Tasks for "Nuclear density functional theory: Shapes and radii"

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(Dated: November 2022)

In this set of training exercices, you will study the deformation and root-mean-square (rms) radii of Uranium isotopes with nuclear energy density functionals. You will explore the link between deformation and nuclear radii by repeatedly solving the mean-field equations for different shapes and different nuclei for the time-tested SLy4 parameterization of the Skyrme EDF [1]. To do this, you will employ the EV8 code of Refs. [2, 3], which solves the Skyrme-HF+BCS equations on a three-dimensional code mesh. You will learn how to (i) initialize and run the code, (ii) judge its convergence and (iii) understand its outputs regarding total energy and nuclear shape.

I. PRELIMINARY THINGS

1. Get the code and all auxiliary files from https://github.com/wryssens/EV8. The `ev8` and `nil8` codes can be found in codes/, the relevant files for this training in LISA-training/.

2. Create a clean directory and copy the `ev8.f`, `nil8.f`, and `compile.sh` files there.

3. In order to compile the code, we will use the `compile.sh` bash script.

   - Verify that you have a FORTRAN compiler such as `gfortran` installed.
   - Optional: if you wish to use a compiler that is not `gfortran` , you should modify the script.
   - Execute the script and verity that you now also have `ev8.exe` and `nil8.exe` in your working directory.

4. Inspect the param8.h file. It tells you that we have compiled the code(s) to work with a Cartesian mesh with $mx = my = 10$ points in the x- and y-directions and $mz = 14$ in the z-direction, with a $dx = 1.0$ fm spacing. These conditions are such that a typical EV8 can be done in 1-2 minutes on a modern personal laptop. Since we will run the code many different nuclei, the total numerical effort will still be non-negligible. If you want to reduce the required effort further, I suggest you concentrate on $^{218-234-236-238-276}$U, and calculate only a few isotopes between $A = 218 - 234$.

5. However, the numerical conditions are not good enough to accurately represent large atomic nuclei like Uranium isotopes, particularly for their total energy. Those of you that want to do more realistic calculations can set $mx = my = mz = 18$, $dx = 0.8$ fm and $mw = 300$, but you should be prepared for long CPU times.

6. The basic operation of both `nil8` and `ev8` is the following

   ```
   ./code.exe < input.data > output.out
   ```

   where `input.data` is an input file you prepared and `output.out` is a file where you want to save the output. For the creation of the input data, I provide examples for both nil8 and ev8. For each of these, you should modify only the relevant parts. As we will be running the code several times for different nuclei in different conditions, I strongly recommend that you (i) write a bash script to automate multiple code runs for multiple nuclei and (ii) choose a clear labelling scheme for the output files.

7. Aside from the input and output, running `nil8` also requires the presence of a file named `fort.12` in the working directory. This file contains a nuclear configuration and determines the starting guess of the self-consistent iterations. `nil8` serves to generate this starting point and will create a file named `fort.13`. It is sufficient to rename this file to `fort.12` to be able to start `ev8`. As an optional challenge, consider automating the gathering of information from the output files using, for example, the 'grep' bash command.

8. For more practical information on the code and its inputs, you can always refer to the slides of the training or the published papers, Ref. [2] and particularly the later sections in Ref. [3]. When you are truly stuck, you can always ask me at wryssens@ulb.be.

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II.   TASKS

1. Run `nil8` twice: once taking `nil8.prolate.data` and once taking `nil8.oblate.data` as input. These inputs tell the code to initialize a nucleus with a prolate and oblate shape, respectively. After each run, verify that the code created a `fort.13` file and rename it with an appropriate name.

2. Run `ev8` twice for ^{238}U, each time for 100 iterations, starting from the starting guesses generated in the previous step. Copy the parameters from `EV8.example.data` and modify the iteration numbers and particle number(s) accordingly. Verify that you are dealing with a prolate shape and an oblate shape depending on the initialization. Did these calculations converge? Repeat these calculations for larger amounts of iterations, until you are satisfied with their convergence. Which configuration is the ground state? Look up the binding energy of ^{238}U [4]. How close is the calculation to the experimental value in absolute and relative terms?

3. Now perform two similar calculations for very exotic proton-rich ^{218}U. What shapes do you obtain? Do calculations started from prolate/oblate configurations give different results? Did you expect this outcome?

4. Moving to the other extreme of neutron-rich nuclei, repeat similar calculations for ^{276}U. What do these results make you suspect about this particular number of neutrons?

5. Let us now do things a bit more systematically. Initializing everything with a prolate shape, perform a calculation for all even-even Uranium isotopes from ^{220}U up to ^{236}U. Combining these results with those you obtained for the ground states of ^{218}Pu and ^{238}U, make separate plots of the following quantities as a function of neutron number: (i) rms proton radii, (ii) isotopic shifts with respect to ^{238}U and (iii) quadrupole deformation. Include experimental information on the radii and isotopic shifts from Ref. [5] and experimental information on the quadrupole deformation from Ref. [6]. Which one is better described, the rms charge radii or the isotopic shift? Does this change if you correct for the finite size of the proton? Is the quadrupole deformation well described?

6. Plot the hexadecapole (β_{40}) and hexacontetrapole (β_{60}) deformation as a function of the neutron number. Do you think these contribute meaningfully to the charge radius?

7. What about the neutron rms radii? Do they differ strongly from the charge radii? Plot the difference of the neutron and proton radii, also known as the 'neutron skin', as a function of neutron number. Are there also significant differences between the quadrupole deformation of protons and neutrons?

8. Repeat question 5, but this time initialize the calculations with oblate shapes. Make a combined plot with (i) the charge radii for the prolate solutions and (ii) the charge radii for the oblate solutions. What do you conclude?

Optional questions:

- Mapping the shell closures: perform calculations for all even-even nuclei from ^{212}U to ^{282}U. How do the charge radii behave?

- How do any of these results depend on the interaction? Change the parameterization from SLy4 to SLyIII$_{0.7}$ (`EV8` keyword= 'SLyIII0.7'), and redo the calculations and plots of question 5.

Caution: answering these additional questions will cost you a significant amount of CPU time on a typical laptop!

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