

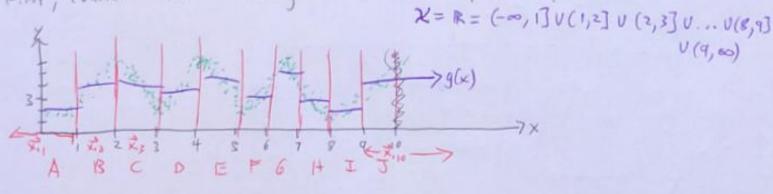
By question: How to provide the M nodels to select from in the model selection procedure? How to provide the transformations that defin the global search space in the forward stepwise moto-algorithm? In other words, how do we provide an algorithm that can flexibly create the for us on-the-fly without overfitting? This problem is the main thing that's addressed by "non-parameter" machine learning.

we will study tree models. The name of the algorithm is called Classification and Regression Trees (CART, 1984), which is really two algorithms!

Classification Trees for y = { C1, C2, ..., Cx} Regression Trees for y = R

we will start with regression trees and build it up step-by-step. First, consider the following data with Prow = 1: X=R=(-0,1]V(1):

V (9,00)

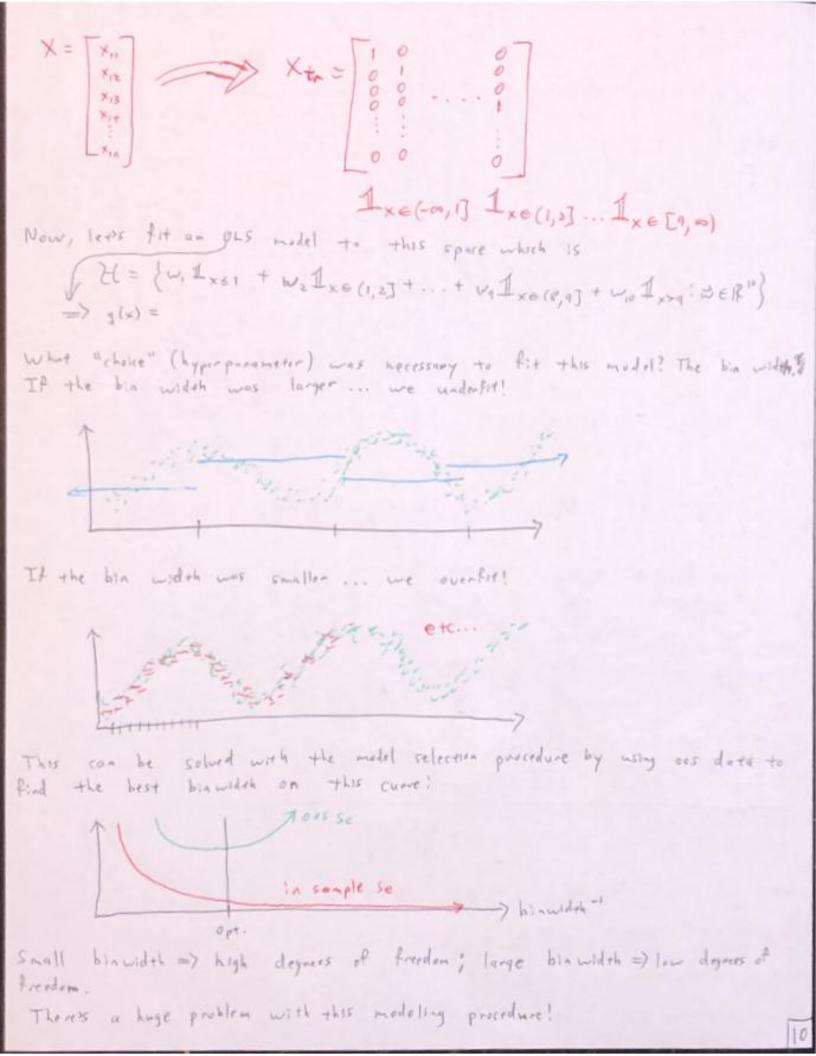


H, = { wo + w, x ! I = R2} BAD!

Hz= {wo +w,x+w2x2: & = R3 | BAP!

H3= (w, +w, sla(w,x): = = R3) 6,001.

You can figure this out with p=1, But high p... forget It! We need a simple, generalizable idea. Consider:



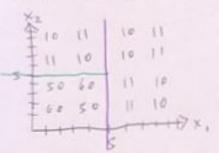
In two dimensions, bias are square. And you fit a level at a certain height (9). In three dimensions, bias are cubes and each case has its own 9. The problem is: in high p (dimension), the number of different coefficients grows exponentially.

E.g. Boston Housing data with p=13. It each veriable had only 5 his, then there would by 518 = 1,220,703,125 lie. a billion parameters. Clearly this per 7n and it cannot be estimated in and if it were to be estimated it would be overfit.

What about an algorithm that only considers bias that improve predictive performance? No need for bias to be equally sized or speced.



Letis design such an algorithm. Letis consider two dimensions:



Restrict bins to be separated by an orthogonalto-axis split of the entire space.

Step 1: Get best two-bin model.

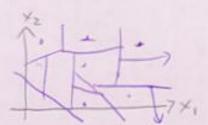
Step 2: Get best three-bin model assuming we split a bin's subspace.

At some print we have to the X2 = 5 No.

Stop splitting into new bias 55 10.5

and call it quits with out "binary tree model."

You can also consider non-orthogonal to split bin models or curved bin models such as:



A. C. X.

but such models are hard to fit... We will consider in this course only orthogonal -+0-axis-split hypernectangular & vegions.