Lecture 14 3/17/21

ln (7) = bo + b, x, + ... + b, xp

7 = ebo ebix, ... ehxx

If x, increases by 1, then of has a proporeson change of b, . So if b, = 0.25 and x, goes up by 1, then \$ increases by 25%.

= mo mixioner mpxr (multiplicated model). If x, increases by I then & is multiplied by mi. If x, and log(x,) are both in the model, then the model is less later pretable.

We talked about polynomials and logs. Angmenting the function space I with these allow for a model with curres, a model looks like!

 $g(x_1,...,x_p)=g_1(x_1)+g_2(x_2)+...+g_p(x_p)=\frac{2}{2x_1}Ig_1(x_2)]=0$ this is called a generalized additive model (GAM). What are we missing in this candidate space? The possibility of features interacting with one another. Consider the following transformation:

This transformation is called a liftest-order interaction." Consider come an OLS model on this new design matrix:

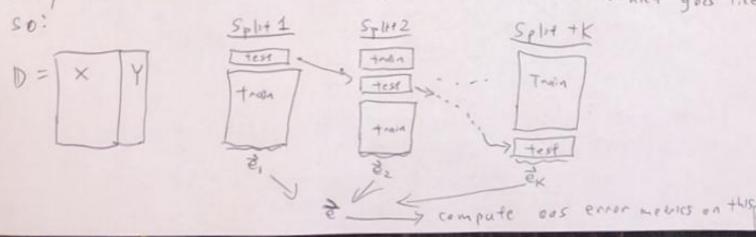
$$q(x_1,x_2) = \hat{y} = b_0 + b_1x_1 + b_2x_2 + b_3x_1x_2$$

$$\hat{x} = b_0 + (b_1 + b_3x_2)x_1 + b_2x_2 = b_0 + b_1x_1 + (b_2 + b_1x_1)x_2$$

$$\widehat{slope}$$

Let's go back to our discussion about validation. Our validation procedure split the original dataset randomly by taking 1/K no observations into a test set and the rest into a training set. Thus, the oos error metales can vary based on the specific random split. The oos error metales are random variables. And it their variance is high, then our estimates aren't so useful.

How can we reduce the vanlance in our ors error metales? Answer: make many splits and repeat the train-test validation procedure, There are many ways ato "make many splits". One popular way is called "cross-validation" (CV) or "K-Rold CV" which goes like



Each observation in the original dataset gets represented once inside of a test set. Each split "crosses over" the test set to this the next set of 1/K × n indires. This reduces variance because we are averaging many realizations of the n.v. (the our error metals).

Another bonus is that we can also compute our metrics in each of the K splits. For example our Sei, Sez,..., Sex. So you can gauge the variability of the our se via:

$$S_{se} := \sqrt{\frac{1}{K-1}} \sum_{k=1}^{K} (s_{e_K} - \overline{s}_e)^2$$

This gloss you some degree of guarantee of your oos estimate. Cantion: for this to be valid, the Se's have to be independent. Are they? No... since they were use a lot of the same data. But ... we use if anyway.

Midtern I 1

Mid term 2 V

We talked about K = 5 and K = 10 being good defaults? what is the tradeoft of K being lower us. higher?