## lab 13

## 2025-06-23

```
#13.1 and 13.2 model
data = putts_train %>%
mutate(
  m1 = mean(X),
  m2 = X
)
#EF1
data = data %>%
mutate(
  EF1 = {
    C = mean(X)*(1 - mean(X))
     sig = sqrt(C/N)
    xi_ = X/sig
    x_bar = mean(xi_)
    s2x_ = sum((xi_ - x_bar)^2)
    theta = x_bar + (1 - (n() - 1)/s2x_) * (xi_ - x_bar)
    theta * sig
  }
 )
#EF2
data = data %>%
 mutate(
   EF2 = {
     H = X * N
     num = H + 3/8
     denom = N + 3/4
     X2 = asin(sqrt(num / denom))
     nu = 1 / (2 * sqrt(N))
     X3 = X2 / nu
     x_bar = mean(X3)
      s2x_ = sum((X3 - x_bar)^2)
      theta = x_bar + (1 - (n() - 1)/s2x_) * (X3 - x_bar)
     sin(nu * theta)^2
    }
  )
#EB1
data = data %>%
 mutate(
EB1 = {
```

```
C = mean(X) * (1 - mean(X))
      u = m1
     tau2 = var(X) - (C/mean(N))
     u + (tau2)*(X-u)/(tau2 + C/N)
  )
#EB2
data <- data %>%
 mutate(
   EB2 = {
     H = X * N
     X2 = asin(sqrt((H + 3/8) / (N + 3/4)))
     nu2 = 1 / (4 * N)
     mu = mean(X2)
     tau2 = var(X2) - mean(nu2)
     shrink = tau2 / (tau2 + nu2)
      theta = mu + shrink * (X2 - mu)
     sin(theta)^2
    }
 )
```

```
## model mse
## 1 EB2 0.0006213173
## 2 EB1 0.0006221690
## 3 m1 0.0007470204
## 4 EF1 0.0008291139
## 5 EF2 0.0008637432
## 6 m2 0.0008902228
```

Bayes by far the best, with simple estimate=x the worst

