Sheet1

Report CNC Parametric Curve Interpolation and Trajectory Tracking Part 1 of 5 Teardrop and Butterfly (x-y) parametric curves

Author: wruslandr@gmail.com

Date: 2023-06-06

ITEM	DESCRIPTION	TEARDROP CURVE					BUTTERFLY CURVE					
	Run user feedrate command (mm/s)	FC10 FC20 FC25 FC30 FC40										
2	Total interpolated u-points	10261	7599	7385	7347	7347	35656	18029	14577	12343	9732	
	Parameter completion (reached u-end)	1.00	1.00	1.00	1.00	1.00		1.00	1.00			
	Pushdown epsilon eps(u) algorithm	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	1.00	
4	Count before pushdown, eps(u) is below (1E-6)	8498	1427	527	0	0	35465	17421	13602	11010	7256	
5	Count pushdown points, eps(u) to below (1E-6)	1763	6172	6858	7347	7347	191	608	975		2476	
6	Check Total u-points	10261	7599	7385	7347	7347	35656	18029	14577	12343	9732	
	Epsilon eps(u) chord error											
7	Count eps(u) above (1E-6)	0	0	0	0	0	0	0	0	0	0	
8	Count eps(u) in (1E-7, 1E-6)	10261	7599	7385	7347	7347	2995	12494	13794	12343	9732	
9	Count eps(u) in (1E-8, 1E-7)	0	0	0	0	0	32661	5535	783	0	0	
10	Count eps(u) in (1E-9, 1E-8)	0	0	0	0	0	0	0	0	0	0	
11	Count eps(u) in (1E-10, 1E-9)	0	0	0	0	0	0	0	0	0	0	
12	Count eps(u) below (1E-10)	0	0	0	0	0	0	0	0	0	0	
13	Check Total eps(u) points	10261	7599	7385	7347	7347	35656	18029	14577	12343	9732	
	Count interpolated u-points											
14	Count_rising_S_curve u-points	960	480	389	370	370	1323	693	575	500	418	
15	Count_frate is_lower than fratelimit	4734	4342	4260	4202	4049	17751	8968	7255	6129	4772	
16	Count_frate is_equal to fratelimit	0	0	0	0	0	0	0	0	0	0	
17	Count_frate is_higher than fratelimit	3608	2298	2348	2406	2559	15254	7673	6171	5213	4124	
18	Count_falling_S_curve u-points	959	479	388	369	369	1328	695	576	501	418	
19	Check Total u-points	10261	7599	7385	7347	7347	35656	18029	14577	12343	9732	
	Count u-points histogram (G01 codes)											
	Count u-points [0.00 <= u < 0.10)	1734	875	768	748	748		1763	1431	1214	952	
21	Count u-points [0.10 <= u < 0.20)	1120	791	791	791	791	4332	2167	1733	1444	1112	
22	Count u-points [0.20 <= u < 0.30)	809	794	794	794	794	2983	1554	1287	1117	927	
24	Count u-points [0.30 <= u < 0.40)	726	710	710	711	711	3220	1611	1293	1098	877	
25	Count u-points [0.40 <= u < 0.50)	741	629	629	629	629	3832	1920	1545	1299	998	
26	Count u-points [0.50 <= u < 0.60)	742	629	629	628	629		1919	1544	1298	997	
27	Count u-points [0.60 <= u < 0.70)	726	710	711	711	711	3222	1612	1294	1098	878	
28	Count u-points [0.70 <= u < 0.80)	809	794	793	794	793		1553	1286		926	
29	Count u-points [0.80 <= u < 0.90)	1120	791	791	791	792		2162	1730		1110	
30	Count u-points [0.90 <= u <= 1.00]	1734	876	769	750	749		1768	1434		955	
31	Check Total u-points	10261	7599	7385	7347	7347	35656	18029	14577	12343	9732	
32	Total curve error (sum of epsilon(u))						0.001939					
33	Total dist traversed (sum of chord lengths)	101.835	101.841	101.834	101.859	101.835	356.0747	356.073	356.072	356.072	356.073	

Sheet1

Notes and remarks										
Pushdown or reducing eps(u) algorithm means reducing chord length, thus reduces u_next and so results in generation of more interpolated upoints. See row Item(7). None of the eps(u) values exceed (1E-6).	feedrate t net feedra	o follow th	e calculate	ed feedrate	e limit, an	d stay just	below this	s feedrate	limit. The	
	(C1) Absolute constraint not to exceed the user feedrate command, example FC20 (20 mm/s),									
	(C2) Constrain the feedrate to stay within the velocity range (min, max) allowable for the CNC									
	(C3) Constraint the feedrate to have chord error eps(u) absolutely below tolerance (1E-6) mm, as tracks the curve trajectory, See row Item(7).								mm, as it	
	(C4) Constraint feedrate such that the normal acceleration (not tangential) stay wit acceleration range (min, max) allowable for the CNC machine.							within the		
	sometime	s the curre	ent feedrat	e at point	u maybe l	nigher than	n fratelimit	calculated		taneously, bint u. Our atelimit.