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JUNE 10-12,  
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**WRI2025HH**



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L / V ratios - what

do they mean?

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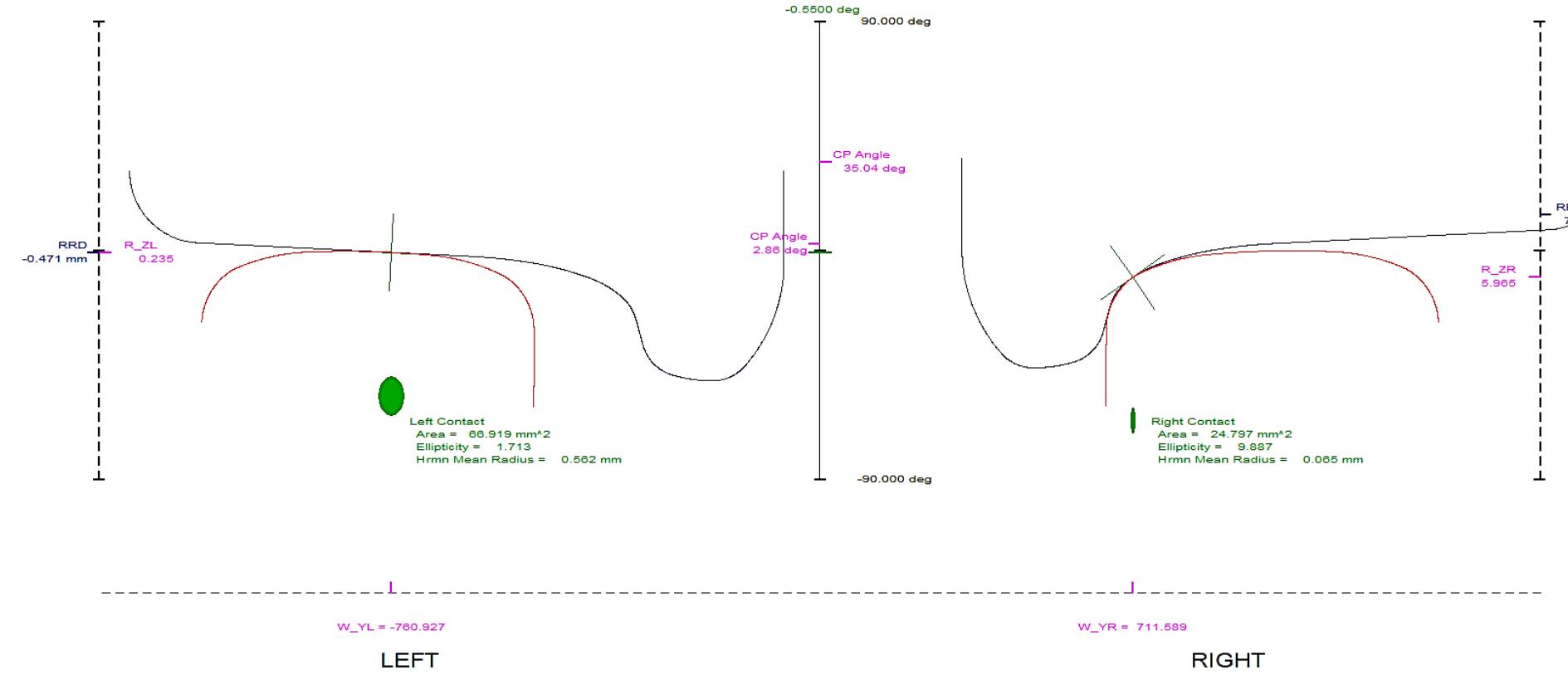
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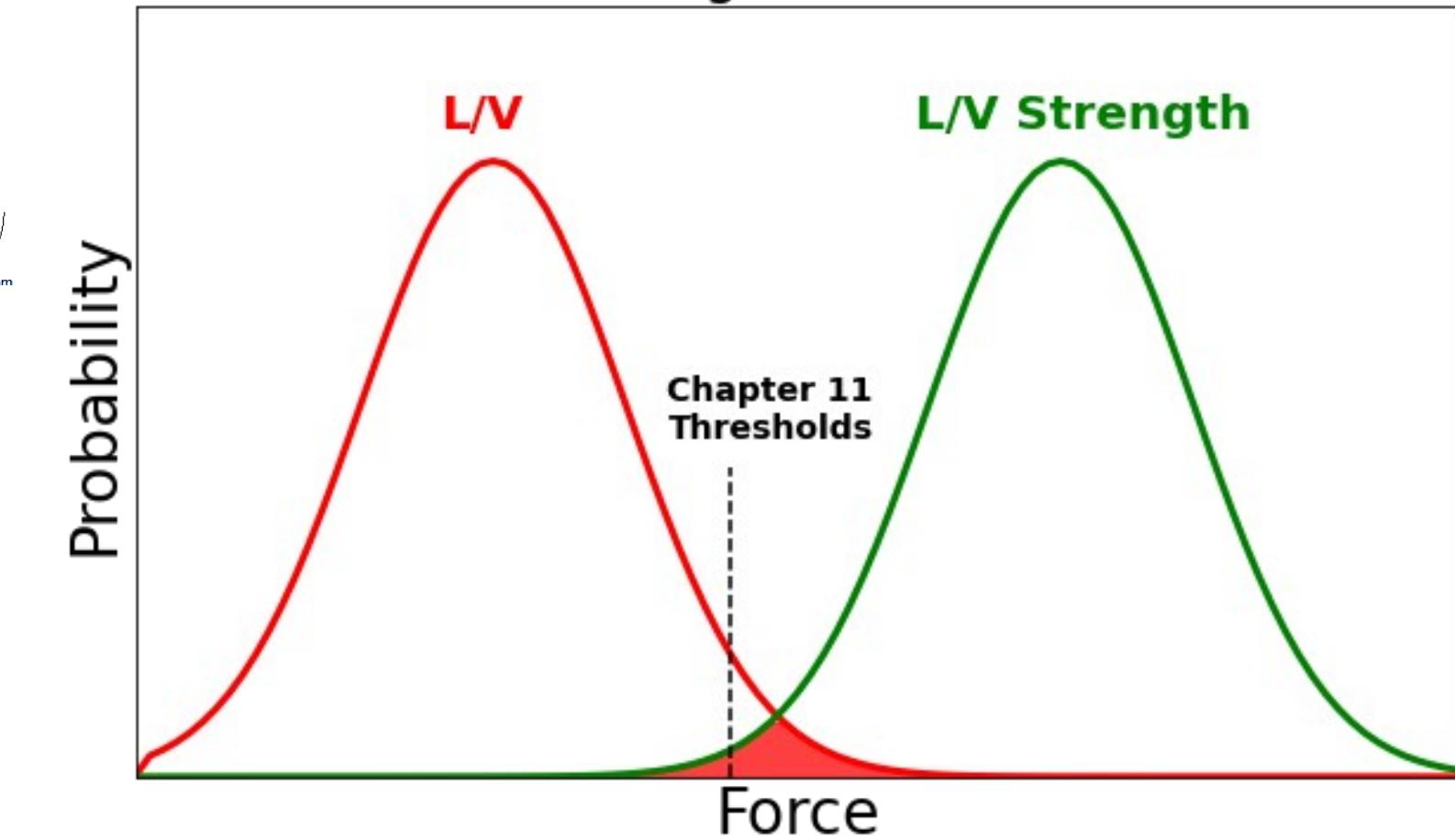
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# Motivation and goal



Force v. Strength Risk Distribution



- L/V, aka Y/Q, derailment quotient, etc. – seemingly omnipresent
- Fundamental to wheel/rail interaction and railway safety
- Risk depends on both vehicle track interaction and track strength
- Often talked about in the vehicle track interaction community – are we speaking the same language and considering vehicle and track as a system?



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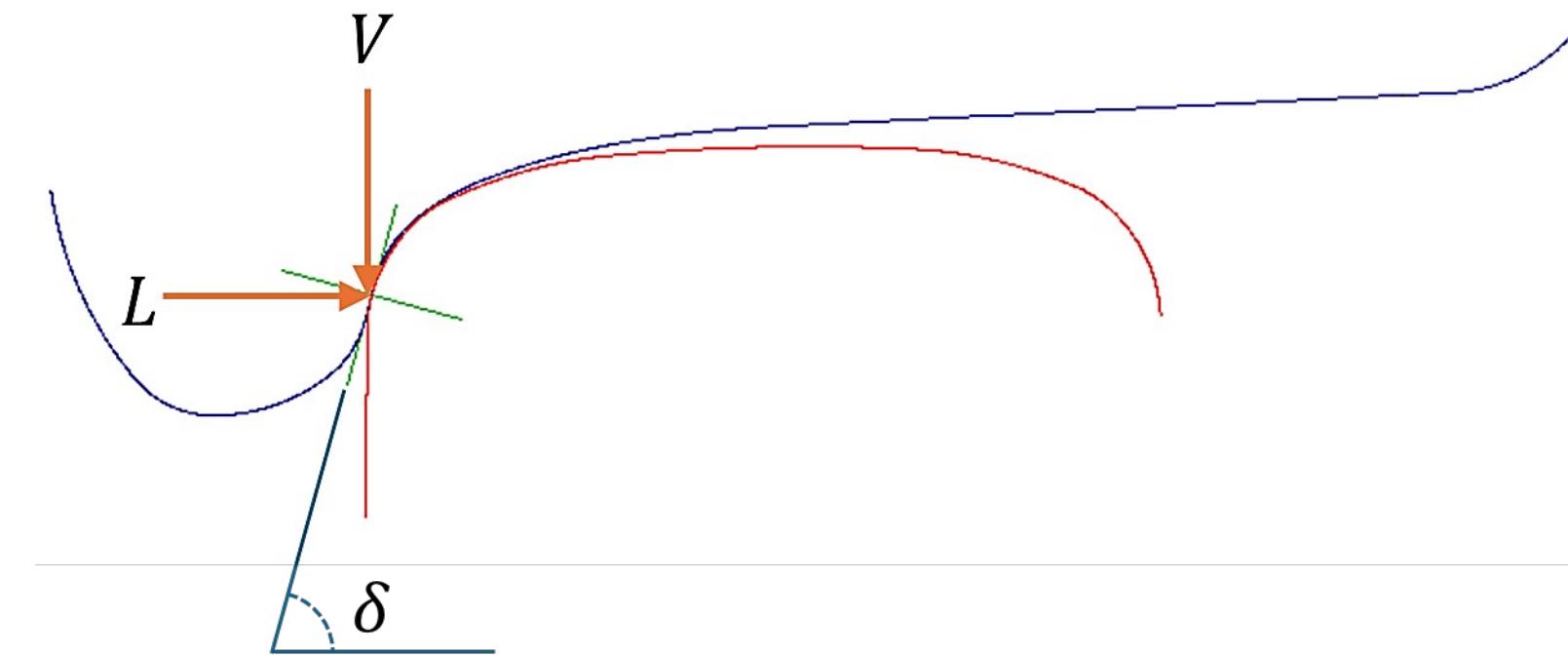
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# The classic case

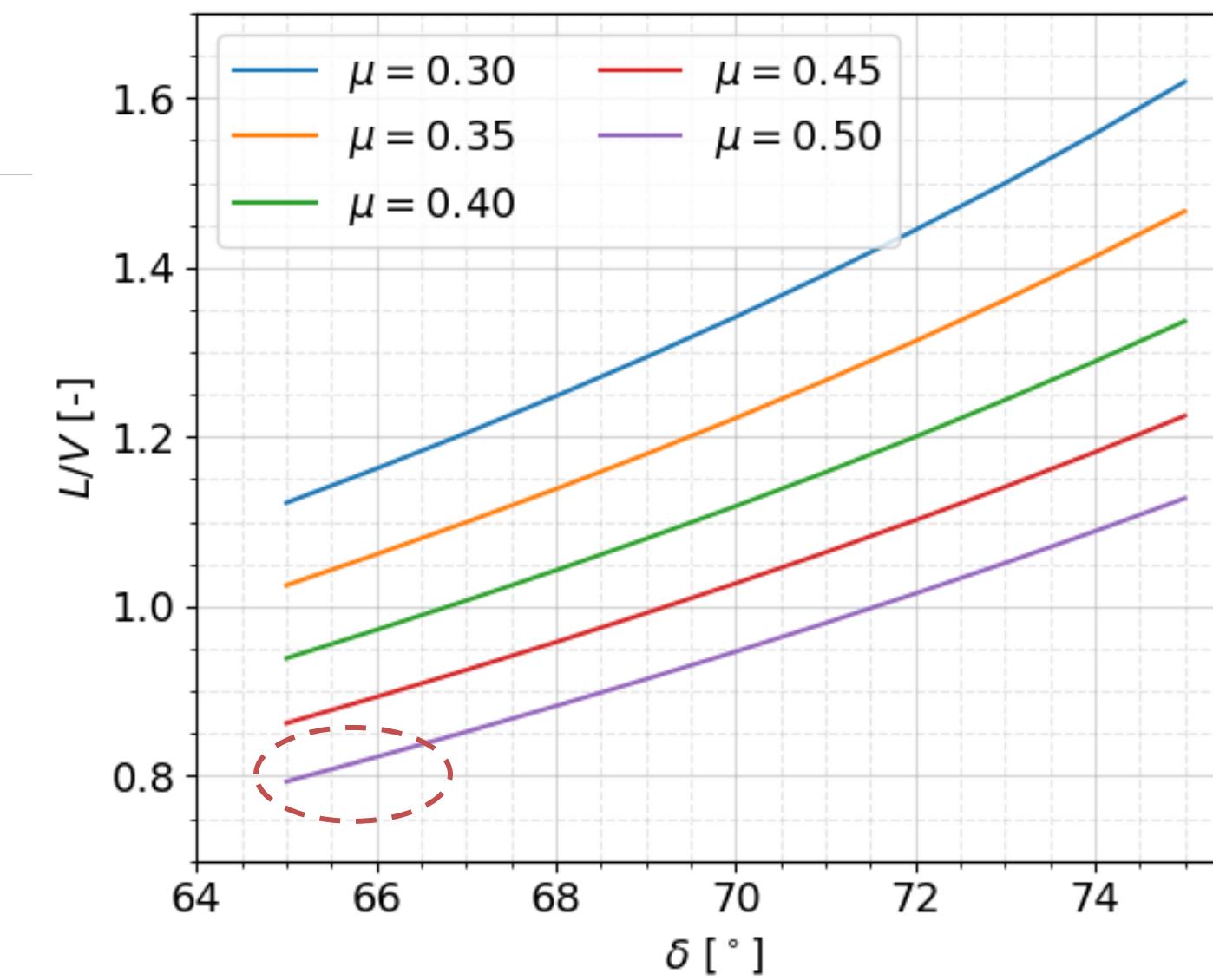


Flange climb L/V criteria start with Nadal (Nadal, 1908)



- The number 0.82 is often referenced
- Why 0.82?

$$\frac{L}{V} < \frac{\tan \delta - \mu}{1 + \mu \tan \delta}$$



0.82

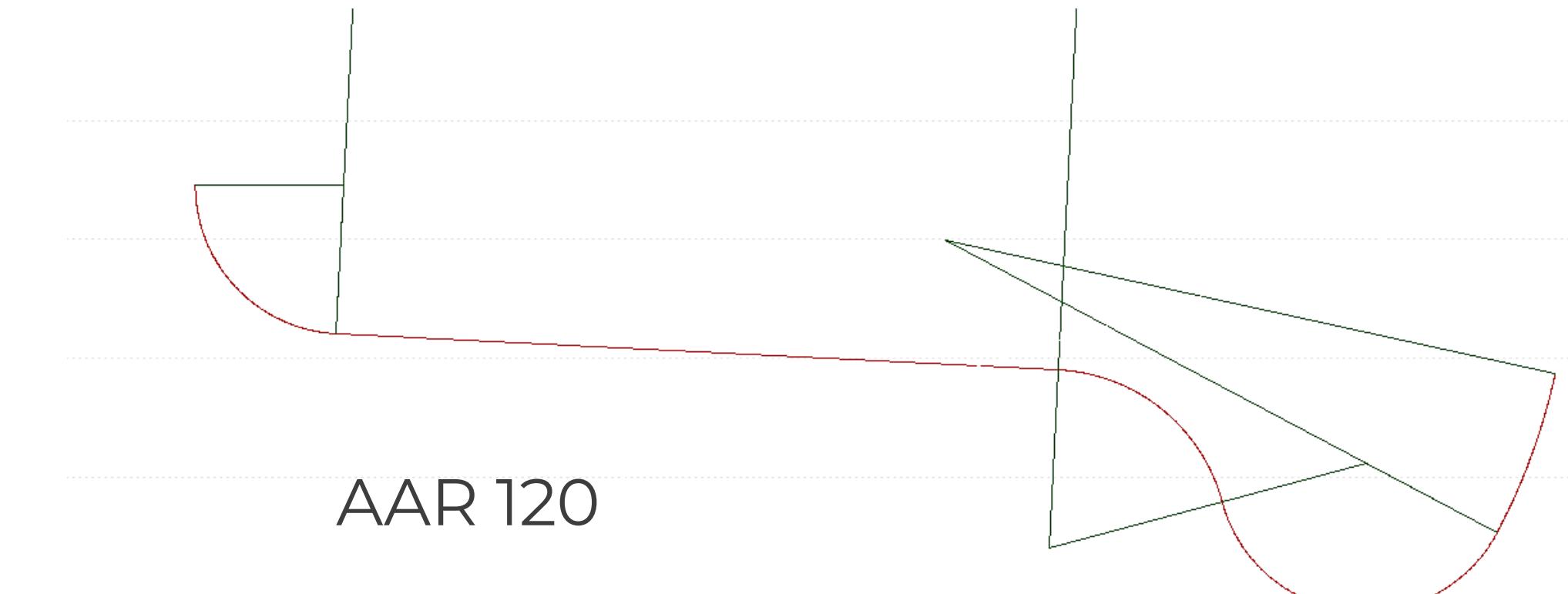


For the Nadal limit to be 0.82, we need:

- A wheel whose flange angle is less than  $68^\circ$
- A coefficient of friction of 0.5 or greater

How seriously should we take 0.82 today?

Guess the wheel profile (no prizes)



AAR 120



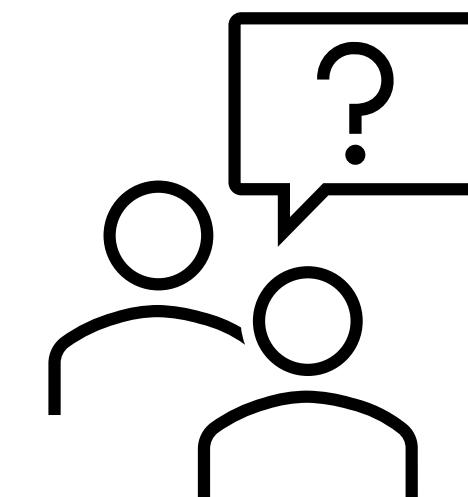
## Nadal limit

Considers two variables:

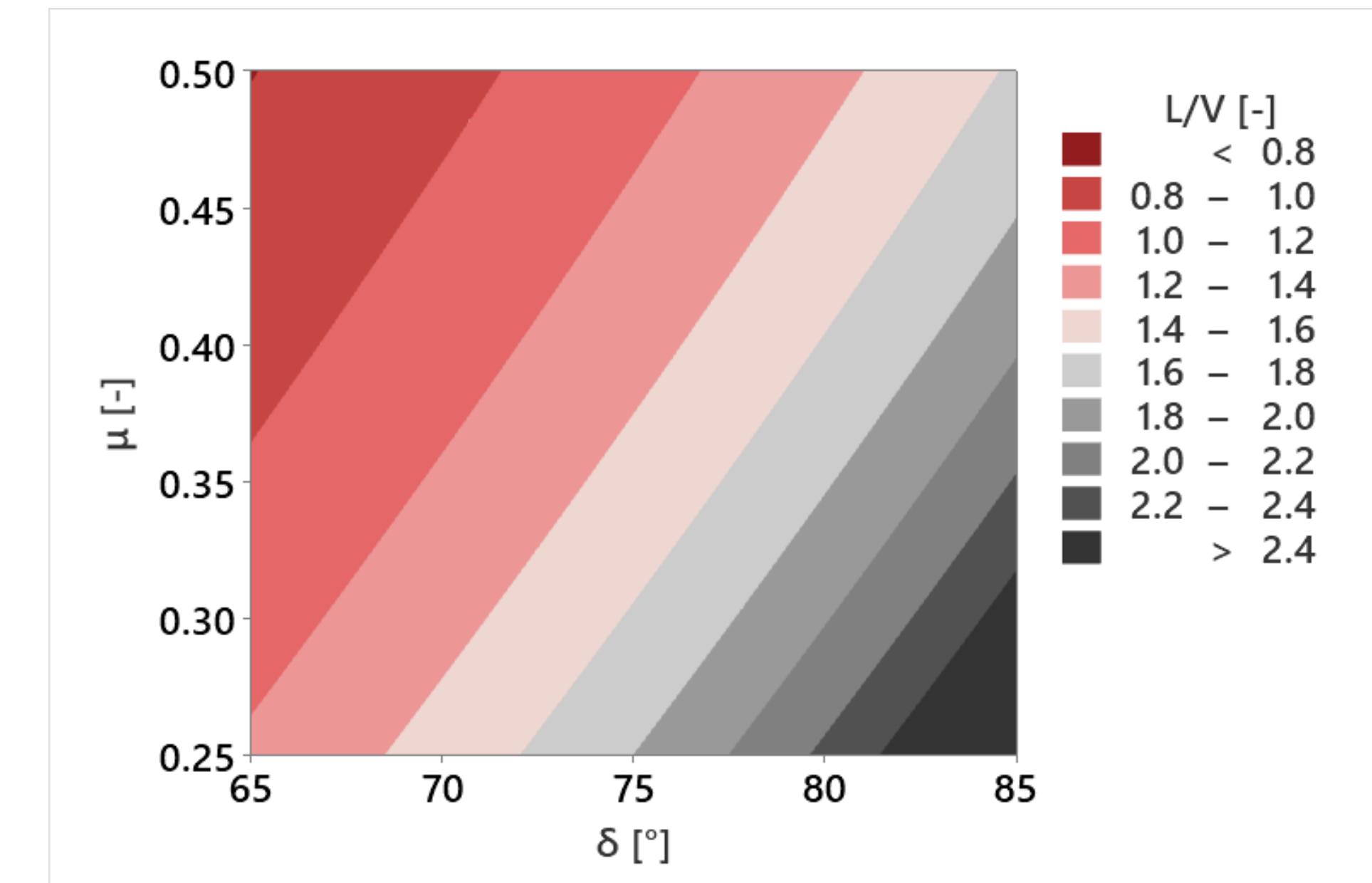
- Coefficient of friction ( $\mu$ )
- Contact angle ( $\delta$ )

Question: does  $\mu$  or  $\delta$  stay constant?

- For the same train?
- During the same run?
- At the same location?



$$\frac{L}{V} < \frac{\tan \delta - \mu}{1 + \mu \tan \delta}$$

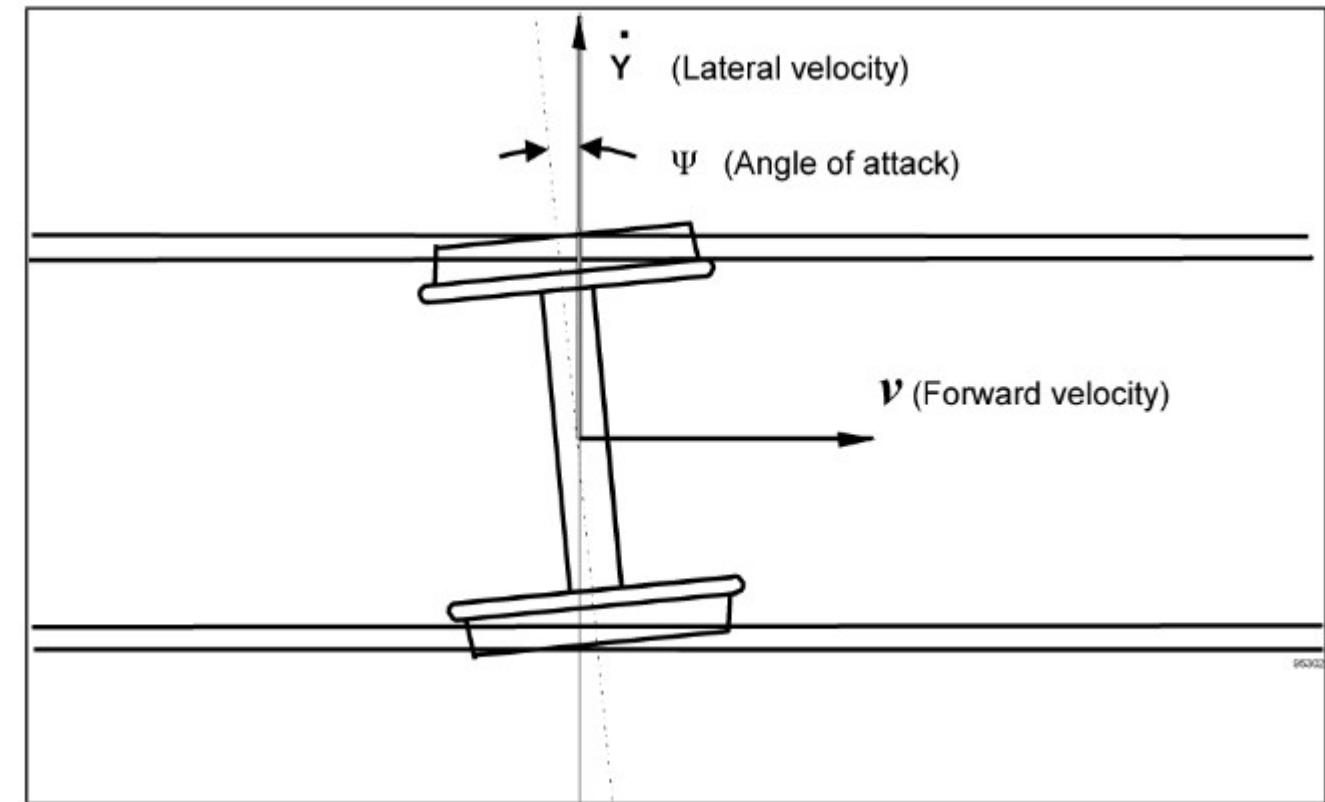


# Weinstock



$$\left| \frac{L_F}{V_F} \right| + \left| \frac{L_{NF}}{V_{NF}} \right| < \frac{\tan \delta_F - \mu_F}{1 + \mu_F \tan \delta_F} + \mu_{NF}$$

- Nadal is correct for high angle of attack (AoA) and low longitudinal creep
- Nadal is “quite conservative” for lower angle of attack and larger longitudinal creep



Derailment will not occur if any of the following is true (Weinstock, 1984):

- All wheels below Nadal
- $\left| \frac{L_F}{V_F} \right| + \left| \frac{L_{NF}}{V_{NF}} \right| < 1.0$
- $V_F < V_{LF}$  and  $\left| \frac{L_F}{V_F} \right| + \left| \frac{L_{NF}}{V_{NF}} \right| < \frac{\tan \delta_F - \mu_F}{1 + \mu_F \tan \delta_F} + \mu_{NF}$
- $\text{sgn } L_F = \text{sgn } L_{NF}$  and  $\left| \frac{L_F}{V_F} \right| + \left| \frac{L_{NF}}{V_{NF}} \right| < \frac{\tan \delta_F - \mu_F}{1 + \mu_F \tan \delta_F} + \mu_{NF}$

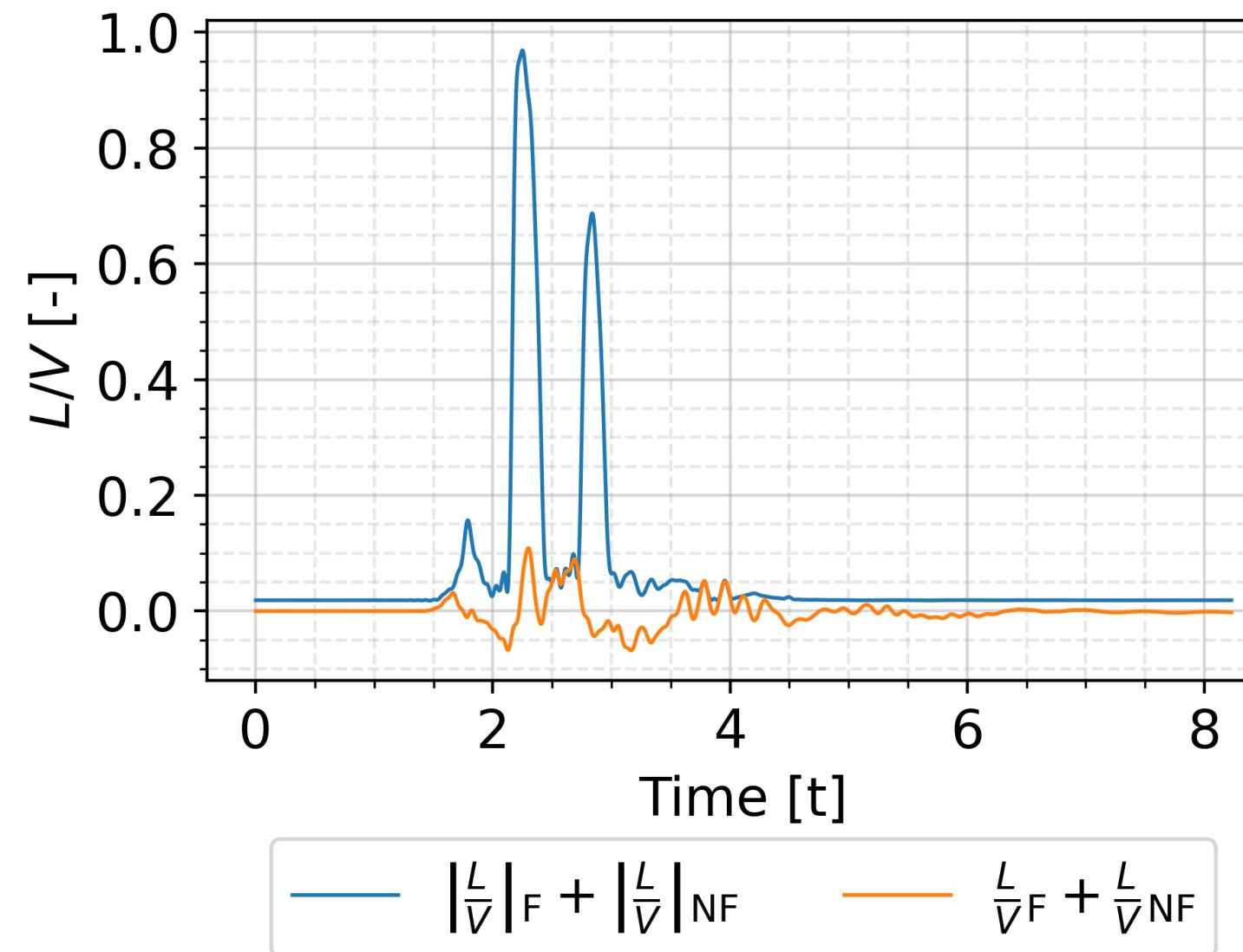


# Weinstock example

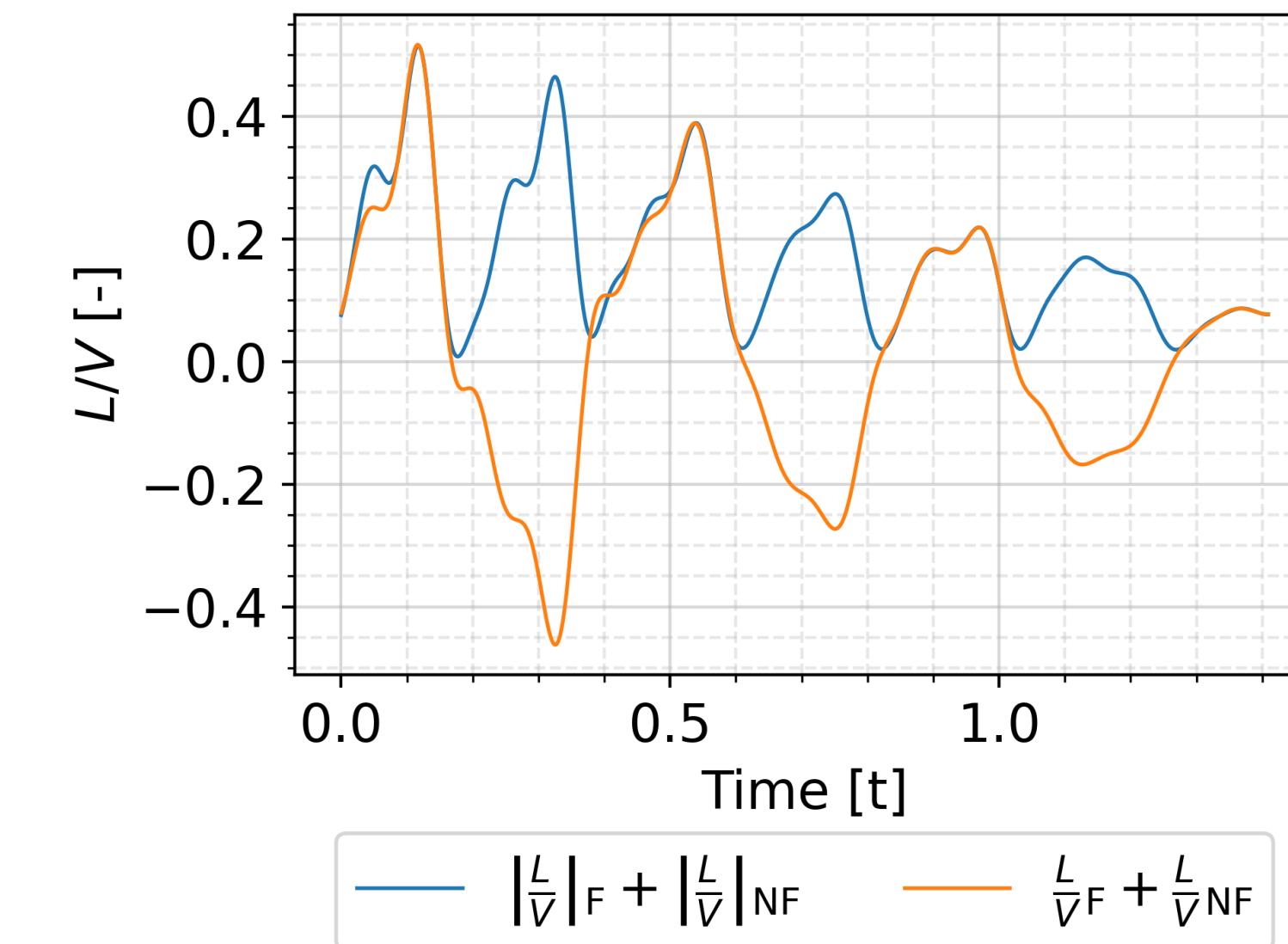


Weinstock is useful and widely used in analysis, but one should always take a pause and think about what the axle sum L/V means.

**Further analysis may not be needed:**



**Further analysis most likely needed:**



## Other factors

- L/V by itself can be insufficient in describing derailment risk
- For a wheel to climb, a positive AoA and sufficient time are also required
  - Verified in testing (Shust & Elkins, 1997)



## Further development

QUESTION

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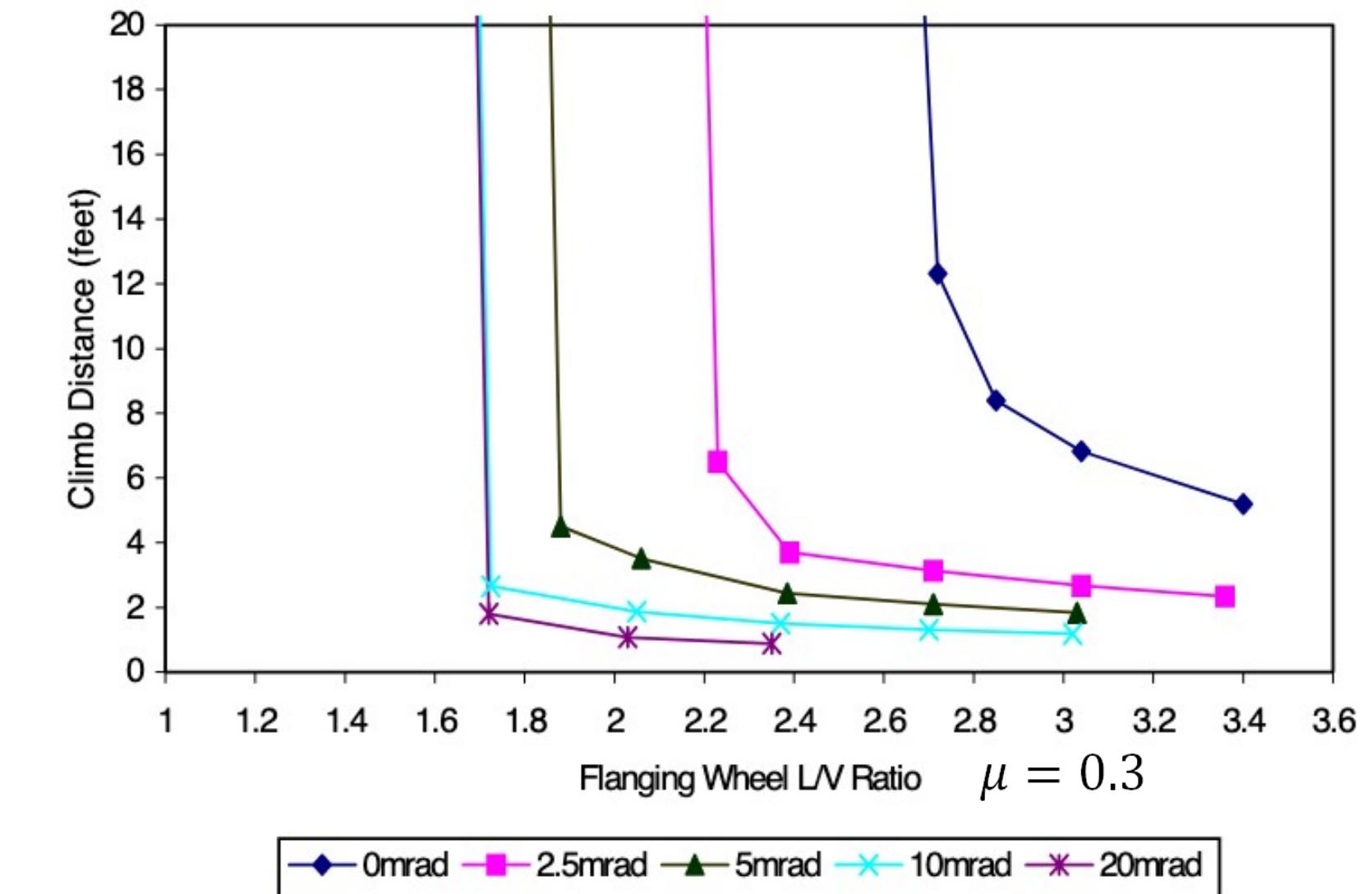
Other often cited criteria:

- Time duration based, i.e., JNR, EMD
- Distance based, i.e., 49 CFR 213.333
- Time or distance based, i.e., Chapter 11, AAR M-1001

Tests have shown that these can be exceeded without causing flange climb derailment (Wu & Elkins, 1999).

- Also need to look at angle of attack

$$20 \text{ mrad} = 1.15^\circ$$



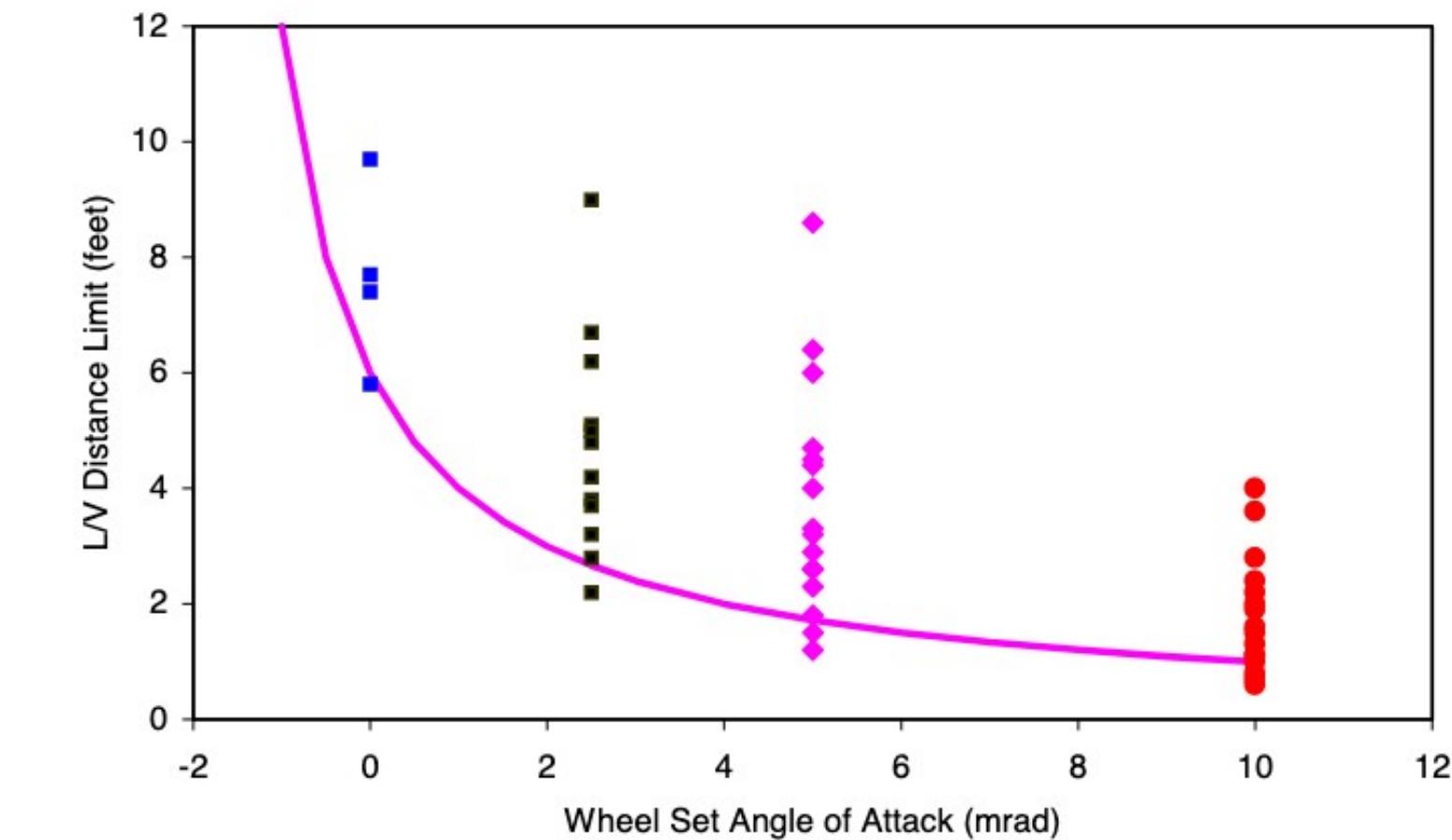
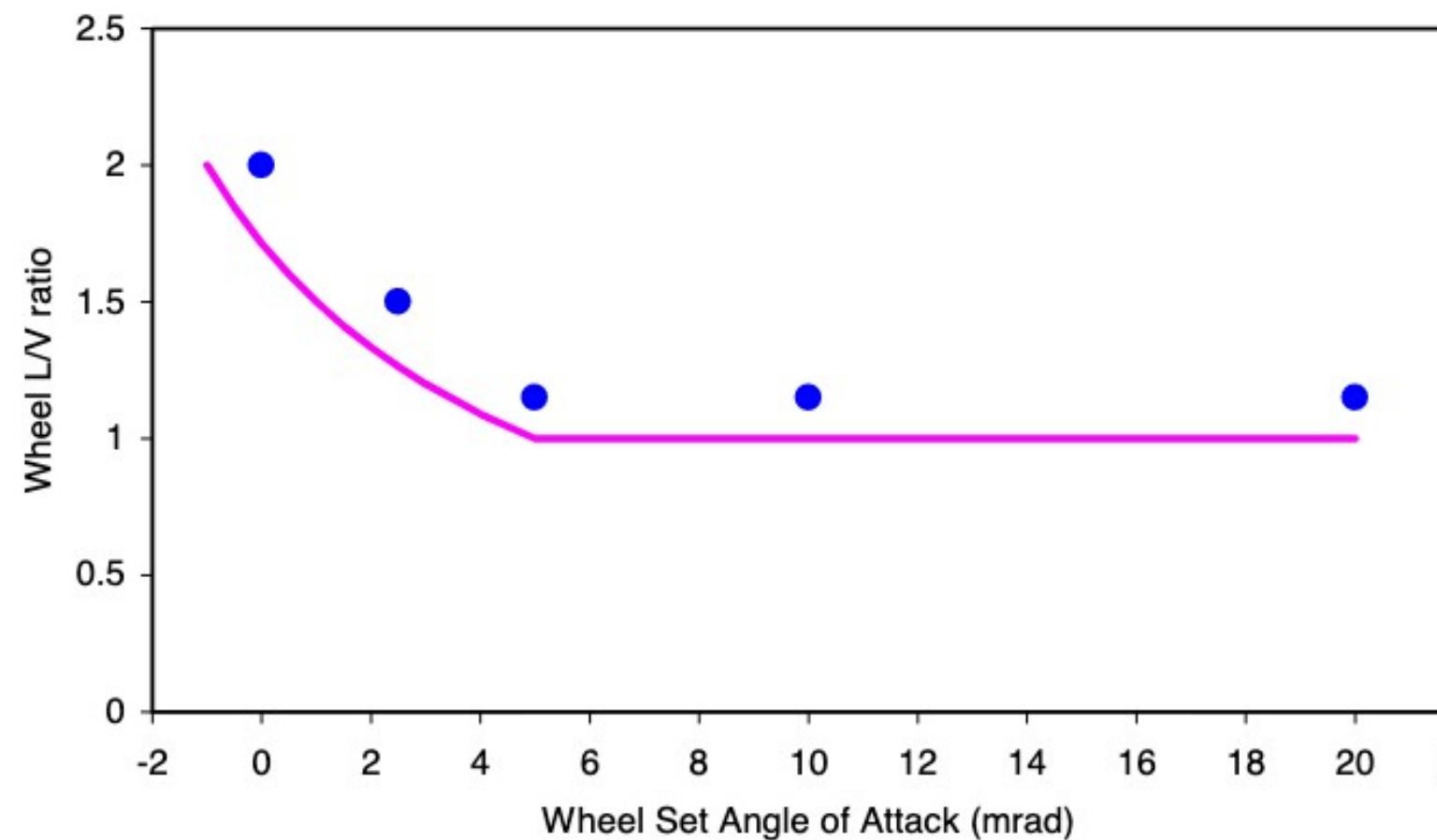
## Elkins/Wu criteria

Combined angle of attack ( $\Psi$ ) and climb distance ( $d$ ) derailment criteria (Wu & Elkins, 1999)

$$\frac{L}{V} \leq \begin{cases} 1.0, & \Psi < 0.5 \text{ mrad} \\ \frac{12}{\Psi + 7}, & \Psi \geq 0.5 \text{ mrad} \end{cases}$$

and

$$d < \begin{cases} \frac{12}{\Psi + 2}, & \Psi > -2 \text{ mrad} \\ \infty, & \Psi \leq -2 \text{ mrad} \end{cases}$$

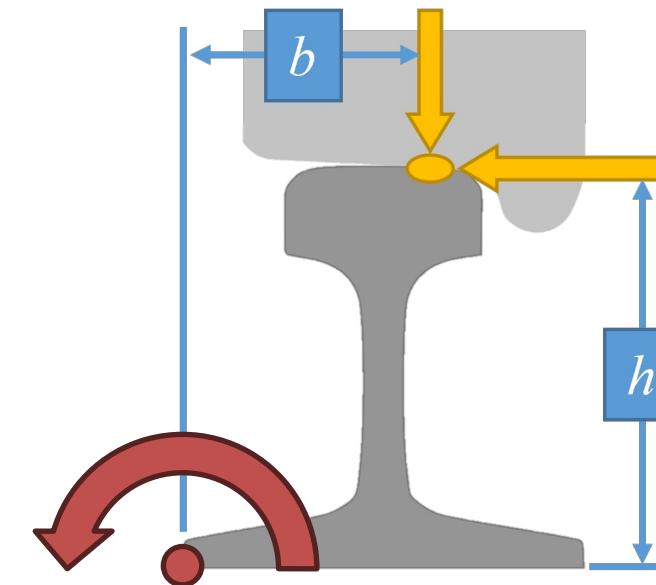


# Rail rollover L/V



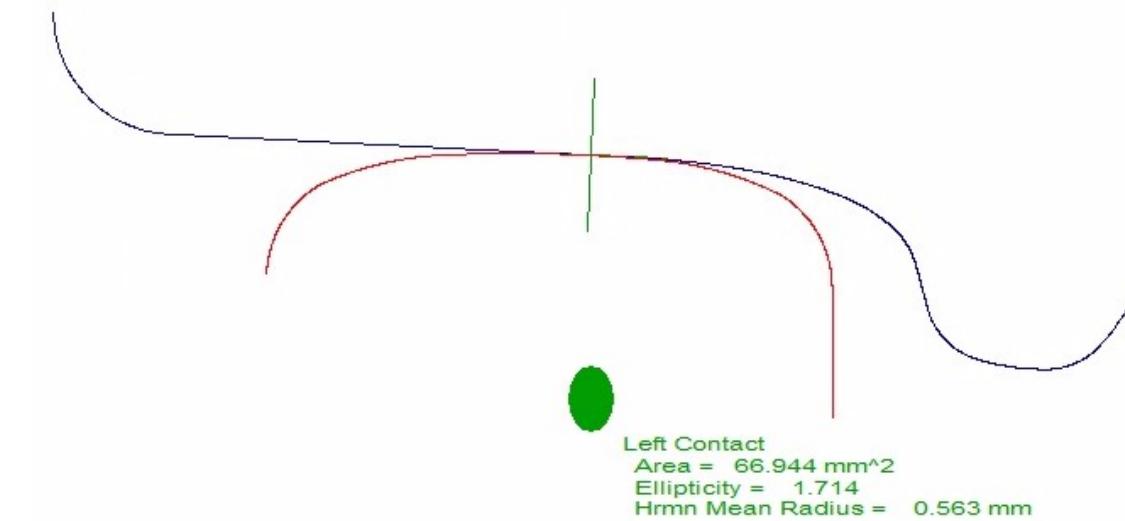
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Often discussed L/V ratio that signifies the risk of rail rollover (Stetson, 1909)



$$\left(\frac{L}{V}\right)_{\text{Trucksides}} < \frac{b}{h}$$

Often emphasized example of rail rollover risk comparison



VS.



We will revisit this later in this presentation





## Net axle or truck L/V

Sum of all wheel L/V on the axle or truck, i.e., gage spreading forces cancel each other out, however, there are times when it is the directional sum of the wheel lateral forces that matters more.

- The net lateral force could be high enough that in the right (wrong) conditions, the entire track panel shifts laterally
- Net axle or truck L/V is also a commonly used design value, e.g.,
  - Prud'homme
  - 49 CFR 213.333

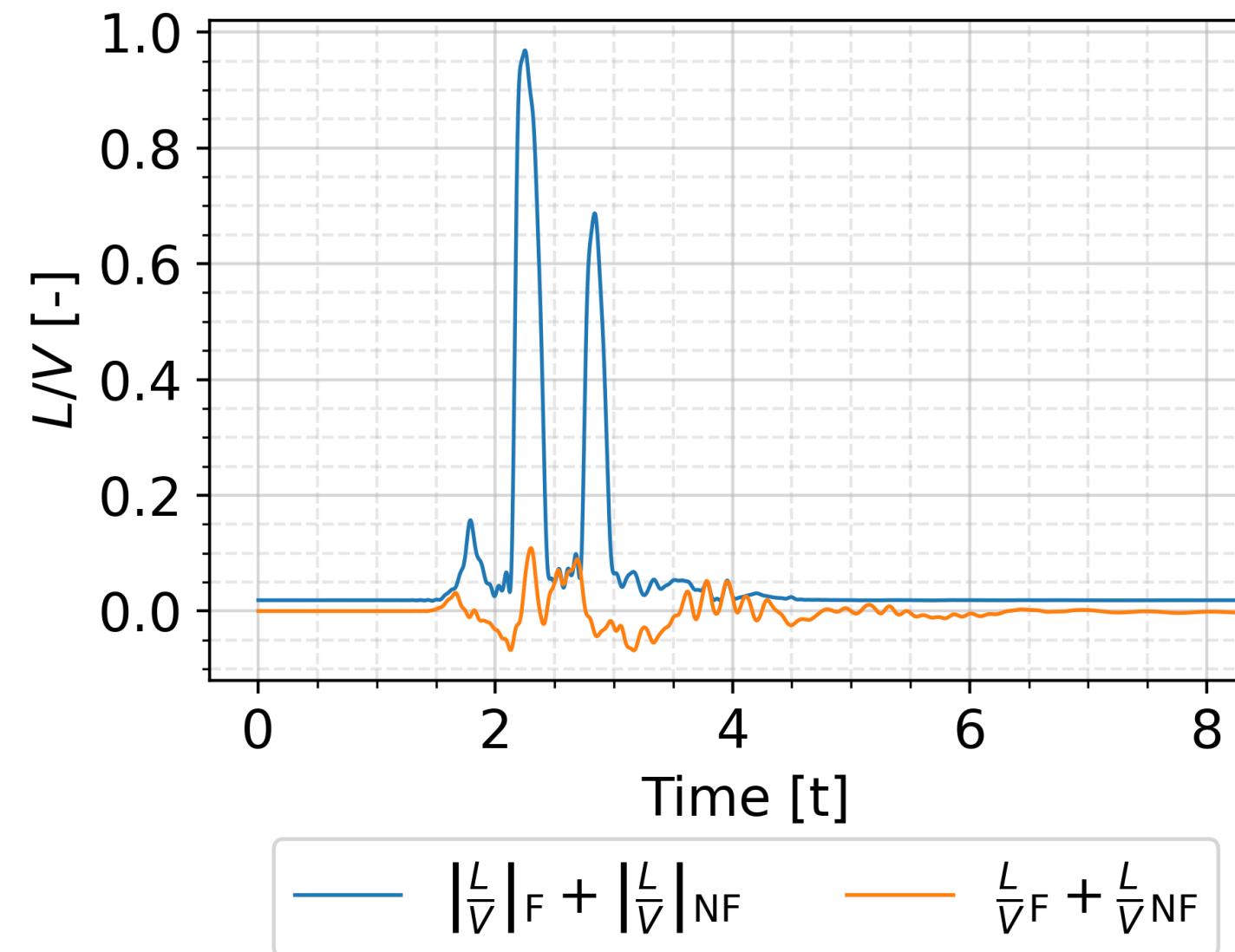


# Example revisited

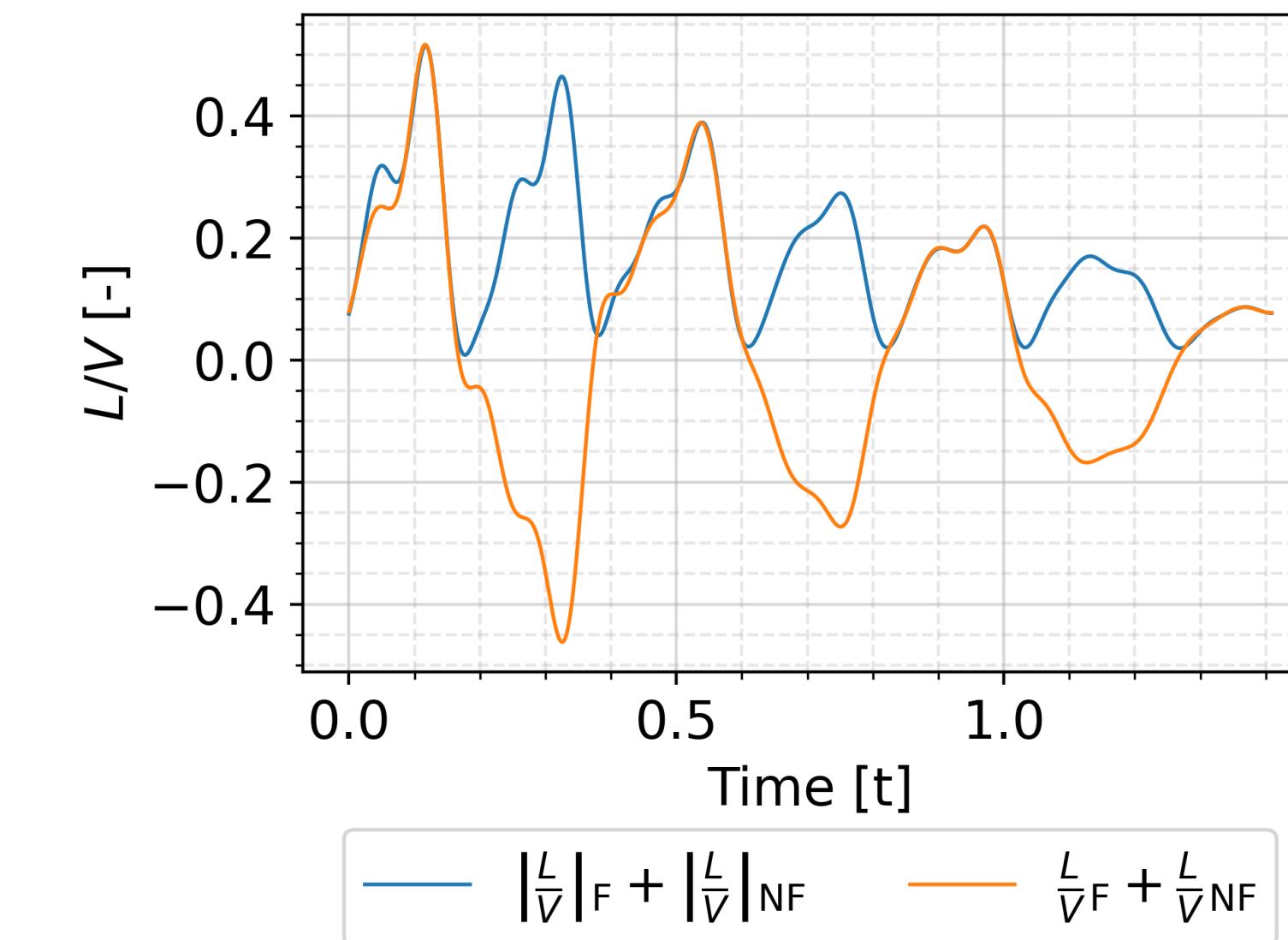


Although relatively low in axle sum L/V, the simulation on the right produces much higher net axle L/V than the simulation on the left.

**Further analysis may not be needed:**



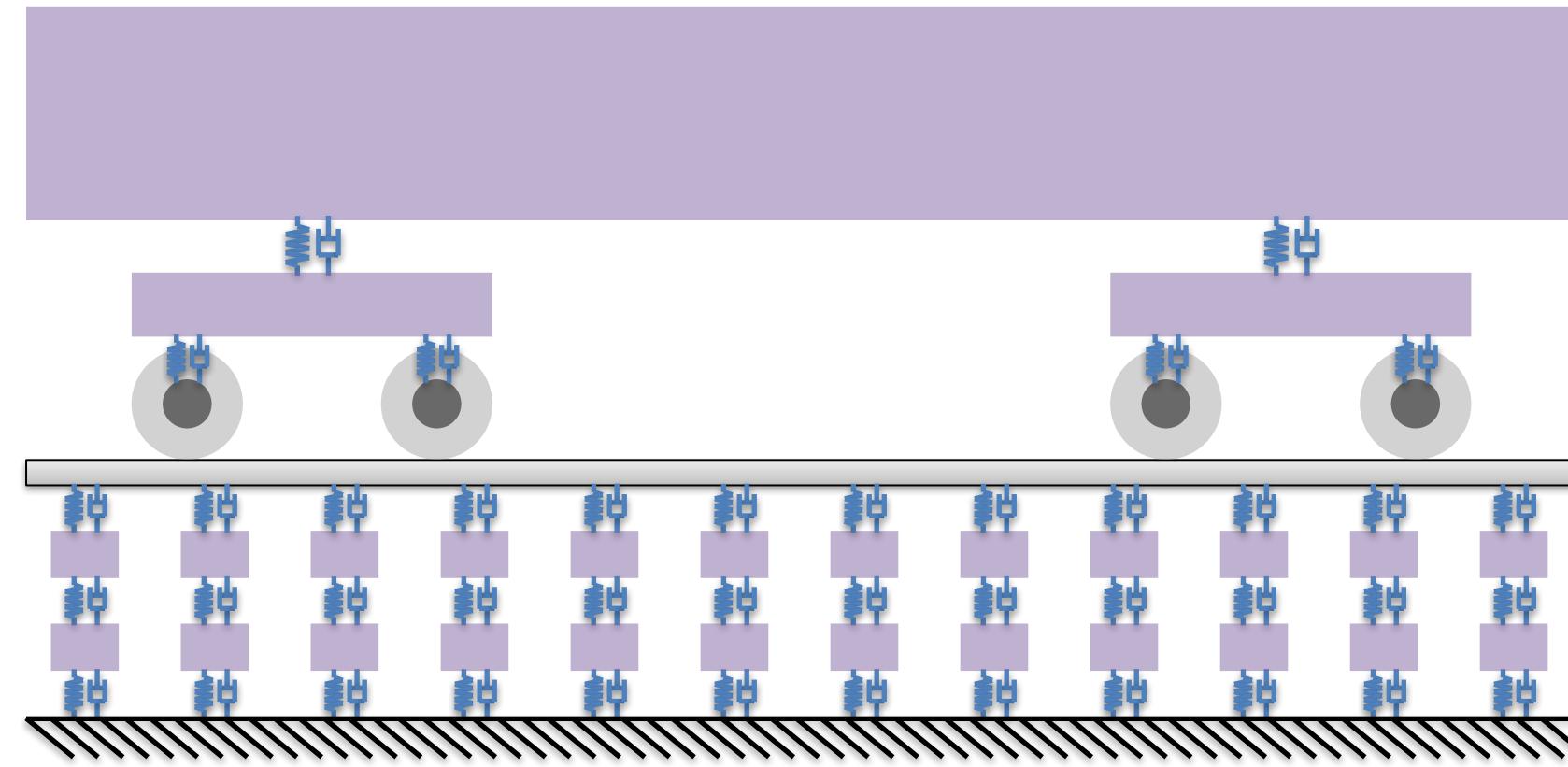
**Further analysis most likely needed:**



# Vehicle-Track Interaction



- Criteria presented thus far focus on the static geometries of the wheel and rail profiles
- Track is not infinitely strong, displacements happen
  - Track displacement is not a binary



\*Simplified diagram showing connections in one dimension – other dimensions also apply



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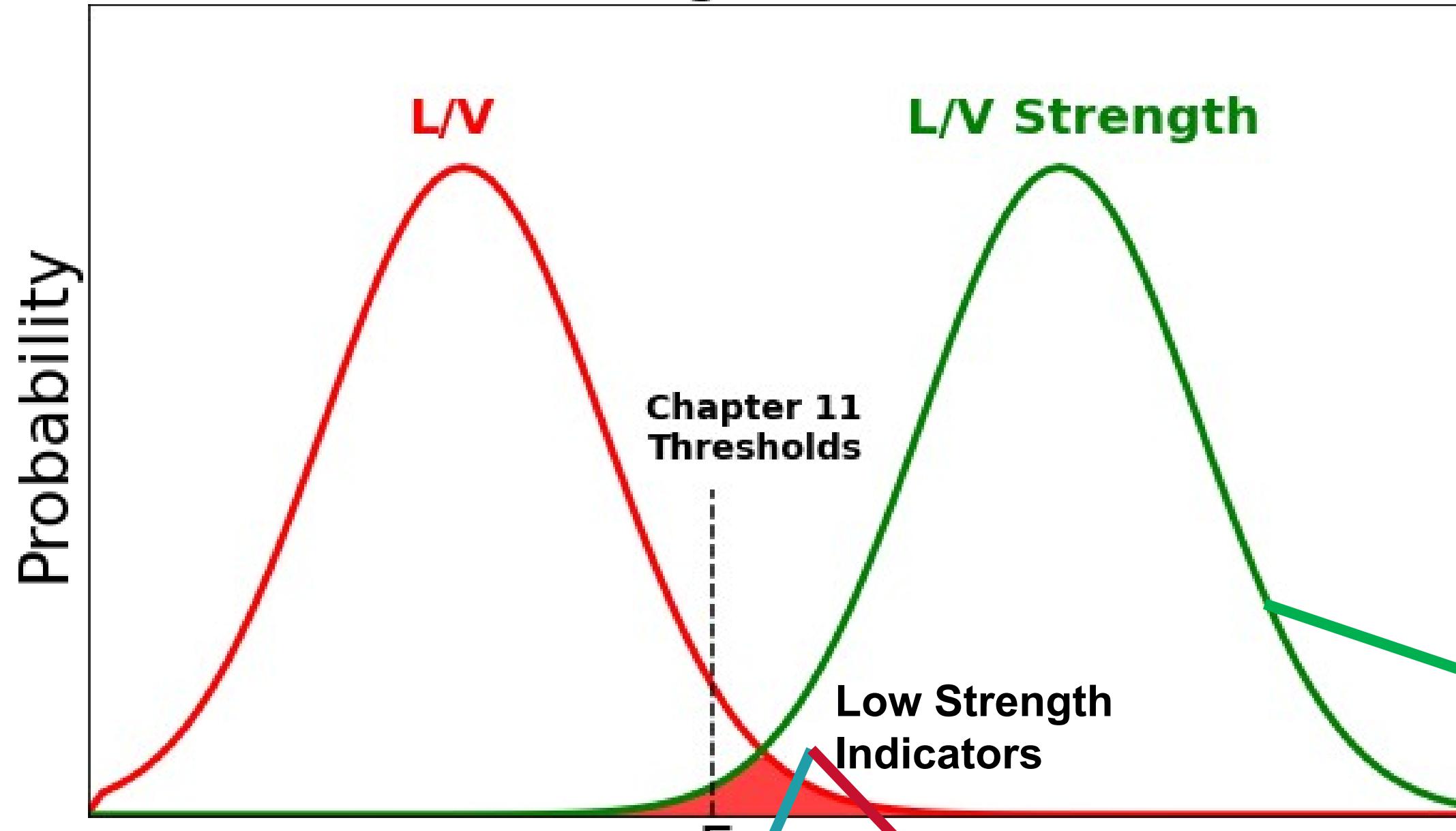
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# Rail Rollover / Gage Widening

## Force v. Strength Risk Distribution



### Fastening System

- Plate Cutting / Rail Seat Abrasion
- Loose Spikes / Broken Fasteners

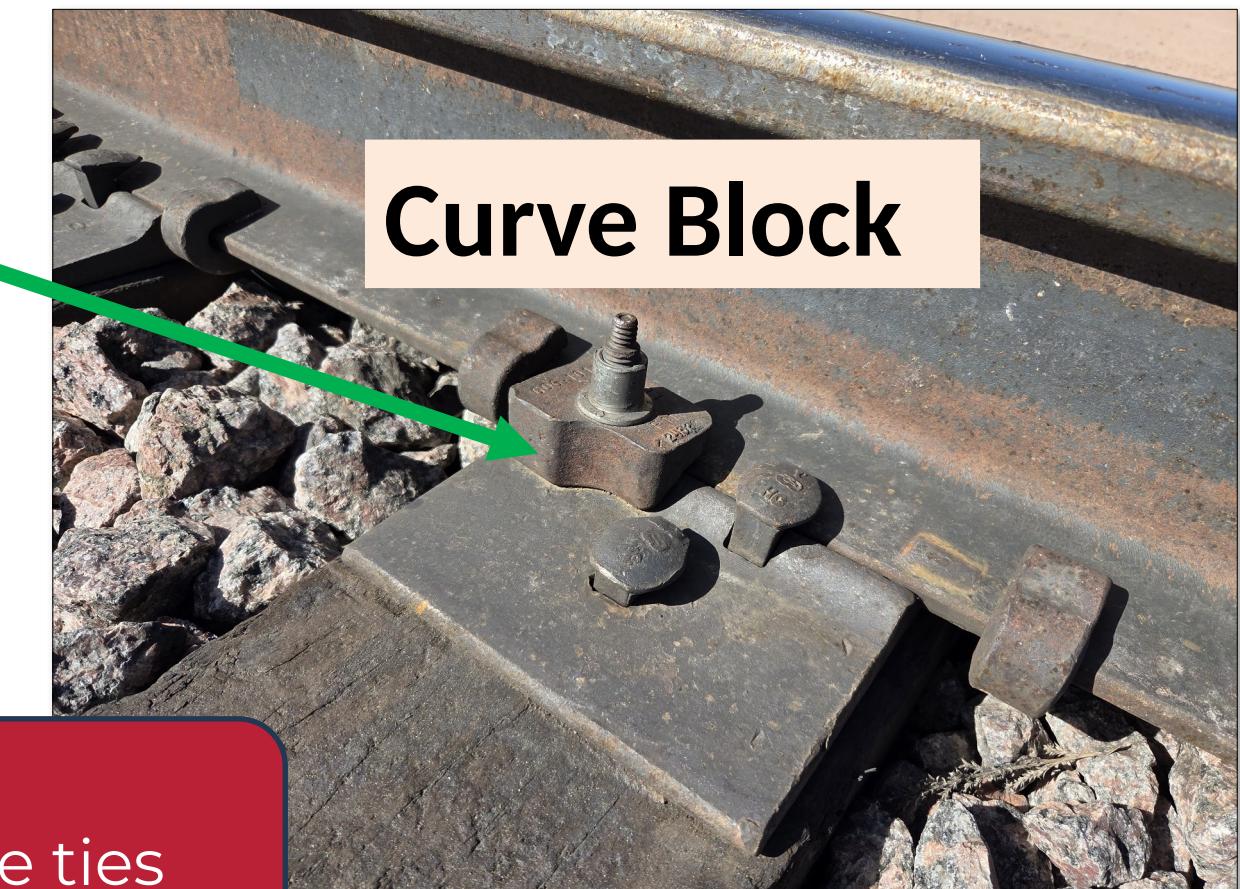
### Ties

- Cracked concrete/composite ties
- Thermal bending of composite ties

Loose Spikes



Curve Block

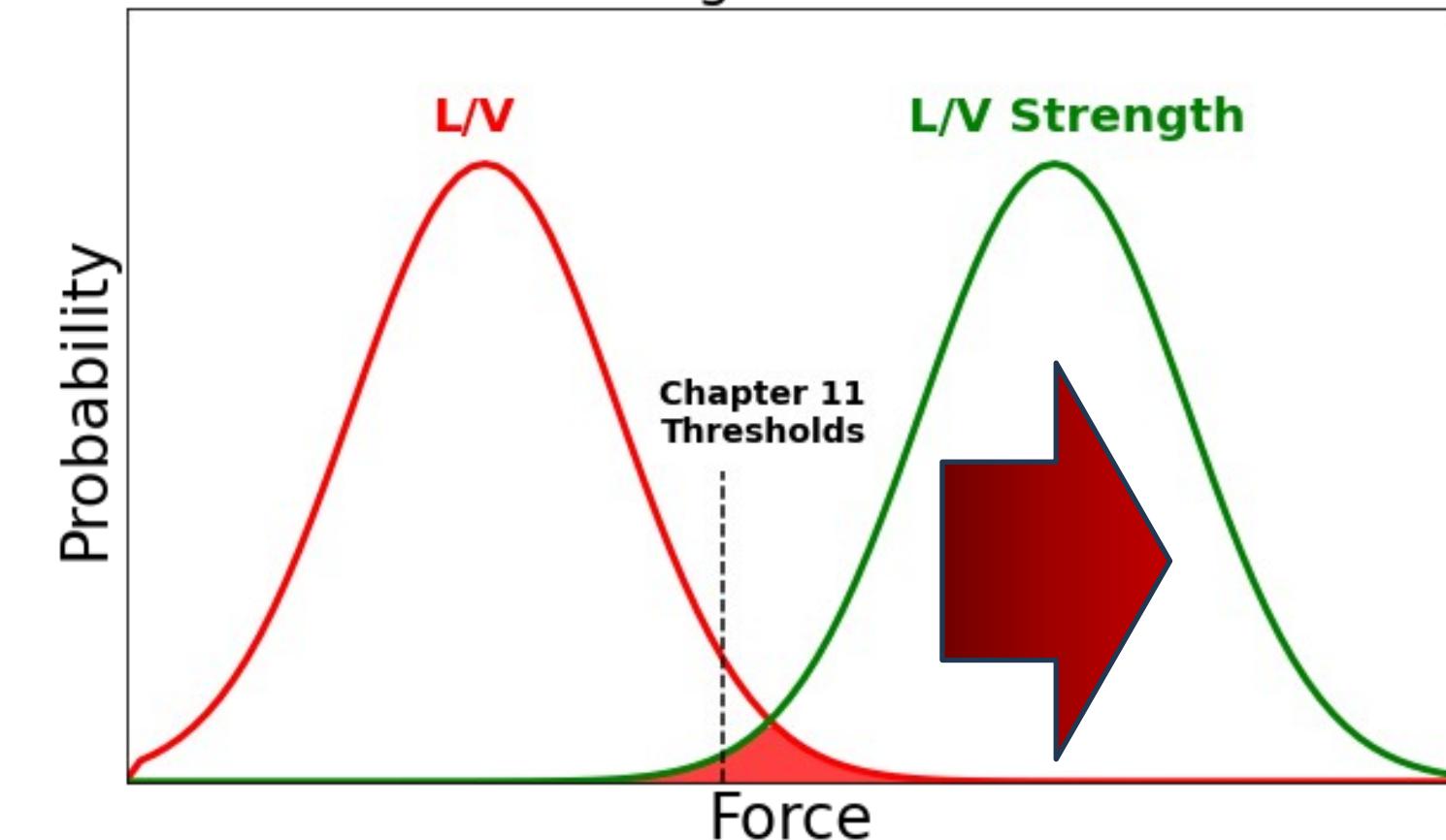




# Measurements

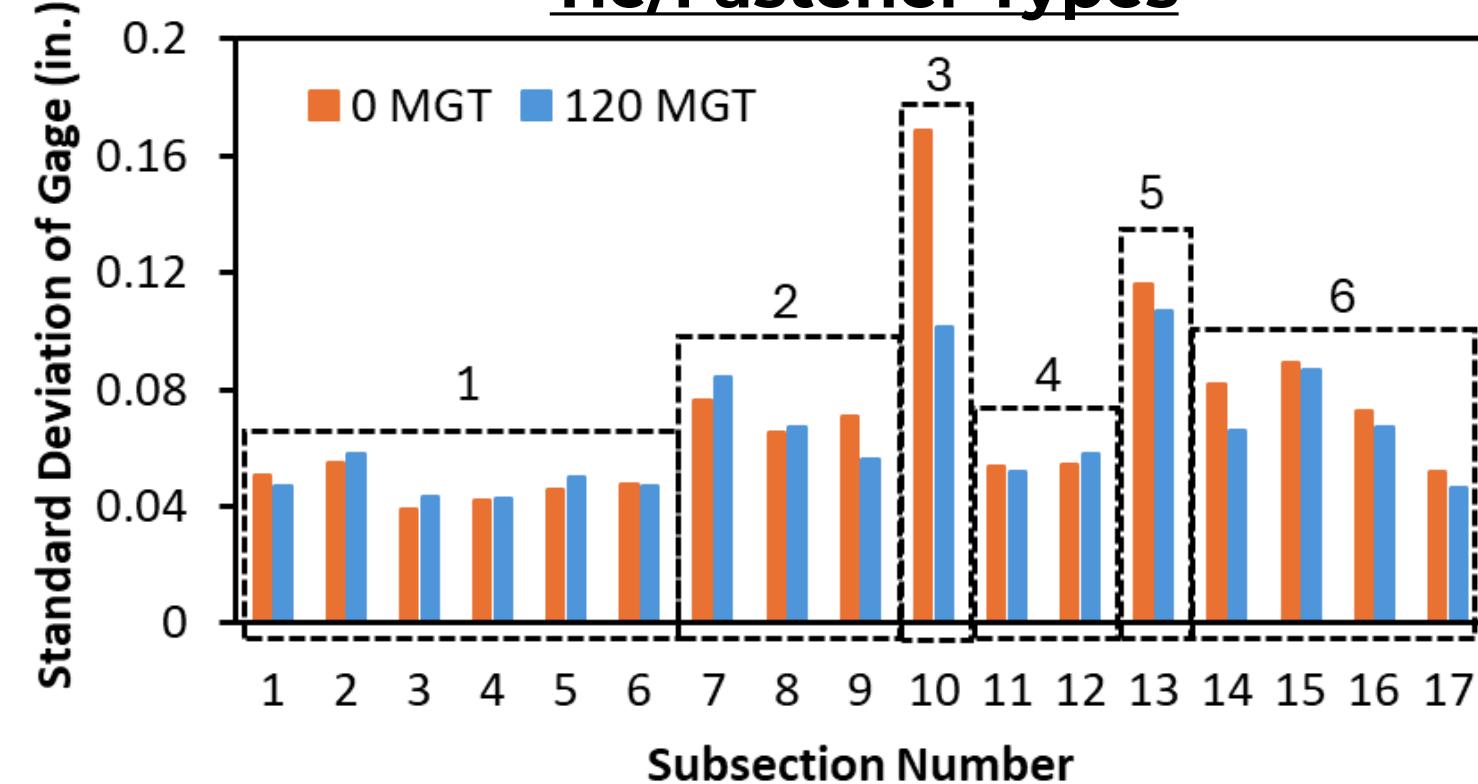
- Ensuring new ties and fasteners resist gage widening is of the largest testing efforts for 'Ties and Fasteners'
- 'Truckside L/V strength' not directly measured

Force v. Strength Risk Distribution



LTLF Testing at FAST® (unloaded gage strength)

## Gage Measurements of Different Tie/Fastener Types



- Concrete ties
- wood ties with AREMA plates
- Composite ties with AREMA plates
- Wood ties with curve block plates
- Interspersed concrete/wood ties
- Wood ties with elastic fasteners

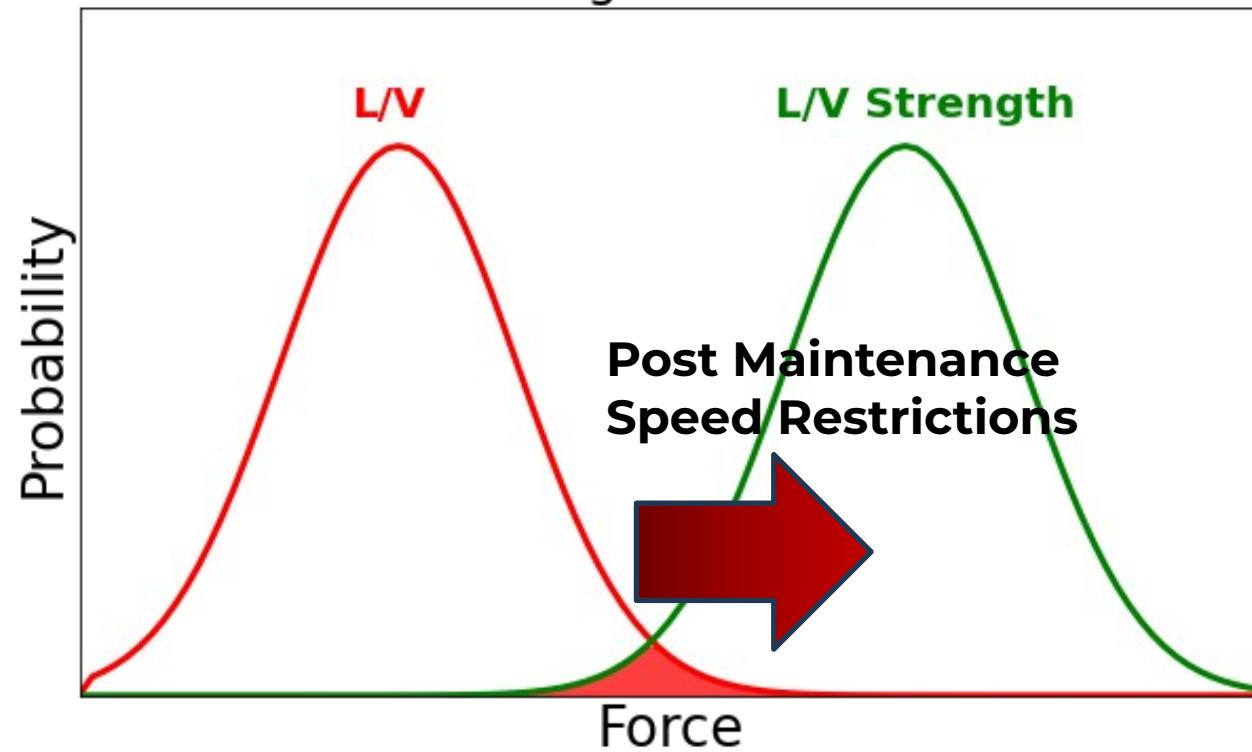




## Net Truck L/V Strength

- NTLV and track buckle strength primarily resisted by the tie/ballast interface strength
- Track movement typically not from single factor but combination of factors

Force v. Strength Risk Distribution



### Ballast Contributors

- Recent Maintenance (disturbing tie/ballast interface)
- Tie and ballast types (friction and engagement)
- Amount of ballast

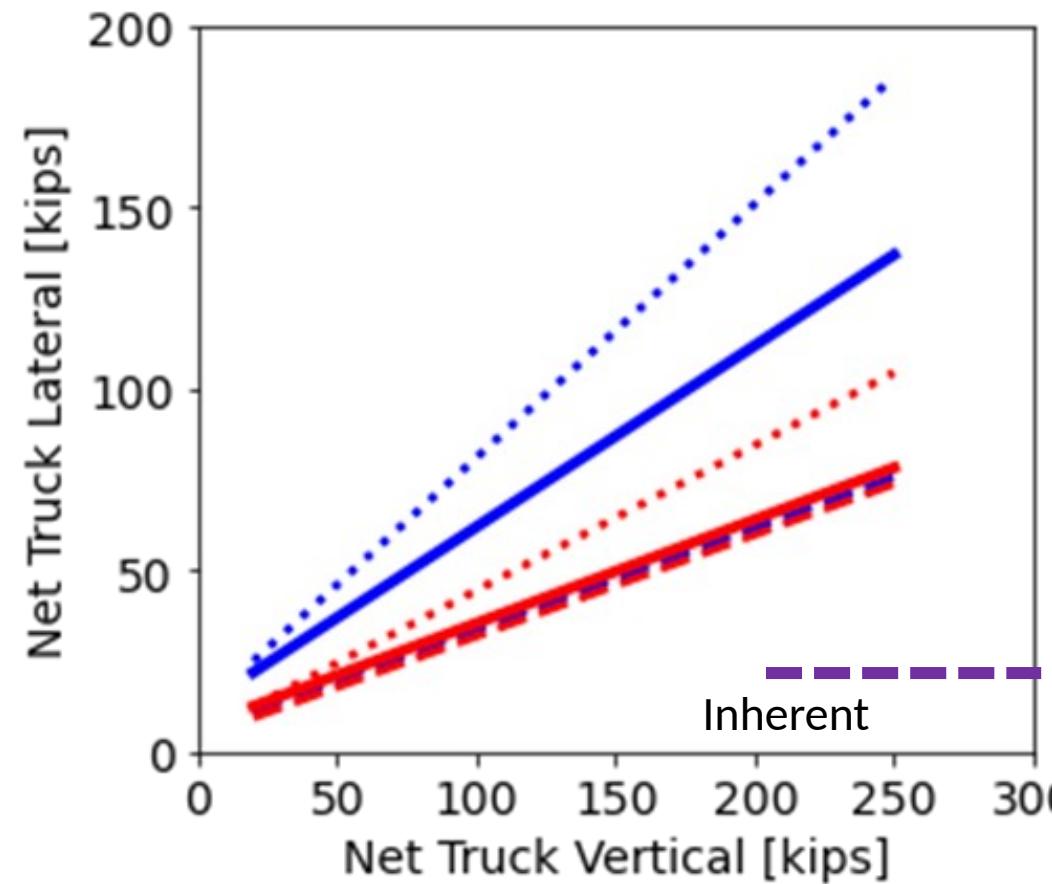
### Other Contributors

- Longitudinal rail forces
- Fastener type and condition
- Anchors
- Track geometry
- Track curvature



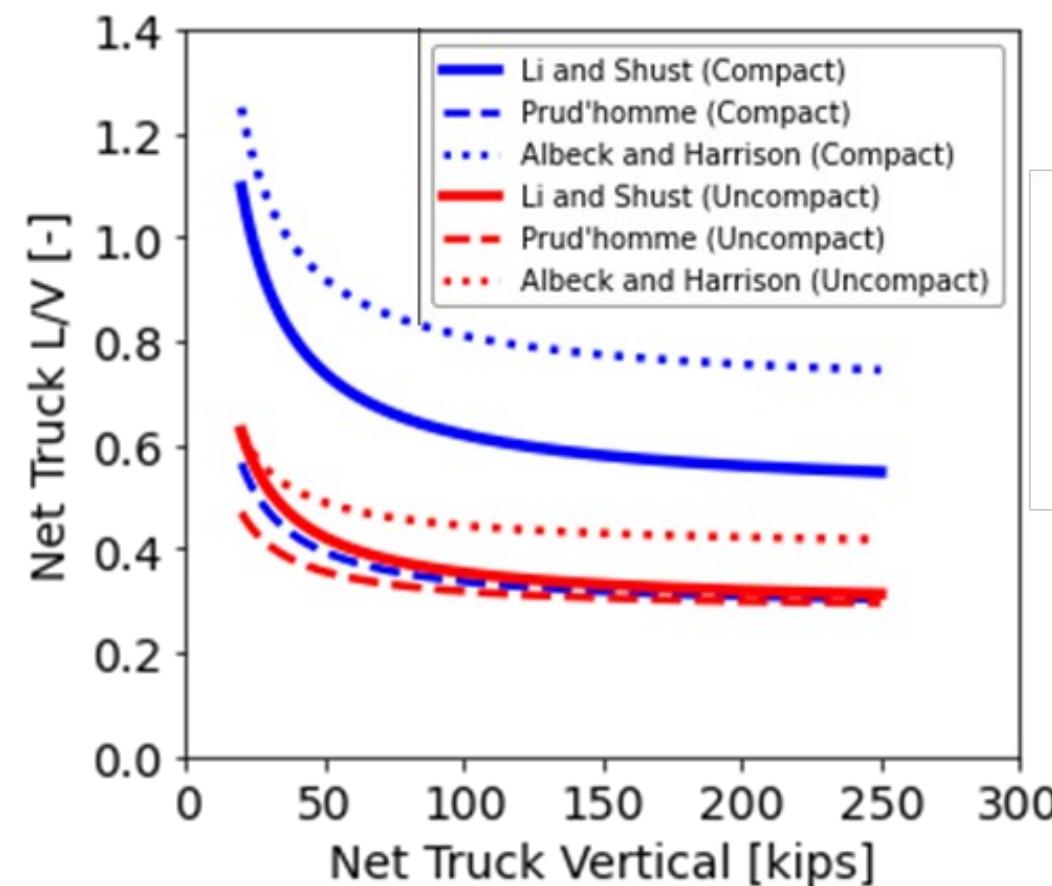


# Measurements and Criterion



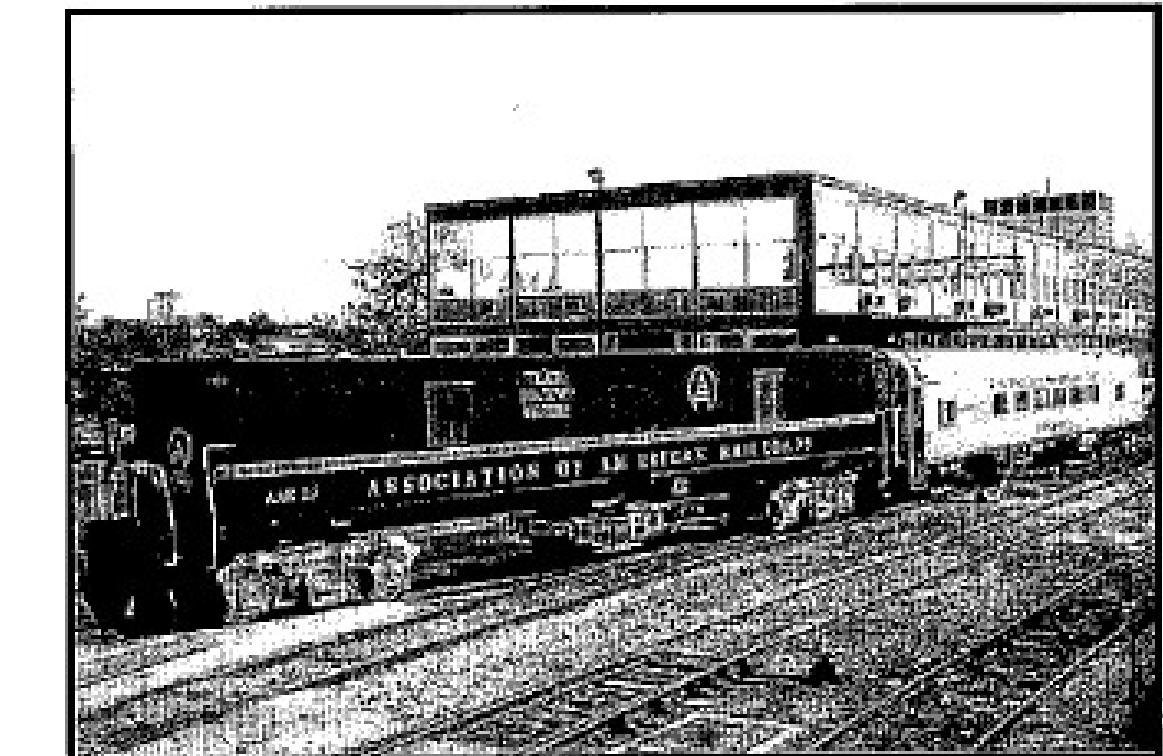
- NTLV and track buckle strength is highly frictional
- Inherent strength (truss-like track structure)

## Single Tie Push Test (STPT) - Unloaded



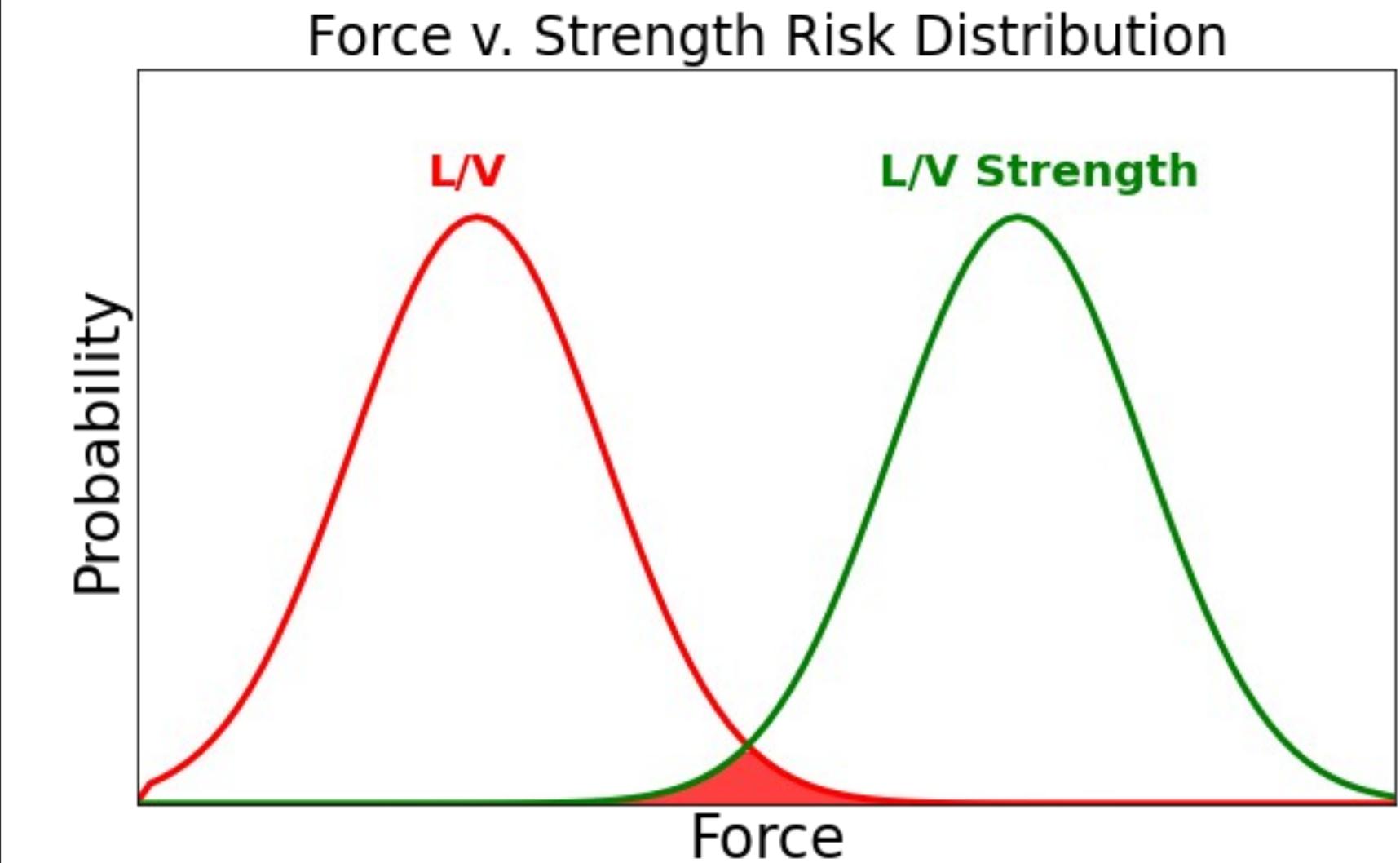
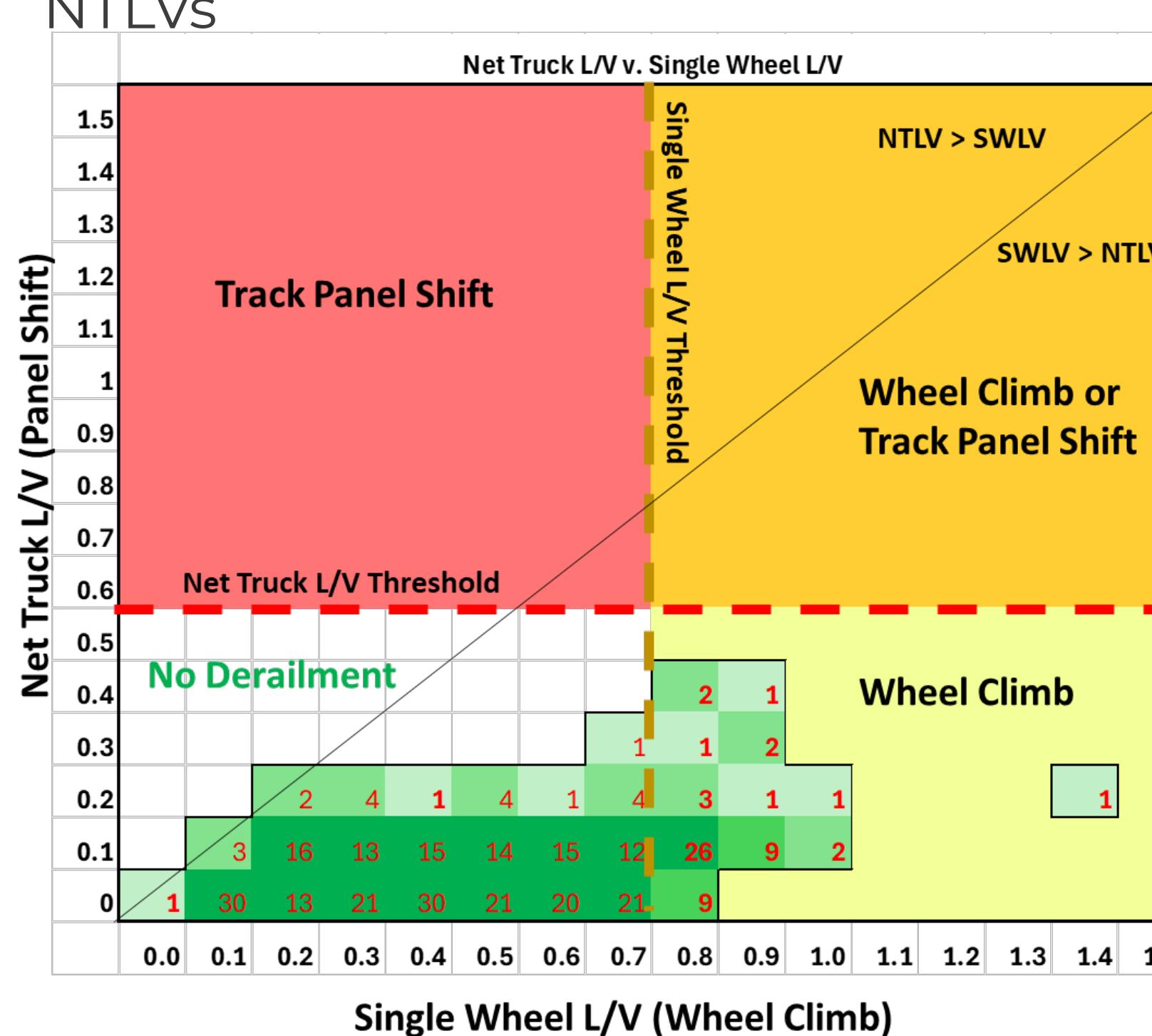
- ### Multiple Criterion
- Prud'homme
  - Li and Shust
  - Others

## Track Loading Vehicle (TLV) - Loaded

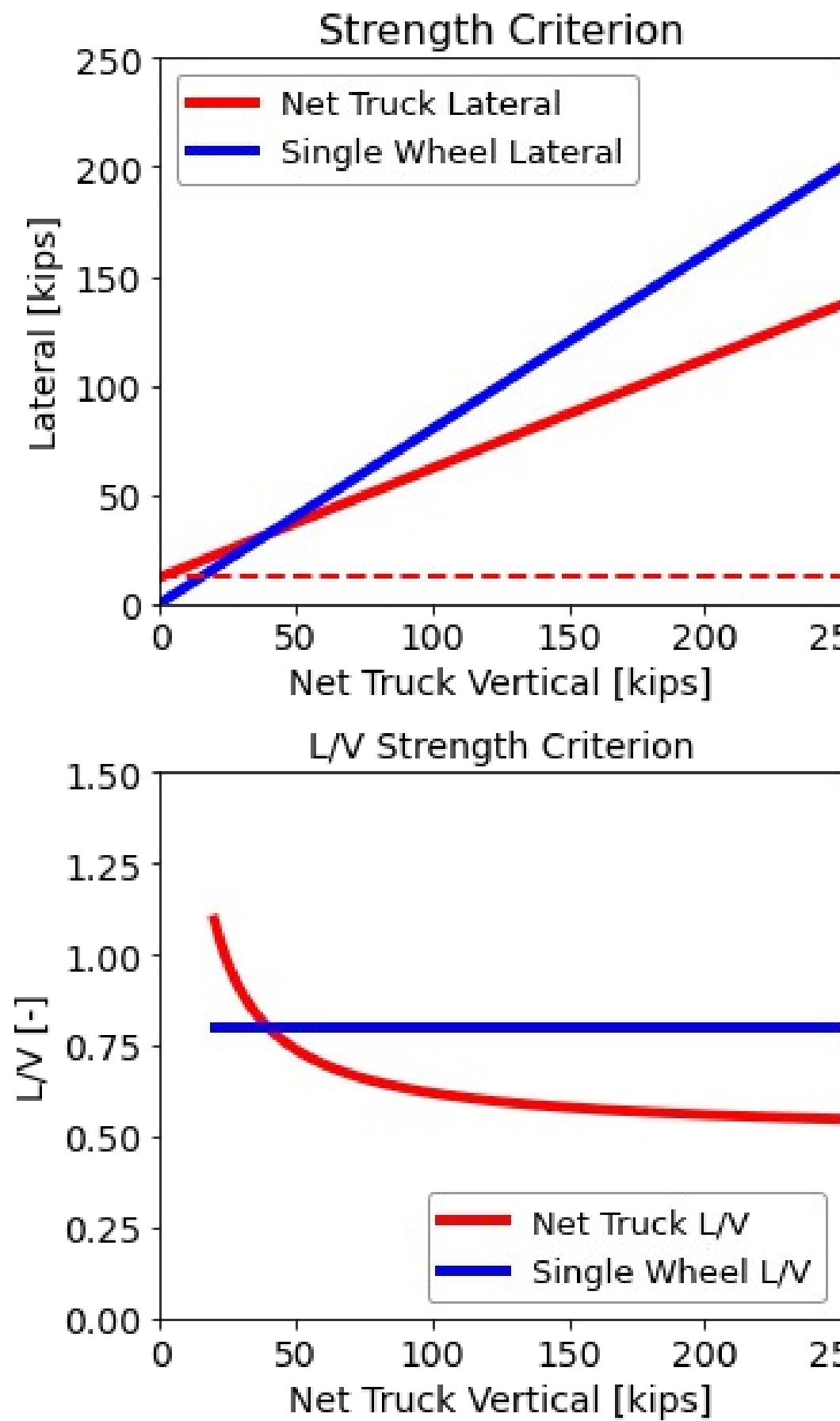


# Different L/V Strengths

- Single Wheel L/V  $\geq$  Truckside L/V  $\geq$  NTLV
  - Assuming Chapter 11 thresholds, Wheel climb > Rail Rollover > NTLV
  - Need unique combination of L/Vs and strengths to get track misalignments from NTLVs

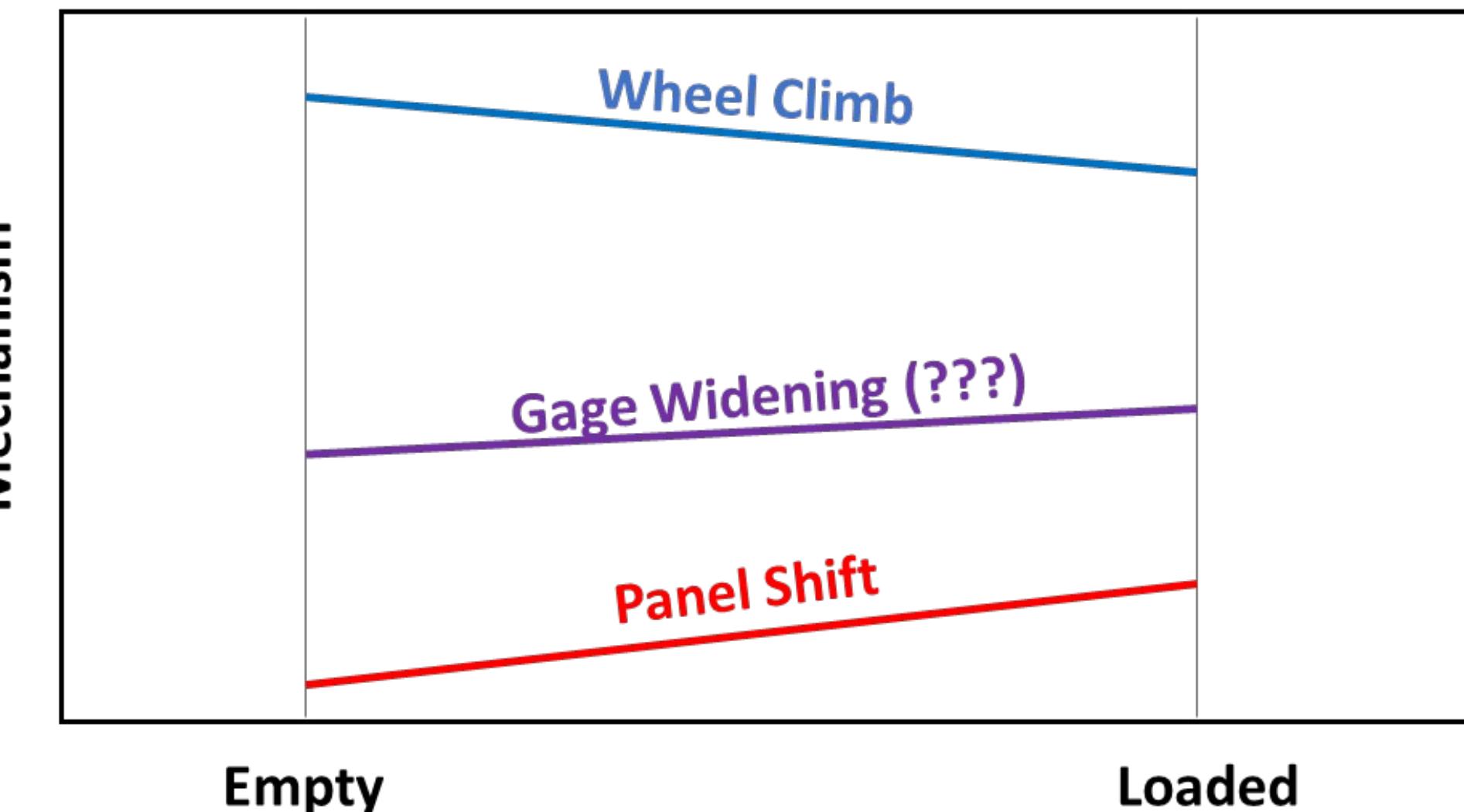


# Effect of Load



- Inherent track strength for panel shift and gage widening/rail rollover may make wheel climb even more likely for lighter axle loads

Possible Risk Diagram (Speculative and Conceptual)





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# Vehicle track system

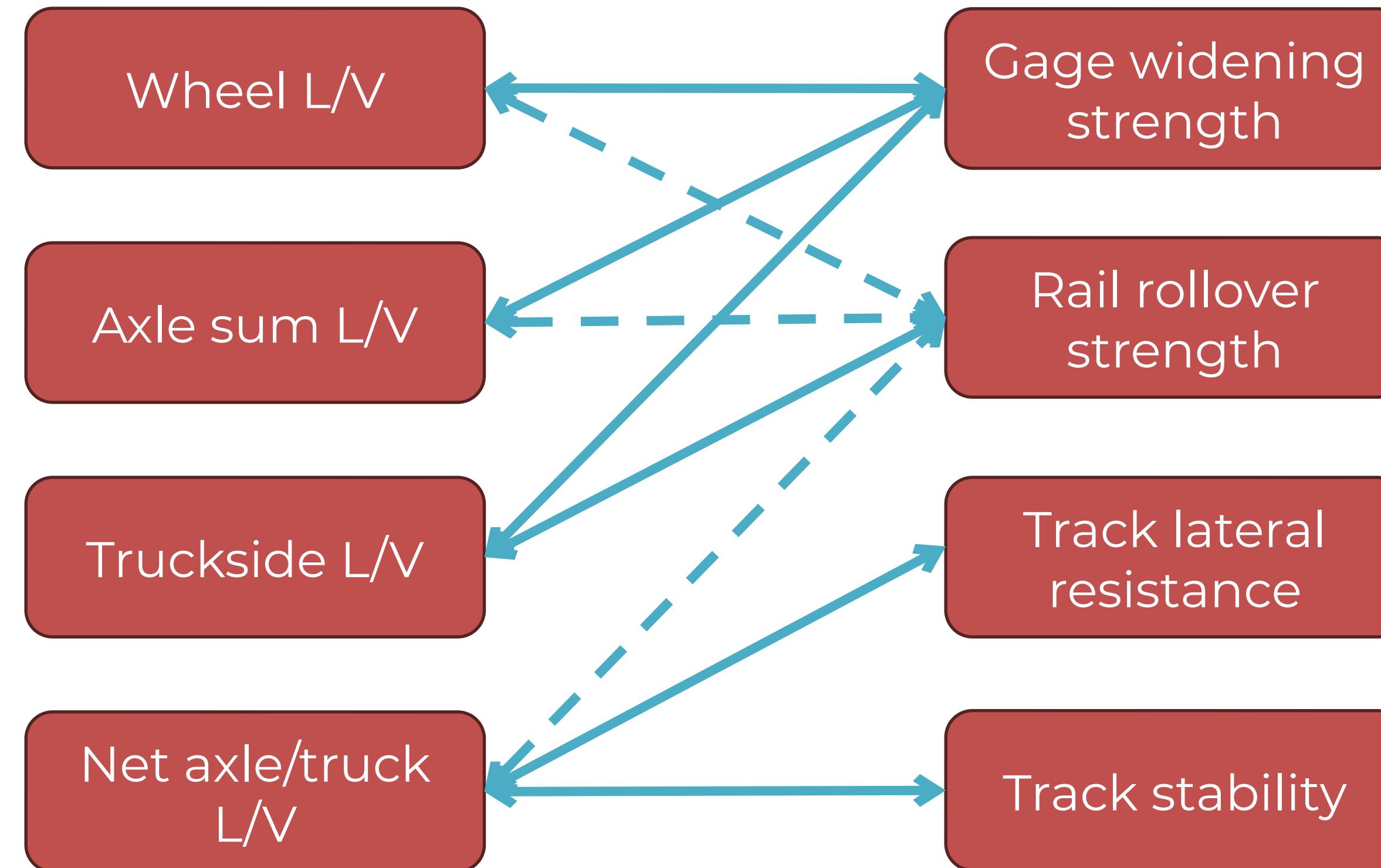


- L/V thresholds are not static in practice – affected by many factors related to both vehicle and track
- For an action generated by the vehicle, there exists a reaction from the track structure

# Vehicle track system



Links between the factors presented. More can be considered.





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# Summary



Topics discussed in this presentation:

- Backgrounds of various L/V ratios and their applications
- Angle of attack and duration considerations for wheel climb
- L/V thresholds are not static – they correspond to contact conditions and track strength
- Track strength factors that affect L/V thresholds

Vehicle dynamics and track strength are integral to each other and often should be considered as a system in practice.





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