

indexes

# Observation 1 (from sequence)

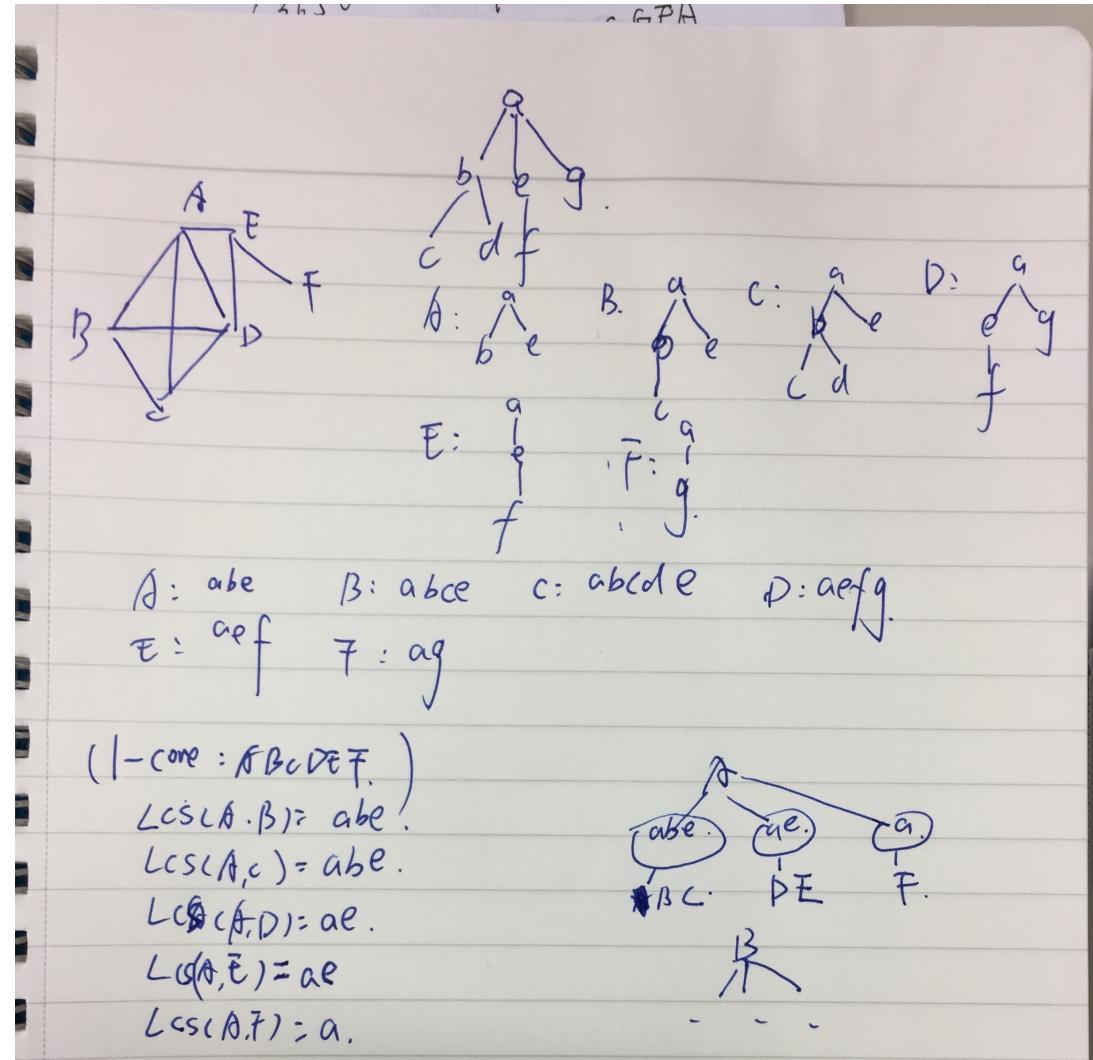
- In a k-core, if we first compute all maximal frequent( $\text{sup}=k$ ) subsequence, then use query vertex  $q$  to compute intersection. Finally we will get the maximal common subsequence shared by  $q$ .
- E.g., in a 2-core:{Q: ab, A: abcdef, B: abcde, C:cdef , D:abct}.
  - All maximal frequent ( $\text{sup}=2$ ) subsequence  $S_{max1}$ =“cde” shared by ABC.  $S_{max2}$ =“abc” shared by ABD.
  - Then  $S_Q \cap S_{max1} = \emptyset$ ,  $S_Q \cap S_{max2}$ =“ab” shared by QABC.

# One strategy(index 1)

- Step 1: Compute all k-cores.
- Step 2: For each k-core, pre-compute all maximal frequent ( $\text{sup}=k$ ) subsequences and store it.
- While querying, get intersection with them.

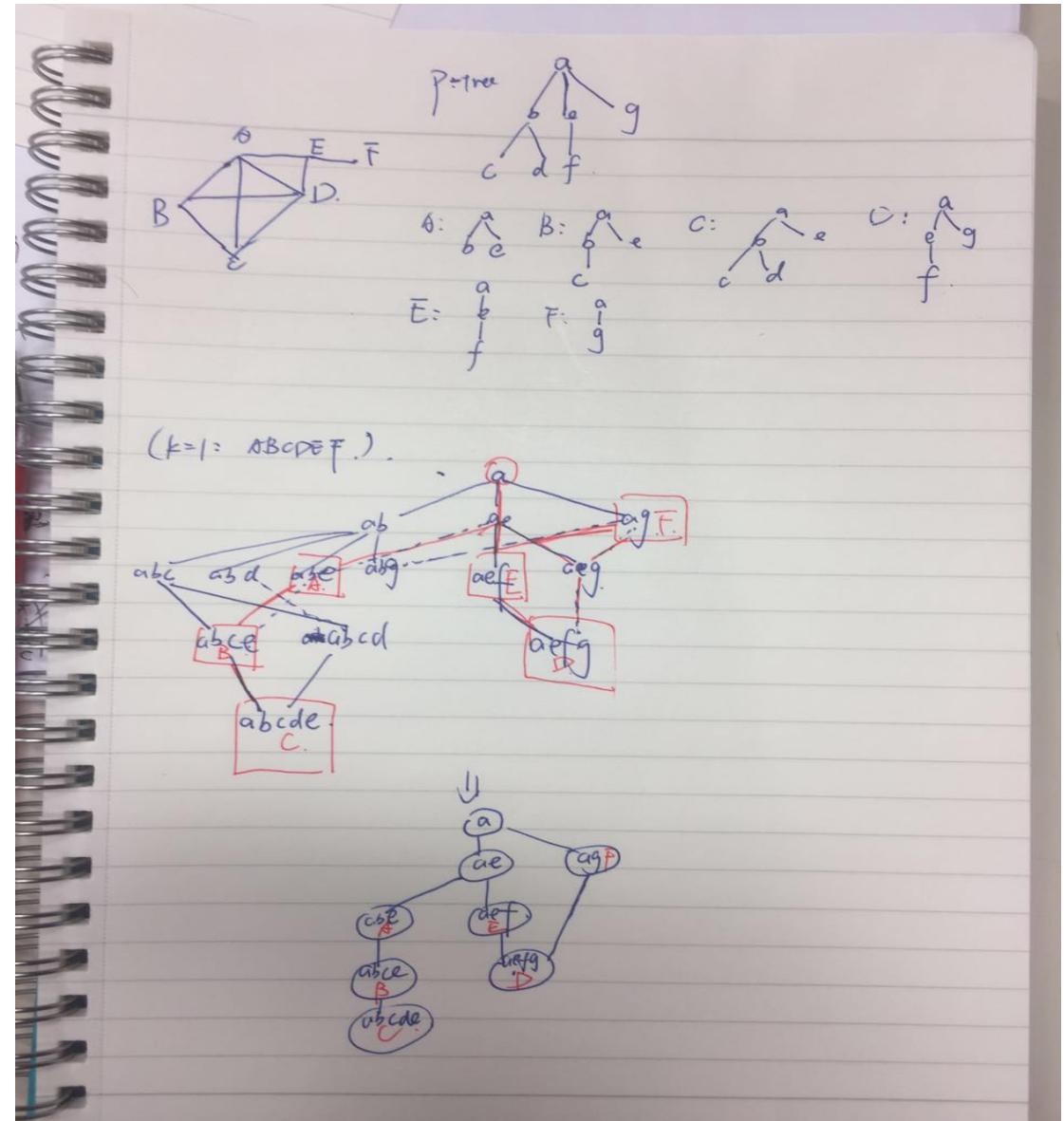
# Trade-off

- In step 2: For each k-core, pre-compute all maximal frequent ( $\text{sup}=k$ ) subsequences and store it.
- We do not pre-compute all maximal frequent subsequences. We do longest common subsequence for each vertex.

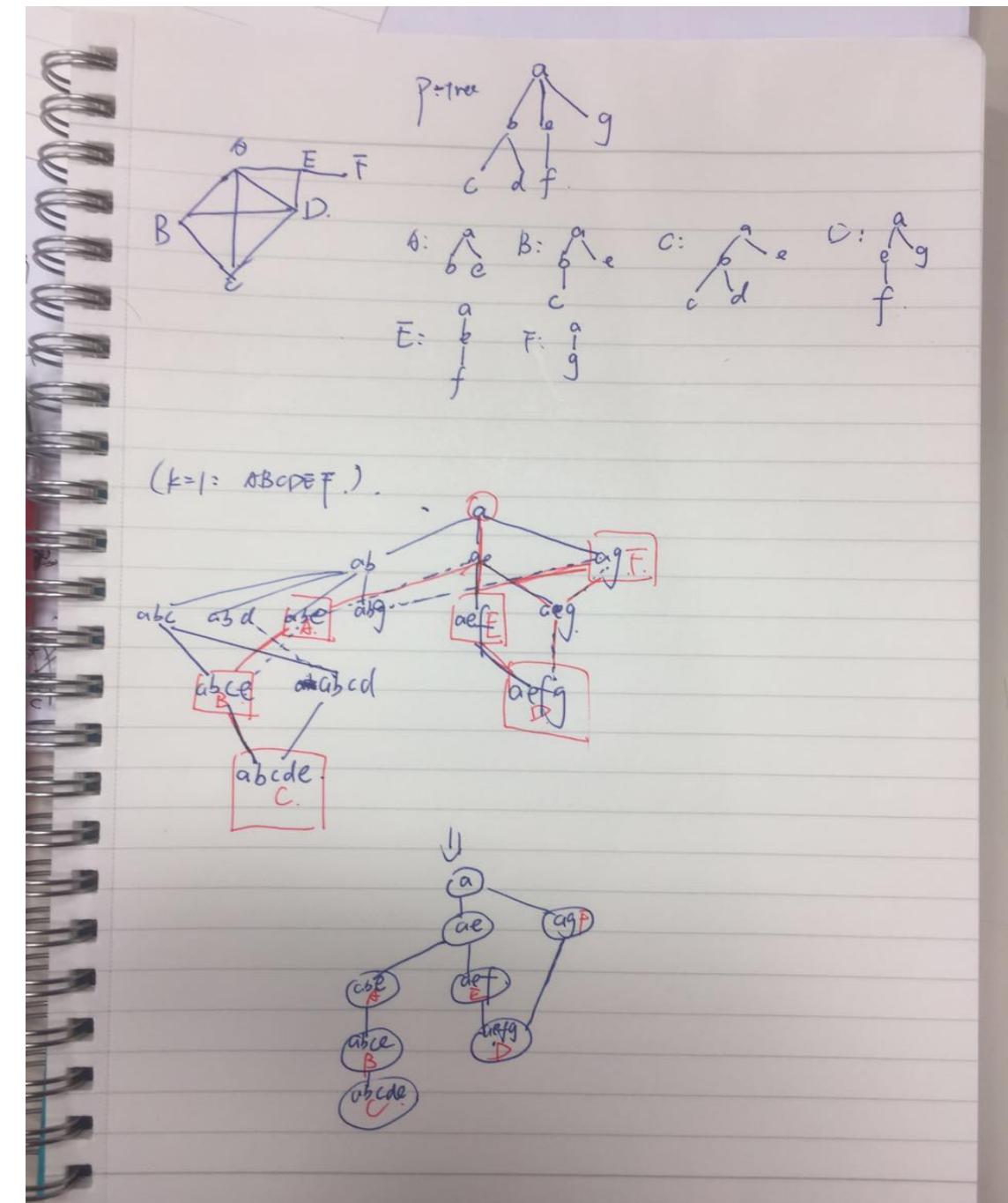


# Observation 2(from tree) index2

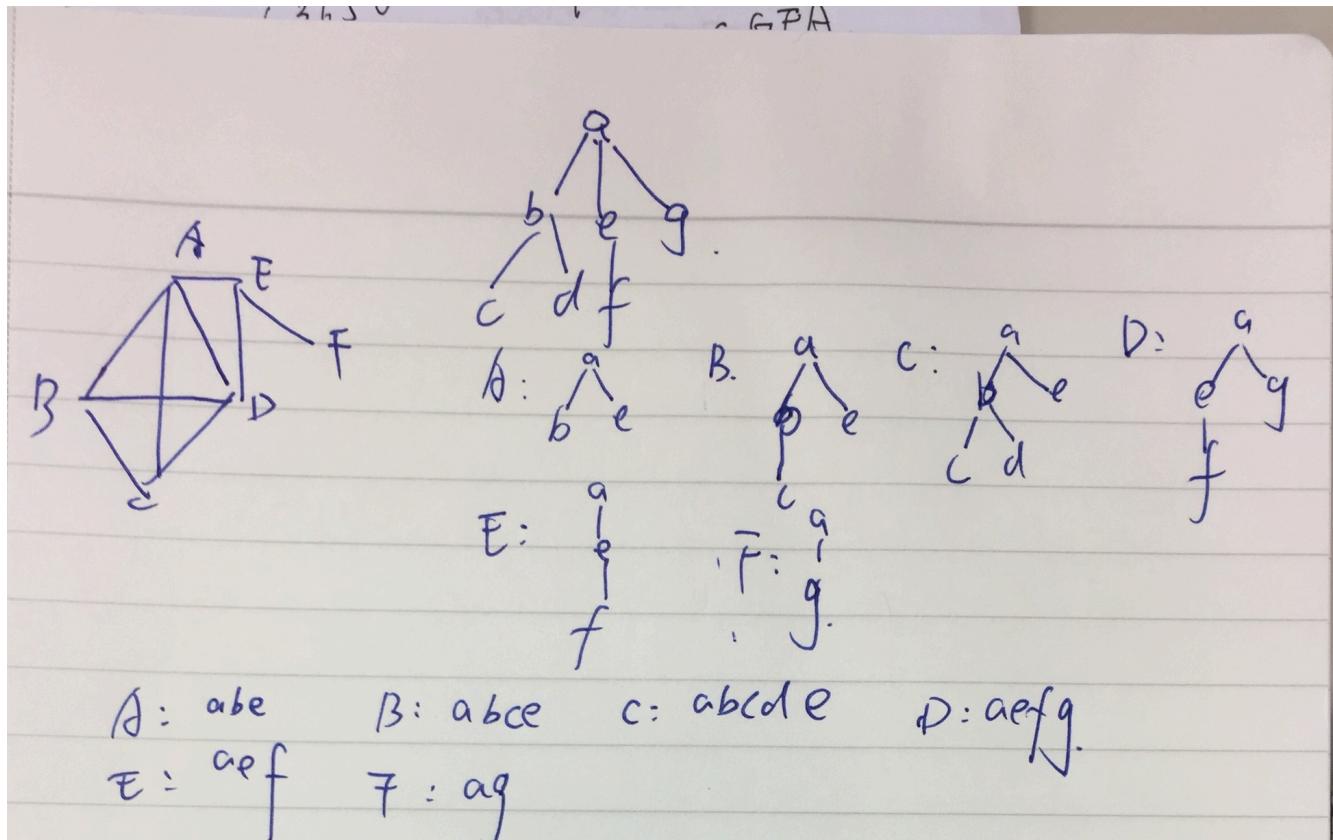
- If we focus on the relationship of subsequences.
  - Step 1 : We can enumerate all possible subsequences. We call it *enumeration lattice*.
  - Step 2 : vertex's sequence can be located in one of *enumeration lattice*.



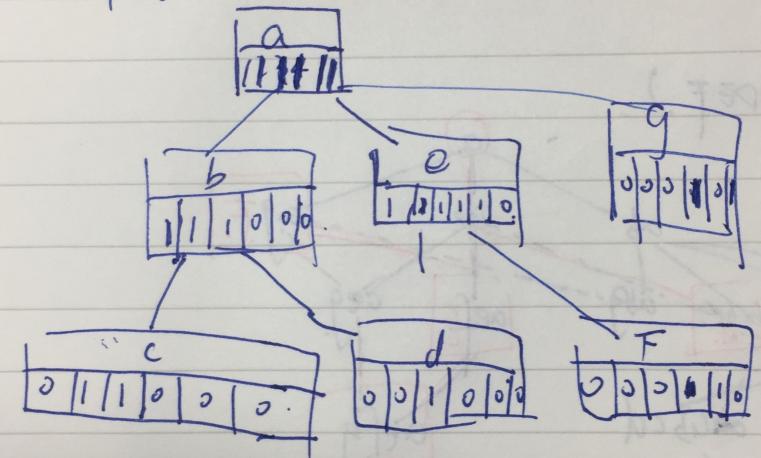
- Step 3: We can compress an enumeration lattice to omit some redundant patterns.
  - Details and techniques of compressing should be noticed.
- While querying, low common ancestor(lca) of query vertex and targeted vertices is the maximal subsequence pattern.
- E.g., in 1-core, query vertex is A, then ABC will be return. LCA pattern of {ABC} “abe” which is the maximal common subsequence.



# Index 3



$A = 1$   
 $B = 2$   
 $C = 3$   
 $D = 4$   
 $E = 5$   
 $F = 6$



query vertex A: [1|-----]  $\rightarrow$  "abe".

# compressed index-mathematic preliminary

- The only divisors of a prime integer  $p$  ( $p > 1$ ) are 1 and  $p$ .
- Every positive integer  $n$  is either 1 or can be expressed as a product of several prime integers, and this factorization is unique with the order of prime integers. The *standard form* of  $n$  factorization of  $n$ :  
 $n = p_1^{m_1} p_2^{m_2} \cdots p_n^{m_n}$ ,  $p_i$  is a distinct prime integer,  $m_i$  is called the *multiplicity* of  $p_i$ .
- Give two integers  $a$  and  $b$ , the great common divisor of  $a, b$  is  $\gcd(a, b)$ . E.g.,  $a = 2^3 \cdot 3^2 \cdot 7 = 504$ ,  $b = 2^2 \cdot 3^1 \cdot 7 \cdot 11 = 924$ ,  $\gcd(a, b) = 2^2 \cdot 3^1 \cdot 7 = 84$ .
- if we set  $m_i$  as 1. Then  $n = p_1 p_2 \cdots p_n$ .  $\gcd(a, b) = \prod_{i=1}^m p_{x_i}$ .

# compressed index-example

- $G = \{2,3,5,7\}$ ,  $a = 2 \cdot 3 = 6$ ,  $b = 5 \cdot 7 = 35$ ,  $\gcd(a,b)=1$ .
- $S_a = 1100$ ,  $S_b = 0011$ ,  $S_a \cap S_b = 0000 = 1$ .
- Set 4 bits as a block.  $S_a = \{10, \dots\}$ .  
Then  $S_a \cap S_b = \{\gcd(S_{a_i}, S_{b_i}) \mid i \in \text{number of blocks}\}$ .
- If  $G=\{2,3,5,7\}$ , then  $\gcd(a,b)$  has  $2^4 \cdot 2^4 \cdot 0.5 = 128$  types which can be pre-computed and stored in a table.