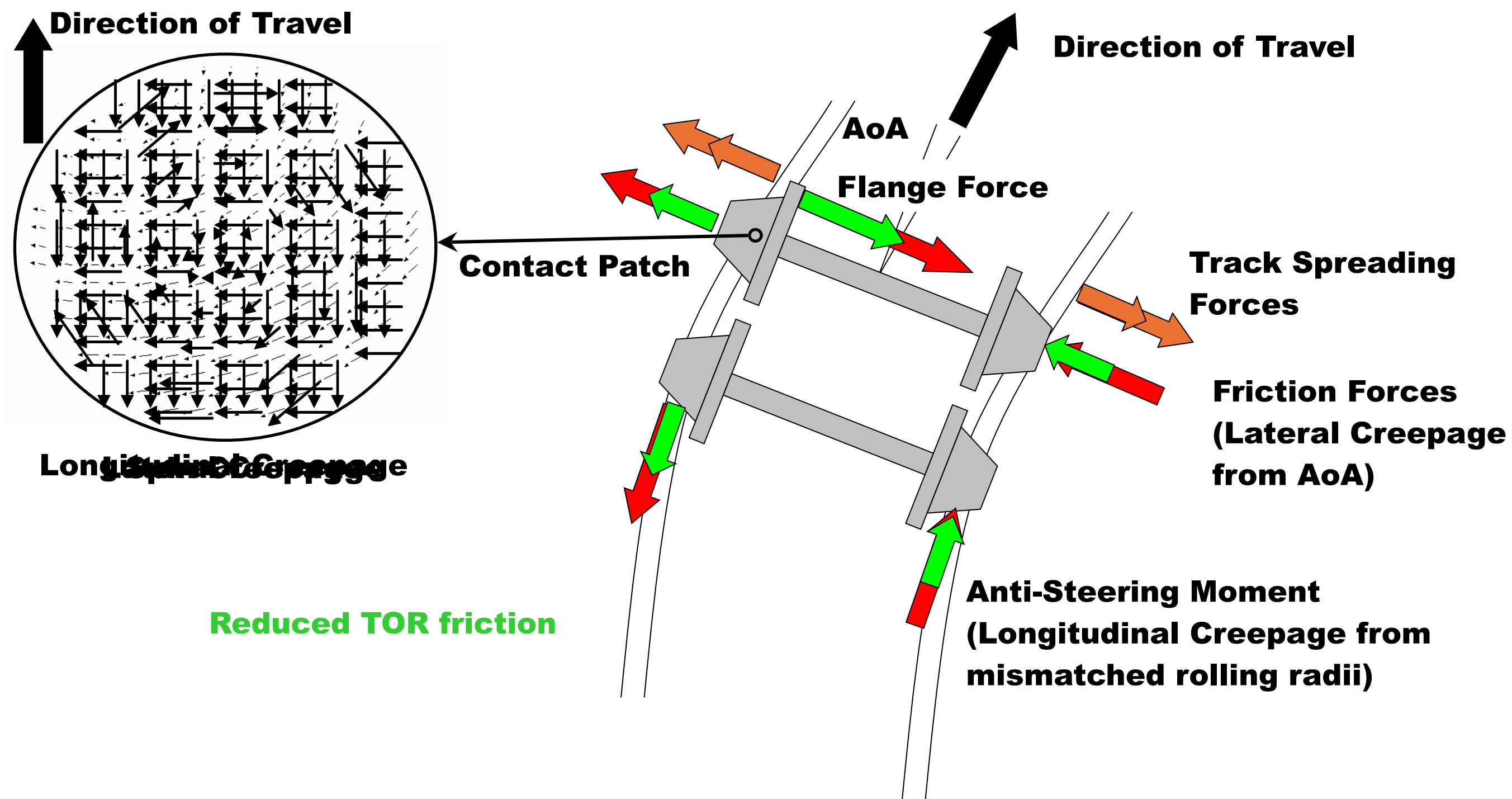


The Wheelset in a Curve

**(Leading) wheelset shifts
to outside of curve**



Lateral Forces (Creep) in Curves





WHEEL-RAIL PROFILE DESIGN AND PERFORMANCE



Design of Engineered Rail Profiles

Rail design considers:

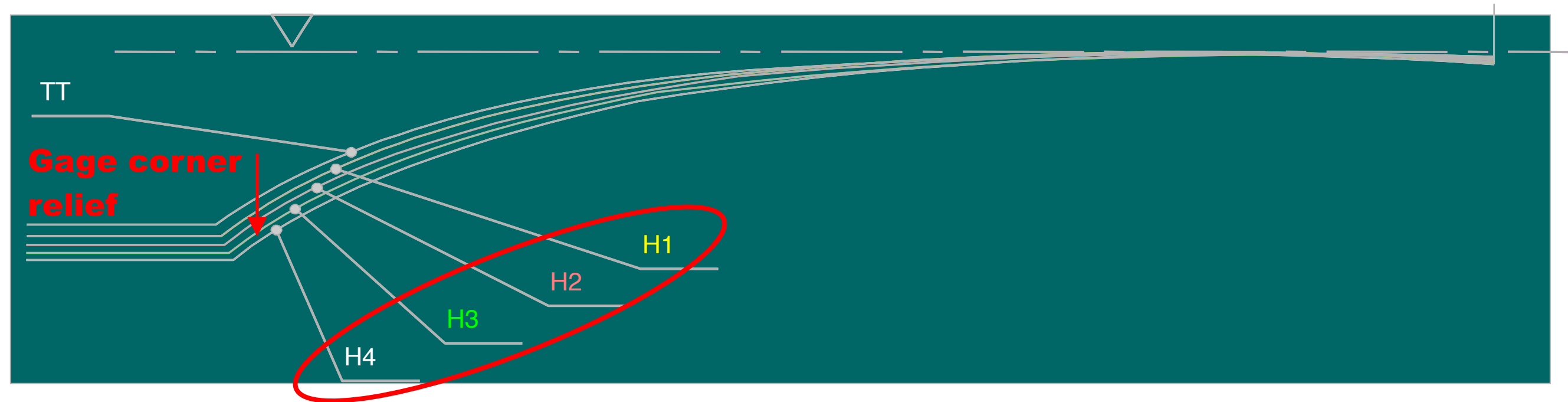
- Track curvature
- Worn wheel shapes
- Types of vehicle and speed (hunting)
- Dynamic rail rotation
- Rail hardness
- Grinding interval (profile deterioration between intervals)
- Static gage

Goals

- Control contact stress
- Inhibit hunting
- Minimize wear



The NRC Family of Heavy Haul Rail Templates from the 1990s





Rail Profile Design Criteria

Goals are to reduce/control:

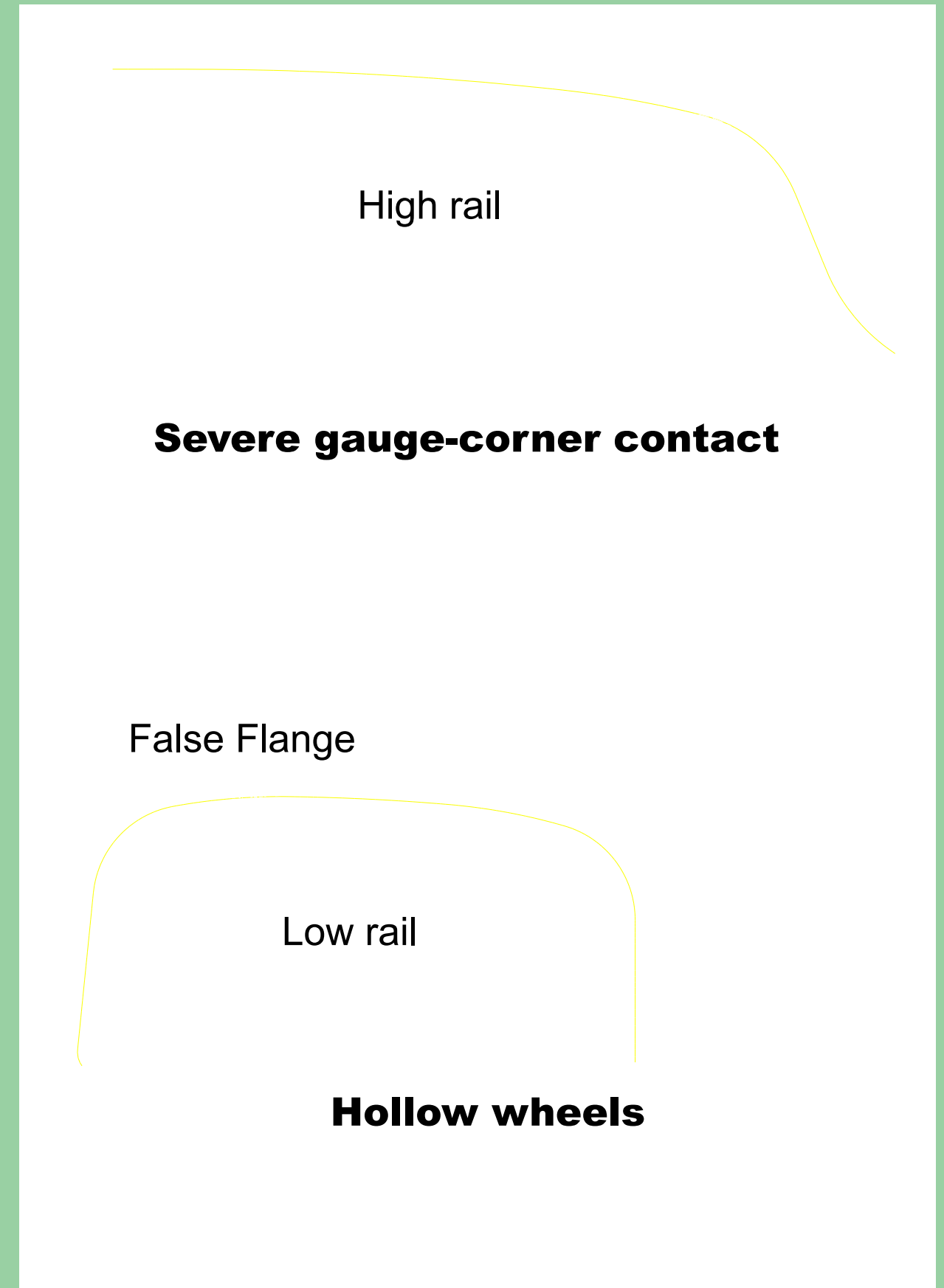
- Gauge face and TOR wear
- Rolling contact fatigue (RCF)
- Dynamic instability (hunting)
- Corrugation formation
- Wheel hollowing
- Easily or practically implemented by grinding



Wheel-Rail Contact Stresses

Stress and damage depend on:

- Wheel radius
- Wheel load
- Friction coefficient
- Wheel/rail profiles (contact geometry)





Wheel-Rail Conformality

- Closely conformal
0.1 mm (0.004") or less
- Conformal
0.1 mm to 0.4mm
(0.004" to 0.016")
- Non-conformal
0.4 mm (0.016") or larger



Some Typical Issues Associated with Wheel-Rail Conformality

Closely conformal profiles

- Dynamic instability (hunting)
- Corrugation formation by spin creepage

Conformal profiles

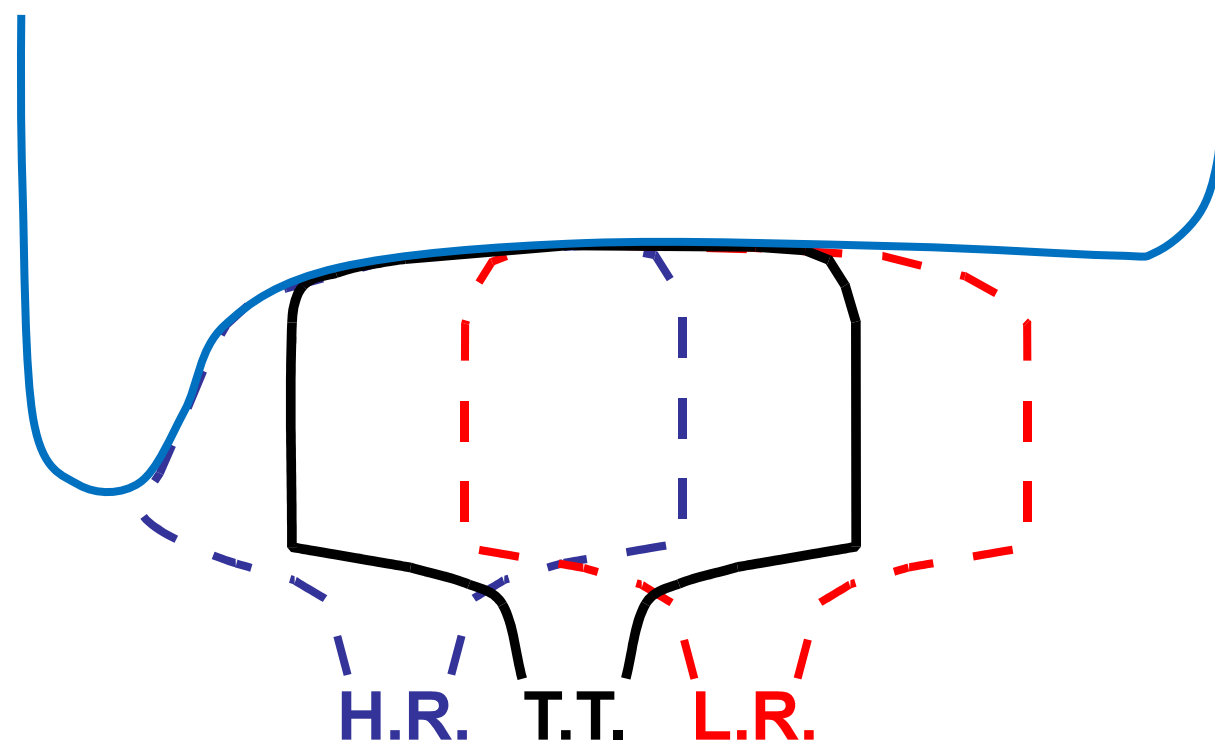
- Low stress state W/R interface
- Heavy haul = 2PT conformal (balance contact stress steering and wear)

Non-conformal profiles

- High stress state W/R interface
- 1PT: cracks (RCF) at GC of HR and FS of LR
- 2PT: high gauge face wear in curves

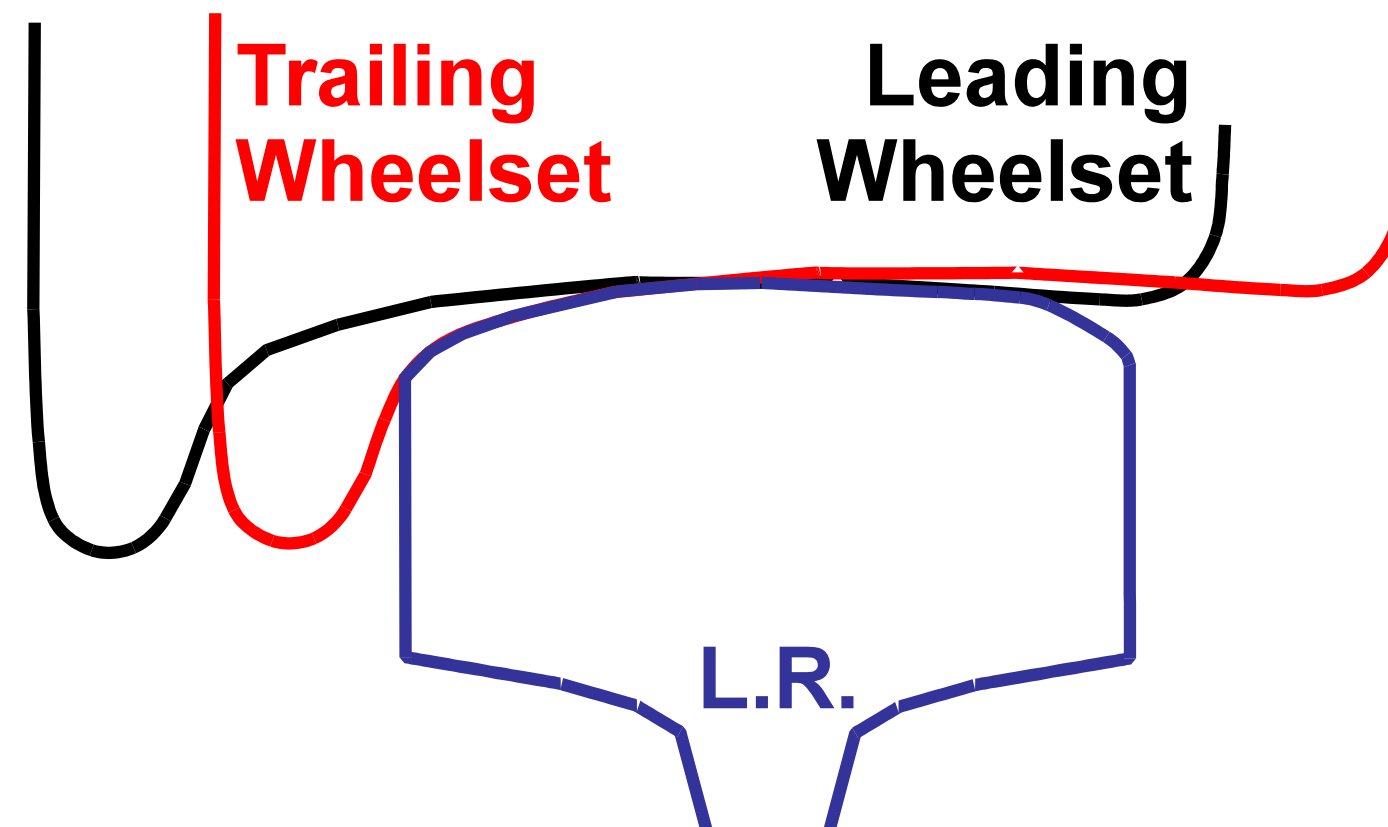


Worn Wheel and Rail Profiles are Envelopes of Each Other



Worn wheel is an envelope of all rail profiles it encounters on a particular route

Worn rail is an envelope of all wheel profiles that pass over it





Pummelling Analysis

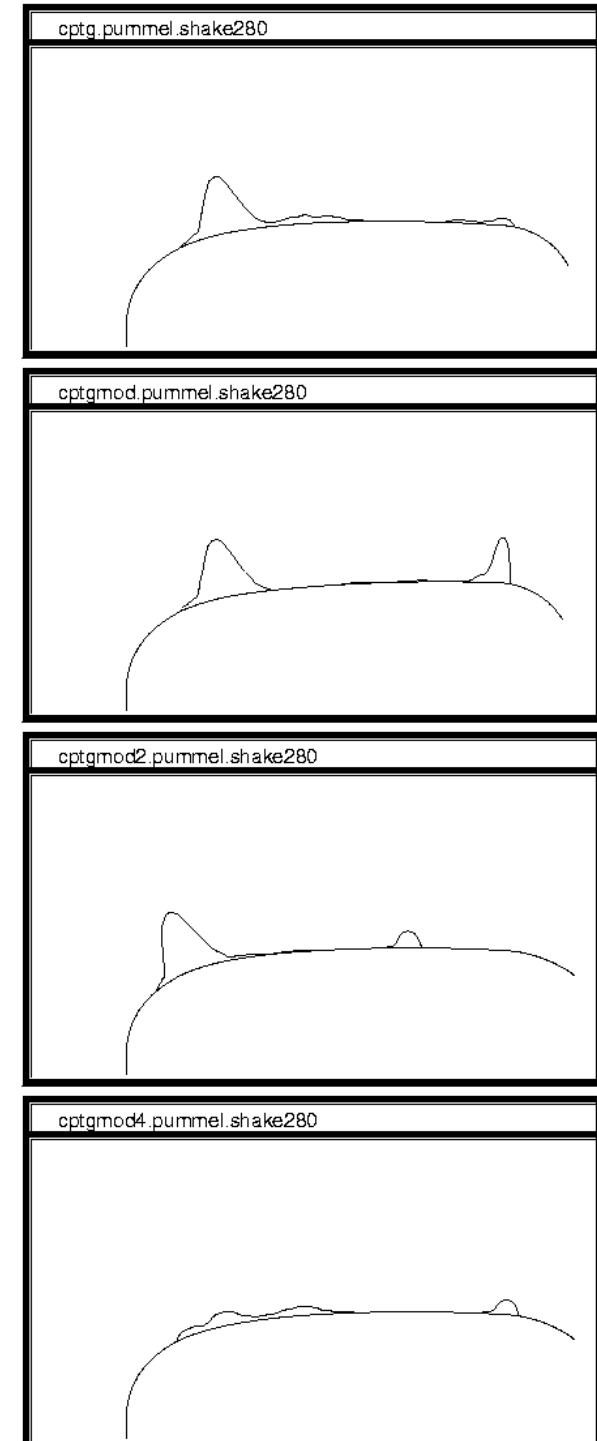
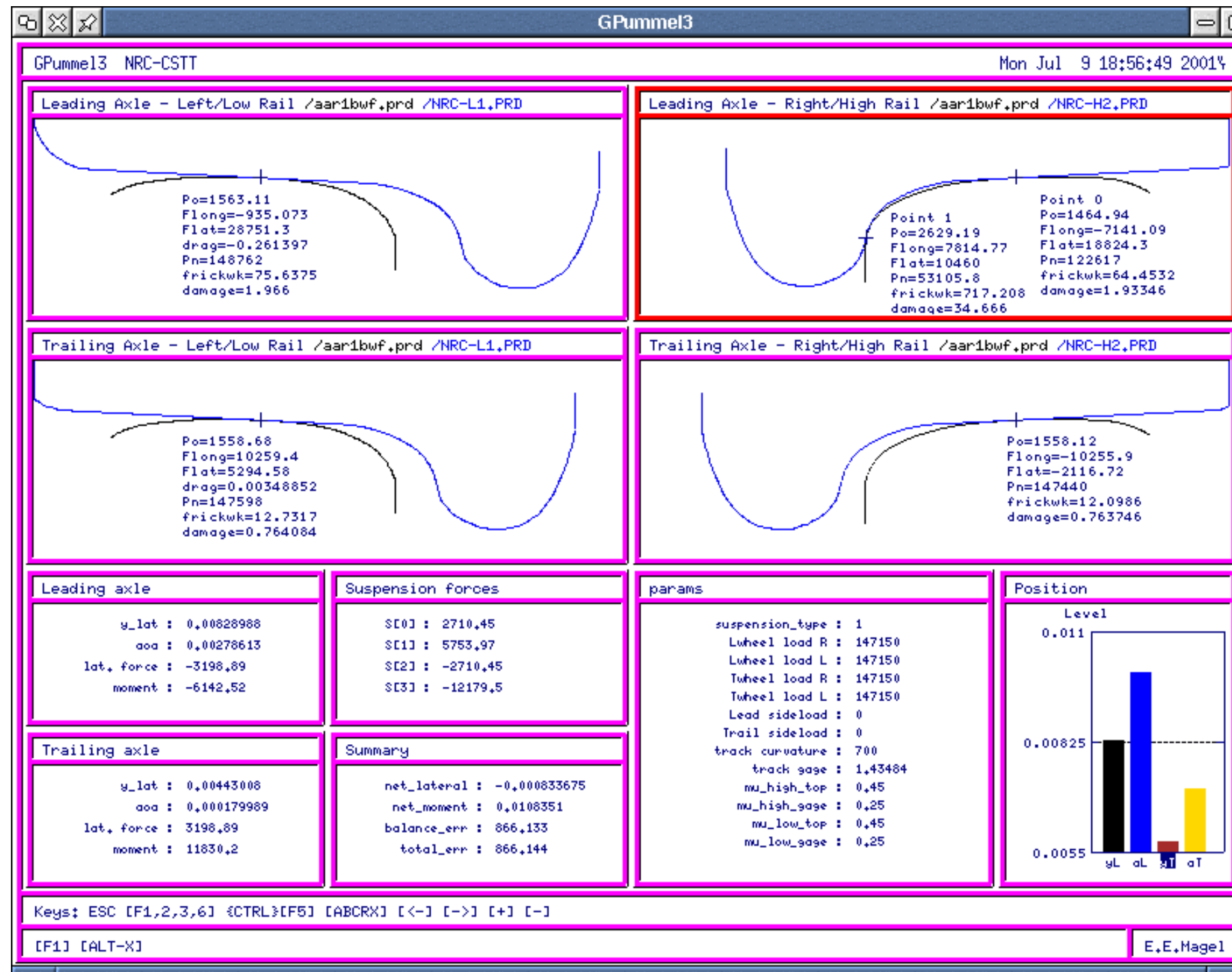
Simulation

- Measured wheel profiles
- Vehicle characteristics (stiffness, wheelbase etc.)
- Rail hardness (for damage evaluation)
- Rail curvature, super-elevation, dynamic rail rotation etc.

Evaluate distributions of

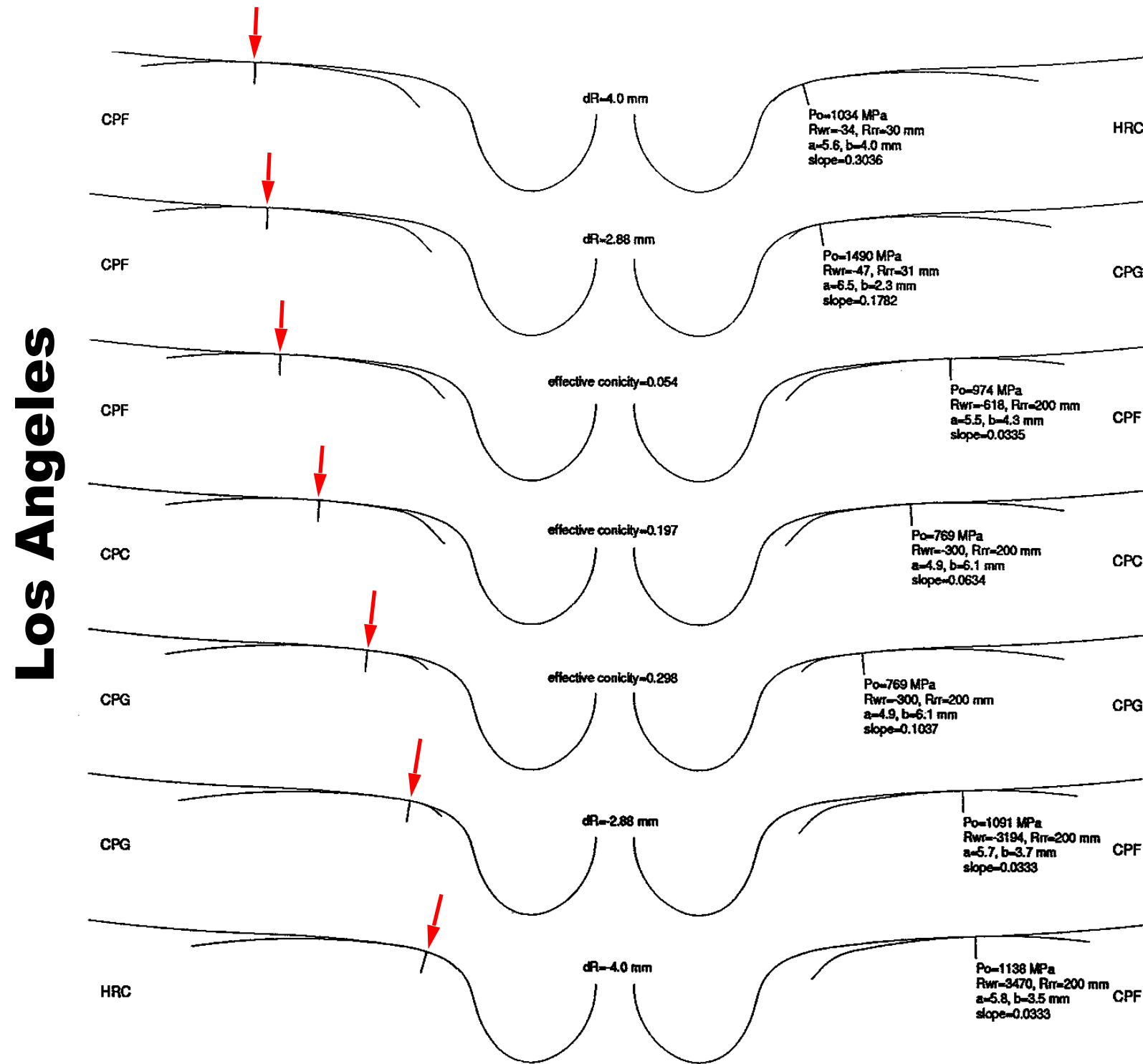
- Contact stress
- Steering moments
- Effective conicity

Pummelling: Design/Analysis Tool



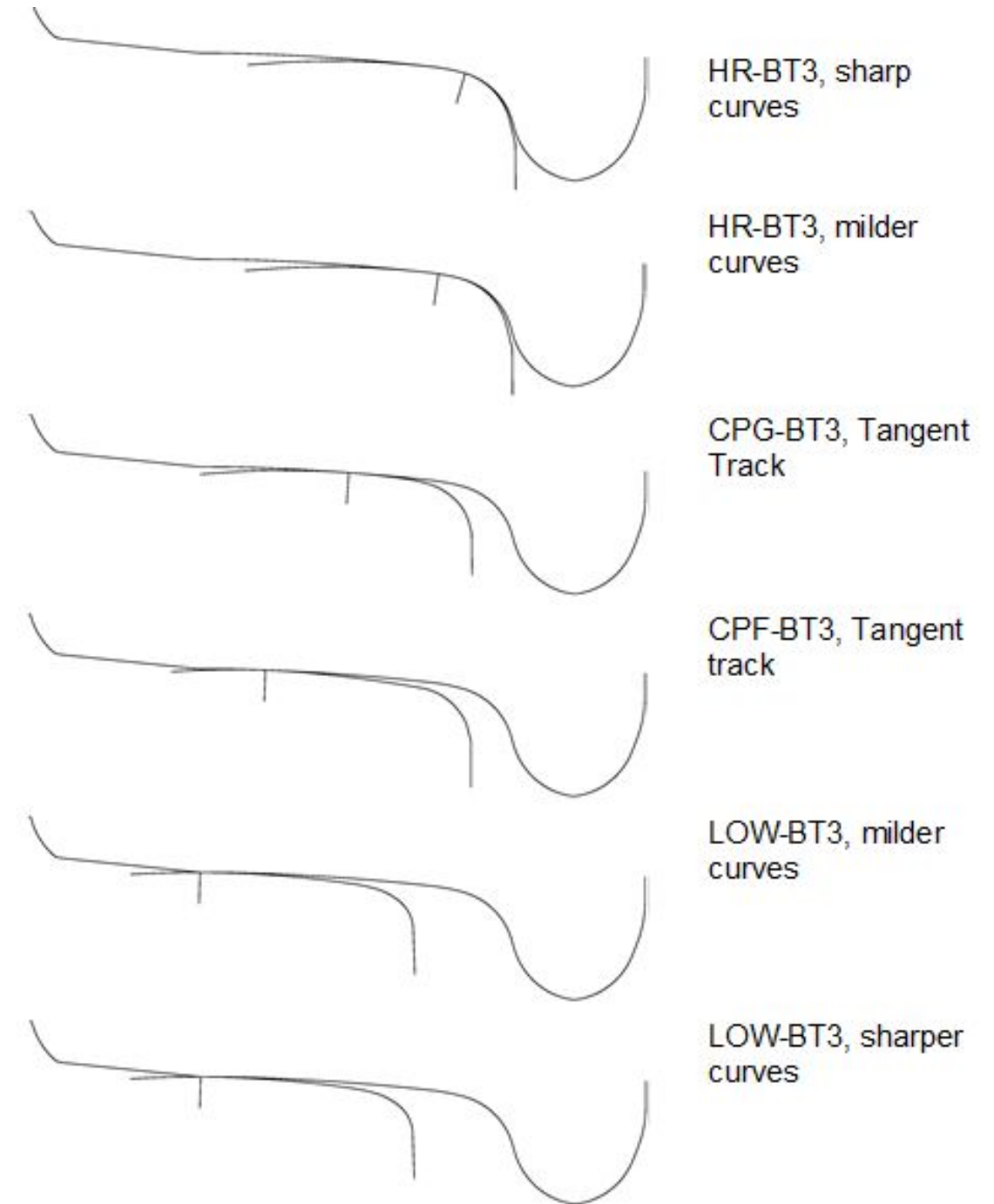


Families of Rail Profiles



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San Francisco





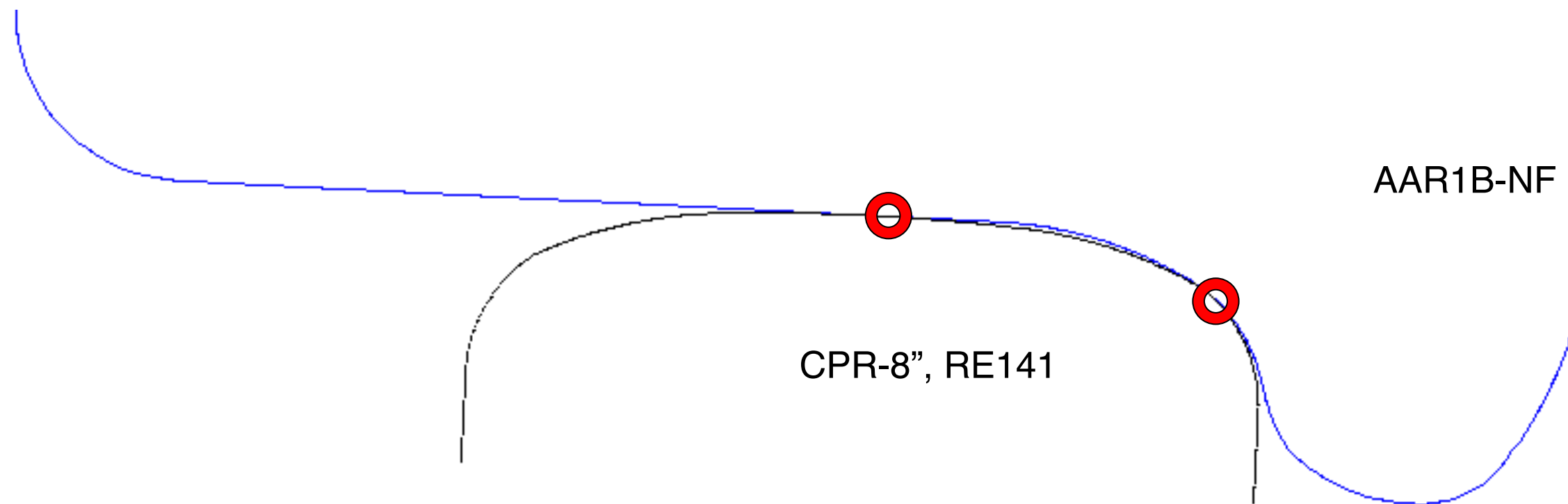
VEHICLE-TRACK DERAILMENT MECHANISMS AND RISK ASSESSMENT

WHEEL CLIMB



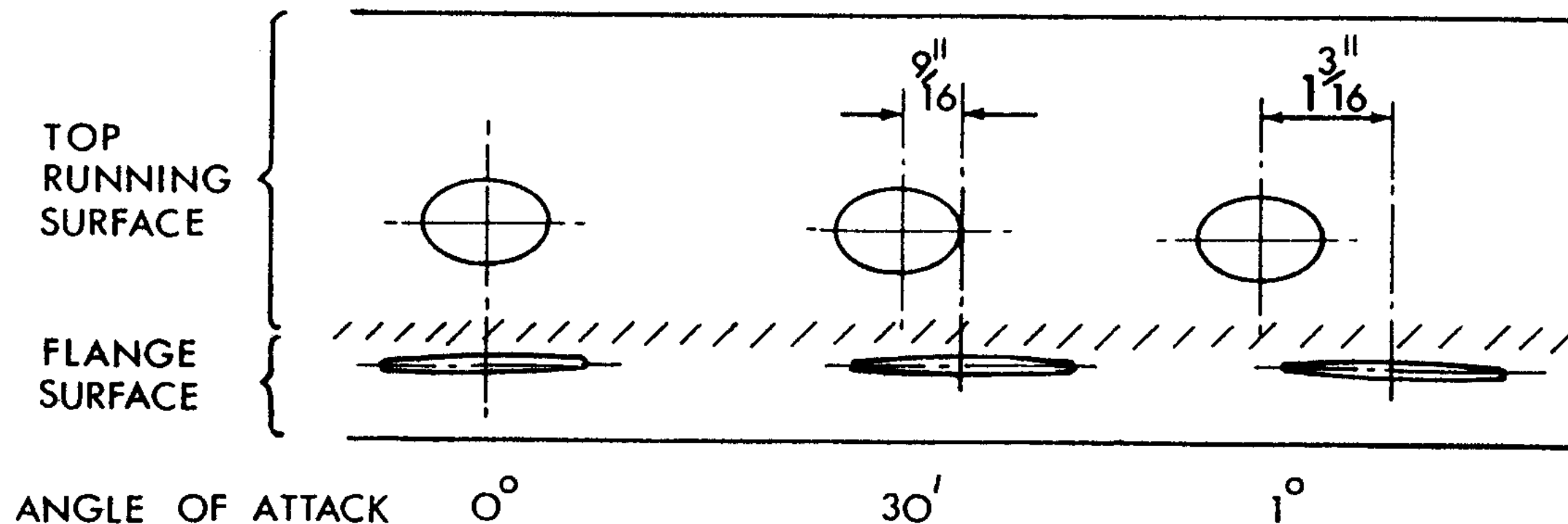
Wheel-Rail Contact

W/R contact often takes place at two points simultaneously (some new wheels especially)

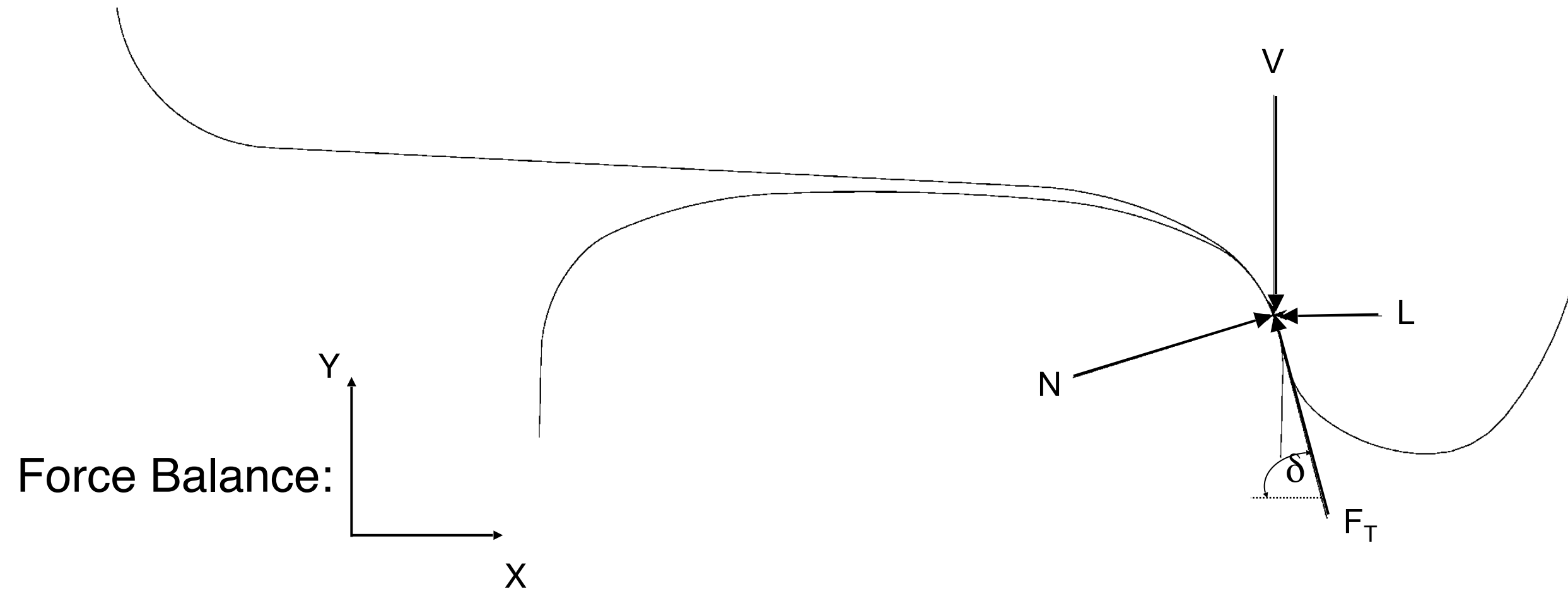


Wheel-Rail Contact (continued)

Plan view of contact ellipses on high rail for different angles of attack



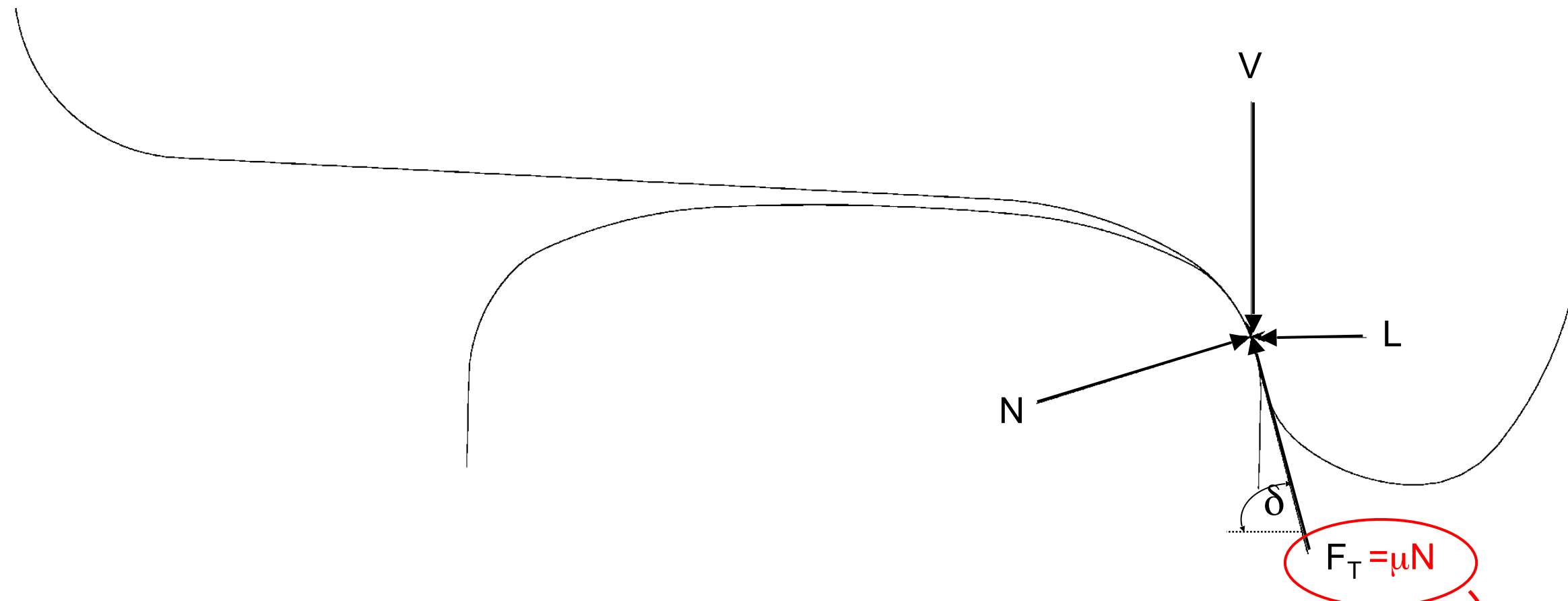
Deriving Nadal



$$\left. \begin{aligned} \sum F_x = 0 &\Rightarrow N \sin(\delta) - F_T \cos(\delta) - L = 0 \\ \sum F_y = 0 &\Rightarrow F_T \sin(\delta) + N \cos(\delta) - V = 0 \end{aligned} \right\} \frac{L}{V} = \frac{\tan \delta - F_T / N}{1 + F_T \tan \delta / N}$$



Nadal's Relationship

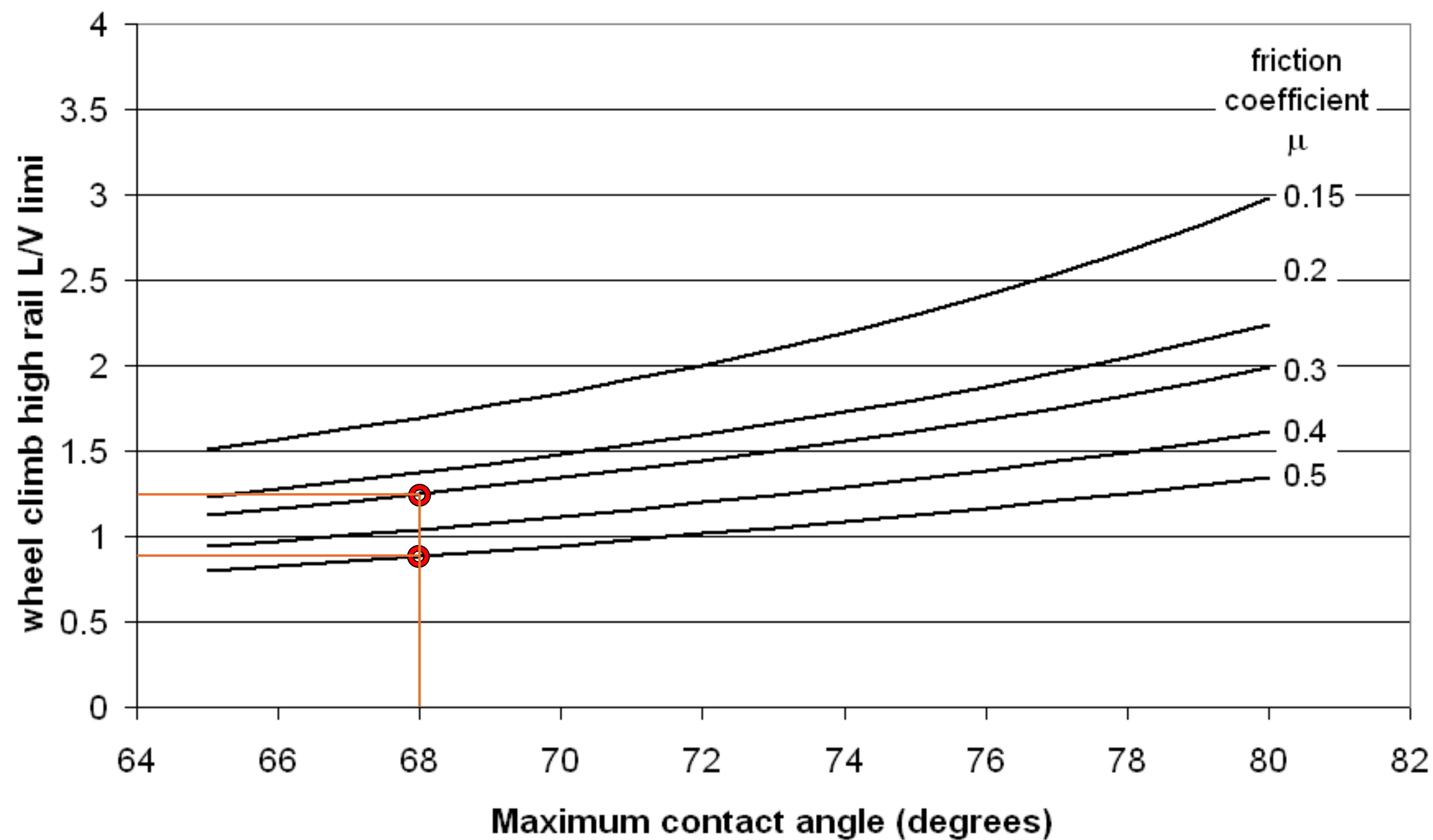


$$\frac{L}{V} = \frac{\tan \delta - \mu}{1 + \mu \tan \delta}$$

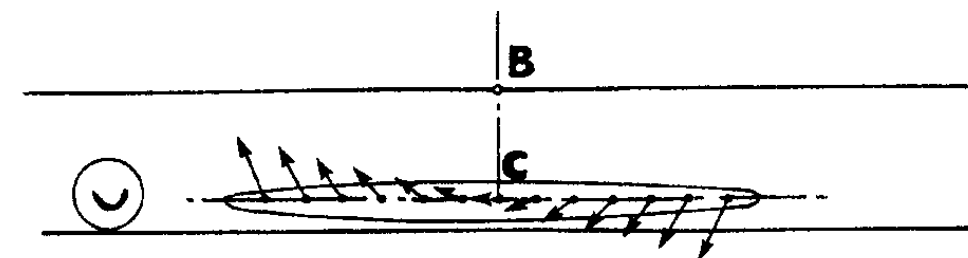
$$\frac{L}{V} = \frac{\tan \delta - F_T / N}{1 + F_T \tan \delta / N}$$



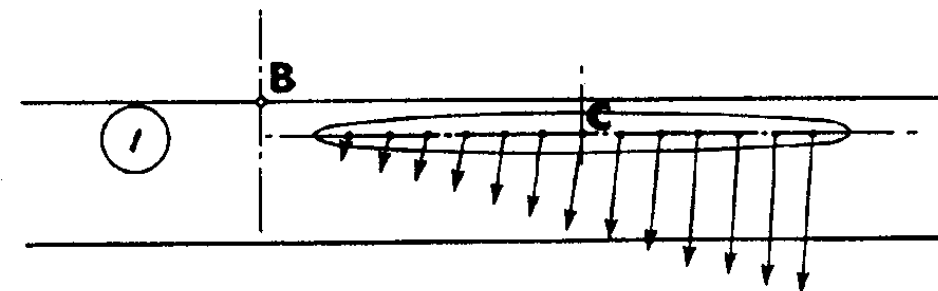
Nadal Index (1908)



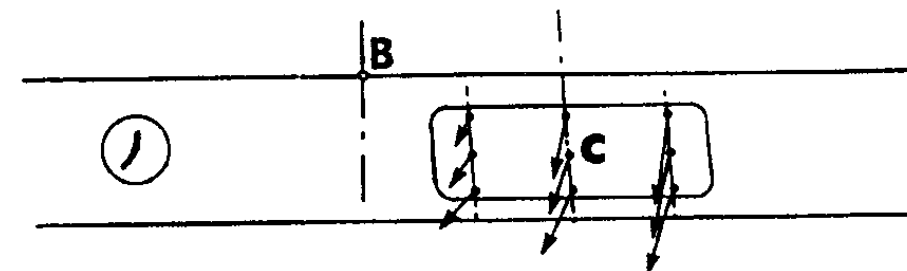
Slip Vectors at the Gage Face Contact



(a) $\alpha > \beta$, $\psi = \text{zero}$



(b) $\alpha < \beta$, large ψ

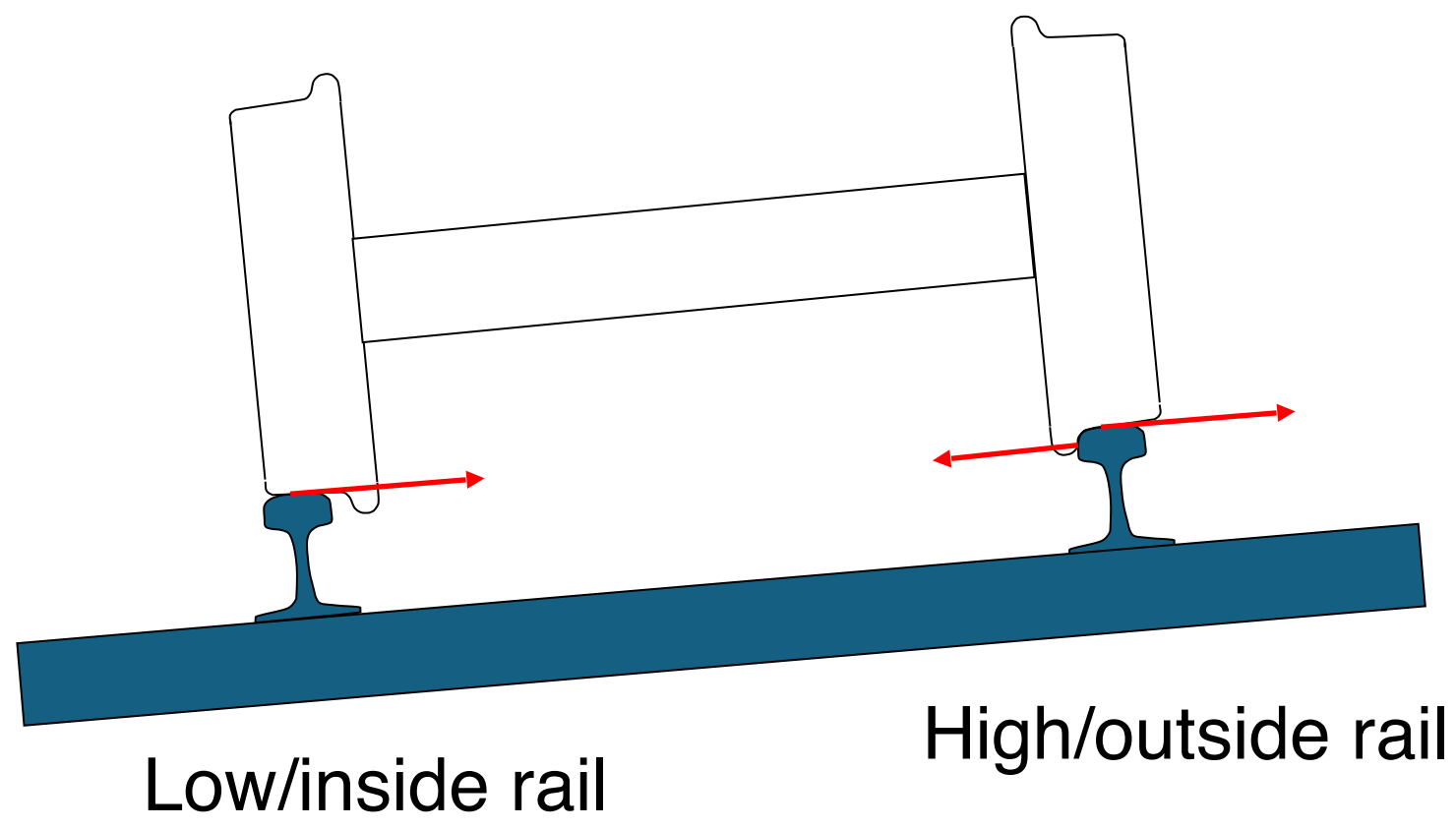


(c) $\alpha = \beta$, moderate ψ

α = angle of attack

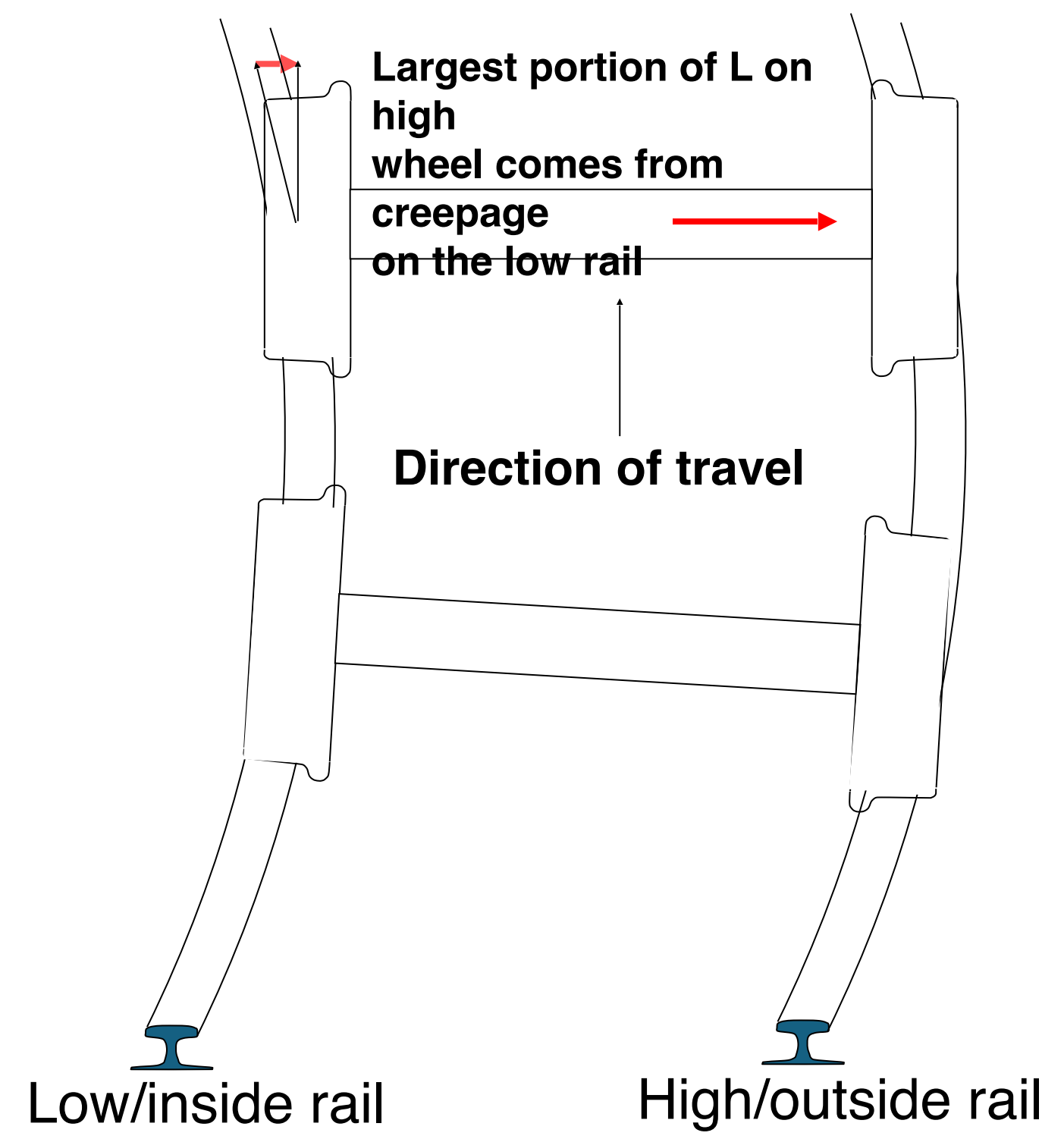
δ = wheel flange angle

β = gage face angle

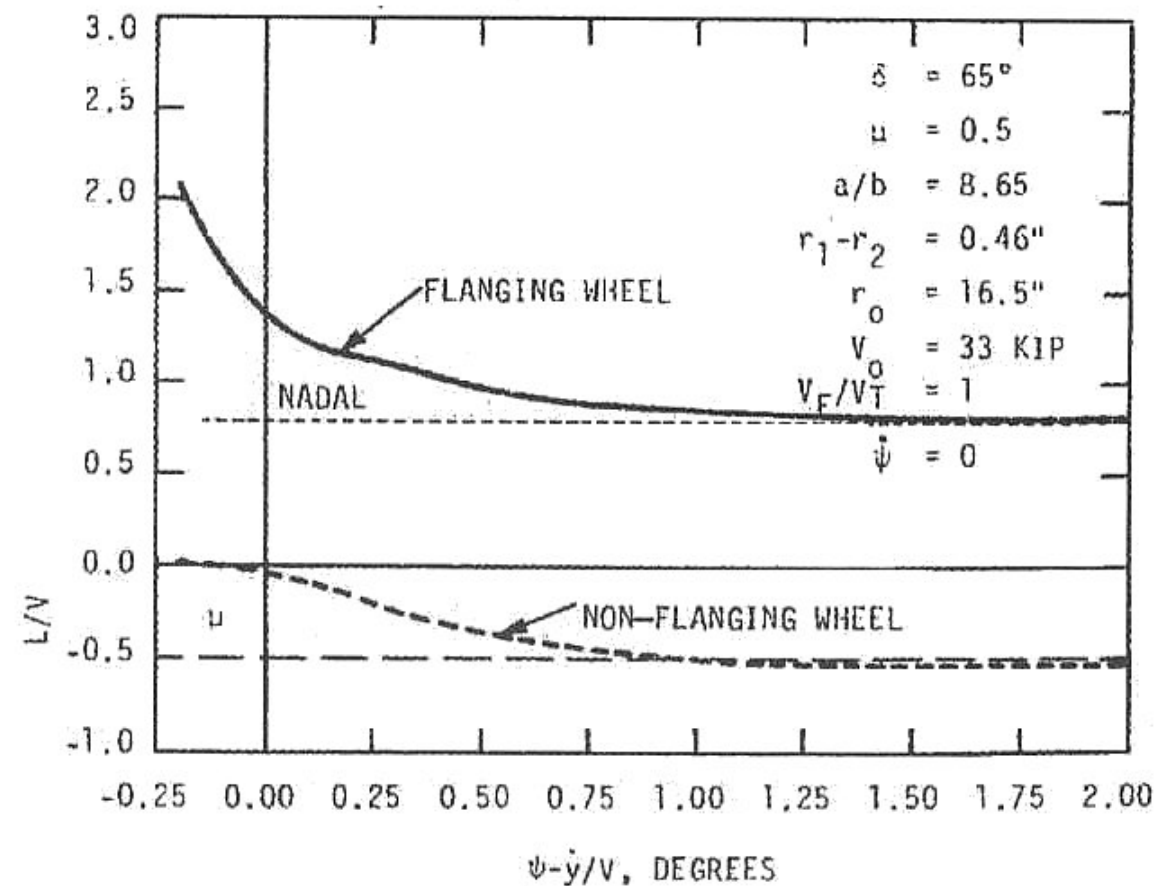


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Lateral wheel/rail forces



Weinstock Derailment Criterion



$$|L/V|_{\text{flanging}} + |L/V|_{\text{non_flanging}} > (L/V_{\text{NADAL}} + m)$$

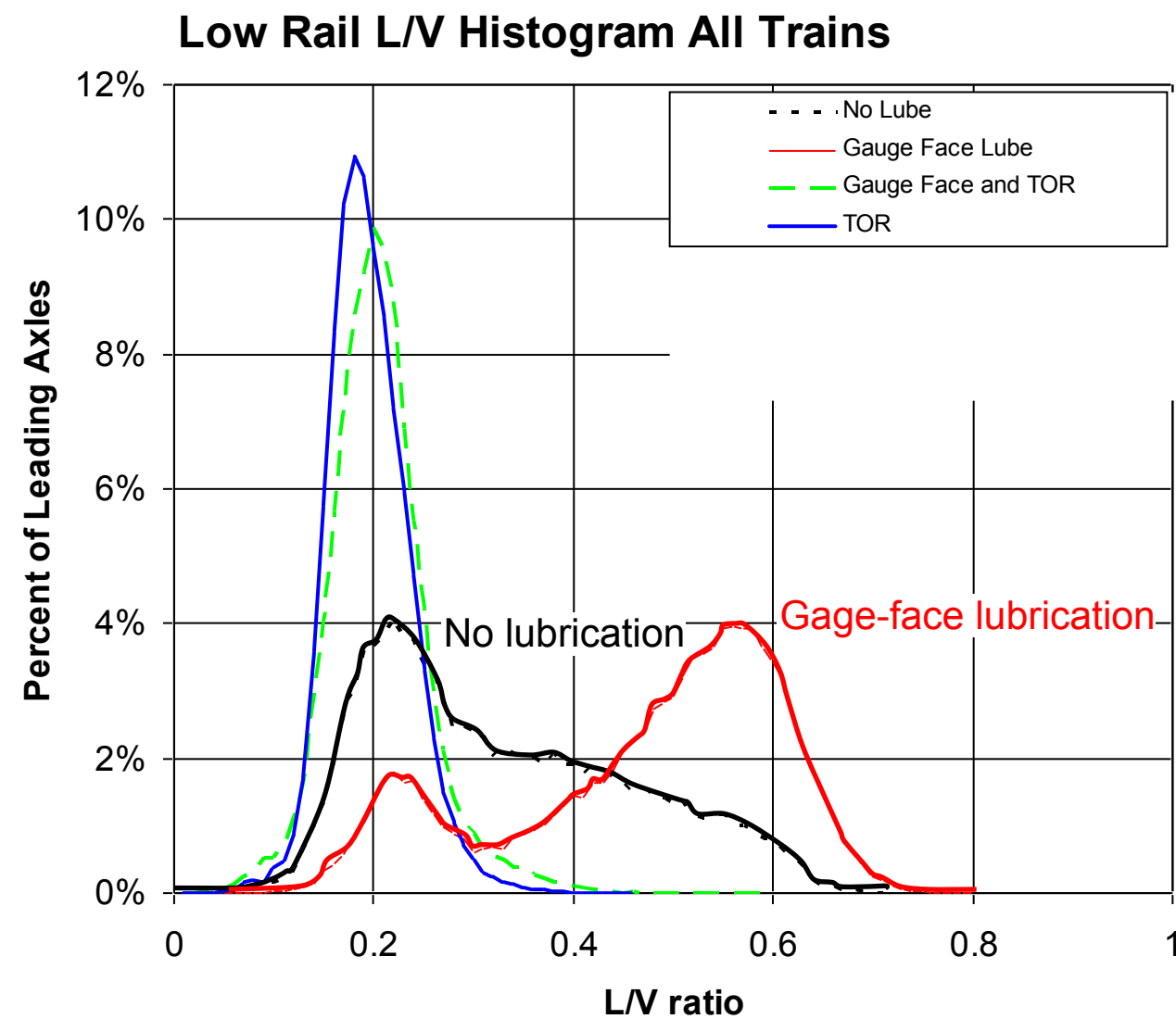
- Holds for all positive angles of attack,
- Less accurate for +ve cant deficiency

- At incipient wheel climb, the L/V values on the flanging and non-flanging wheels are, for positive angles of attack, separated by a roughly constant value equal to the Nadal limit plus the coefficient of friction on the top of the low rail



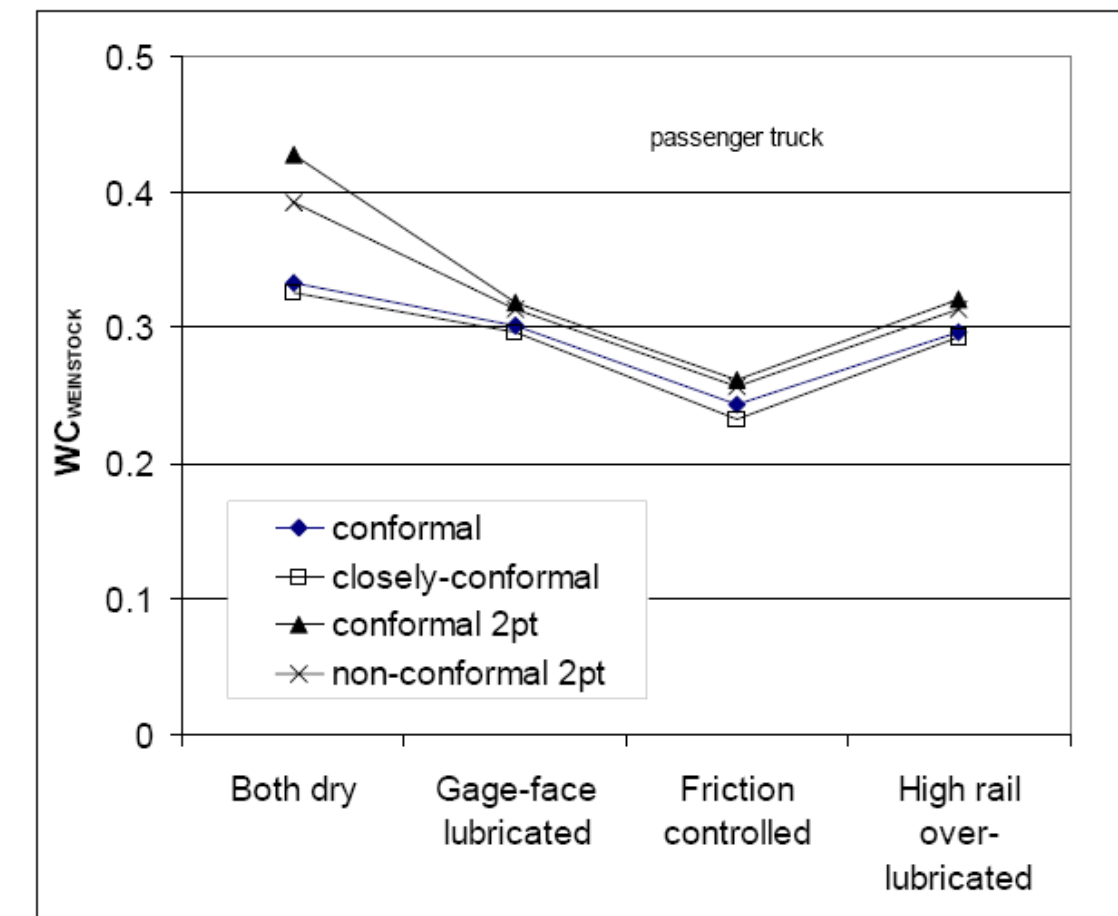
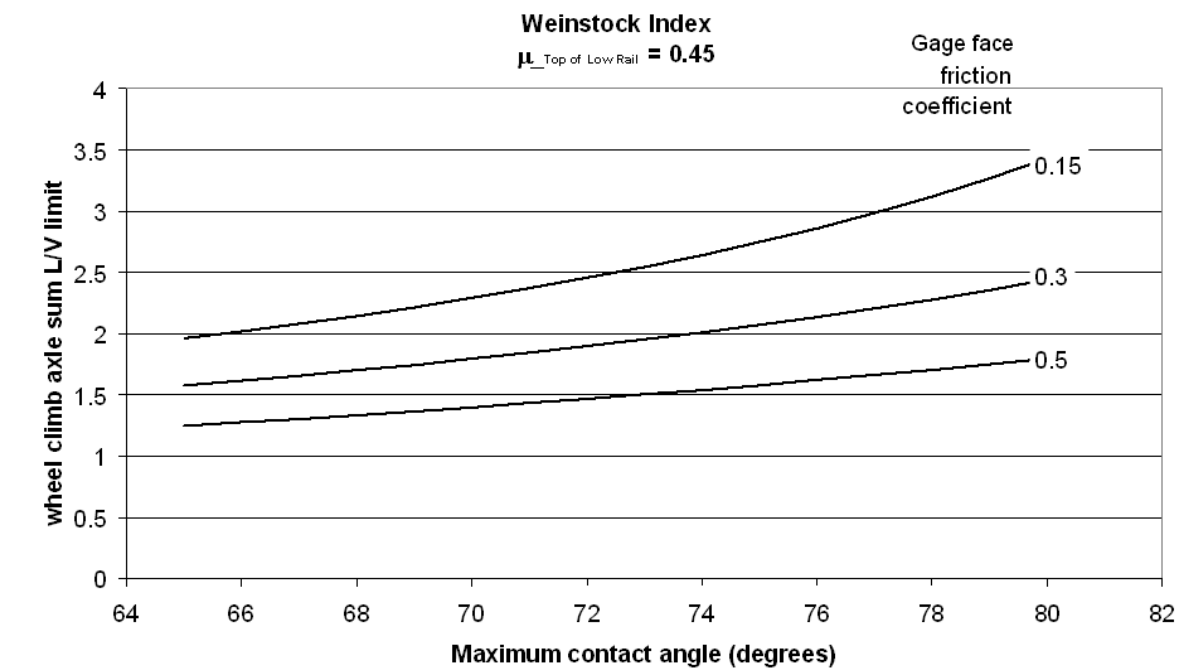
An Example

- Is lubrication a good thing?



L/V goes up, but Weinstock limit also.

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Wheel Climb - Conclusions

- Nadal – provides a relationship between contact angle and friction coefficient
- Is based upon simplified view of the slip conditions
- Wheel climb threshold matches Nadal at most practical angles of attack, but not for low angles of attack.
- Weinstock rectifies that (for positive angles of attack) and includes explicitly the effect of friction on top of low rail.
- A safe L/V is some fraction of the (Nadal or Weinstock) threshold value, say 60-80%.
- These are static and quasi-static derivations.

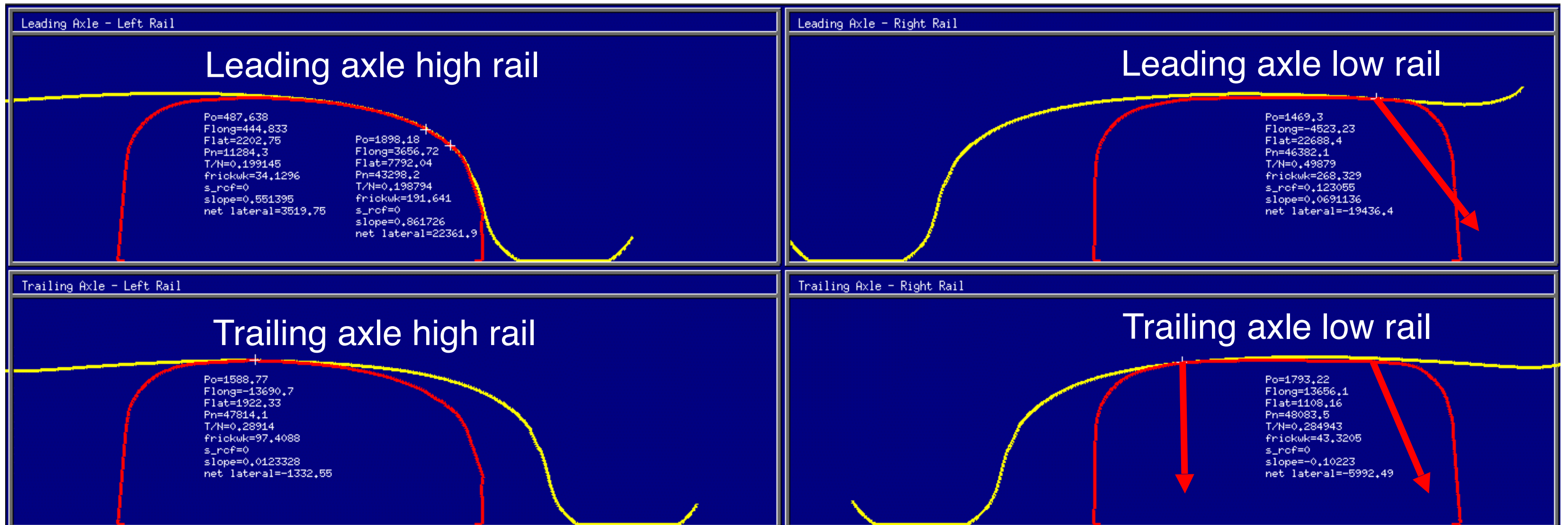


VEHICLE-TRACK DERAILMENT MECHANISMS AND RISK ASSESSMENT

RAIL ROLLOVER

Low Rail Rollover

- Wide gauge, hollow wheels, poor restraint, underbalanced running, high friction





Conclusions

Matching of wheel/rail profiles

- Rolling radius difference: stability and curving
- Strong impact on stress, curving forces, stability, surface damage, safety/derailment (with friction conditions, truck suspensions, track geometry etc.)
- Must consider both new and worn shapes (pummelling)

Nadal formula is adequate for most wheel climb analyses

- Wheel climb risks grow with a sustained increase in lateral force or decrease in vertical force.