PhD Proposal Writeup

A realtime and parallel look-ahead control and feedrate compensation strategy for CNC reference-pulse interpolation.

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1 Experiment

Describe Section 5.1, 5.2 and 5.3

1.1 The Parametric Equations

The ten(10) 2D parametric curves covered in this work are:

- 1. Teardrop
- 2. Butterfly
- 3. Ellipse
- 4. Skewed-Astroid
- 5. Circle
- 6. AstEpi = Astroid + Epicycloid combination
- 7. Snailshell
- 8. SnaHyp = Snailshell + Hypotrocoid combination
- 9. Ribbon-10L
- 10. Ribbon-100l = 10 times scaleup of Ribbon-10L

The parametric equations describing each of the curves x(u), and y(u) are provided in the next table. The independent parameter u is limited to

$$u \in [0.0, 1.0]$$

The curves were selected based on their different characteristics like closed loop curves, open ended curves, symmetric or non-symmetric about the x-axis and y-axis, and having concave or convex turns. The x and y dimensions (sizes) vary among the different curves.

The main objective of the selection criteria is to ensure that the interpolation algorithm for the parametric curve succeeds and does not break in all cases.

The results for the feedrates in machining the ten(10) curves show continuity, smoothness, with no abrupt jumps as the CNC machine traverse the entire curve from the start (u = 0.0) until the end (u = 1.0).

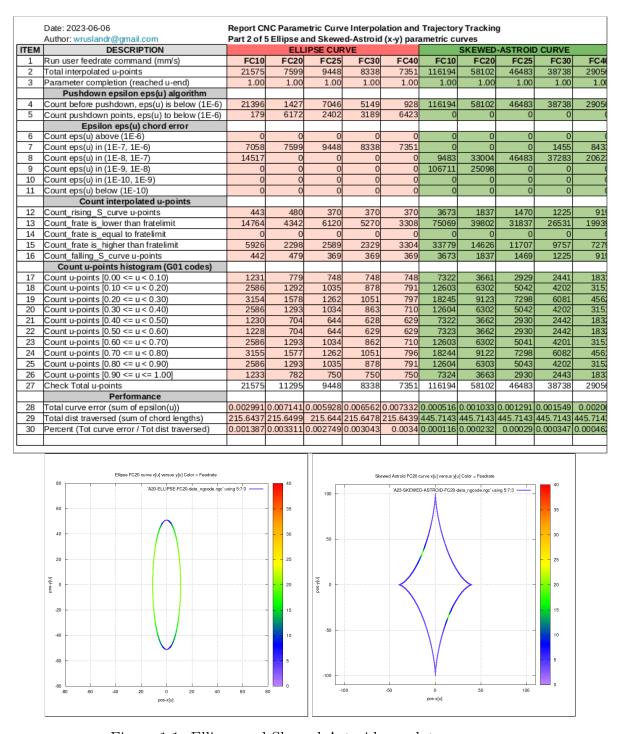


Figure 1.1: Ellipse and Skewed-Astroid run data summary

	Author: wruslandr@gmail.com		NC Param 5 Circle aı		(x-v) nara		-	-	-		
ГЕМ	DESCRIPTION	Partson		CLE CUF		metric cu		TEDOID 4	EDICYCL	OID CUR	VE
	Run user feedrate command (mm/s)	FC10				FC40	FC10	FC20	FC25		FC
	Total interpolated u-points	49641	24822	19859		12413	76275	38169	30563	25499	191
	Parameter completion (reached u-end)	1.00		1.00	1.00	1.00	1.00	1.00	1.00	1.00	191
3	Pushdown epsilon eps(u) algorithm	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1
4	1 1 1 7 9	49641	24822	10050	16549	12413	76275	38061	30413	25200	189
5	Count before pushdown, eps(u) is below (1E-6)	49641	24822	19859	16549	12413	/62/5	108	150	25309 190	189
э	Count pushdown points, eps(u) to below (1E-6)	U	U	U	U	U	U	100	150	190	- 4
	Epsilon eps(u) chord error				0						
6	Count eps(u) above (1E-6)	0			0	0	0	0	0		
7	Count eps(u) in (1E-7, 1E-6)	0		17603	16549	12413	407	820	4011	6679	139
8	Count eps(u) in (1E-8, 1E-7)	49641	17863	2256	0	0	23373	37349	26552	18820	52
	Count eps(u) in (1E-9, 1E-8)	0	0	0	0	0	52495	0	0	0	
10	Count eps(u) in (1E-10, 1E-9)	0		0	0	0	0	0	0	0	
11	Count eps(u) below (1E-10)	0	0	0	0	0	0	0	0	0	
	Count interpolated u-points										
12	Count_rising_S_curve u-points	2483	1242	993	828	621	4437	2219	1775	1479	1:
13	Count_frate is_lower than fratelimit	22363	11171	8936	7449	5586	33349	16686	13352	11144	80
14	Count_frate is_equal to fratelimit	0		0	0	0	0	0	0	0	
	Count frate is higher than fratelimit	22313		8937	7445	5585	35536	17787	14254	11891	9.
	Count falling S curve u-points	2482		993	827	621	2953	1477	1182	985	-
	Count u-points histogram (G01 codes)	2-102	12-71	555	ULT	OLI	2000	2411	1102	000	
17	Count u-points [0.00 <= u < 0.10)	4964	2482	1985	1654	1241	8110	4055	3244	2704	2
	Count u-points [0.00 <= u < 0.10)	4964		1986	1655	1241	4901	2478	2009	1702	1
	,	4964		1986	1655	1241	7391	3696	2957	2464	1
	Count u-points [0.20 <= u < 0.30)	4964		1986	1655	1241	7234	3617	2894	2412	
	Count u-points [0.30 <= u < 0.40)										1
21	Count u-points [0.40 <= u < 0.50)	4964	_	1986	1655	1242	9182	4592	3673	3061	2
_	Count u-points [0.50 <= u < 0.60)	4964		1985	1655	1241	7216	3608	2887	2406	1
_	Count u-points [0.60 <= u < 0.70)	4964	_	1986	1655	1241	9831	4916	3933	3278	2
	Count u-points [0.70 <= u < 0.80)	4964		1986	1655	1241	7525	3763	3010	2508	1
25	Count u-points [0.80 <= u < 0.90)	4964		1986	1654	1242	8801	4401	3521	2935	2
26	Count u-points [0.90 <= u <= 1.00]	4965	2483	1987	1656	1242	6084	3043	2435	2029	1
27	Check Total u-points	49641	24822	19859	16549	12413	76275	38169	30563	25499	19
	Performance										
28	Total curve error (sum of epsilon(u))	0.001094	0.001094	0.002188	0.002735	0.004375	0.00084	0.001642	0.00202	0.00239	0.003
29	Total dist traversed (sum of chord lengths)	496.3786	496.3772	496.3964	496.3757	496.3943	426.2622	426.2622	426.2622	426.2622	426.26
30	Percent (Tot curve error / Tot dist traversed)	0.00022	0.00022	0.000441	0.000551	0.000881	0.000197	0.000385	0.000474	0.000561	0.00
	Circle FC20 curve x[u] versus y[u] Color = Feedrate										
100	'A20-CIRCLE-FC20-data_ngcode.ngc' usin	ng 5:7:3	40	100		Astepi FC		sus y[u] Color = Fe EPI-FC20-data_ng		5:7:3	40
50		ng 5:7:3	40 35 30	100		Astepi FC:				5:7:3	40 - 35 - 30
		ng 5:7:3	35			Astepi FC:				5.7.3	35
50 -		99 5:7:3	35 30 25 20	50		Astepi FC:				5.7.3	35 30 25 20

Figure 1.2: Circle and Ast Epi run data summary

	Author: wruslandr@gmail.com	Fait 4 UI) paramet	ric curves	3			
ΓEΜ	DESCRIPTION			SHELL C					HYPOTR	OCOID CL	JRVE
1	Run user feedrate command (mm/s)	FC10	FC20	FC25	FC30	FC40	FC10	FC20	FC25	FC30	FC
2	Total interpolated u-points	15621	9883	8935	8370	7766	38672	20223	16618	11497	88
3	Parameter completion (reached u-end = 1.00)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	0.706104	0.7035
	Pushdown epsilon eps(u) algorithm									***	***
4	Count before pushdown, eps(u) is below (1E-6)	12245	5010	3569	2671	1592	37227	18167	14266	0	
5	Count pushdown points, eps(u) to below (1E-6)	3376	4873	5366	5699	6174	1445	2056	2352	0	
	Epsilon eps(u) chord error										
6	Count eps(u) above (1E-6)	0	0	0	0	0	0	0	0	0	
7	Count eps(u) in (1E-7, 1E-6)	7893	9323	8935	8370	7766	4106	6971	9900	0	
8	Count eps(u) in (1E-8, 1E-7)	7728	560	0	0	0	24178	13252	6718	0	
	Count eps(u) in (1E-9, 1E-8)	0	0	0	0	0	10388	0	0	0	
10	Count eps(u) in (1E-10, 1E-9)	0			0		0	0			
	Count eps(u) below (1E-10)	0			0	0	0	0	0	0	
	Count interpolated u-points	-	-	-	-	-	-	-	-	-	
12	Count rising S curve u-points	2320	1161	929	774	581	3177	1589	1272	0	
	Count frate is lower than fratelimit	11722	6605	5826	5386		18305	9773		0	
	Count_frate is_equal to fratelimit	0			0		0	0		0	
	Count_frate is_equal to fratelimit	1210		1811	1859		14859	7695	_	0	
16	Count_falling_S_curve_u-points	369	370	359	369	369	2331	1166		0	
10	Count u-points histogram (G01 codes)	309	3/0	339	309	309	2331	1100	933	***	**
17	Count u-points fistogram (GO1 codes) Count u-points [0.00 <= u < 0.10)	4435	2210	1774	1.470	1100	4631	2217	1856	1563	
	Count u-points (0.00 <= u < 0.10) Count u-points (0.10 <= u < 0.20)	3237	2218 1619		1479 1080		8961	2317 4480		2987	1
	, ,										
	Count u-points [0.20 <= u < 0.30)	2054			796		6140	3074		2072	1
	Count u-points [0.30 <= u < 0.40)	1312	714	710	711	711	2960	1526		1086	
	Count u-points [0.40 <= u < 0.50)	881	629	629	629		4860	2431	1945	1620	1
	Count u-points [0.50 <= u < 0.60)	657	628	628	629		3973	1987	1589	1325	
	Count u-points [0.60 <= u < 0.70)	710	711	711	710		1324	841	769	732	
	Count u-points [0.70 <= u < 0.80)	794	794	794	794		794	794		112	
25	Count u-points [0.80 <= u < 0.90)	791	791	792	792	792	1141	828	798	0	
	Count u-points [0.90 <= u <= 1.00]	750	751	750	750		3888	1945	1556	0	
27	Check Total u-points	15621	9883	8935	8370	7766	38672	20223	16618	11497	8
	Performance										
28	Total curve error (sum of epsilon(u))	0.005115	0.00627	0.006558	0.006764	0.007046	0.002847	0.004003	0.004459	0	
29	Total dist traversed (sum of chord lengths)	138.5595	138.5614	138.5607	138.5602	138.5599	478.9871	478.9987	479.0064	0	
30	Percent (Tot curve error / Tot dist traversed)	0.003692	0.004525	0.004733	0.004882	0.005085	0.000594	0.000836	0.000931	0	
10 -	Snallshell FC20 curve x[u] versus y[u] Color = Feedrate		40		s	nailshell + Hypotre					40
10	Snallshell FC20 curve x[u] versus y[u] Color = Feedrate 'A20-SNAILSHELL-FC20-data_ngcode.ngc' using	5:7:3	40	100	s	nailshell + Hypotre			Color = Feedrate	5:7:3	40
10		5:7:3	40	100	s	nailshell + Hypotro				5:7:3	40
		5:7:3	40	100	s	nailshell + Hypotre				57.3	
		5:7:3 ——		100	s	nailshell + Hypotri				5:7:3	
30		5:7:3	35	100	s	nailshell + Hypotri				5:7:3	35
30		5.7.3		100	s	nailshell + Hypotri				5:7:3	35
30		5:7:3	35		S	nailshell + Hypotre				5:7:3	35
20		15:7:3	35		s	nailshell + Hypotre				5.7.3	35 30
20		5:7:3	35		s	nailshell + Hypotri				5773	35 30
20		15:73	35	50 -	S	nailshell + Hypotri				i-7.3	35 30
20		15:7:3	35	50 -	S	nalishell + Hypotr				57.3	35 30 25
20		5:7:3	35	50	S	nailshell + Hypotro				57.3	35 30 25
20		15:7:3	= 35 = 30 = 25 = 20	50 -	S	nailshell + Hypotro				57.3	35 30 25 20
20		5:73	35	50 -	s	nailshell + Hypotre				57.3	35 30 25 20
20		15:7:3	= 35 = 30 = 25 = 20	50 -	S	nailshell + Hypotr				57.3	35 30 25 20
0		15.7.3	35 30 25 20	50 -	S	nalishell + Hypotr				57:3	35 30 25 20
0		5:73 —	= 35 = 30 = 25 = 20	50 · · · · · · · · · · · · · · · · · · ·	S	nailshell + Hypotro				57.3	35 30 25 20
220		15:7:3	35 30 25 20	50 · · · · · · · · · · · · · · · · · · ·	S	nailshell + Hypotr				57.3	35 30 25 20
110		15.7.3 ——	35 30 25 20 15	50 · · · · · · · · · · · · · · · · · · ·	S	nailshell + Hypotr				57.3	35 30 25 20
0		15.7.3	35 30 25 20	50 · · · · · · · · · · · · · · · · · · ·	S	nalishell + Hypotr				57:3	25 20 10 10 10 10 10 10 10 10 10 10 10 10 10
0		5:7:3 —	35 30 25 20 15	50 · · · · · · · · · · · · · · · · · · ·	S	nailshell + Hypotro				57.3	25 20 10 10 10 10 10 10 10 10 10 10 10 10 10
0		5.7.3	- 35 - 30 - 25 - 20 - 15 - 10	50 - 50 - 50 -	S S	nailshell + Hypotre		YP-Fc20-data_ng		57:3	25 20 10 10 10 10 10 10 10 10 10 10 10 10 10

Figure 1.3: Snailshell and SnaHyp run data summary

	Author: wruslandr@gmail.com	Part 5 of				DL (x-y) pa	arametric				
ΓEΜ	DESCRIPTION		RIBB	ON-10L C	URVE			RIBBO	N-100L C	URVE	
1	Run user feedrate command (mm/s)	FC10	FC20	FC25	FC30	FC40	FC10	FC20	FC25	FC30	FC
2	Total interpolated u-points	7351	7352	7352	7353	7353	7480	7348	7349	7349	73
3	Parameter completion (reached u-end)	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.
	Pushdown epsilon eps(u) algorithm										
4	Count before pushdown, eps(u) is below (1E-6)	0	0	0	0	0	919	0	0	0	
5	Count pushdown points, eps(u) to below (1E-6)	7351	7352	7352	7353	7353	6561	7348	7349	7349	73
	Epsilon eps(u) chord error										
6	Count eps(u) above (1E-6)	0	0	0	0	0	0	0	0	0	
7	Count eps(u) in (1E-7, 1E-6)	7351	7352	7352	7353	7353	7480	7348	7349	7349	73
8	Count eps(u) in (1E-8, 1E-7)	0	0	0	0	0	0	0	0	0	
9	Count eps(u) in (1E-9, 1E-8)	0	0	0	0	0	0	0	0	0	
10	Count eps(u) in (1E-10, 1E-9)	0	0	0	0	0	0	0	0	0	
11	Count eps(u) below (1E-10)	0	0	0	0	0	0	0	0	0	
	Count interpolated u-points										
12	Count rising S curve u-points	370	370	370	370	370	436	370	370	370	- ;
13	Count_frate is_lower than fratelimit	3491	3310	3310	3308	3309	5562	3939	3733	3545	3
14	Count frate is equal to fratelimit	0		0	0	0	0	0		0	
15	Count_frate is_higher than fratelimit	3121	3303	3303	3305	3305	1047	2670	2877	3065	3
16	Count falling S curve u-points	369	369	369	370	369	435	369	369	369	
	Count u-points histogram (G01 codes)		230		0.0		.50				
17	Count u-points [0.00 <= u < 0.10)	749	749	749	749	749	815	748	748	748	
18	Count u-points [0.10 <= u < 0.20)	791	792	792	792	792	791	792	792	792	
19	Count u-points [0.20 <= u < 0.30)	795	794	794	794	794	794	794	794	794	
20	Count u-points [0.30 <= u < 0.40)	711	711	711	711	712	711	711	711	711	
21	Count u-points [0.40 <= u < 0.50)	629	629	629	630	629	629	628	629	629	
22	Count u-points [0.50 <= u < 0.60)	629	630	630	629	629	628	629	628	629	
23	Count u-points [0.60 <= u < 0.70)	711	711	711	711	711	711	711	712	711	
24	Count u-points [0.70 <= u < 0.70)	794	711	794	795	795	711	794	794	711	
2 4 25		794	794	794	795	795	794	794	794	794	
26	Count u-points [0.80 <= u < 0.90)	750	750	750	751	750	816	750	750	750	
27	Count u-points [0.90 <= u <= 1.00]										
21	Check Total u-points	7351	7352	7352	7353	7353	7480	7348	7349	7349	7
28	Performance Total curve error (sum of epsilon(u))	0.007222	0.007221	0.00722	0.007221	0.00722	0.007227	0.007224	0.007335	0.007224	0.007
										0.007334	
29	Total dist traversed (sum of chord lengths)									152.1103	
30	Percent (Tot curve error / Tot dist traversed)	0.048201	0.048194	0.048195	0.048185	0.048187	0.004752	0.004822	0.004821	0.004821	0.00
10 -	Ribbon-10L FC20 curve x[u] versus y[u] Color = Feedrate		40	60 -		Ribbon-100L F	C20 curve x[u] v	ersus y[u] Color =	Feedrate		40
10	Ribbon-10L FC20 curve x[u] versus y[u] Color = Feedrate 'A23-RIBBON10L-FC20-data_ngcode.ngc' usin	g 5:7:3 ———	40	60	!	Ribbon-100L F			Feedrate code.ngc' using 5	7:3 ——	40
10		g 5:7:3 ———	40	60		Ribbon-100L f				7:3	40
10		g 5:7:3 ———	40			Ribbon-100L F				7:3	40
10		g 5:7:3 ———		60		Ribbon-100L F				7:3	40
10		g 5:7:3 ——				Ribbon-100L F				7.3	40 - 35 - 30
		g 5:7:3	35			Ribbon-100L F				7.3 —	
		y 5:7:3	35			Ribbon-100L F				73	30
		95:7:3	35	40 -		Ribbon-100L F				7.3	
		95:7:3	35	40 -		Ribbon-100L F				7.3	30
5 —		y 5:7:3 ——	35 30 25	40 -		Ribbon-100L I				7.3	30 25
5 —		y 5.7.3	35	40 -		Ribbon-100L f				7.3	30
5 —		957.3 —	35 30 25	40 -		Ribbon-100L f				933	30 25
		95.7.3 ——	35 30 25	40 -		Ribbon-100L 1				73	30 25
5 -		95.7.3	35 30 25 20	40 -		Ribban-100L I				73 —	30 25 20
5 —		35.7.3	35 30 25 20	40 - 20 - [n]/keod		Ribban-100L f				73	30 25 20
0		g 5.7.3 ———————————————————————————————————	35 30 25 20	40 - 20 - [n]/keod		Fibbon-100L f				73	30 25 20
5 —		957.3	35 30 25 20	40 - 20 - [n]/keod		Ribbon-100L I				73	30 25 20
5		957.3	35 30 25 20 15	40 - 20 - [n]/keod		Ribban-100L I				73	30 25 20 - 15
0 -		J 5.7:3 ——	35 30 25 20	20 - 10 - 20 - 20 - 20 - 20 - 20 - 20 -		Ribban-100L f				73 —	30 25 20
5		35.7.3	35 30 25 20 15	20 - 10 - 20 - 20 - 20 - 20 - 20 - 20 -		Ribban-100L f				73	30 25 20 15
5		95.7.3	35 30 25 20 15	20 - 10 - 20 - 20 - 20 - 20 - 20 - 20 -		Fibbon-100L f				73	30 25 20 15

Figure 1.4: Ribbon-10L and Ribbon-100L run data summary

1.1.1 Teardrop parametric equation

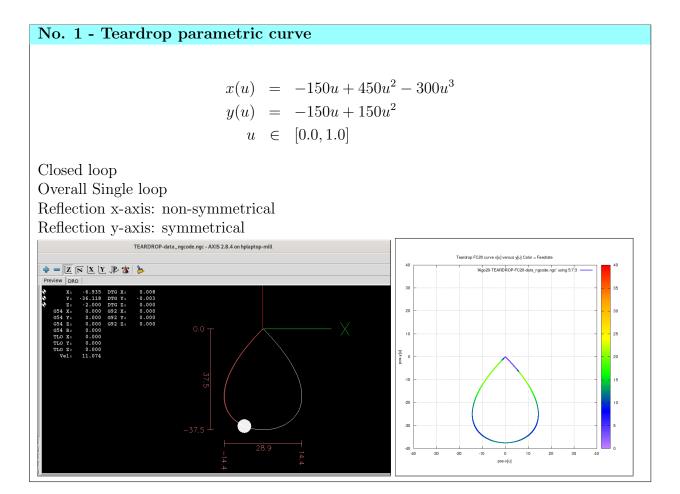


Table 1.1: Teardrop parametric equation and dimensions

1.1.2 Butterfly parametric equation

No. 2 - Butterfly parametric curve $x(u) = \sin(2\pi u) \left[e^{\cos(2\pi u)} - 2\cos(8\pi u) - (\sin(2\pi u/12))^5\right]$ $y(u) = \cos(2\pi u) \left[e^{\cos(2\pi u)} - 2\cos(8\pi u) - (\sin(2\pi u/12))^5\right]$ $u \in [0.0, 1.0]$ Closed loop Overall Multiple loops Reflection x-axis: non-symmetrical Reflection y-axis: symmetrical Reflection y-axis: symmetrical

Table 1.2: Butterfly parametric equation and dimensions

1.1.3 Ellipse parametric equation

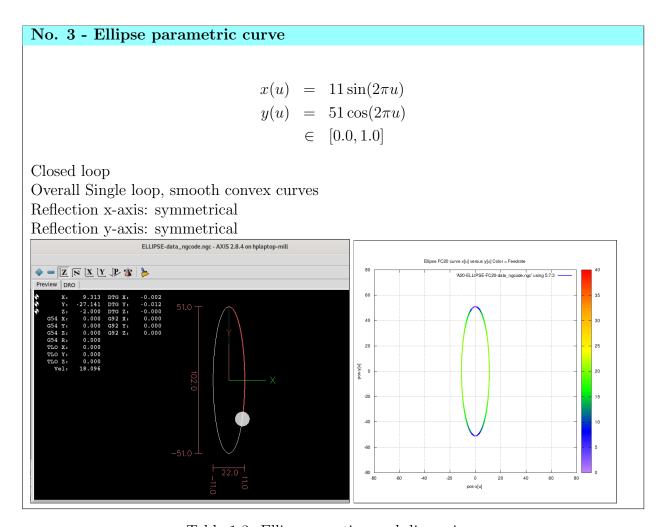


Table 1.3: Ellipse equation and dimensions

1.1.4 Skewed-Astroid parametric equation

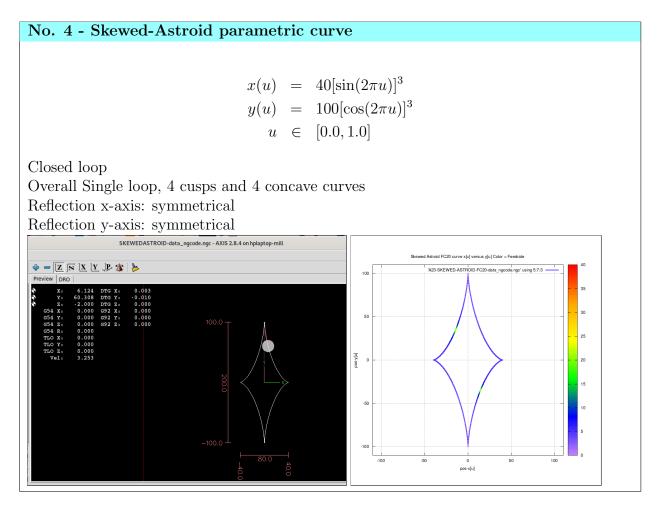


Table 1.4: Skewed-Astroid and dimensions

1.1.5 Circle parametric equation

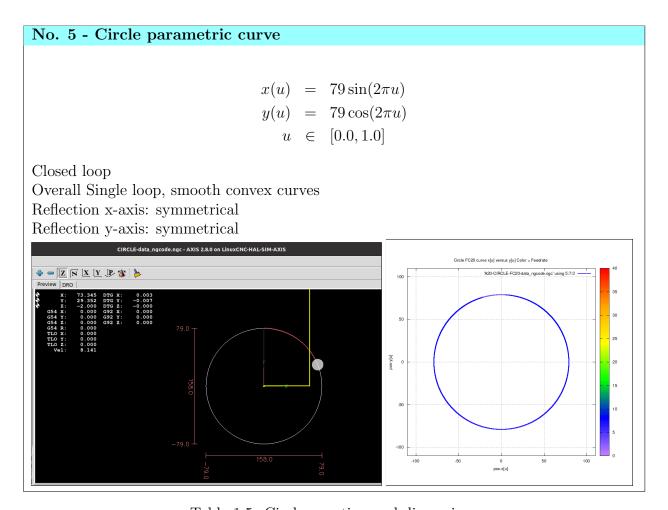


Table 1.5: Circle equation and dimensions

1.1.6 AstEpi parametric equation

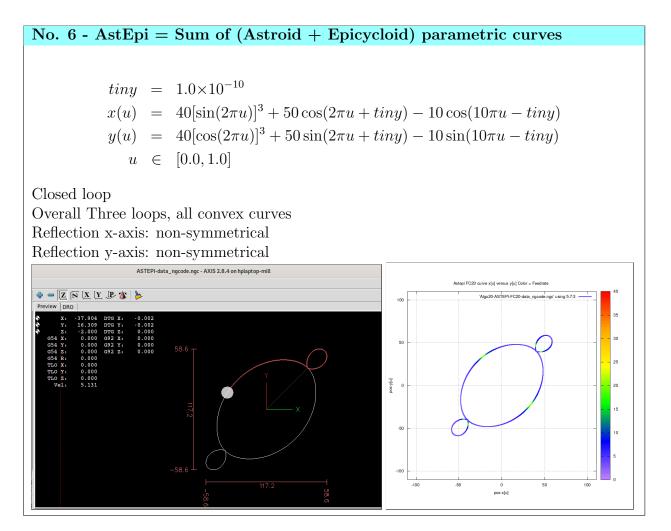


Table 1.6: Astepi equation and dimensions

1.1.7 Snailshell parametric equation

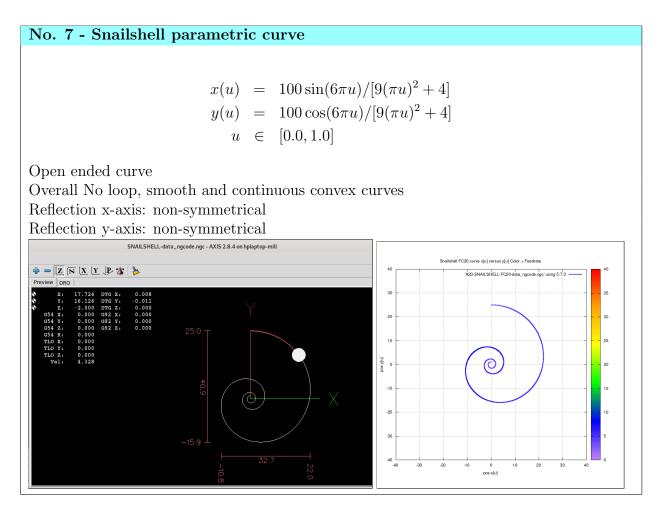


Table 1.7: Snailshell equation and dimensions

1.1.8 SnaHyp parametric equation

No. 8 - SnaHyp = Sum of (Snailshell + Hypotrocoid) parametric curves $xsna(u) = [4\sin(8\pi u)]/[16(\pi u)^2 + 4]$ $xhyp(u) = [2\cos(4\pi u) + 5\cos(8\pi u/3)]$ x(u) = 10[xsna(u) + xhyp(u)] $ysna(u) = [10\cos(8\pi u)]/[16(\pi u)^2 + 4]$ $yhyp(u) = [2\sin(8\pi u) - 5\sin(8\pi u/3)]$ y(u) = 10[ysna(u) + yhyp(u)] $u \in [0.0, 1.0]$ Open ended curve Overall 1 loop, except for 1 concave curve, the rest are convex curves Reflection x-axis: non-symmetrical Reflection y-axis: non-symmetrical $x = x\sin(\pi u) + x\cos(\pi u) + x\cos($

Table 1.8: SnaHyp equation and dimensions

1.1.9 Ribbon-10L parametric equation

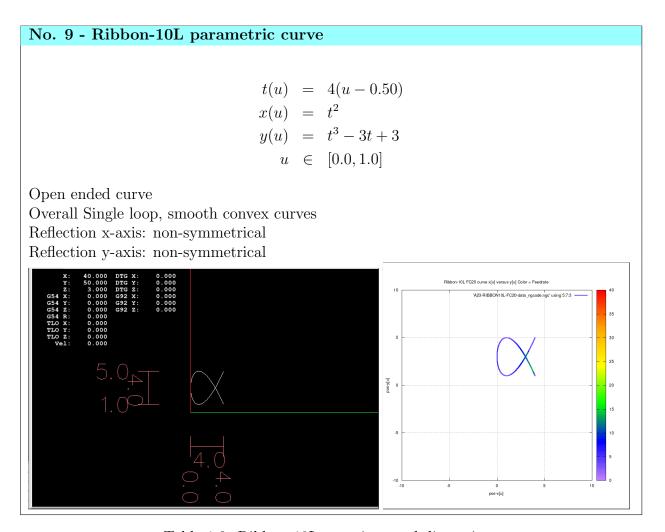


Table 1.9: Ribbon-10L equations and dimensions

1.1.10 Ribbon-100L parametric equation

No. 10 - Ribbon-100L parametric curve t(u) = 4(u - 0.50) $x(u) = 10t^2$ $y(u) = 10t^3 - 30t + 30$ $u \in [0.0, 1.0]$ Open ended curve (10 times larger than RIBBON-10L) Overall Single loop, smooth convex curves Reflection x-axis: non-symmetrical Reflection y-axis: non-symmetrical Reflection y-axis: non-symmetrical

Table 1.10: Ribbon-100L equation and dimensions

1.2 Experimental Run Results

Bismillah

Describe the Table FC10, FC, 20, FC25, FC30 and FC40

1.2.1 Teardrop and Butterfly Run Data

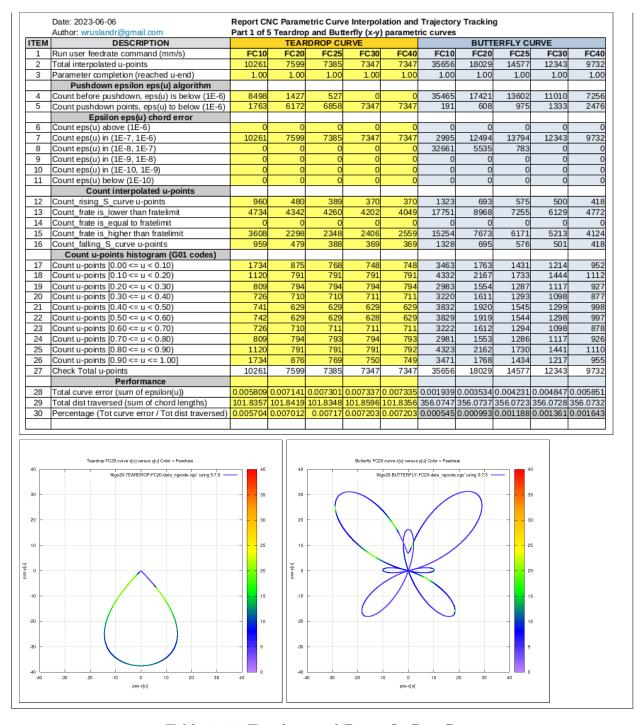


Table 1.11: Teardrop and Butterfly Run Data

Bismillah Allah huakbar

1.2.2 Ellipse and Skewed-Astroid Run Data

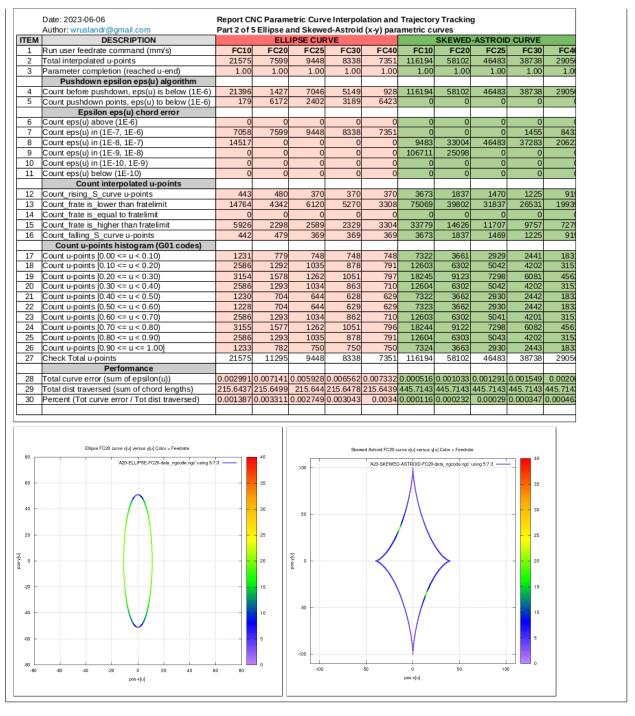


Table 1.12: Ellipse and Skewed-Astroid Run Data

1.2.3 Circle and Astepi Run Data

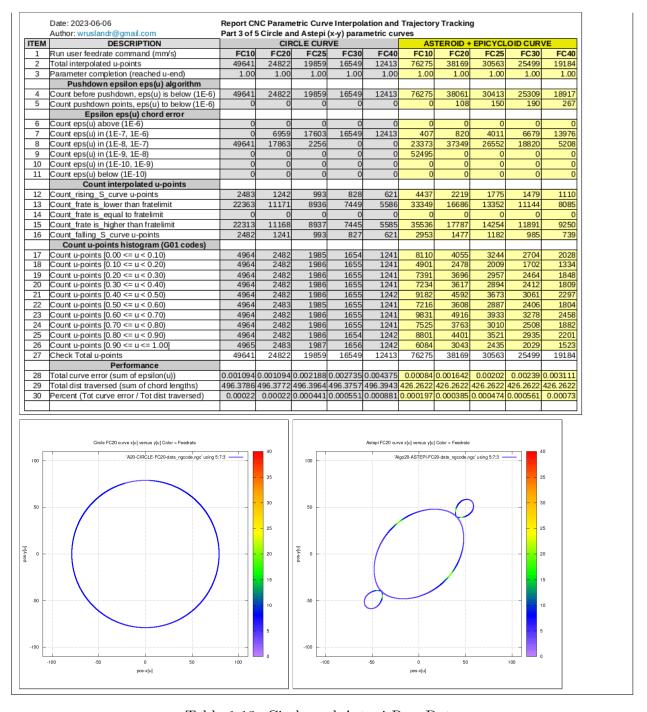


Table 1.13: Circle and Astepi Run Data

1.2.4 Snailshell and SnaHyp Run Data

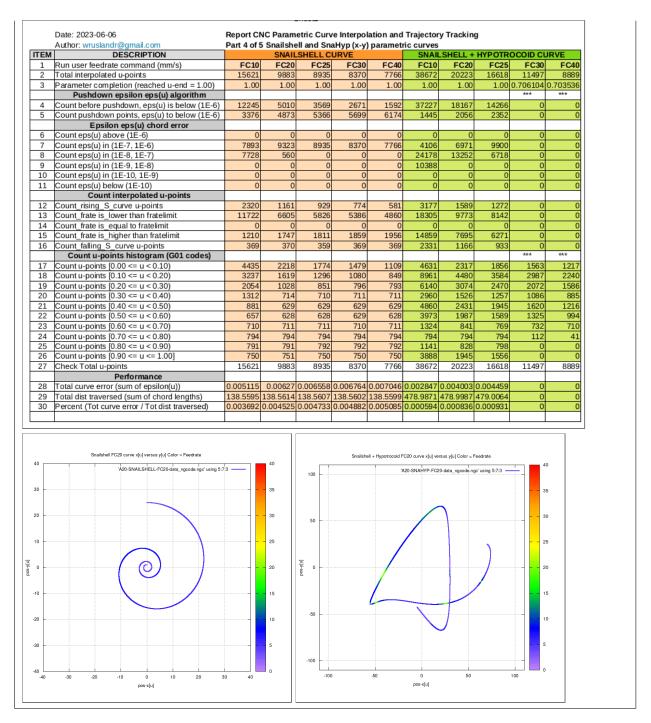


Table 1.14: Snailshell and SnaHyp Run Data

1.2.5 Ribbon-10L and Ribbon-100L Run Data

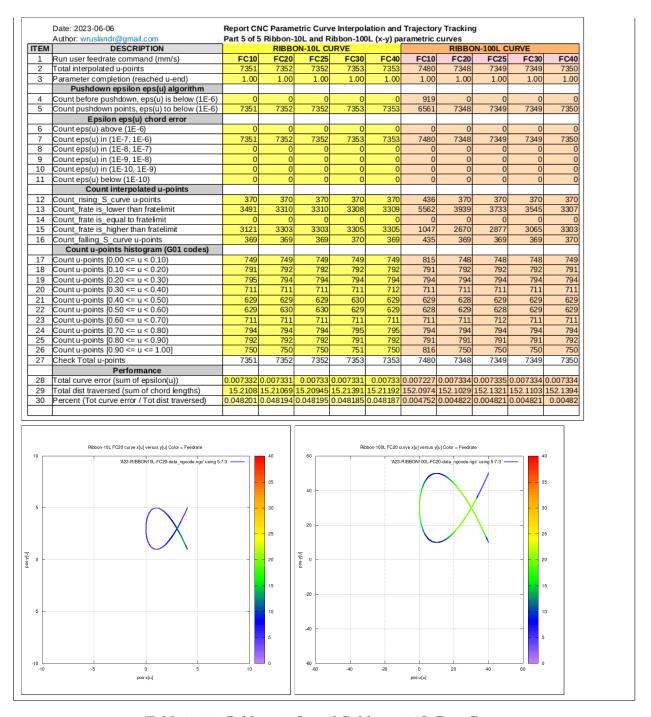


Table 1.15: Ribbon-10L and Ribbon-100L Run Data